

How do we evaluate the contribution of anthropogenic climate change to sea level rise from Antarctica?

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10
11 **Abstract**

12 The relative contributions of anthropogenic climate change and internal variability in sea level
13 rise from the West Antarctic Ice Sheet are yet to be determined. Even the framework required
14 to address this question is not yet clear, since these two are linked through ice-ocean feedbacks
15 and probed using models with substantial structural uncertainty. Here, via a synthetic marine ice-
16 sheet example, we demonstrate how their relative contributions can be assessed. Using a Bayesian
17 approach, we construct distributions of sea level rise (SLR), accounting for uncertainties arising
18 from both poorly-constrained model parameters and stochastic variations in climatic forcing, and
19 demonstrate that it is necessary to account for both. We identify characteristic effects of climate
20 change on SLR distributions, most notably that climate change increases both the median and the
21 weight in tails of distributions. From these findings, we construct metrics quantifying the role of
22 climate change, demonstrating that robust attribution of SLR is possible even for unstable marine
23 ice sheets. This paves the way for real-world attribution studies, which have significant implications
24 for climate damage reparations and greenhouse-gas emissions policy.

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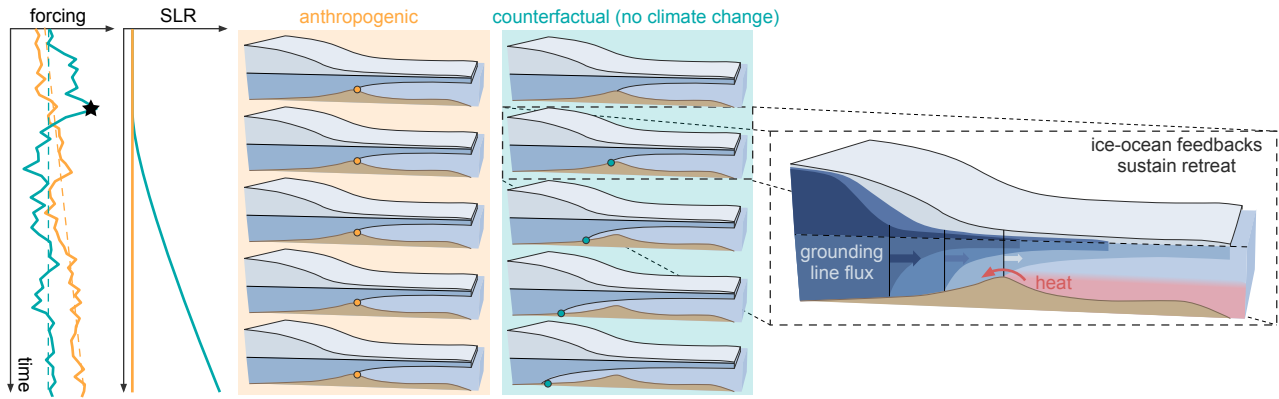


Fig. 1: Sea level rise from marine ice sheets is not necessarily an indicator of climate change. Schematic diagram demonstrating how an ice sheet configuration that remains stable under a realization of forcing including anthropogenic climate change (orange) may experience runaway retreat under a different, counterfactual realization of forcing with no anthropogenic climate change (green). As a result, grounding line retreat (filled dots in ice shelf configurations) and sea level rise are much higher in the counterfactual case. Once initiated (say, at the star), retreat from a topographic high is sustained by ice-ocean feedbacks.

26 Introduction

27 The West Antarctic Ice Sheet (WAIS) has changed significantly over the satellite era, characterized by ice
 28 acceleration [1], thinning [2], retreat [3], and ice loss [4]. The WAIS currently contributes approximately 10%
 29 of global SLR [5, 6] and could add tens of centimeters over the coming decades, possibly dominating by the end
 30 of the century [7]. However, despite being key symbols of anthropogenic climate change [8, 9], Antarctic ice
 31 loss, and thus associated sea level rise contributions, are yet to be formally attributed to anthropogenic climate
 32 change [10].

33 A robust causal relationship between WAIS ice loss and anthropogenic climate change is yet to be established
 34 because of strong internal variability in the region’s climate and ice-ocean feedbacks which perpetuate ice
 35 loss [10]. There are several lines of evidence highlighting their complex interplay. While WAIS retreat was
 36 initiated in the 1940s [11–13], after an approximately 10,000-year quiescent period [14], anthropogenic influence
 37 on key climatological drivers in the region only became significant in the 1960s [15]. This suggests that the
 38 ‘trigger’ for retreat would have occurred even without anthropogenic forcing. Following its initiation, WAIS
 39 retreat was likely sustained by ice-ocean feedbacks [16–21] (figure 1). Most notably, retreat of this marine ice
 40 sheet across a retrograde bed (upward sloping in the flow direction) is associated with increased ice flux across
 41 the grounding line (where the ice transitions from sitting on bedrock to a floating ice shelf), which promotes
 42 further retreat [22, 23] (figure 1). Thus, one possibility is that the ongoing ice loss was triggered naturally
 43 in the 1940s and retreat is dominated by self-perpetuating feedbacks, playing out on the long timescales on
 44 which ice-sheets evolve [11, 13, 15, 24]. However, this retreat cannot be purely self-sustaining, independent of
 45 external forcing, because ice discharge remains responsive to ocean variability [25–27]. This picture is further
 46 complicated by a proposed centennial scale warming of the Amundsen Sea [24, 28], which is partly attributed
 47 to anthropogenic changes in large-scale climate systems [15, 28–30]. While all of these processes may contribute
 48 to the ongoing ice loss, the relative contributions of a historical trigger, ice-ocean feedbacks, and changes in
 49 climatic forcing are still unknown.

50 Determining the role of anthropogenic climate change in SLR from the WAIS is important for providing
51 causal evidence to support recourse for the myriad social [e.g. 31], economic [e.g. 32], and ecological [e.g. 33]
52 impacts of SLR, which are borne primarily by poorer and low-lying island nations [34]. This is particularly
53 pertinent in light of the recent outcomes of the COP27 conference, in which a ‘loss and damage’ fund was
54 established to compensate countries for the harm inflicted by anthropogenic climate change. In addition,
55 attribution (or lack thereof) has implications for the future of the WAIS: if the observed ice loss is due solely to
56 internal variability and ice-ocean feedbacks, sea level rise is likely already committed and irreversible; whereas,
57 a significant anthropogenic component might suggest that ongoing contributions strongly depend on future
58 greenhouse gas emissions.

59 Despite the importance of this question, a framework (i.e. an outline of the necessary experiments and
60 analysis) to address it is not yet clear. Progress has been made towards such by Christian et al. [35], who
61 considered how ice sheet retreat from a local topographic high under variable forcing may be attributed, using
62 a one dimensional ice sheet model. Using a set retreat threshold as the ‘event’ to be detected, they showed
63 that while an observation of significant retreat under a single realization of climatic forcing does not necessarily
64 indicate that anthropogenic climate change was present in the forcing (figure 1), even modest anthropogenic
65 trends in forcing make retreat more likely when averaged over multiple realizations. They conclude that a
66 probabilistic approach, with multiple realizations of forcing, must be taken if robust attribution statements are
67 to be made. Additionally, they showed that model parameter choices have a large impact on the likelihood of
68 retreat, and thus the attribution statement; this suggests that multiple model parameters should be considered
69 simultaneously in the attribution assessment, particularly when these are poorly constrained. Here, we present
70 a framework for attributing sea level rise contributions from the WAIS which uses a probabilistic approach
71 integrating multiple realizations of forcing; we build upon [35] by, firstly, explicitly accounting for the role of
72 poorly-constrained model parameters in the attribution assessment and, secondly, considering sea level rise
73 contributions, rather than retreat, as the metric to be attributed. Both of these advances emerge from our
74 use of a Bayesian framework, which, in particular, allows an attribution metric to be constructed for any
75 observed sea level rise, avoiding the need to specify a single ‘event’ that is to be attributed at the outset.
76 We demonstrate this framework via an example of a marine-terminating ice sheet, which is highly susceptible
77 to ice-ocean feedbacks and subject to forcing with strong internal variability, the characteristic features that
78 are thought to obscure signals of anthropogenic climate change in SLR contributions from the WAIS. We
79 explicitly construct distributions of SLR which simultaneously account for parametric uncertainty (that arising
80 from poorly constrained model parameters) and aleatory uncertainty (that arising from an ice sheet’s variable
81 response to different realizations of stochastic forcing). We demonstrate their intimate interplay, as well as
82 the necessity of considering both in WAIS ice loss projections, a feature that is lacking in current assumed
83 estimates of sea level rise. These distributions also reveal characteristic signatures of anthropogenic forcing on
84 distributions of SLR from marine ice sheets.

85 Results

86 Aleatory and parametric uncertainty in distributions of sea level rise

87 We adopt a Bayesian approach in which parametric uncertainty and aleatory uncertainty are simultaneously
88 accounted for. As is standard, parametric uncertainty is accounted for by performing multiple simulations with
89 different model parameters spanning the parameter space (for each realization of forcing), with the resulting
90 SLR contributions weighted according to the level of agreement between a simulated and observed quantity [e.g.
91 36–40]. It is straightforward to incorporate aleatory uncertainty into such an approach (see methods) by placing
92 no preference on the specific realization of forcing. Although accounting for parametric uncertainty in this way
93 is now standard, no study has yet combined parametric and aleatory uncertainty, primarily because of the
94 computational expense of doing so [38] (multiple simulations with different model parameters must be run for
95 each additional realization of forcing).

96 To illustrate the approach, we focus on parametric uncertainty arising from the use of a parametrisation of
97 ice shelf basal melting. Parameterisations of basal melting are often used instead of coupled-ice ocean models
98 to reduce computational expense (in coupled ice-ocean models, the ocean component typically represents the
99 vast majority of the expense [41]). Coupled ice-ocean models remain computationally intractable for the large
100 ensembles of simulations [41] required to account for both aleatory and parametric uncertainty. However,
101 parameterisations of melting neglect processes that have been shown to be important in determining basal
102 melting [16, 42, 43], and simulations employing parameterisations have been shown to yield basal melt rates
103 which result in poor skill at reproducing observed grounding line retreat [44] and ice loss [45–47], compared
104 to coupled ice-ocean models. Our approach is intermediary: we use a parameterisation of basal melting to
105 achieve computational efficiency and adopt a Bayesian approach to the model parameters within: simulations
106 are weighted by comparing their predictions of basal melt rates with those from an offline ocean model at
107 different snapshot times throughout a simulation (methods); the ocean model thus plays a role analogous to
108 a ground-truth observation. We employ a common parameterisation of melting with quadratic dependence of
109 melting on ocean temperature, in which a single dimensionless parameter M (effectively a calibration coefficient)
110 is varied (methods).

111 Our example configuration features a prominent seabed ridge (figure 2a) on which the ice shelf is stably
112 grounded (figure 2b) during an initialization stage with temporally constant ocean forcing, corresponding to
113 typical conditions in the Amundsen Sea offshore of the WAIS (methods). This grounding line position, located
114 at a topographic high, is reminiscent of the WAIS prior to the 1940s [11] and renders the system highly sensitive
115 to ice-ocean feedbacks once grounding line retreat has been initiated [46]. We consider evolution from this
116 steady state under variable ocean forcing, which is imposed by varying the depth of the pycnocline in the
117 ambient ocean conditions (figure 2c–d). This forcing includes a stochastic internal variability component, which
118 mimics the observed amplitude [48, 49] and persistence [35] of internal variability in ocean conditions in the
119 Amundsen Sea on decadal and shorter timescales. Superimposed on this forcing is either an anthropogenic
120 trend – a 100 m/century linear shallowing of the pycnocline, illustrating a plausible historical anthropogenically

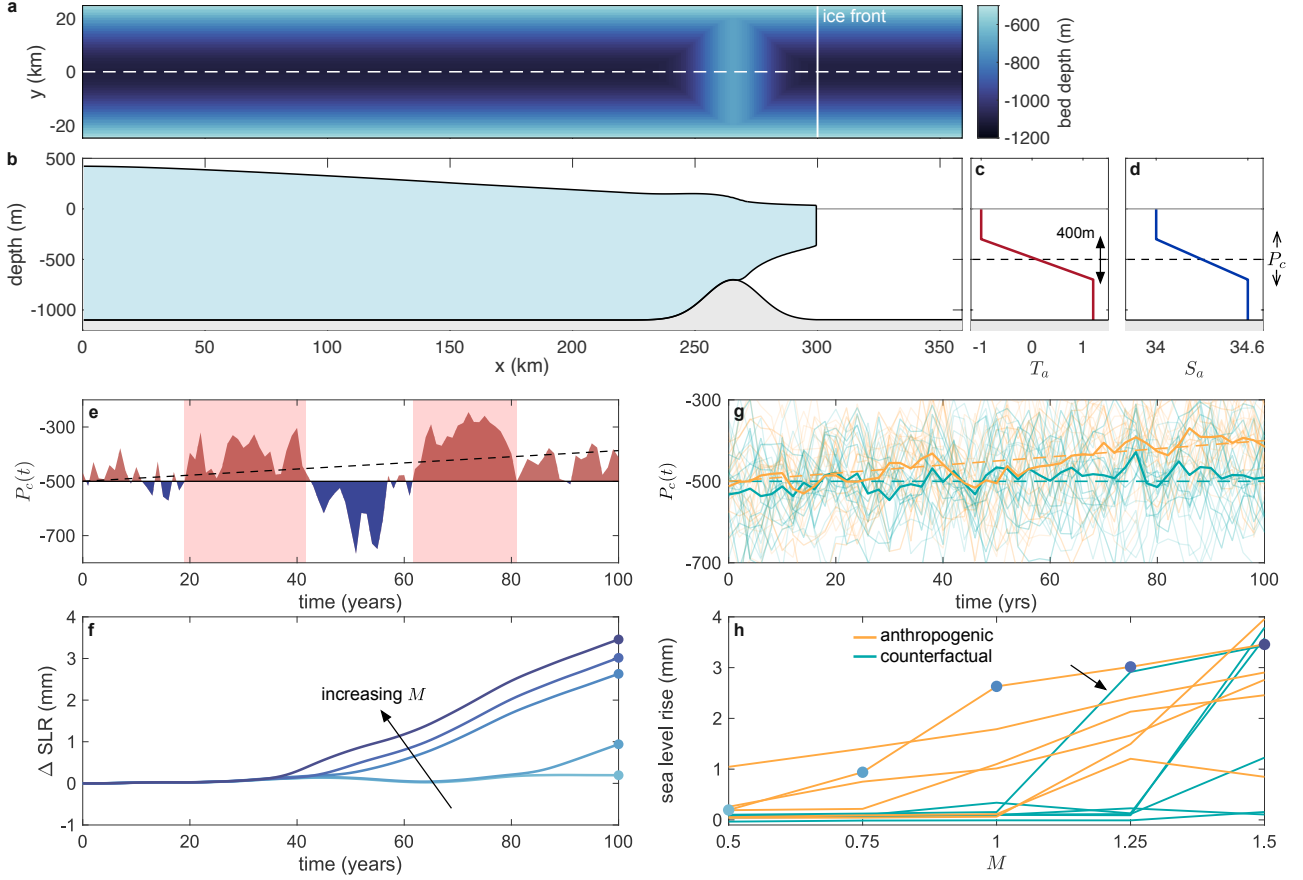


Fig. 2: Strong dependence of simulated marine ice sheet sea level rise on both forcing and model parameters. (a) Bathymetry (given by equation 7) of the marine ice sheet configuration. (b) Initial ice thickness along the dashed centerline in (a) for $M = 1$. The gray line indicates sea level. (c)–(d) Ambient temperature T_a (c) and salinity S_a (d) used in the parameterisation of melting and as restoring boundary conditions in the ocean model (methods). P_c denotes the pycnocline center, which parameterizes the piecewise linear forcing profiles and is oscillated to mimic variability. (e) Time evolution of a single realization of forcing and (f) corresponding SLR contributions for different values of $M \in \{0.5, 0.75, 1.0, 1.25, 1.5\}$ (the arrow indicates the direction of increasing M). Blue and red regions in (e) indicate whether the forcing is warmer (shallower pycnocline) or colder (deeper pycnocline) than during the calibration phase, where $P_c = -500$ m (black horizontal line), and shaded red regions indicate two prominent warm periods. The black dashed line indicates the 100 m/century anthropogenic trend in the pycnocline depth. (g) Time evolution of pycnocline centres P_c in all realizations of forcing. Here, orange curves correspond to forcing scenarios with an anthropogenic trend of a 100 m/century shallowing of the pycnocline, while green curves correspond to a counterfactual scenario, with no trend in the forcing (methods). In both cases, faint curves indicate individual ensemble members, while solid curves indicate ensemble means, and the dashed lines indicate the respective trends in these. (h) Sea level rise after 100 years as a function of M for a sub-set of the different realizations of forcing. Each line corresponds to an individual realization of forcing, and colors indicate whether the forcing is drawn from the anthropogenic (orange) or counterfactual (green) ensemble. Blue hue points correspond to the points shown in panel f. The arrow indicates the curve referred to as the ‘highlighted’ curve in the main text.

121 driven trend in Amundsen Sea conditions [28, 50] – or no trend, representing the counterfactual scenario in
122 which no anthropogenic climate change has taken place (figure 2g). For both of these trends (referred to as
123 anthropogenic and counterfactual, respectively), we perform simulations with 40 independent realizations of
124 forcing (the realizations in each of the two ensembles are also independent).

125 For each realization of forcing, we perform simulations sampling the set of M parameter space values.
126 Requiring that the ice shelf remains stably grounded at the ridge crest during the initialization phase, and
127 retreats under forcing corresponding to the warmest observed conditions applied constantly, restricts us to
128 considering the range $0.5 < M < 1.5$ (methods); we sample this range by taking $M \in \{0.5, 0.75, 1.0, 1.25, 1.5\}$.
129 Thus, the total number of simulations is 400 (2 ensembles \times 40 members \times 5 M values).

130 Examining the response to a single illustrative realization of forcing (figure 2e), for different melt parameters
131 M , highlights the interplay between stochastic forcing and parameter variability, elucidating the inextricable
132 relationship between aleatory and parametric uncertainty. On the centennial scale, this realization of forcing
133 features two warm periods (figure 2e). During the first warm period (approximately between $t = 20$ and $t = 40$
134 years), retreat is triggered in those simulations with the largest values of M ($M = 1, 1.25, 1.5$; figure 2f). This
135 retreat is initiated towards the end of the first warm period (figure 2f), when the time-integrated melt anomaly
136 has caused enough ice shelf thinning to reduce ice shelf buttressing to the level at which retreat is initiated.
137 Accordingly, retreat is initiated soonest in the simulation with the largest melt parameter M (figure 2f), which
138 has the highest melt rates and accumulates the time-integrated melt anomaly most rapidly. Once initiated,
139 retreat proceeds at a rate approximately independent of forcing (figure 2f), suggesting that, once triggered,
140 retreat is set primarily by ice-ocean feedbacks, although it remains weakly responsive to changes in forcing.
141 Simulations with smaller M (lower melting) remain grounded at the ridge crest during the first warm period.
142 Retreat is initiated in the $M = 0.75$ simulation during the second warm period, again towards the end of the
143 period. A simulation with the same realization of forcing with the anthropogenic trend removed, and $M = 0.75$,
144 does not retreat during this period (note that this simulation is outside the ensemble structure outlined above,
145 for which anthropogenic and counterfactual ensembles are independent): the integrated melt anomaly required
146 to initiate retreat is achieved more easily during a given time period if there is an anthropogenic trend in the
147 forcing, than if not.

148 Under the same realization of forcing, SLR may be highly non-linear in M (figure 2h). For example, SLR
149 contributions in the highlighted curve in figure 2h increase by 1800% (from 0.15 mm to 2.91 mm after 100 years)
150 when the melt rate parameter is increased from $M = 1$ to $M = 1.25$. This strong sensitivity demonstrates the
151 necessity of considering a range of parameter values in determining SLR contributions, particularly when the
152 system is susceptible to ice-ocean feedbacks, or so-called ‘tipping points’ may be passed. Furthermore, there
153 are simulations in the anthropogenic ensemble which yield lower SLR than simulations in the counterfactual
154 ensemble (figure 2h), and this behavior is strongly influenced by the value of M . Thus, an observation of
155 high SLR under a single realization of forcing is not necessarily an indicator of strong anthropogenic influence
156 (figure 1). Taken together, these results – a strong sensitivity to the parameter M and to the specific realization
157 of forcing – demonstrate that parametric and aleatory uncertainty must be simultaneously accounted for in SLR

158 distributions, and thus any framework attempting to determine the role of anthropogenic trends in forcing in
159 them.

160 The non-linearity of sea level rise in M also demonstrates how single-point calibration (where the set of
161 model parameters are specified based on agreement with a single observation, say the total melt flux out of
162 an ice shelf cavity) may be problematic. Such single-point calibrations are often applied when tuning melt
163 rate parameterisations [e.g. 47, 51, 52]. In the example presented here, the mean melt rate at the start of the
164 simulation (at the end of the initialization stage, which is performed separately for different values of M) is only
165 weakly dependent on the melt rate parameter (supplementary figure 7d), owing to a feedback between melting
166 and ice geometry (methods). As a result, a small change in the target calibration value would result in a small
167 change in the selected value of M (supplementary figure 7d), but may ultimately result in a large change in the
168 simulated SLR at the end of the simulation (figure 2h).

169 **Influence of anthropogenic forcing on sea level rise probability distributions**

170 Applying the melt rate calibration procedure (methods), yields, for each time in each simulation, a distribution
171 of sea level rise associated with the particular realization of forcing applied (supplementary figure 8). Then, by
172 marginalizing over the realizations of forcing (methods), we obtain calibrated probability distributions of SLR
173 for both anthropogenic and counterfactual ensembles, at each time (figure 3a).

174 The time evolution of both ensembles display qualitatively similar behavior. The evolution of the distri-
175 butions can be categorized into two temporal parts: ‘tail emergence’ and ‘shift towards tails’ (figure 3c). At
176 early times, the distributions are symmetric (figure 3a), with low skewness (figure 3c) reflecting retreat having
177 not been triggered in any simulations. As retreat begins to be triggered in individual simulations, the ‘tail
178 emergence’ period begins: a tail emerges (skewness increases, figure 3c) – supported by increasing SLR con-
179 tributions from those already retreating simulations – and kurtosis increases (figure 3d), indicating that the
180 relative weight in the tails is reducing (kurtosis quantifies the proportion of weight placed in the tails, with low
181 kurtosis corresponding to heavy tails). The timescale on which the tails emerge depends on the forcing (see
182 below). Median sea level rise remains small in the tail emergence period (figure 3b).

183 As retreat is triggered in an increasing number of ensemble members, weight begins to shift to the tails;
184 the ‘shift towards tails’ period begins when skewness and kurtosis reach a maximum (figure 3c–d). Beyond this
185 maximum, weight moves towards the tails (kurtosis reduces, figure 3d) and, in response to this, the median
186 increases (figure 3a), continuing to the end of the simulation. (The median is a more appropriate metric than
187 the mean given the skewed data.) Both medians display a non-linear evolution, reflecting non-linear SLR
188 contributions in individual simulations once retreat has been initiated. Although the precise details of the
189 evolution of the distributions depends on both the system and the forcing (see below), we expect that this
190 qualitative behavior is generic in marine ice sheets with tipping points under high variability stochastic forcing.

191 Despite these qualitative similarities between the anthropogenic and counterfactual distributions, there are
192 clear quantitative differences, which highlight the importance of the anthropogenic trend in forcing. Firstly,

193 the tail emerges sooner in the anthropogenic ensemble (figure 3c), because retreats are initiated sooner when
194 a trend in forcing is imposed (supplementary figure 5). This is despite the anthropogenic additional forcing
195 being zero at the start of the simulation (figure 2g), highlighting the role played by increases in forcing during
196 the time period in which the destabilizing integrated melt anomaly is accumulating: if forcing did not change
197 over this period (or, if the changes did not matter), the first retreats would take place at approximately the
198 same time in both ensembles. This is consistent with [15], who suggest that the current retreat of WAIS was
199 triggered naturally in the 1940s, but may have subsequently failed to recover due to increasing influence of
200 anthropogenic forcing towards the start of the 1960s. Secondly, the maximum skewness is lower, and achieved
201 sooner, in the anthropogenic case (figure 3c). In a given time period, retreat is triggered in a greater proportion
202 of simulations in the anthropogenic ensemble than in the counterfactual ensemble (supplementary figure 5),
203 resulting in probability distributions shifting more quickly towards the heavy-tailed regime. This difference
204 in retreat rate triggering is because, as time proceeds, melt anomalies under anthropogenic forcing become
205 increasingly large, so a shorter positive anomaly duration is required to initiate retreat (more specifically, with
206 a linear anthropogenic trend, the melt anomaly scales with the square of time, which rapidly outweighs any time-
207 integrated negative internal component). Finally, and most importantly, on the centennial timescale, both the
208 median is larger, and the kurtosis smaller, in the anthropogenic ensemble than in the counterfactual ensemble;
209 i.e. not only does anthropogenic forcing increase the median of the distribution, it also results in greater
210 weight in the tails: extreme events, with high sea level rise contributions, have relatively large probabilities in
211 the anthropogenic ensemble. This emphasizes the need to consider the shape, as well as the spread (i.e. the
212 variance), when communicating how emissions pathways affect future SLR scenarios with policymakers.

213 Figures 3b-d also indicate how summary statistics differ between the calibrated and uncalibrated distribu-
214 tions, with the latter obtained by setting the posterior probability equal to the prior probability (methods). In
215 both ensembles, parametric calibration of M has an important effect on the median, evidencing the need to
216 apply parametric calibration in projections of SLR from ice sheets. Reduced uncertainty in projections is often
217 (perhaps implicitly) cited as a key benefit of parametric calibration [e.g. 36, 38]; whilst our simulations provide
218 evidence to support this, displaying increased kurtosis (reduced weight in the tails; figure 3d) in the calibrated
219 case, there remain significant uncertainties in calibrated distributions (figure 3a). This suggests that aleatory
220 uncertainty is an unavoidably large part of uncertainty in projections of SLR from ice sheets, particularly those
221 highly susceptible to ice-ocean feedbacks, and cannot be neglected: parametric calibration alone is not sufficient,
222 and there is irreducible uncertainty in SLR from marine ice sheets.

223 **Quantifying signals of anthropogenic climate change**

224 The role of anthropogenic climate change in individual ‘weather’ events is often framed as an anthropogenic
225 enhancement [53]: how many times more (or less) likely was the event made by anthropogenic climate change?
226 Having constructed distributions of SLR in both anthropogenic and counterfactual cases, the ratio of these –
227 the anthropogenic enhancement ratio (AER) – naturally emerges as a metric to quantify how many times more

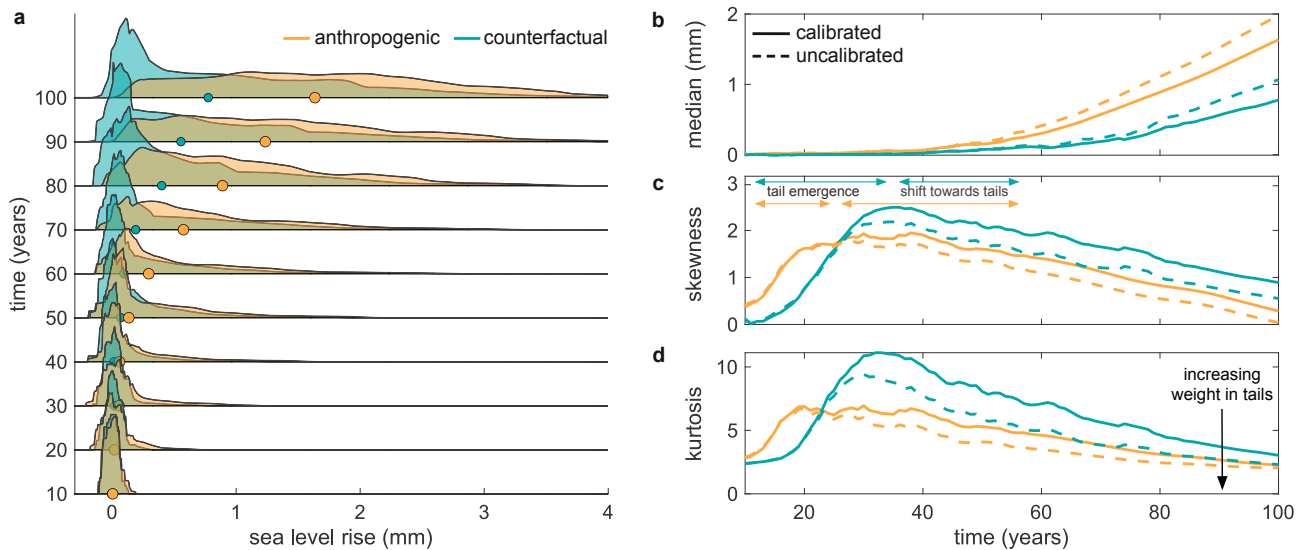


Fig. 3: Influence of anthropogenic forcing on distributions of sea level rise. (a) Time evolution (running bottom to top) of distributions of sea level rise from ensembles with anthropogenic forcing (orange) and counterfactual (no-trend) forcing (green). Filled markers indicate the median of the distributions at the corresponding time. (b)–(d) Summary statistics of the distributions in (a) as follows: (b) median, (c) skewness and (d) kurtosis. In each, the dashed lines indicate the corresponding summary statistics for distributions obtained without parametric calibration, obtained by setting the posterior probability equal to the prior probability.

likely an observed sea level rise was made by the presence of an anthropogenic trend in forcing, and go beyond the qualitative comparisons of the previous section. An AER of 2, for example, indicates that anthropogenic forcing made a given SLR contribution 100% more likely (or, equivalently, twice as likely). The AER for our ensembles is shown in figure 4a, where values along each line of constant time represent the ratio between the two distributions (as shown for specific times in figure 3a).

There is a band in which the AER is infinite, which is caused by the tails of the anthropogenic distribution extending to higher SLR values than those in the counterfactual distribution (figure 4a). An observation of SLR in this band would have been impossible without anthropogenic climate change—no counterfactual simulations produce this value. The band spreads out in time from an area close to the origin (recall that the tail of the anthropogenic distribution emerges soon after the start of the simulation) at a rate that is set by the retreat of the individual simulation with the highest SLR.

The AER is generally increasing in SLR, indicating that a higher SLR over many realizations of forcing is a stronger indicator of anthropogenic climate change. This demonstrates the importance, and value, of accounting for aleatory uncertainty: under a single realization of forcing, higher SLR does not necessarily indicate a strong influence of anthropogenic climate change (figure 1), but, does when appropriately averaged over many realizations of forcing. This also highlights the shift from a binary yes-no question, to a probabilistic approach, that necessarily takes place when accounting for aleatory uncertainty [35]. The AER has a slightly banded structure (figure 4a), which results from the finite size of our ensembles (there are periods when relatively more retreats are initiated than the background trend, see figure 5). While we expect that the banding would disappear as the number of realizations of forcing goes to infinity, we note that increasing this number is particularly computationally expensive when accounting for aleatory and parametric uncertainty simultaneously.

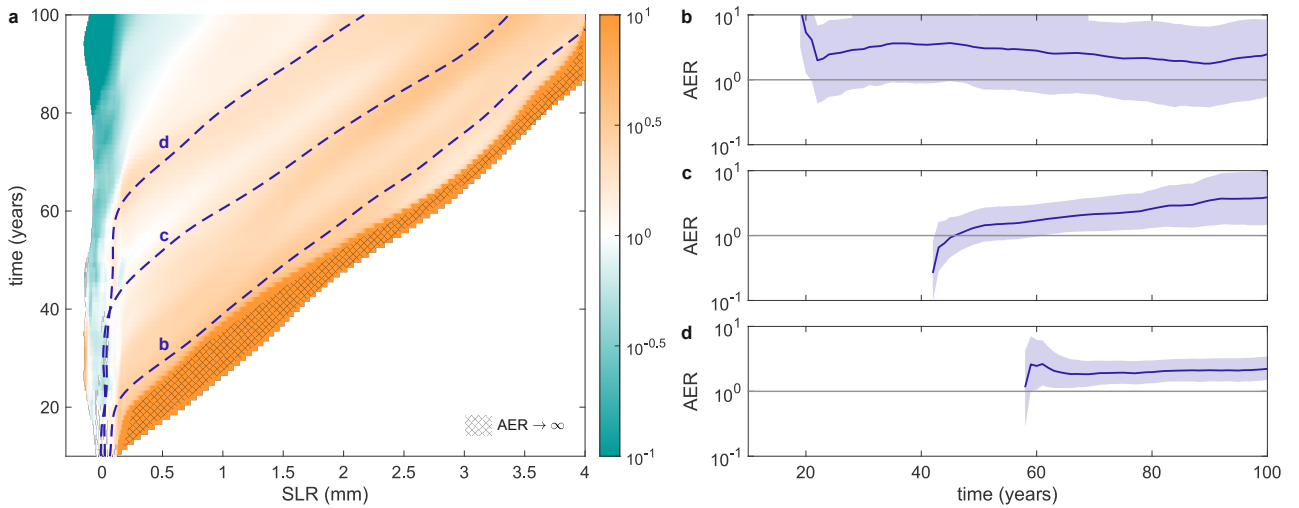


Fig. 4: Signals of anthropogenic climate change in sea level rise from marine ice sheets. (a) Contour plot of anthropogenic enhancement ratio (AER) as a function of time and space, with colors as indicated by the colorbar. The hatched region indicates the area where $AER \rightarrow \infty$. (b)–(d) Time evolution of AER (solid lines) along selected simulation trajectories of sea level rise, corresponding to labelled lines in (a). The shaded region indicates the uncertainty in this metric, obtained by bootstrapping values of distributions that result from individual realizations of forcing (methods). Data are shown only for times where $SLR > 0.1$ mm for clarity.

249 In practice, observed sea level rise follows a single trajectory through this AER space, such as the selected
 250 simulations shown in figure 4b–d, in which retreat is triggered after approximately 20, 40, and 60 years, respec-
 251 tively (figure 4a). Their values are indicative of the clear signal of anthropogenic climate change: at the end of
 252 the simulation, AER is approximately 2.5, 3.9 and 2.2 respectively, corresponding to increases in probability of
 253 150%, 290%, and 120%, respectively. These values are common along their paths, and once retreat has been
 254 triggered, the AER remains fairly constant. It is worth noting that these values are perhaps modest compared
 255 to glaciological attribution studies applied to mountain glaciers [e.g. 54, 55]. This is a direct consequence of
 256 our choice of setup: we consider a scenario in which internal variability is relatively large compared to the
 257 anthropogenic trend (and these selected trajectories don't enter the tail band, for which $AER \rightarrow \infty$).

258 From a policy perspective, a third useful question, beyond how to address and how to quantify the attribution
 259 question, is: what is the uncertainty in this quantification? Having constructed distributions associated with
 260 each realization of forcing (which the distributions shown in figure 3 are the mean over), such uncertainties can
 261 be probed. To do so, we bootstrap values of the distributions from individual realizations of forcing to determine
 262 a confidence interval (methods and supplementary figure 9) – a measure of the likely spread in AER – around
 263 our central estimates (figure 4b–d). Uncertainty in AER is generally smaller along contours corresponding to
 264 later retreat (figure 4b–d). This is commensurate with relatively few simulation trajectories entering the region
 265 in and around the tail band, leading to increased uncertainty: although the central estimate of anthropogenic
 266 enhancement is itself largest in the tails, there is most uncertainty in the value there. We expect that this
 267 error bound would reduce with increasing numbers of realizations of forcing. Thus, we expect that real world
 268 attribution studies will have to grapple with the limitation that increasing ensemble size is required to reduce
 269 uncertainty in the role of anthropogenic forcing, but requires substantial additional computational resource.

270 Discussion

271 The example presented here provides a probabilistic framework to assess the role of anthropogenic climate
272 change in sea level rise contributions from the West Antarctic Ice Sheet, including both quantifying the strength
273 of the anthropogenic signal and its uncertainty. Determining the precise influence of anthropogenic climate
274 change on sea level rise contributions from the WAIS requires ‘real-world’ simulations to be performed. A key
275 challenge to overcome will be determining an appropriate prior distribution for the historical state of the system:
276 projections of ice sheet evolution are sensitive to their initial states, similar to numerical weather forecasts [56],
277 but relatively little is known about the configuration of the WAIS prior to the satellite record beyond broad
278 bounds on grounding line locations [11]. As such, it may be necessary to adopt semi-empirical approaches,
279 such as expert elicitation [57], to construct such a prior. Our simplified example, with assumed knowledge of
280 the initial state, circumvents this considerable difficulty, allowing the key interaction between parametric and
281 aleatory uncertainty to be examined in detail.

282 In considering a generic marine ice sheet, we are also able to neglect uncertainty arising from model param-
283 eters governing basal sliding and ice viscosity, as well as processes such as damage [19, 58] and calving [43, 59,
284 60], which should be included in assessments of sea level rise and thus its attribution to anthropogenic climate
285 change. By abstracting in this way, we are able to focus on errors in melting, with the hope that the melt cali-
286 bration approach may help to bridge the considerable gap in fidelity to observations between parameterisations
287 of melting and coupled ice-ocean simulations. It is important to note that additional parametric uncertainty, as
288 well as uncertainties arising from incomplete knowledge of the initial state, can be succinctly assimilated into
289 Bayesian approaches to sea level rise distributions [61]. The work presented can be considered, more gener-
290 ally, as a framework for producing calibrated distributions of sea level rise, in addition to their application to
291 attribution statements. We have demonstrated that both aleatory and parametric uncertainty are important
292 components of ice sheet sea level rise projections, and suggest that future assessments of sea level rise from
293 ice sheets must account for these sources of uncertainty. As we have shown, parametric calibration reduces
294 uncertainty, but the susceptibility to ice-ocean feedbacks renders broad distributions inevitable [62]: much like
295 other aspects of the climate system [63], ice sheets have irreducible uncertainty. In addition, considering a range
296 of initial states (which may be broad) will only increase this uncertainty. The glaciological community must
297 become more comfortable with these fundamental aspects of uncertainty and appropriately communicate them
298 to policy-makers and stakeholders.

299 By constructing calibrated distributions of sea level rise contributions, we showed that anthropogenic climate
300 change increases both the median of distributions, and the relative weight of their tails: much like many
301 other weather events [64], even modest anthropogenic climate change can make extreme scenarios many times
302 more likely. Using these distributions, we constructed a metric to quantify the role of anthropogenic forcing,
303 concluding that even in highly unstable marine ice sheets, the impact of anthropogenic forcing is detectable
304 in principle, given sufficiently large simulation ensembles under anthropogenic and natural forcings and a full
305 treatment of model parameter uncertainty. In other words, attribution studies are tractable for the WAIS.

306 The implications of attributing ice loss from the WAIS, both for the harms caused by sea level rise, and the
307 implications for the future of the WAIS, provide strong motivation to pursue such studies.

308 **Data Availability**

309 Code to analyze data and produce figures herein is contained in an open GitHub repository at <https://github.com/alexbradley/WAISAttribution-figures>. Processed ice sheet and ocean model data is contained in a
310 permanent Zenodo repository at <https://zenodo.org/record/7900762#.ZFUyk0zMLPa>.

312 **Methods**

313 **Sea level rise contributions accounting for parametric and aleatory uncertainty**

314 For a given trend in forcing, denoted \mathcal{F} , (i.e. after specifying whether the trend is anthropogenic or counter-
315 factual), the probability of a given SLR, ΔSLR , accounting for aleatory and parametric uncertainty may be
316 expressed as [61]

$$P(\Delta\text{SLR}|\mathcal{F}, \mathcal{I}_0) = \frac{1}{n} \sum_{i=1}^n \int P(\Delta\text{SLR}|\mathcal{F}, \mathcal{N}, \mathcal{R}_i, \mathcal{I}_0) P(\mathcal{N}|\mathcal{R}_i, \mathcal{F}, \mathcal{I}_0) d\mathcal{N}. \quad (1)$$

317 Here, \mathcal{N} is the space of model parameters, n is the total number of realizations of forcing, \mathcal{R}_i is the specific
318 realization of forcing (with i a dummy index), and \mathcal{I}_0 represents the initial conditions. The expression (1)
319 follows from a first-principles probabilistic expression of SLR [61], after assuming that each specific realization
320 of forcing has equal prior probability, $P(\mathcal{R}_i) = 1/n$, and that the initial state \mathcal{I}_0 is known. For our specific
321 application of (1), \mathcal{N} is the space of melt rate parameters, $0.5 < M < 1.5$. Note that the expression (1) does not
322 include any account of model structural uncertainty, which arises from the approximations that ice sheet models
323 make, as well as their incomplete representation or omission of physical processes [61]. Such uncertainties can
324 only be accurately probed by performing the same numerical experiments with an ensemble of different ice
325 sheet models, typically in a model intercomparison exercise [e.g. 65] and is therefore beyond the scope of this
326 work. (It should be noted that the WAVI ice sheet model used herein demonstrates good agreement with other
327 state-of-the-art ice sheet models in the most recent ice sheet model intercomparison exercise [65].)

328 **Melt Rate Calibration**

329 The calibration of model parameters M enters distributions of SLR through the probability $P(M|\mathcal{R}_i, \mathcal{F}, \mathcal{I}_0)$,
330 which appears in (1) (here we use the specific parameter name M , rather than the generic name \mathcal{N}). Following
331 a standard Bayesian approach, we assume a prior distribution on the parameters M (with hyperparameter μ),
332 which is then updated as new information is assimilated through the likelihood. In our case, this assimilated
333 information is melt rates from an offline ocean model (see below); denoting this information by \mathcal{O} , Bayes' rule
334 states that

$$P(M|\mathcal{O}, \mu) = \frac{P(\mathcal{O}|M, \mu) P(M|\mu)}{P(\mathcal{O}|\mu)} \quad (2)$$

335 The first term in the numerator on the right-hand side of (2) represents a likelihood function, describing how the
336 prior distribution (second term in the numerator on the right-hand side) is updated to assimilate ocean model
337 results. The prior distribution describes the state of belief in model parameters N prior to comparison with the
338 ocean model. The left-hand side of (2) represents the posterior distribution – the distribution of parameters M
339 following ocean model assimilation. The denominator of the right-hand side of (2) simply acts to normalize the
340 probability distribution.

341 Here, we assume a Gaussian prior, which maximizes the relative entropy when only estimates of the prior

342 mean μ and standard deviation σ_P are available [66, 67]:

$$P(M|\mu) = \frac{\alpha}{\sqrt{2\pi\sigma_P^2}} \exp\left(-\frac{|M-\mu|^2}{2\sigma_P^2}\right). \quad (3)$$

343 Here α is a normalization constant, which ensures that the distribution (3) integrates to unity when calibration
 344 bounds on M are imposed (see ‘Ice Sheet Model Initialization’ below). σ_P can be thought of as describing the
 345 strength of confidence in the initial estimate of M , which is centered about the hyperparameter μ : a low (high,
 346 respectively) σ_P corresponds to high (low) confidence that the hyperparameter μ represents the ‘true’ value
 347 of M . In the results contained herein, we use $\mu = 1.25$, based on agreement in the mean melt rate after the
 348 initialization stage (see ‘Ice Sheet Model Initialization’) but retain a broad prior ($\sigma_P = 0.2$, see supplementary
 349 figure 8), representing weak confidence in the prior distribution, which captures the relative insensitivity of
 350 mean melt rate on M during the initialization stage (see ‘Ice Sheet Model Initialization’).

To determine the likelihood $P(\mathcal{O}|M, \mu)$, we first specify calibration timeslices $\tau = \{\tau_1, \dots, \tau_n\}$ and, for each
 timeslice, run the ocean model in the geometry set by the ice-only model. After doing so, we have two melt
 rate fields,

$$\dot{m}_{\text{param}}^k = \dot{m}_{\text{param}}(x, y, t = \tau_k | M), \quad (4)$$

$$\dot{m}_{\text{ocean-model}}^k = \dot{m}_{\text{ocean-model}}(x, y, t = \tau_k | M) \quad (5)$$

351 from the parameterisation of melting and from the ocean model, respectively, and for each timeslice $k = 1, \dots, n$.
 352 (Note that the ocean model depends on the melt rate parameter M via the ice-shelf cavity geometry.) A melt
 353 error functional D_j is determined by comparing these two fields. The particular choice of the form of the D_j
 354 is subjective, reflecting how melting should be penalized. Here, we take D_j to be the mean absolute error in
 355 the two melt fields on grid cells below 500 m depth. This reflects the fact that deep areas, typically close to
 356 grounding lines, have disproportionately large impacts on the dynamics of the grounded ice [68–70].

357 From the timeslice errors D_j , we determine an average error $D = (1/n) \sum_{j=1}^n D_j$. The likelihood is then
 358 determined from an exponential error model,

$$P(\mathcal{O}|M, \mu) = \frac{1}{\sqrt{2\pi\sigma_L^2}} \exp\left(-\frac{D^2}{2\sigma_L^2}\right). \quad (6)$$

359 Here σ_L is a melt error covariance, which describes how harshly errors in the melt rate from the parameterisation
 360 are penalized (with respect to the ocean model): for low σ_L , errors are penalized more harshly, whereas for high
 361 σ_L , errors are penalized less harshly. In the limit $\sigma_m \rightarrow \infty$, each parameter value M is assigned equal weight,
 362 and the posterior distribution is identical to the prior (supplementary figure 8). In the results presented here,
 363 we use $\sigma_L = 10$.

364 Details of end-member configuration

365 The setup of the generic marine ice sheet configuration is very similar to that of [46], who interrogated how
366 ice-ocean feedbacks perpetuate retreat of an ice sheet from a seabed ridge using a coupled ice-ocean model under
367 constant forcing scenarios. In this setup, the bathymetry (figure 2a) can be expressed as the sum of along-flow
368 and cross-flow components:

$$B(x, y) = B_x(x) + B_y(y), \quad (7)$$

where

$$B_x(x) = 400 \exp \left[-\frac{(x - 265 \times 10^3)^2}{2\sigma_b^2} \right] \text{ m}, \quad (8)$$

$$B_y(y) = - \left[500 + 600 \sin \left(\frac{\pi}{2} + \frac{\pi y}{5 \times 10^4} \right) \right] \text{ m}. \quad (9)$$

369 Here, x and y are co-ordinates in the along- and cross-flow directions, respectively (the ridge is aligned along the
370 cross-flow direction, see figure 2a). The cross-flow bathymetry contribution, $B_y(y)$, corresponds to a symmetric
371 valley-like configuration, whose margins are located 500 m below sea level and whose center is 1100 m below
372 sea level; the cross-flow bathymetry contribution, $B_x(x)$, corresponds to a Gaussian ridge with height 400 m
373 and lengthscale $\sigma_b = 1.1 \times 10^4$, which is superimposed on the valley at a position centered on $x = 265$ km.

374 Following [46], ice rheology is described by Glen’s law with flow exponent $n = 3$. A constant rate factor
375 $A = 2.94 \times 10^{-9} \text{ a}^{-1} \text{ kPa}^{-3}$ is applied everywhere, except for within 5 km of the ice margins (i.e. for $y < -20$ km
376 and $y > 20$ km), where the rate factor is set to $A = 5.04 \times 10^{-9} \text{ a}^{-1} \text{ kPa}^{-3}$; this is to mimic the narrow, low
377 viscosity, shear margins which are characteristic of WAIS outlet glaciers, particularly Pine Island Glacier [71].
378 The sliding coefficient is set to $20 \text{ m a}^{-1} \text{ kPa}^{-1}$ everywhere. Surface accumulation varies linearly from 15 m a^{-1}
379 at the ice divide ($x = 0$ km) to 1 m a^{-1} at $x = 150$ km and is set to a constant value of 1 m a^{-1} between
380 $x = 150$ km and the ice front ($x = 300$) km. The resulting total surface accumulation, 67.5 Gt a^{-1} , closely
381 matches observations [72], while the spatial pattern respects reduced accumulation with reducing altitude.

382 WAVI Ice Sheet Model

383 Sea level rise contributions are determined from simulations using the Wavelet-based Adaptive-grid Vertically-
384 integrated Ice-sheet model (WAVI) [67, 73], a finite volume ice sheet model including a treatment of both
385 membrane and simplified vertical shear stresses [74]. WAVI uses a regular solution grid (here 1 km in both
386 directions), which is refined dynamically during the solution procedure to facilitate solution speed and accuracy.
387 The configuration contained herein is included in the WAVI documentation as an example ([https://rjarthern.
388 github.io/WAVI.jl/](https://rjarthern.github.io/WAVI.jl/)). WAVI assumes a fixed ice front position, which is set to $x = 300$ km (this is equivalent
389 to prescribing a calving law that the calving flux is equal to the normal ice velocity at the ice front).

390 Melt rate parameterisation

391 Melting in the ice sheet model is parameterized according to a quadratic temperature law [75],

$$\dot{m} = M\Gamma(T_a - T_f)^2. \quad (10)$$

392 Here, M is a dimensionless melt rate parameter, which can be thought of as a calibration coefficient to be
 393 freely varied [47], T_a is the ambient temperature far from the ice shelf base (see below), T_f is the local freezing
 394 temperature and $\Gamma = 0.56 \text{ m yr}^{-1} \text{ }^\circ\text{C}^{-2}$ plays the role of an exchange coefficient between temperature and
 395 melt rate. (Using the nomenclature of [47, 76], $\Gamma = \gamma_T[\rho_w c_p / (\rho_i L)]^2$, where γ_T is an exchange velocity, ρ_w
 396 is water density, ρ_i is the ice density, c_p is the specific heat capacity of water, L is the latent heat of fusion).
 397 The formulation (10) essentially encodes two mechanisms which strongly affect ice shelf basal melting: (1) ice
 398 shelf melting is governed by the turbulent heat flux from the ocean to the ice, which varies like the product
 399 of ocean temperature and velocity; (2) ocean velocity increases with the local thermal forcing ($T_a - T_f$) as
 400 meltwater is released, increasing the buoyancy forcing and thus circulation strength. This parameterisation has
 401 been used in numerous ice sheet modelling studies [see 41, and references therein], including the latest ISMIP
 402 assessments [76].

403 As is standard, we assume that the local freezing point depends linearly on pressure and salinity, $T_f =$
 404 $\lambda_1 S_a + \lambda_2 + \lambda_3 z_b$, where $\lambda_1 = -5.73 \times 10^{-2} \text{ }^\circ\text{C}$ is the liquidus salinity slope, $\lambda_2 = 8.32 \times 10^{-2} \text{ }^\circ\text{C}$ is the liquidus
 405 intercept, $\lambda_3 = 7.61 \times 10^{-4} \text{ }^\circ\text{C m}^{-1}$ is the liquidus depth slope, S_a the ambient salinity (see below), and z_b is
 406 the depth of the ice shelf base.

407 We take a layered structure for the ambient temperature and salinity (figure 2c-d), parameterized solely via
 408 the depth of the pycnocline centre, P_c (which is in general time-dependent), and the pycnocline half-width w :

$$T_a(z; P_c, w) = \begin{cases} 1.2 & z < P_c - w \\ 1.2 - 2.2 \frac{z - (P_c - w)}{2w} & P_c - w \leq z \leq P_c + w \\ -1 & z > P_c + w \end{cases} \quad (11)$$

$$S_a(z; P_c, w) = \begin{cases} 34.6 & z < P_c - w \\ 34.6 - 0.6 \frac{z - (P_c - w)}{2w} & P_c - w \leq z \leq P_c + w \\ 34.0 & z > P_c + w \end{cases} \quad (12)$$

410 The profiles (11) and (12) are piecewise linear functions of depth (figure 2b): they are constant in both an
 411 upper (temperature -1°C , salinity 34 PSU, corresponding to Winter Water) and lower layer (temperature
 412 1.2°C , salinity 34.6 PSU, corresponding to Circumpolar Deep Water), which are separated by a pycnocline
 413 of $2w$ m thickness, across which the temperature and salinity vary linearly. These piecewise linear profiles are
 414 approximations to typical conditions in the Amundsen Sea [26, 49]. Here, we take $w = 200$ m, corresponding to
 415 a pycnocline width of 400 m, which is consistent with observations. Time varying stochastic forcing is applied

416 by varying the pycnocline center (see ‘Stochastic Forcing’ below).

417 MITgcm Ocean Model

418 Ocean model melt rates used as calibration data are calculated by resolving the ice shelf cavity circulation using
419 the Massachusetts Institute of Technology General Circulation Model (MITgcm) [77]. The procedure applied to
420 determine ocean model melt rates at timeslices τ_1, \dots, τ_n under a given forcing $P_c(t)$ is as follows: (1) run the
421 ice sheet model (with parameterized melting) under this forcing profile; (2) use the output of this to determine
422 ice shelf geometries at timeslices $t = \tau_1, \dots, \tau_n$; (3) for each of these geometries, run the ocean model in this
423 geometry, with forcing applied via a restoring boundary condition corresponding to the profiles $P_c(\tau_k)$. The
424 restoring boundary condition is applied at the downstream end of the domain at $x = 360$ km (figure 2a), where
425 the temperature and salinity are restored to vertical profiles T_a and S_a over a distance of five horizontal grid
426 cells with a restoring timescale of 12 hours. An example of melt rates fields \dot{m}_{param}^k and $\dot{m}_{\text{ocean-model}}^k$ produced
427 by this procedure is shown in figure 6.

428 The ocean model grid has 55 layers with a vertical spacing of $dz = 20$ m, and a horizontal resolution
429 of $dx = 1$ km. We use the MITgcm in hydrostatic mode with an implicit nonlinear free surface scheme,
430 a third-order direct space-time flux limited advection scheme, and a non-linear equation of state [78]. The
431 Pacanowski-Philander [79] scheme parameterizes vertical mixing. Constant values of 15 and $2.5 \text{ m}^2 \text{ s}^{-1}$ are used
432 for the horizontal Laplacian viscosity and horizontal diffusivity, respectively. The equations are solved on an
433 f -plane with $f = -1.4 \times 10^{-4} \text{ s}^{-1}$. For each geometry, the MITgcm is run for three months, using a timestep
434 of 30 seconds, after which the configuration is in quasi-steady state. The ocean model melt rate is taken as
435 the melt rate after three months of the simulation. The drag coefficient in the three-equation formulation of
436 melting [80] used in the MITgcm is taken to be 9×10^{-3} ; this value ensures that the ocean model melt rate in
437 the post-initialization geometries (see ‘Ice Sheet Model Initialization’) closely matches observed total meltwater
438 flux values [e.g. 49] from Pine Island Glacier.

439 Ice Sheet Model Initialization

440 Following [46], we apply a two-stage initialization procedure, outlined in figure 7a. In the first initialization
441 stage, the ice geometry is timestepped from an initial configuration in which the ice-surface is 150 m above sea
442 level for 50 years (note that WAVI uses a hydrostatic flotation condition, so specifying the ice surface and bed
443 elevation prescribes the ice thickness everywhere). Following this, the ice is approximately in steady state, with
444 ice shelf geometry shown in figure 7c.

445 In the second stage of the initialization procedure, melting is turned on (figure 7). The ice geometry is then
446 timestepped from that at the end of the first initialization stage for fifty years using a constant ocean forcing
447 with $P_c = -500$ m. This pycnocline depth corresponds to typical conditions offshore of the WAIS (i.e. neither
448 warm nor cold) [48, 49]. In the following, we refer to warm forcing as constant forcing with $P_c = -400$ m,
449 corresponding approximately to the shallowest recorded pycnocline depth [48]. Similarly, we refer to cold

450 forcing as constant forcing with $P_c = -600$ m, corresponding approximately to the deepest recorded pycnocline
 451 depth [48]. The second initialization stage is performed independently for each value of M . The (M -dependent)
 452 state at the end of the second initialization stage (figure 7c) is then used as the initial condition in the following
 453 retreat simulations (figure 7).

454 Note that for a consistent estimate of sea level rise contributions from simulations with different values of
 455 M , we require similar initial conditions, chosen to be a grounding line at or near the seabed ridge crest. For
 456 $M \gtrsim 1.5$, the ice retreats irreversibly down the ridge during the second initialization stage. We therefore consider
 457 only M values smaller than this. In addition, we should impose that a constant warm forcing applied to the
 458 shelf should initiate retreat (WAIS retreat was, in practice, hypothesised to be initiated with forcing oscillating
 459 between warm and cold [11]); we found that for $M \lesssim 0.5$, no ice sheet retreat was initiated under warm forcing.
 460 Therefore, we restrict ourselves to the range $0.5 \leq M \leq 1.5$. Note that this restriction is consistent with our
 461 Bayesian framework: it is equivalent to setting the prior density to zero outside the range $0.5 \leq M \leq 1.5$, based
 462 on observational constraints.

463 During the second initialization stage, the ice shelf thins in response to applied melting, but the grounding
 464 line does not retreat (figure 7c). The mean melt rate after the second initialization stage is only weakly dependent
 465 on M (figure 7b). If the geometries at the end of the second initialization were identical for different values of
 466 M , the mean melt rate in the simulation with $M = 1.5$ would be 3 times as large as that with $M = 0.5$ (black
 467 dashed line in figure 7b); however, owing to temperature-depth effects, this value is only approximately 1.1 times
 468 (approximately 23.5 m year^{-1} in the $M = 1.5$ case versus approximately 21.3 m year^{-1} in the $M = 0.5$ case,
 469 see figure 7b). As the ice shelf thins in response to melting, it shallows, exposing it to colder ocean conditions,
 470 reducing melt rates sharply and restricting further thinning (the melt rate is proportional to $(T_a - T_f)^2$, which
 471 varies sharply with depth, particularly in the depth range occupied by the ice shelf in the second calibration
 472 phase, see figure 7d).

473 Stochastic Forcing

474 Following the two stage initialization in outlined above, stochastic forcing is applied via ambient ocean condi-
 475 tions:

$$P_c(t, \mathcal{F}) = p_{c,0} + T(\mathcal{F}) + A\mathcal{R}(t) \quad (13)$$

476 where $P_{c,0} = -500$ m is the pycnocline depth in the second stage of the initialization procedure, $T(\mathcal{F})$ is a forcing-
 477 scenario-dependent (i.e. anthropogenic or counterfactual) trend (see below), A is the amplitude of random
 478 forcing, and $\mathcal{R}(t)$ is a first-order autoregressive process, containing the stochastic part of the forcing. In the
 479 results shown here, we use $A = 100$ m, which agrees with observed internal variability in the Amundsen Sea [49].
 480 In a first-order autoregressive time-series, the following value is decomposed into a component proportional to
 481 the current entry, whose constant of proportionality describes the persistence timescale of the variability, and
 482 an additive white-noise term. We take the same autocorrelation function as [35], with yearly-to-interdecadal
 483 timescales represented.

484 Anthropogenic and counterfactual ensembles are distinguished via the trend $T(\mathcal{F})$: realizations of forcing
 485 from the counterfactual ensemble have no trend added to them, $T = 0$; realizations of forcing in the anthro-
 486 pogenic ensemble have a linear trend, $T = A_0(t/100 \text{ yrs})$, where $A_0 = 100 \text{ m}$ is the per-century shallowing trend
 487 of the pycnocline (figure 2g).

488 **Bootstrapping distributions of sea level rise**

489 Each of the n realizations of forcing yields a parametrically-calibrated distribution of sea level rise for each
 490 time in the simulation. Thus, for any time and any sea level rise, we have n values of the distributions from
 491 both anthropogenic and counterfactual ensembles (supplementary figure 9). An uncertainty estimate in the
 492 anthropogenic enhancement ratio is constructed by bootstrapping these values – resampling from these n values
 493 with replacement (here, we sample 1000 times); the resulting set yields a standard deviation $\lambda = \lambda(SLR, t)$
 494 for both anthropogenic and counterfactual ensembles (supplementary figure 9). Using subscripts to denote the
 495 ensemble (that is, counterfactual or anthropogenic), the upper bound shown in figure 4b–d is then computed as

$$AER_{\text{upper}} = \frac{\ell_{\text{anthro}} + \lambda_{\text{anthro}}}{\ell_{\text{counter}} - \lambda_{\text{counter}}} \quad (14)$$

496 where $\ell = \ell(SLR, t)$ is the probability density. Similarly, the lower bound is computed as

$$AER_{\text{lower}} = \frac{\ell_{\text{anthro}} - \lambda_{\text{anthro}}}{\ell_{\text{counter}} + \lambda_{\text{counter}}}. \quad (15)$$

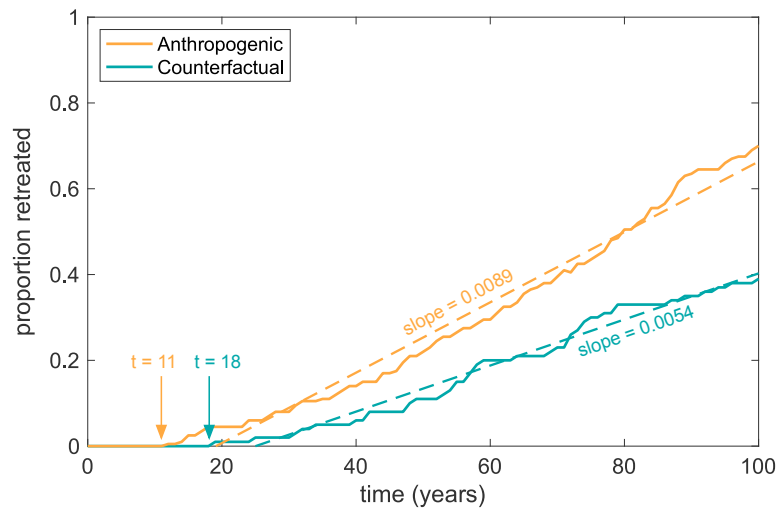


Fig. 5: Time evolution of retreats. Time evolution of the number of retreats (defined as a sea level rise contribution greater than 0.2 mm) for all simulations from the anthropogenic ensemble (yellow) and counterfactual (green). Arrows indicate the time at which the first retreat is initiated.

497 **Supplementary Figures**

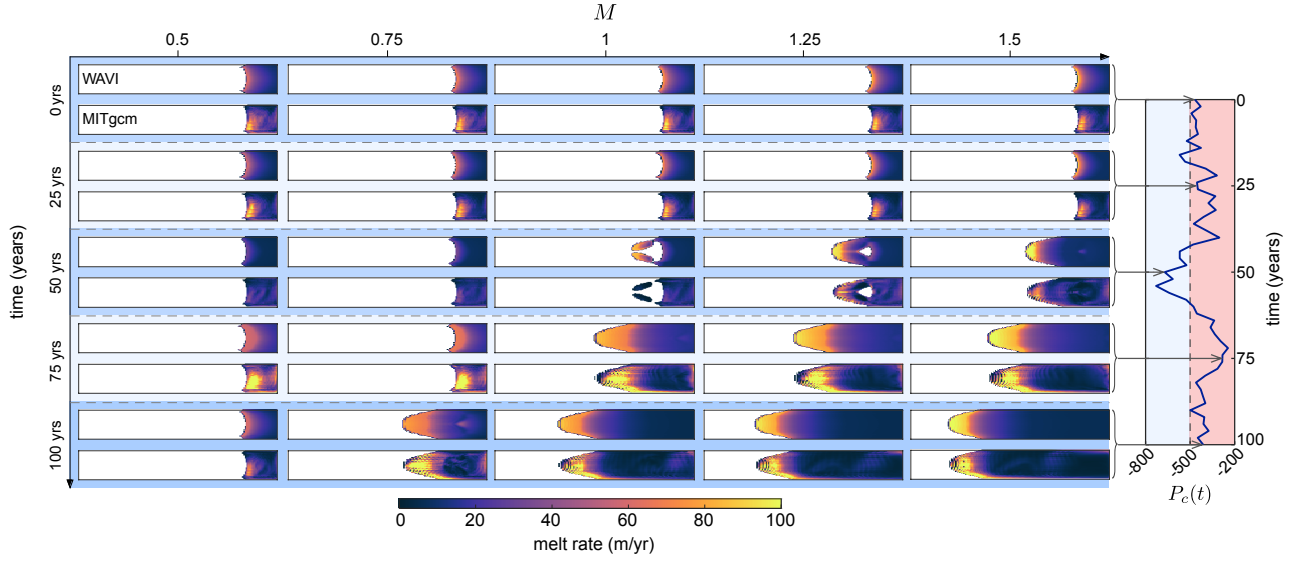


Fig. 6: Calibrated retreat of ice sheets under stochastic forcing. Ice shelf melt rates (colors) computed using parameterized melting in the WAVI ice sheet model (top of each sub-panel) and the MITgcm ocean model (bottom of each panel). Data are shown for different calibration timeslices (rows) and different melt rate parameter values M (columns). Note that the x - and y -axes are the same in each, and zoomed in on the ice shelf ($100 \text{ km} < x < 300 \text{ km}$, $-25 \text{ km} < y < 25 \text{ km}$). The side-panel indicates the realization of forcing corresponding to the main panel, showing pycnocline depth (abscissa) as a function of time (ordinate). Red (blue, respectively) indicates where the pycnocline is shallower (deeper) than its initial position, $P_c(0) = -500 \text{ m}$.

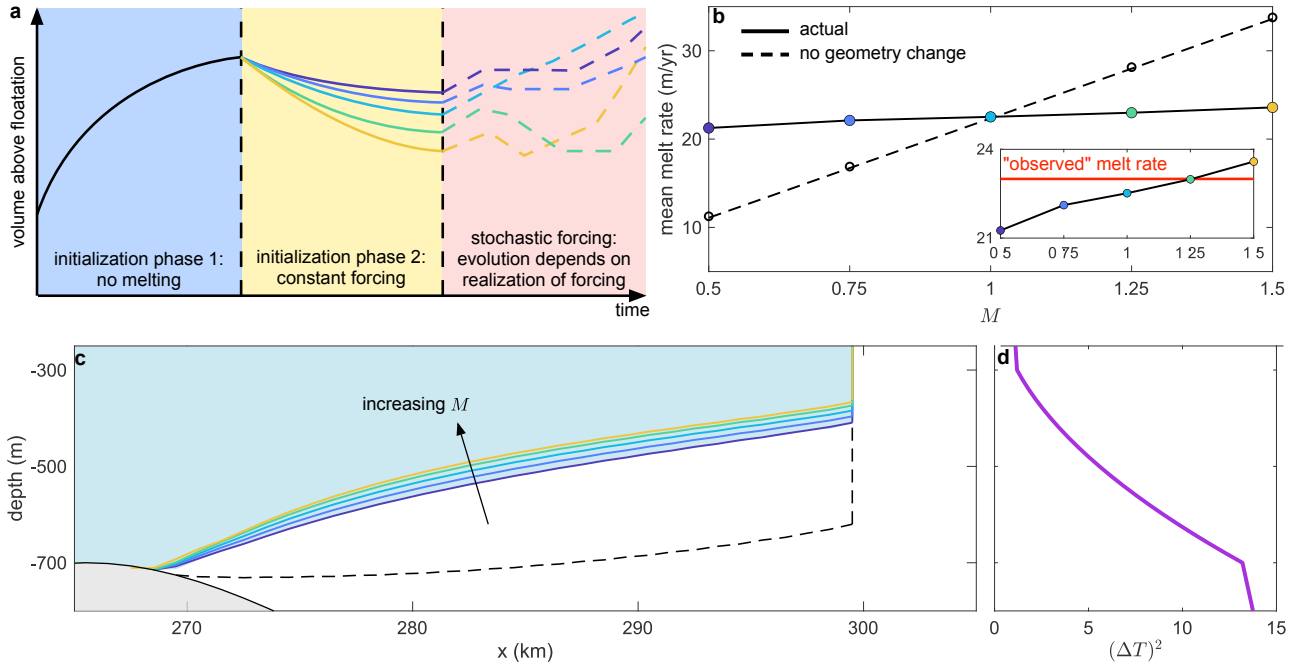


Fig. 7: Two stage initialization procedure. (a) Schematic diagram of the initialization procedure, described in ‘Ice Sheet Model Initialization’. Colors in the second calibration phase correspond to different values of M , as indicated by points in (b). (b) Mean melt rate after the second calibration phase as a function of M (solid line). The dashed line indicates what the mean melt rate would be if the same geometry (that of the $M = 1$ case) were used for each value of M . Inset: as in main panel with a zoomed ordinate axis. The red line is the target calibration value of 23 m year^{-1} , which acts as an artificial observation. (c) Ice shelf geometry after the first (black) and second (colors, according to colors in (b)) initialization stages. (d) Squared thermal forcing $(\Delta T)^2 = (T_a - T_f)^2$ as a function of depth (note that (c) and (d) share an ordinate axis).

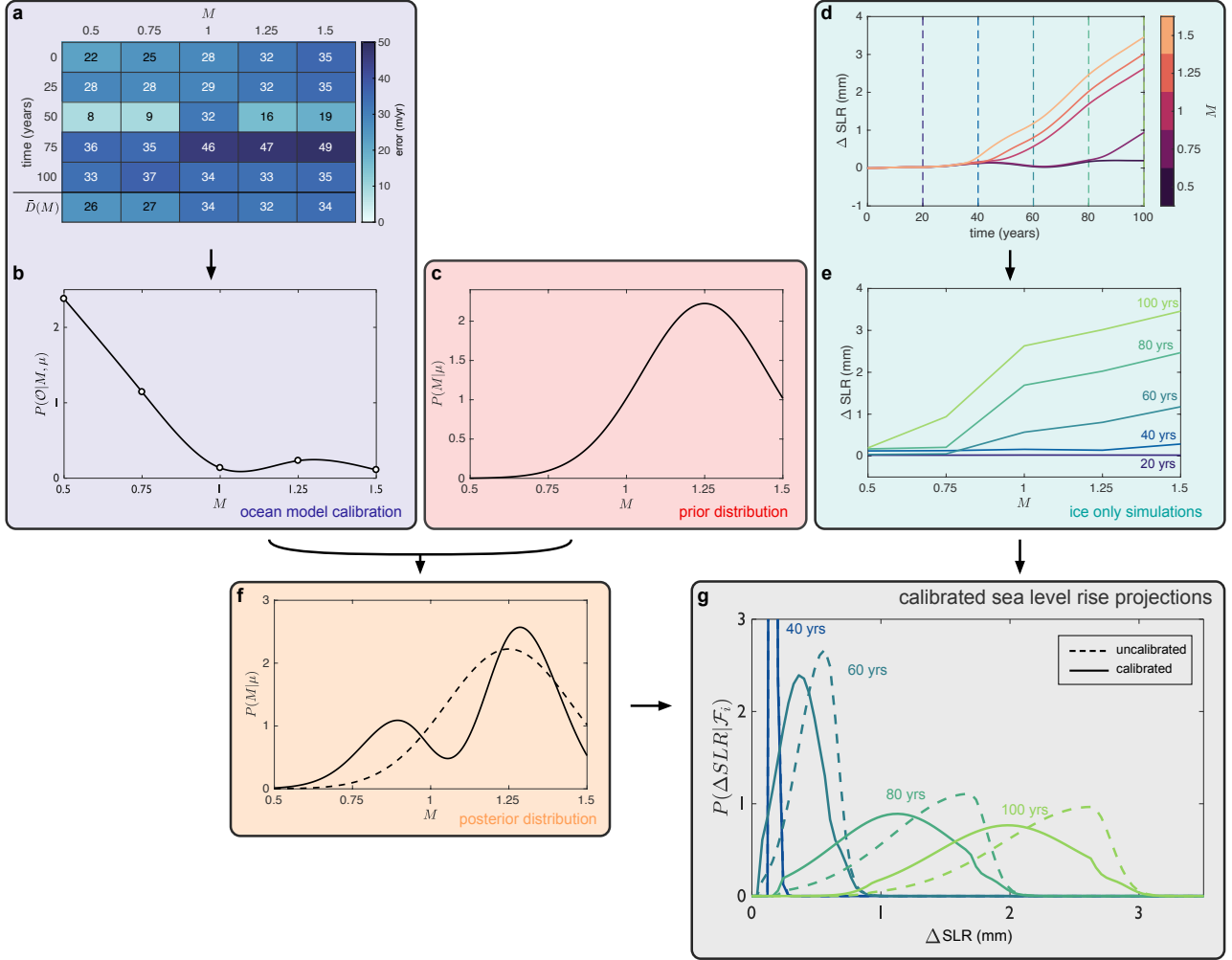


Fig. 8: Producing parametrically calibrated distributions for a given realization of forcing. (a) Likelihood values at each calibration timeslice (rows) as a function of M , for the realization of forcing shown in figure 2e and supplementary figure 6. Dark (light, respectively) colors indicate high (low) errors in melting. The final row indicates the discrepancy D as a function of M , computed as the mean over calibration timeslices. (b) Likelihood function $P(\mathcal{O}|M, \mu)$ (given by equation (6)), describing how the prior distribution is updated to account for information introduced by the ocean model. Here, $\sigma_L = 10 \text{ m year}^{-1}$. (c) Prior distribution, given by equation (3), representing the state of knowledge of parameters M prior to calibration. Here, $\sigma_P = 0.2$. (d) Sea level rise as a function of time for different values of M (indicated by colors), for the realization of forcing shown in figure 2e. (e) Sea level rise at fixed times (indicated by colors, corresponding to dashed vertical lines in (d)) as a function of M . (f) Posterior distribution of M (solid black line), obtain by combining the prior and likelihood according to (2). The dashed black line shows the posterior distribution for M for reference. (g) Combining the posterior distribution with sea level rise data yields calibrated probability distributions, for the forcing profile shown in figure 2e. Data are shown for different times, as labelled.

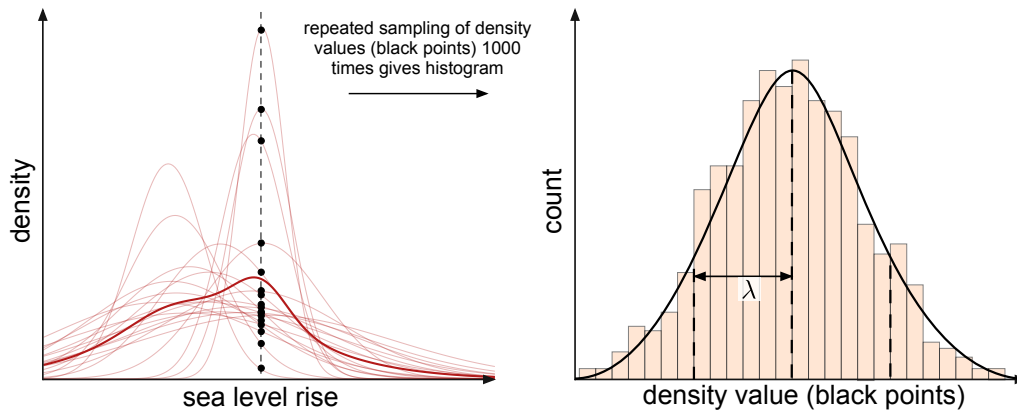


Fig. 9: Schematic diagram of the bootstrapping procedure. (left) For any given time, we obtain a unique distribution of sea level rise for each realization of forcing (faint lines), whose ensemble mean (solid line) is the central distribution after accounting for aleatory uncertainty. For a given sea level rise value, an estimate of the variance λ is determined by sampling the values of the individual PDFs 1000 times and taking the standard deviation of the resulting distribution (right).

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