

# Fiber-optic observations of internal waves and tides

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# Fiber-optic observations of internal waves and tides

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## Key Points:

- Distributed acoustic sensing on seafloor cables can resolve temperature changes associated with internal wave and boundary layer dynamics.
- We show temperature transients from solitons in the Strait of Gibraltar and bore-like propagation of the internal tide at Gran Canaria.
- We also recover a signal proportional to barotropic tidal pressure including the fortnightly variation.

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## 38 **Abstract**

39 Although typically used to measure dynamic strain from seismic and acoustic waves,  
40 Rayleigh-based distributed acoustic sensing (DAS) is also sensitive to temperature, of-  
41 fering longer range and higher sensitivity to small temperature perturbations than con-  
42 ventional Raman-based distributed temperature sensing. Here, we demonstrate that ocean-  
43 bottom DAS can be employed to study internal wave and tide dynamics in the bottom  
44 boundary layer, a region of enhanced ocean mixing but scarce observations. First, we  
45 show temperature transients up to about 4 K from a power cable in the Strait of Gibralt-  
46 ar south of Spain, associated with passing groups of internal solitary waves in water depth  
47  $< 200$  m. Second, we show the bore-like propagation of the nonlinear internal tide on the  
48 near-critical slope of the island of Gran Canaria, off the coast of west Africa, with per-  
49 turbations up to about 2 K at 1-km depth and 0.2 K at 2.5-km depth. With spatial av-  
50 eraging, we also recover a signal proportional to the barotropic tidal pressure, includ-  
51 ing the lunar fortnightly variation. In addition to applications in observational physi-  
52 cal oceanography, our results suggest that contemporary chirped-pulse DAS possesses  
53 sufficient long-period sensitivity for seafloor geodesy and tsunami monitoring if ocean  
54 temperature variations can be separated.

## 55 **Plain Language Summary**

56 Distributed acoustic sensing, or DAS, measures changes in the propagation time  
57 of light along finite segments of an optical fiber, which can be caused by both elastic de-  
58 formations and temperature variations. We present two case studies of long-period tem-  
59 perature signals recorded with DAS on submarine cables offshore southern Spain and  
60 in the Canary Islands. These temperature signals are associated with internal waves, grav-  
61 ity waves that propagate on the ocean's density stratification. We also recover a signal  
62 matching the tidal pressure, which likely represents elastic strain, suggesting potential  
63 value of ocean-bottom DAS for seafloor geodesy and tsunami monitoring.

## 64 **1 Introduction**

65 Internal gravity waves generated by tides, currents, and atmospheric forcing me-  
66 diate the intensity of ocean mixing, with broad implications for circulation, climate, and  
67 biogeochemistry. Early work by Munk (1966), Garrett and Munk (1972), and others pro-

68 posed that mixing is primarily accomplished through nonlinear interactions and break-  
69 ing of topographically generated internal waves distributed throughout the ocean inte-  
70 rior. However, over the past three decades, observational campaigns have found that the  
71 most vigorous mixing occurs near the bottom at sloping boundaries and in regions of rough  
72 bathymetry, and that rates of turbulent dissipation vary by at least two orders of mag-  
73 nitude (e.g., Toole et al. (1994); Polzin et al. (1997); Ledwell et al. (2000); Moum et al.  
74 (2002); Rudnick et al. (2003); Kunze et al. (2012); Waterhouse et al. (2014)). Yet, ob-  
75 servations of internal wave-driven ocean mixing remain exceedingly sparse, especially in  
76 the bottom boundary layer. Moored and towed thermistor arrays, current meters, and  
77 microstructure profilers can provide high-resolution, local estimates of diapycnal diffu-  
78 sivity and turbulent dissipation rates (e.g. Toole et al. (1994); van Haren (2006)). Global  
79 budgets of internal wave generation and dissipation can be constructed by compiling many  
80 such in-situ measurements (Waterhouse et al., 2014; Kunze, 2017) or through satellite  
81 altimetry (Egbert & Ray, 2000, 2001). Reconciling internal wave and boundary layer dy-  
82 namics across the vast gulf in scales from astronomical forcing to turbulent dissipation  
83 and understanding the physical processes governing the generation and distribution of  
84 turbulence are outstanding theoretical and observational challenges, especially for the  
85 parameterization of mixing in ocean circulation models.

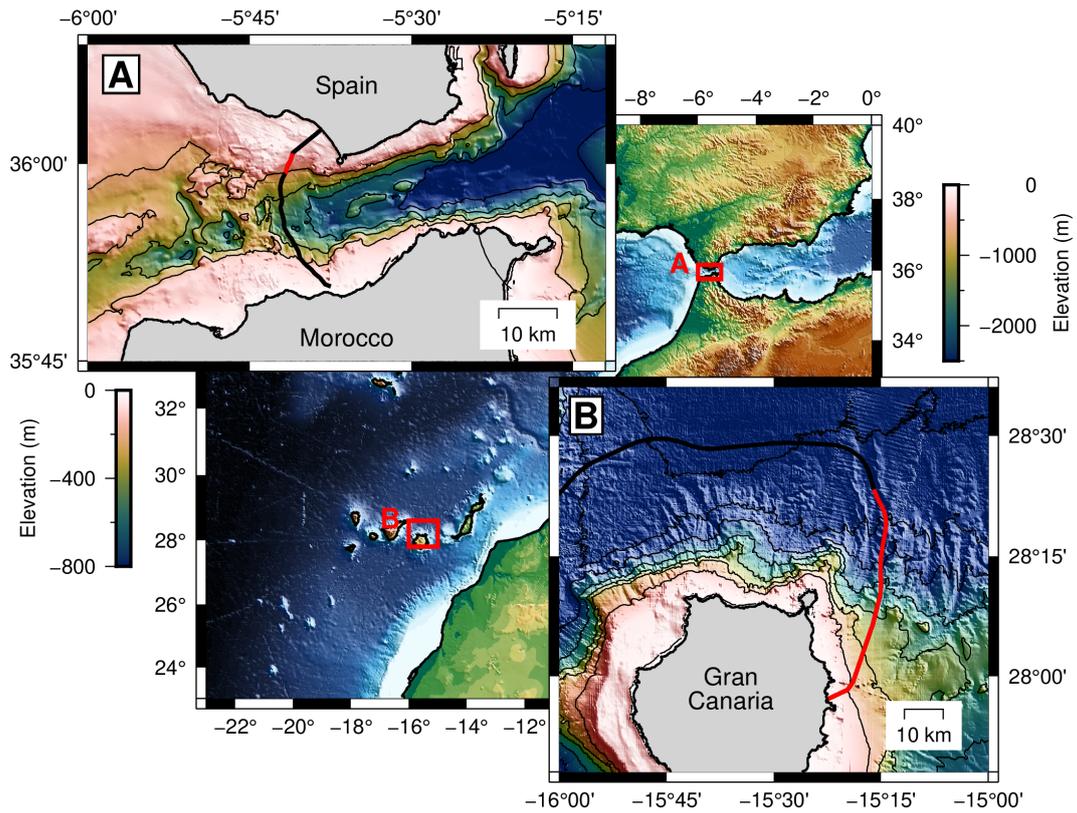
86 Distributed fiber-optic sensing offers a promising new approach to observe inter-  
87 nal wave dynamics at the seafloor by converting a fiber-optic cable into a dense array  
88 of high-resolution temperature sensors. Recently, Connolly and Kirincich (2019), Davis  
89 et al. (2020), and others have demonstrated the value of distributed temperature sens-  
90 ing (DTS) for studying shoaling internal waves. Most DTS systems use the intensity of  
91 Raman scattering from a repeated laser pulse to estimate temperature along a fiber and  
92 are insensitive to other variables like fiber strain. With proper calibration (e.g. Sinnett  
93 et al. (2020)), DTS offers absolute temperature measurements with a sensitivity of about  
94 0.01 K and sub-meter sampling up to a range of 10–30 km (Li & Zhang, 2022). How-  
95 ever, DTS suffers from a trade-off between distance and sensitivity, which limits its ap-  
96 plication to shallow water environments insomuch as the DTS laser interrogator must  
97 remain onshore. Further, DTS is best suited for multi-mode fiber, which means that pre-  
98 existing ocean-bottom telecommunication “dark” fiber cannot be easily repurposed as  
99 temperature sensing arrays because it is mostly single-mode. Another fiber-optic sens-  
100 ing technology, distributed acoustic sensing (DAS) uses the phase of Rayleigh-scattered

101 laser light to estimate changes in the optical path length, which can be caused by both  
 102 temperature and elastic deformation with an equivalence of  $1\text{ K} \approx 10\ \mu\epsilon$  (where  $1\mu\epsilon =$   
 103  $10^{-6}\text{ m/m}$ ) (Fernandez-Ruiz et al., 2020; Lindsey & Martin, 2021). At short periods ( $<50$ -  
 104  $100\text{ s}$ ) or in shallow water ( $<100$ - $200\text{ m}$ ), mechanical strain from ocean surface gravity,  
 105 acoustic, and seismic waves always dominates over temperature effects, permitting di-  
 106 verse applications of ocean-bottom DAS from earthquake detection and structural char-  
 107 acterization of the seafloor (Sladen et al., 2019; Cheng et al., 2021; Williams et al., 2021)  
 108 to monitoring sea state and tracking coastal currents (Lindsey et al., 2019; Williams et  
 109 al., 2019, 2022). However, at long periods or in deep water, temperature transients as-  
 110 sociated with internal waves and tides may rise to the fore. Ide et al. (2021) first reported  
 111 complex temperature signals at tidal periods in ocean-bottom DAS measurements off-  
 112 shore Cape Muroto in southern Japan. With a field sensitivity of about  $0.001$ – $0.01\mu\epsilon =$   
 113  $0.1$ – $1\text{ mK}$ , DAS is actually more sensitive to small temperature signals than DTS and  
 114 can operate up to  $100\text{ km}$  without significant reduction in sensitivity, permitting oceano-  
 115 graphic investigations at abyssal depths where temperature anomalies are small. How-  
 116 ever, DAS faces several challenges of its own: temperature and mechanical strain effects  
 117 cannot be definitively separated in a single measurement, temperature calibrations for  
 118 DAS have not yet been standardized, and the instrumental noise increases with period  
 119 on most DAS systems.

120 Here, we present two novel observations of internal wave dynamics from ocean-bottom  
 121 DAS arrays. In Section 3, we show temperature perturbations up to about  $4\text{ K}$  associ-  
 122 ated with internal solitary waves crossing a power-cable in the Strait of Gibraltar, south  
 123 of Spain. In Section 4, we show temperature perturbations up to about  $2\text{ K}$  associated  
 124 with nonlinear, bore-like propagation of the internal tide on the near-critical slope of Gran  
 125 Canaria, in the Canary Islands offshore west Africa. Throughout, we assume that these  
 126 long-period signals solely represent temperature, an assumption which we then discuss  
 127 and justify in Section 5.

## 128 **2 Data**

129 We analyze and compare observations from two DAS datasets acquired on seafloor  
 130 cables containing optical fibers. The first was recorded in October 2019 on a  $30$ -km power  
 131 cable running from Spain to Morocco across the Strait of Gibraltar, with depths up to  
 132 about  $550\text{ m}$  (Figure 1A). The cable is generally buried on the Spanish shelf, and emerges



**Figure 1.** Map of cable locations. (A) Power cable from Spain to Morocco across the Strait of Gibraltar (black) with section shown in Figure 2 in red; 200-m bathymetry contours (B) Telecommunications cable from Gran Canaria to Tenerife (black) with section shown in Figure 3 in red; 1000-m bathymetry contours.

133 at the seafloor at 8.6 km optical distance. The second was recorded in August and Septem-  
134 ber 2020 on a 176-km telecommunication cable connecting Gran Canaria to Tenerife in  
135 the Canary Islands, with depths up to about 4 km (Figure 1B). The cable is entirely un-  
136 buried beyond the surf zone. Fibers in both cables were interrogated with a chirped-pulse  
137 DAS system built by Aragon Photonics and operated by the University of Alcalá (Pastor-  
138 Graells et al., 2016; Fernandez-Ruiz et al., 2018, 2019), using a 10-m gauge length and  
139 10-m channel spacing. The raw DAS data were first decimated from 1 kHz to 1 Hz by  
140 averaging. A five-point median filter was applied to the 1-Hz data to prevent instrumen-  
141 tal noise like spikes and steps from biasing long period results, and then the data were  
142 further decimated to 100 s sampling period. For more information, see Williams et al.  
143 (2022) and Ugalde et al. (2022).

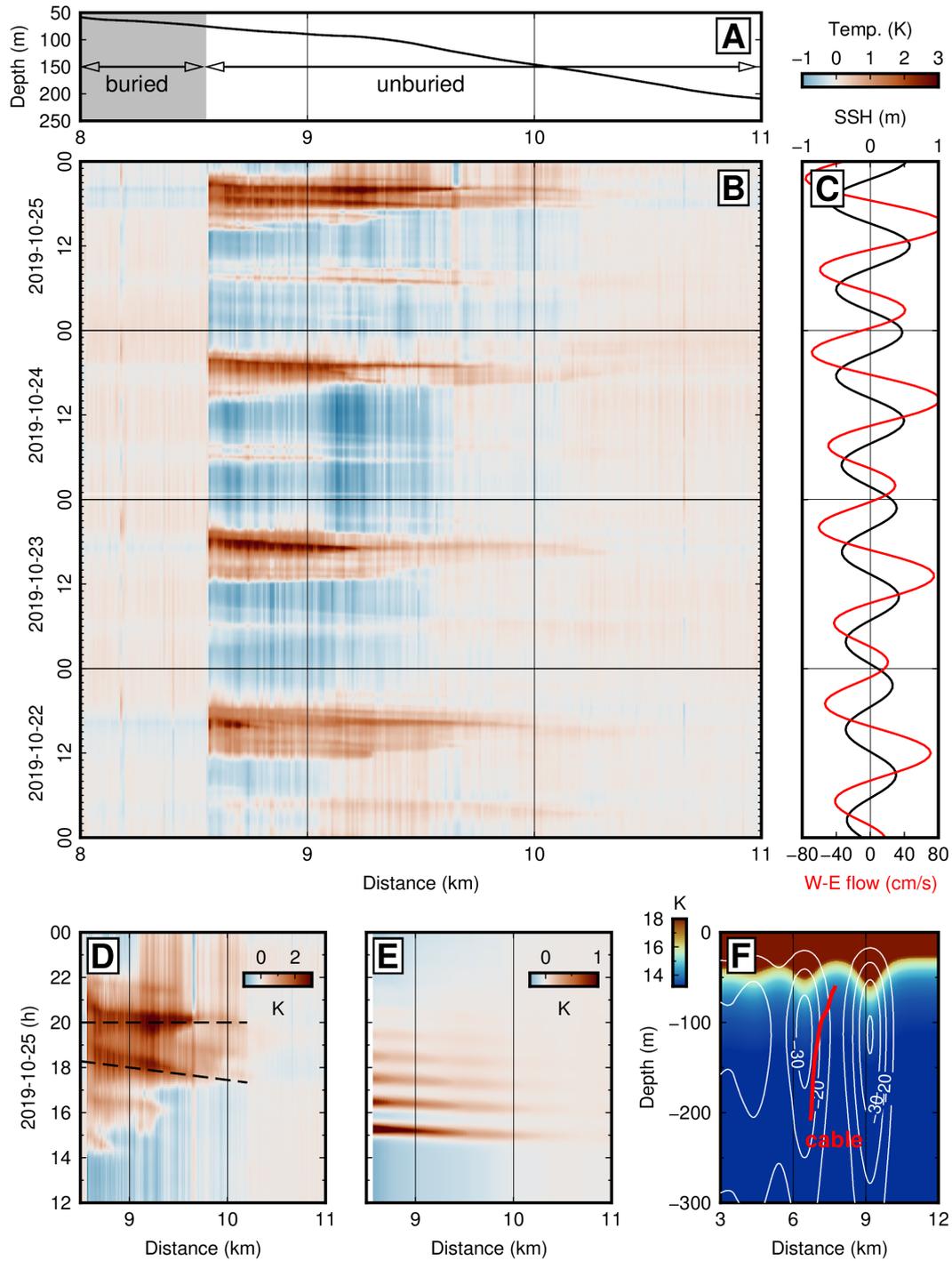
### 144 **3 Internal solitary waves in the Strait of Gibraltar**

#### 145 **3.1 Observations**

146 Four days from the Strait of Gibraltar DAS dataset are plotted in Figure 2. Across  
147 the buried section of the cable, there is no evident temperature signal at any period. Emerg-  
148 ing abruptly at 8.6 km where the cable is exposed at the seafloor, a nearly constant back-  
149 ground temperature is periodically broken by positive excursions up to 4 K, indicative  
150 of internal waves of depression. Each internal wave group lasts 2-8 h and is composed  
151 of 2–6 subsidiary solitary waves, each with a period of 1–2 h (Figure 2B,D). These ex-  
152 cursions occur twice daily immediately following the maximum eastward tidal flow and  
153 exhibit an oscillation in amplitude which correlates with the daily inequality of the di-  
154 urnal and semidiurnal tides as expressed in the TPXO9 shallow-water solution for the  
155 local barotropic current (Figure 2C) (Egbert & Erofeeva, 2002). The amplitude is strongest  
156 where the cable emerges at 8.6 km distance (75 m depth) and decays monotonically with  
157 distance, disappearing before the 11-km mark (200 m depth).

#### 158 **3.2 Interpretation**

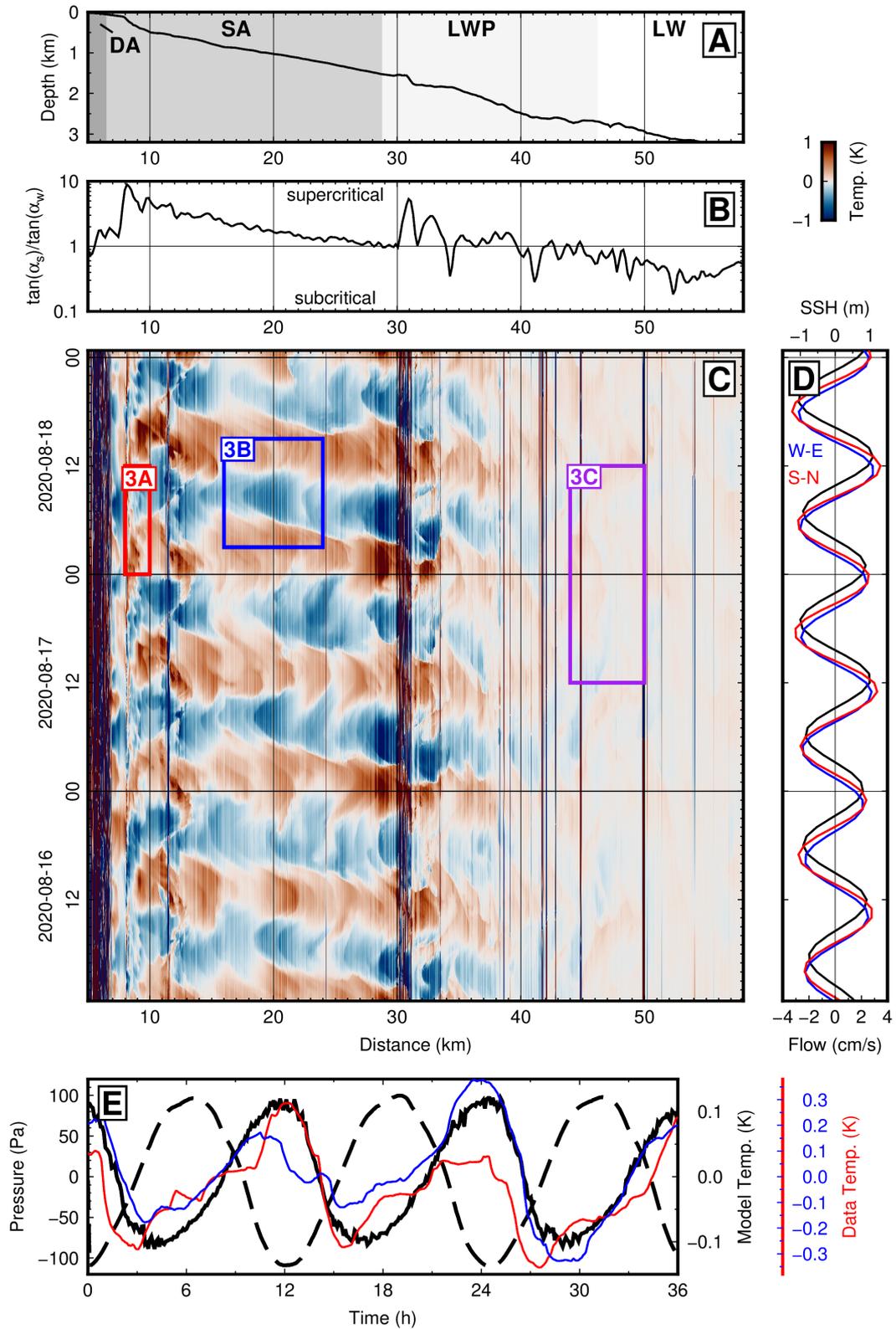
159 Hydrodynamics in the Strait of Gibraltar are characterized by a two-layer exchange  
160 flow between salty Mediterranean water at the bottom and less-salty Atlantic water at  
161 the surface, with a strong pycnocline typically measured at 50-100 m depth near the ca-  
162 ble location east of the Camarinal Sill. Modulation of the exchange by tidal currents re-



**Figure 2.** Internal solitary wave groups on the Gibraltar cable. (A) Cable bathymetry profile with shading to indicate burial. (B) DAS data from 2019-10-22 to 2019-10-25 for the 8–11-km cable section. (C) Tidal predictions for sea surface height (SSH, black) and meridional flow (red) from TPXO. (D) Zoom-in to panel B showing a group of internal solitons, with dashed black lines schematically indicating the difference in moveout (apparent speed) between individual solitons. (E) Synthetic data generated using the “dnoidal” model of Apel (2003) for the 8–11-km cable with a source at the north end of Camarinal Sill on the Spanish shelf. (F) Cross-section of the model after Apel (2003) at  $T = 4$  h with absolute temperature, contours of constant isopycnal displacement (white lines), and depth vs. distance from source for the 8–11-km cable segment (red).

163 sults in partial blocking of the Mediterranean outflow over the Camarinal Sill and the  
164 generation of internal solitary waves, which propagate eastward into the Alboran Sea and  
165 have been widely observed by moorings and in synthetic aperture radar (SAR) imagery  
166 (Brandt et al., 1996; Vazquez et al., 2008; Ziegenbein, 1969, 1970; Watson & Robnson,  
167 1990). Although no clear SAR images of internal waves were acquired during the four-  
168 day data window, the Sentinel-1A satellite captured an internal wave group propagat-  
169 ing past Gibraltar at 2019-10-26 06:27:44 UTC, shortly after the end of DAS acquisition  
170 (Figure S1A). This likely corresponds to the wave group shown in Figure 2D and con-  
171 firms that this well-studied phenomenon occurred during our experiment.

172 In order to understand the relationship between internal wave parameters and the  
173 temperature signals recorded in DAS data, we compare our observations with synthetic  
174 data generated from the “dnoidal” model of Apel (2003) (Figure 2E,F), which combines  
175 an analytical solution of the Korteweg-de Vries equation for weakly-nonlinear solitary  
176 wave propagation with a vertical structure function obtained by numerical solution of  
177 the Taylor-Goldstein equation (see Text S1). While the observed inter-soliton period and  
178 group shape are poorly reproduced by this simplistic model, the synthetic data match  
179 the amplitude of the temperature anomaly within a factor of two and mimic its quasi-  
180 triangular shape with depth and distance (Figure 2D,E). The DAS temperature obser-  
181 vations can consequently be understood as an oblique cross-sectional slice of the inter-  
182 nal wave group along the cable trajectory, where the shape is governed by a combina-  
183 tion of the isotherm displacement with the thermal stratification, and the moveout is de-  
184 termined by the source azimuth and propagation speed (Figure 2F). Though the move-  
185 out along the cable varies slightly from one solitary wave to the next, suggesting a com-  
186 plex source distribution (see dashed lines in Figure 2D), the apparent speed of propa-  
187 gation along the cable direction is almost instantaneous, which requires broad-side in-  
188 cidence of the internal wave group and a source at the northern end of the Camarinal  
189 Sill or on the Spanish shelf (Figure S2). The ESE-ward propagation perpendicular to  
190 the cable azimuth that would result from a dominant source at the northern end of the  
191 Camarinal Sill is supported by SAR imagery (Figure S1B, see also Brandt et al. (1996)  
192 Figure 16B). However, given trade-offs between speed, source time, and source location  
193 as well as refraction across the steep bathymetry, it is impossible to uniquely identify the  
194 source without more elaborate modeling.



**Figure 3.** Nonlinear internal tide on the slope of Gran Canaria. (A) Cable bathymetry profile with shading to indicate cable type: double armored (DA), single armored (SA), light-weight protected (LWP), and light-weight (LW). (B) Slope criticality along the cable profile, defined as the ratio of the absolute slope angle to the angle of internal wave energy propagation. (C) DAS data from 2020-08-16 to 2020-08-18 for the 5–58 km cable section. (D) Tidal predictions for sea surface height (black), meridional flow (blue), and zonal flow (red) from TPXO. (E) Comparison of DAS observations at 22 km (red) and 28 km (blue) with modeled temperature (black solid) and pressure (black dashed) perturbations.

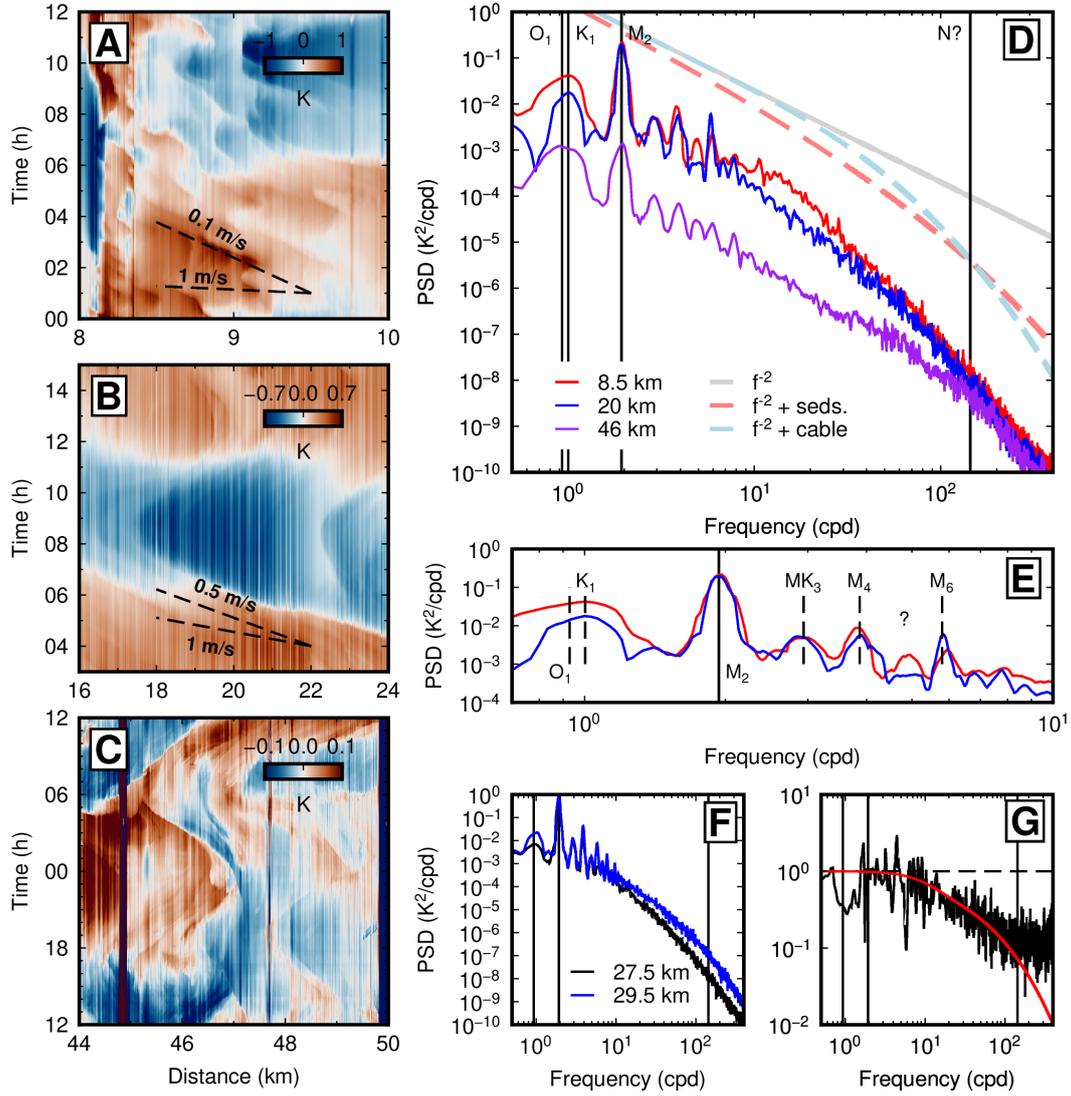
## 195 4 Nonlinear internal tides at Gran Canaria

### 196 4.1 Observations

197 Three days from the Gran Canaria DAS dataset are plotted in Figure 3, showing  
 198 semidiurnal temperature oscillations up to 2 K in amplitude which persist along the en-  
 199 tire slope spanning a depth range  $>3$  km. The observations can generally be divided into  
 200 three domains. On the main slope of Gran Canaria (12–30 km distance, 500–1500 m depth)  
 201 three to five sharp cold fronts form every 12 hrs (Figure 3C, 4B; Movie S1). Here, the  
 202 slope is slightly supercritical, with  $1 \leq \gamma \leq 3$ , where  $\gamma = \tan(\alpha_s)/\tan(\alpha_w)$  is the ra-  
 203 tio of the bathymetric slope angle ( $\alpha_s$ ) to the angle of internal wave energy propagation  
 204 ( $\alpha_w$ , Figure 3B). As these fronts form and accelerate up to an apparent velocity of 0.5  
 205 m/s along the cable, they intensify to a contrast in excess of 1 K over a distance of only  
 206 a few hundred meters. Then, as the tidal flow reverses direction, the cold fronts slow,  
 207 dissipate, and reform into a series of weaker warm fronts that recede down the slope. In  
 208 shallow water (7–12 km distance,  $<500$  m depth,  $\gamma > 3$ ), the shoaling cold fronts slow  
 209 to an apparent velocity of 0.1 m/s and divide into 5–10 weaker fronts across each semid-  
 210 urnal cycle (Figure 4A). Beyond a sharp ridge at 30-km distance, the seafloor fabric is  
 211 much rougher and the flow pattern more complex, but sharp temperature fronts up to  
 212 about 0.2 K still persist and are advected horizontally by the tidal current (Figure 4C).

### 213 4.2 Interpretation

214 Steep submarine topography acts as both a source for the conversion of barotropic  
 215 tidal motions into internal waves and a sink where the internal tide reflects and breaks,  
 216 thus mediating the cascade of energy in the ocean from large to small scales where mix-  
 217 ing occurs (Klymak et al., 2011; St. Laurent & Garrett, 2002; Rudnick et al., 2003). High-  
 218 resolution thermistor observations and modeling of steep, near-critical slopes have shown  
 219 that the generation and shoaling of the internal tide drives the formation and propaga-  
 220 tion of bore-like fronts in the bottom boundary layer (van Haren, 2006; Winters, 2015)  
 221 associated with intensified turbulent mixing and shear instability (van Haren & Gosti-  
 222 aux, 2012; van Haren et al., 2015; van Haren & Gostiaux, 2010). These observations are  
 223 broadly consistent with the temperature oscillations in DAS data from Gran Canaria,  
 224 including frontal velocities in the range 0.1–0.5 m/s and temperature perturbations up  
 225 to 3 K at 500-m depth (van Haren & Gostiaux, 2012), 2 K at 1400-m depth (van Haren,



**Figure 4.** (A) Zoom-in to the 8–10-km cable segment of the Gran Canaria dataset showing many small cold fronts shoaling on the shallow shelf. (B) Zoom-in to the 16–24-km cable segment showing a sharp cold front propagating up slope, slowing around 18-km, and reversing or breaking. (C) Zoom-in to the 44–50-km cable segment showing complex, sharp temperature fronts oscillating at tidal periods. (D) Thirty-day power spectral density (PSD) for a representative channel from each panel of A,B,C, compared with a reference slope of  $f^{-2}$  and dashed lines illustrating the effect of burial (light red) or cable thickness (light blue) on the frequency-dependent temperature response. (E) Zoom-in to D showing the ordinary tidal harmonics ( $O_1$ ,  $K_1$ ,  $M_2$ ) and nonlinear overtones ( $MK_3$ ,  $M_4$ ,  $M_6$ ) present at all water depths. (F) Spectra for two channels on either side of the single-armored to light-weight protected cable transition, showing a frequency-dependent difference in response. (G) Transfer function between the two channels in F (black line) and simple thermal model based on the actual difference in cable diameter (red line).

226 2006), and 0.2 K at 2500-m depth. (van Haren et al., 2015). The observed pattern of the  
 227 shoaling, weakening, and reversal of bore-like fronts is similar to signals observed in very  
 228 shallow water with DTS at Dongsha Atoll, which Davis et al. (2020) termed “relaxation.”

229 We compare the DAS observations to an idealized simulation of near-boundary flow  
 230 driven by reflection of a fundamental mode  $M_2$  internal tide across a slightly supercrit-  
 231 ical sloping bottom, performed using **flow\_solve** (Winters & de la Fuente, 2012) and scaled  
 232 to approximate the conditions at Gran Canaria (see Text S2, Figures S3, S4). Figure 3E  
 233 plots example DAS records from individual channels at 22 and 28 km distance against  
 234 differential temperature from a near-bottom point in the simulation, showing a consis-  
 235 tent pattern over each tidal cycle of a gradual rise in temperature followed by a sharp  
 236 drop, marking the passage of an up-slope propagating front. Notably, this asymmetry  
 237 is not evident in the modeled pressure, which is dominated by vertical displacements of  
 238 the large-scale, linear internal tide throughout the overlying water column and nearly  
 239 independent of the near-bottom flow. The modeled temperature perturbations of 0.2–  
 240 0.3 K are of slightly smaller amplitude than the 0.4–1 K perturbations observed with DAS,  
 241 which is a reasonable level of agreement considering the idealized simulation was con-  
 242 ducted with uniform stratification and only one internal tide mode. The modeled max-  
 243 imum frontal velocity is 0.65 m/s, consistent with the observed 0.5 m/s (Figure S4).

244 The temperature spectra of individual DAS channels exhibit dominant peaks at  
 245 semidiurnal ( $M_2$ ) and diurnal ( $O_1$ ,  $K_1$ ) frequencies (Figure 4D,E). At the latitude of Gran  
 246 Canaria, the inertial frequency is very close to  $O_1$ , so the prominence of the diurnal peak  
 247 could relate to both forcing of the diurnal tide and the presence of near-inertial waves.  
 248 Also evident are several tidal overtones ( $MK_3$ ,  $M_4$ , etc.), which persist in relative am-  
 249 plitude across the full range of observations, indicating nonlinear interactions on the slope  
 250 associated with local conversion of the barotropic tide or steepening of the internal tide  
 251 (van Haren et al., 2002). For the deepest cable segment beyond 40-km distance, the spec-  
 252 trum approximately scales as  $f^{-2}$  (Figure 4D), similar to the canonical Garrett-Munk  
 253 spectrum for internal waves in the ocean interior, away from generation sites (Garrett  
 254 & Munk, 1972). For the 7–30-km cable segment, the spectrum is flatter from about 1  
 255 to 10 cpd, indicative of stronger nonlinearity, approximately scaling as  $f^{-1}$ . At higher  
 256 frequencies, the spectrum steepens beyond  $f^{-3}$ , which may reflect diminished temper-  
 257 ature sensitivity due to the finite thickness of the cable construction or even a few mil-  
 258 limeters of sediment drape (Figure 4D, S5). Comparing adjacent cable segments across

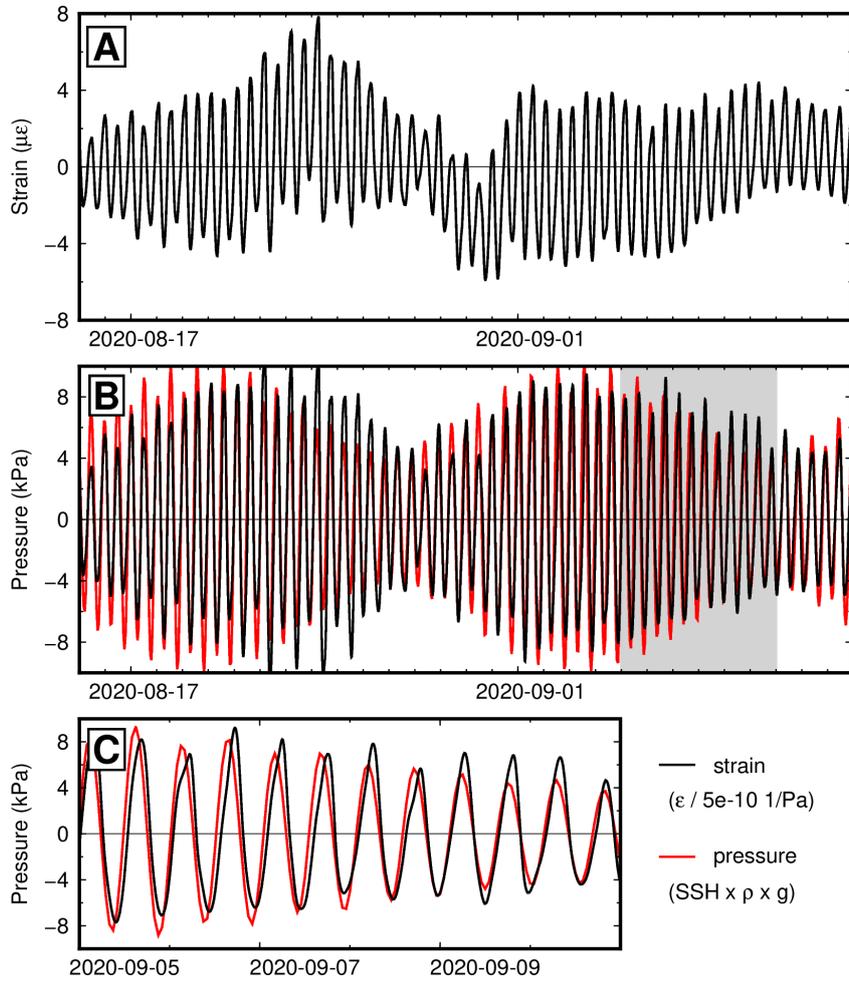
259 the transition from single-armored (SA, 26-mm diameter) to light-weight protected (LWP,  
 260 19.6-mm diameter) cable type, there is a frequency-dependent difference in response, which  
 261 can be adequately described with a simple thermal transfer-function model (Figure 4F,G).  
 262 Consequently, the spectral slope at high frequencies should probably not be interpreted.  
 263 For such a model, the phase response of the cable to external thermal forcing is also frequency-  
 264 dependent and non-negligible, which implies that the sharp temperature fronts observed  
 265 here may truly be sharper still if observed by a thermistor at the same location (see Text  
 266 S3, Figure S5).

### 267 **4.3 Hidden signature of the barotropic tide**

268 While the observation of complex temperature fluctuations with ocean-bottom DAS  
 269 provides a unique opportunity for study of internal wave and boundary layer dynamics,  
 270 the large amplitude of these signals poses a significant challenge to observing pressure  
 271 perturbations and solid-Earth deformations, such as associated with tsunamis and slow  
 272 earthquakes. Exploiting the fact that the wavelength of the barotropic tide is much greater  
 273 than the wavelength of the temperature variations associated with the internal tide on  
 274 a near-critical slope, we compute a spatial median across the 15–30 km cable segment,  
 275 which is plotted in Figure 5 and compared with the barotropic tidal pressure, estimated  
 276 from TPXO (Egbert & Erofeeva, 2002). The recovered signal, plotted in units of pres-  
 277 sure for the purpose of interpretation, matches the predicted phase of the barotropic tide  
 278 including the fortnightly variation ( $M_f$ ), which strongly suggests that this signal rep-  
 279 represents mechanical strain in the cable due to pressure. The observed amplitude is 2–8  
 280  $\mu\epsilon$  and scales to pressure as  $\frac{\epsilon}{\Delta p} \sim 5 \times 10^{-10} \text{ Pa}^{-1}$ , which is a plausible value of hori-  
 281 zontal seafloor compliance (Crawford et al., 1991) though slightly larger than the pre-  
 282 dicted strain induced in a cable from hydrostatic pressure perturbations alone (Mecozzi  
 283 et al., 2021). While we note that this simple averaging procedure does not guarantee the  
 284 full recovery of the tidally-induced mechanical strain signal or complete elimination of  
 285 temperature residuals, the demonstrated sensitivity is promising for application of ocean-  
 286 bottom DAS in seismo-geodesy.

## 287 **5 Discussion and conclusions**

288 Thus far we have assumed that the long-period transients observed in DAS data  
 289 from the Strait of Gibraltar and Gran Canaria are dominated by temperature. Conven-



**Figure 5.** (A) Long-period DAS signal removed by the default laser denoising parameters in units of nanostrain. (B) Same as A with low-pass filter with a corner frequency of 48 h scaled to units of pressure as  $p = \epsilon / (5 \times 10^{-10})$  (black), and barotropic tidal pressure from TPXO (red). (C) Zoom-in to the gray shaded window in B.

290 tional applications of DAS are, however, as a dynamic strain sensor, and the extraction  
 291 of a signal proportional to barotropic tidal pressure indicates that mechanical strain is  
 292 non-negligible. A typical DAS system, such as the chirped-pulse instrument used here  
 293 (Fernandez-Ruiz et al., 2019), estimates changes in optical path length across each fiber  
 294 segment by measuring small perturbations in the phase of backscatter between two con-  
 295 secutive laser pulses. For a finite fiber segment of length  $L$ , the differential phase is given  
 296 by:

$$\Delta\phi = \frac{4\pi nL}{\lambda} \left( \frac{\delta L}{L} + \frac{\delta n}{n} \right)$$

297 where  $n$  is the index of refraction and  $\lambda$  is the laser wavelength. Changes in the opti-  
 298 cal path length measured by DAS can therefore result from mechanical strain or a change  
 299 in temperature. Both mechanisms include a physical strain  $\frac{\delta L}{L}$  and a change in refrac-  
 300 tive index  $\frac{\delta n}{n}$ . Letting  $\phi = \frac{4\pi nL}{\lambda}$ , for mechanical strain  $\varepsilon$ ,  $\frac{\Delta\phi}{\phi} = (1 + \psi)\varepsilon$ , where  $\psi \approx$   
 301  $-0.22$  accounts for the effect of photoelasticity at  $\lambda = 1550$  nm. For a change in tem-  
 302 perature  $\Delta T$ ,  $\frac{\Delta\phi}{\phi} = (\alpha_T + \xi)\Delta T$ , where the thermal expansion coefficient is  $\alpha_T \approx 5 \times$   
 303  $10^{-7} \text{ K}^{-1}$  and the thermo-optic coefficient is  $\xi \approx 6.8 \times 10^{-6} \text{ K}^{-1}$ . Therefore the equiv-  
 304 alence between temperature and strain is  $\frac{\Delta T}{\varepsilon} \approx 10^5 \text{ K}$  (e.g. Koyamada et al. (2009)).  
 305 The uncertainty in these parameters is challenging to quantify, since no calibration has  
 306 been performed in situ, but a factor of two deviation in the strain-to-temperature rela-  
 307 tion is conceivable. Cable construction and burial can only thermally insulate the fiber,  
 308 so the conversion used here should otherwise represent the minimum value of relative  
 309 temperature (Sidenko et al., 2022).

310 Based on five key points of observation, we assert that the long-period transients  
 311 described above are predominately if not entirely changes in the temperature of the fiber:

- 312 1. A 20–40  $\mu\varepsilon$  strain, equivalent to the 2 K observed at Gran Canaria or 4 K observed  
 313 in Gibraltar, is simply too large to be physically plausible as mechanical strain,  
 314 being comparable to the near-field (<1-km epicentral distance) peak strain recorded  
 315 during the 2019 M7.1 Ridgecrest earthquake (Farghal et al., 2020). Given steel  
 316 and aluminum elements in the cable construction (Young’s modulus 100–200 GPa),  
 317 such a strain would require an oscillating 10–40 MPa stress, which is comparable  
 318 to or greater than the weight of the entire water column. Further, the signal ob-  
 319 served at Gran Canaria is coherent over a >10-km distance, which would imply  
 320 an integrated displacement of at least 20 cm every 12 hr across the cable.

- 321 2. The sudden disappearance of a 4 K signal at the point of burial of the Gibraltar  
322 cable over a distance of one channel (10 m) (Figure 2) can only be attributed to  
323 temperature. Any pressure forcing sufficient to deform a cable at the seafloor 40  
324  $\mu\epsilon$  must be transmitted at a measurable level to a shallowly buried cable, as ev-  
325 idenced by much smaller surface gravity wave pressure signals observed on the buried  
326 3–6-km section of this same cable (Williams et al., 2022). Conversely, thermal sig-  
327 nals may be retarded by as little as a few centimeters of sediment, owing to the  
328 small thermal diffusivity of geological materials (Figure S5).
- 329 3. The observed signature of the nonlinear internal tide at Gran Canaria (Figure 3)  
330 is 5–10 times larger than the spatially-averaged signal, the latter of which corre-  
331 sponds with the barotropic tidal pressure (Figure 5). This amplitude ratio is in-  
332 consistent with the expectation for pressure-induced mechanical strain from the  
333 baroclinic tide, as supported by modeling (Figure 3E, S4). The ocean-bottom pres-  
334 sure perturbation from the barotropic tide (order 1–10 kPa) is larger than that  
335 from baroclinic tide (order 10–100 Pa) because the density contrast at the sea sur-  
336 face is about 1000 times larger than the density contrast across the pycnocline,  
337 even though isopycnal displacement may be as much as 100 times larger than the  
338 sea surface displacement (e.g. Moum and Smyth (2006)). Conversely, the ocean-  
339 bottom temperature perturbation from the barotropic tide is negligible, whereas  
340 the baroclinic tide can induce  $>1$  K temperature changes even at depths  $>1$  km  
341 (e.g. van Haren (2006)).
- 342 4. The temporal asymmetry seen in modeled and observed bottom boundary layers  
343 over nearly critical slopes, the frontal velocities consistent with bores, together with  
344 the lack of asymmetry and much larger wavelength inferred from the correspond-  
345 ing modeled pressure signal, provides oceanographic supporting evidence that DAS  
346 measurements are principally responsive to small temperature fluctuations asso-  
347 ciated with nonlinear boundary layer dynamics rather than to the tidally oscil-  
348 lating bottom pressure (Figure 3,S4).
- 349 5. The change in cable type between single-armored and light-weight protected around  
350 29-km on the Gran Canaria cable (Figure 3A) manifests a frequency-dependent  
351 change in sensitivity which can be adequately described using a simple thermal  
352 model for the difference in cable diameter (Figure 4F,G).

353 We conclude that the observed long-period transients in both datasets are dom-  
354 inated by temperature effects. However, the relative contributions of strain and temper-  
355 ature may not be simple to identify in most ocean-bottom DAS datasets. In particular,  
356 DAS has potential as a seafloor geodetic method for monitoring offshore fault zones, but  
357 the solid-Earth strains associated with processes like fault creep and slow earthquakes  
358 will likely be smaller than or comparable to oceanic temperature signals from internal  
359 tide and boundary layer dynamics along the slopes of active margins. Concurrent mea-  
360 surement with both DAS and DTS may provide one solution, but is limited by the short  
361 range of DTS. Another possibility is to utilize bespoke cables with fibers of differing ther-  
362 mal properties so that the temperature signal can be subtracted (Zumberge et al., 2018),  
363 but this excludes pre-existing submarine telecommunication cables. Here, we recovered  
364 mechanical strain associated with pressure by naive spatial averaging, which was suc-  
365 cessful owing to the difference in wavelength between the internal and barotropic tides.  
366 This suggests that a more general multi-scale approach like principal component anal-  
367 ysis might be capable of separating mechanical and thermal signals, as is commonly per-  
368 formed to remove secular and seasonal trends from geodetic time-series.

369 Our study highlights several other outstanding challenges for fiber-optic oceanog-  
370 raphy. DAS sensitivity to temperature has not been calibrated in a field environment,  
371 and the thermal amplitude and phase response of submarine cables is generally not known.  
372 In both the Strait of Gibraltar and Gran Canaria DAS datasets, we observed differences  
373 in amplitude between even adjacent channels (see striping or vertical lines on Figures  
374 2, 3, 4) indicating differences in broadband temperature response, which could result from  
375 partial burial of the cable with a few millimeters of sediment drape or variations in in-  
376 strumental sensitivity (Figure S5). Beyond the instrument itself, the novel observation  
377 of a continuous horizontal profile of seafloor temperature needs to be reconciled with con-  
378 ventional oceanographic measurements. For example, in-situ comparison with data from  
379 current meters and thermistors could help explain whether the dissipation and reversal  
380 of temperature fronts on the slope of Gran Canaria is associated with internal wave break-  
381 ing, and whether the internal tide is being generated locally or remotely. Importantly,  
382 without complementary measurements it is not possible to directly calculate the diapy-  
383 cnal diffusivity or other key parameters necessary to quantify the intensity of tidal dis-  
384 sipation and mixing observed here. Until such calibrations and validations are available,  
385 the ability of ocean-bottom DAS to leverage widespread, pre-existing submarine telecom-

386 munication infrastructure at relatively low cost for monitoring near-bottom dynamics  
387 from the abyssal ocean to the shallow shelf may prove most useful for targeted site se-  
388 lection of conventional oceanographic surveys and generalization of local measurements  
389 to larger scales.

## 390 **Data Availability**

391 All 4.5 days of DAS data from the Strait of Gibraltar necessary to reproduce Fig-  
392 ure 2 and the 3 days of DAS data from Gran Canaria necessary to reproduce Figures  
393 3 and 4 are available through the CaltechDATA repository ([https://doi.org/10.22002/  
394 j8cbw-j1602](https://doi.org/10.22002/j8cbw-j1602)).

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415 The authors declare no conflicts of interest relevant to this study.

416 **Supporting Information for “Fiber-optic observations of**  
 417 **internal waves and tides”**

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429 **Contents of this file**

430 1. Text S1 to S3

431 2. Figures S1 to S5

432 **Additional Supporting Information**

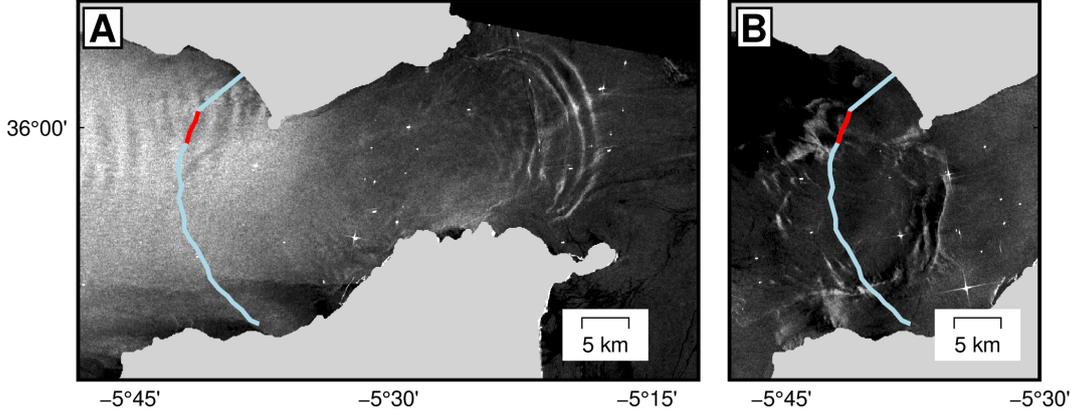
433 1. Movies S1

434 **Text S1. A schematic internal wave model after Apel (2003)**

435 In order to understand the relationship between the temperature excursions ob-  
 436 served with DAS and internal solitary wave parameters, we constructed synthetic data  
 437 using the “dnoidal” model of Apel (2003). We first picked a relatively arbitrary source  
 438 location at the northern end of the Camarinal Sill towards the Spanish shelf (green star  
 439 in Figure S2A) and calculated the propagation distance for each point along the cable  
 440 path. Then, we evaluated Apel’s model to obtain the isopycnal displacement at each point  
 441 along the cable as a function of time:

$$\eta(x, z, t; k) = \eta_0 W_k(z) I(x, t) \left[ 2 \operatorname{dn}_{s(x)}^2 \left( \frac{1}{2} k_0 (x - Vt) \right) - (1 - s^2(x)) \right]$$

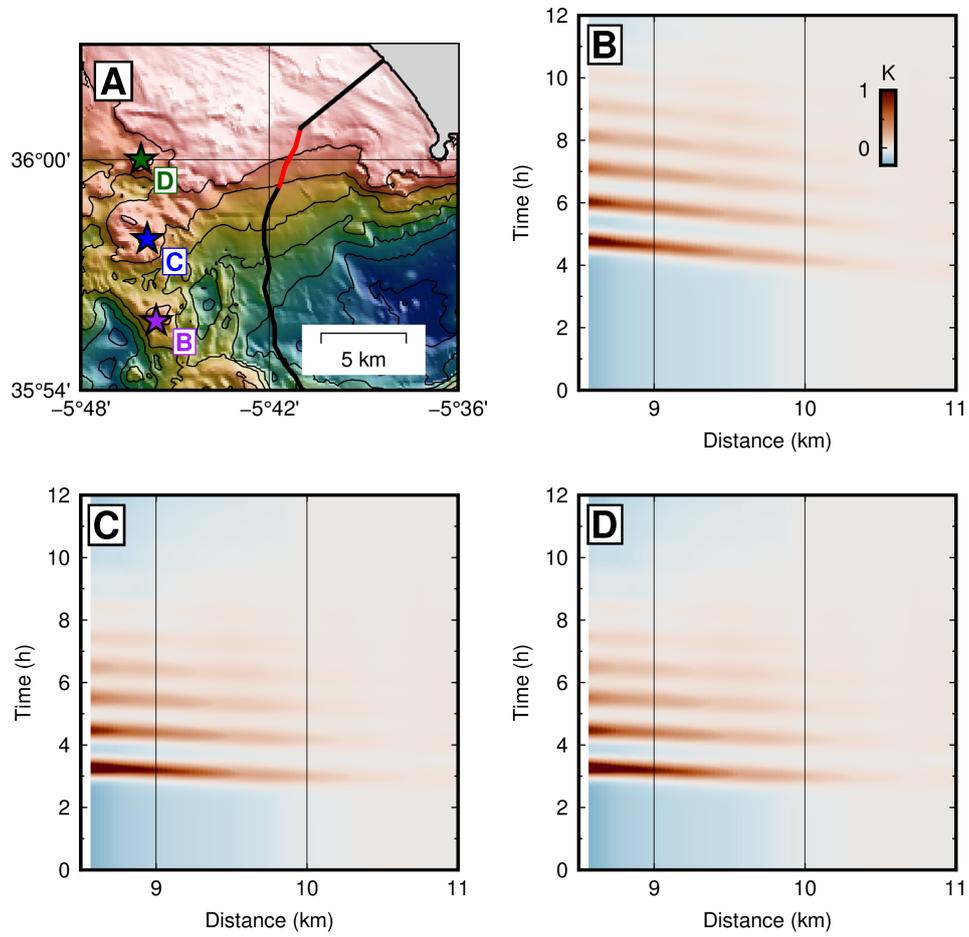
442 Here,  $W_k(z)$  is the vertical structure function determined by numerical solution of the  
 443 Taylor-Goldstein equation given realistic stratification for the Strait of Gibraltar. The



**Figure S1.** (A) Synthetic aperture radar (SAR) image of the Strait of Gibraltar from Sentinel-1A acquired at 2019-10-26 06:27:44 UTC, showing an internal wave group propagating eastward into the Alboran Sea (normalized color scale). (B) SAR image from Sentinel-1B acquired at 2019-10-02 18:17:43 UTC showing a nascent internal wave group near the cable location propagating ESE, suggestive of a source towards the north of the Strait.

444 duration and decay of the wave group is given by  $I(x, t)$ , which is an envelope function.  
 445 The term  $\text{dn}_s(x)$  is a Jacobian elliptic function and a solution to the Korteweg-de Vries  
 446 equation for weakly nonlinear wave propagation. The term  $s(x)$  is a shape parameter  
 447 for the Jacobian elliptic function which determines the dispersion. Apel (2003) provides  
 448 expressions to evaluate each of these terms along with hyperparameters used by Apel  
 449 to model SAR images of internal solitary wave propagation in the Strait of Gibraltar.  
 450 We set the leading-soliton wavelength  $k$  at 2-km to match SAR scenes acquired around  
 451 the time of our experiment (Figure S1) and modified one parameter in  $I$  to make the group  
 452 duration 6-h for comparison with the data. Otherwise, all parameters are as provided  
 453 by Apel (2003).

454 Given the model time-series of isopycnal displacement along the cable, we then mul-  
 455 tiplied the isopycnal displacement by the local temperature gradient  $\frac{\partial T}{\partial z}$  using a CTD  
 456 profile from the 1986 Gibraltar Experiment nearest the cable location (Kinder & Bry-  
 457 den, 1987) in order to obtain the relative temperature at each point. This assumes neg-  
 458 ligible diapycnal transformation during wave propagation. Previous authors have noted  
 459 a persistent change in stratification following the passage of internal solitary wave groups  
 460 in the Strait of Gibraltar (Ziegenbein, 1969), which implies this may be a poor assump-  
 461 tion, although the background temperature observed in DAS data is unchanged between



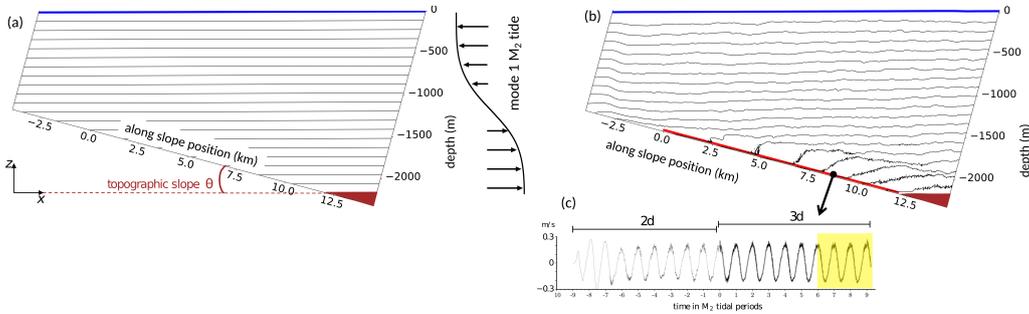
**Figure S2.** (A) Map of the Camarinal Sill and Strait of Gibraltar cable location, with the segment from Figure 1 of the main text shown in red. (B,C,D) Synthetic data generated using the schematic model of Apel (2003) for different point sources shown in (A), assuming straight-ray propagation. Panel (D) is the same as Figure 1E.

462 passing wave groups (Figure 2). The validity of this assumption is relatively minor, how-  
 463 ever, compared to other simplifying assumptions made by this model: any background  
 464 current is neglected, propagation is assumed along a straight raypath, and the effect of  
 465 bathymetry on propagation speed is neglected. Consequently, the synthetic data in Fig-  
 466 ure 2E and S2 should only be considered a schematic representation.

467 **Text S2. Simulation of tidally-driven near-bottom flow**

468 *Model configuration and overview*

469 An idealized simulation of tidally-driven turbulence along a sloping bottom in a  
 470 uniformly-stratified ocean was performed using `flow_solve` (Winters & de la Fuente, 2012),  
 471 a non-hydrostatic model for process studies of rotating, stratified flows (e.g., Winters (2015);  
 472 Ulloa et al. (2019); Lelong et al. (2020); Barkan et al. (2017)). We examined the near-  
 473 boundary flow produced by the reflection of the gravest vertical mode internal tide at  
 474 a slightly supercritical sloping boundary. The back-reflection of the internal tide at nearly  
 475 the slope angle produces an oscillatory boundary layer flow characterized by the peri-  
 476 odic appearance of sharp up-slope propagating bores. See Winters (2015) for discussion  
 477 of a similarly-configured simulation, animations of the bore-like features, and a compar-  
 478 ison with the observations of van Haren (2006).



**Figure S3.** Schematics of the modeling scenario (A) at the initial condition and (B) after 9 tidal periods. The red line indicates the along slope segment analyzed in figure S4. (C) Time series of the  $x$ -velocity component within the boundary layer. The three tidal periods shown in Figure 3E and S4 are shaded in yellow.

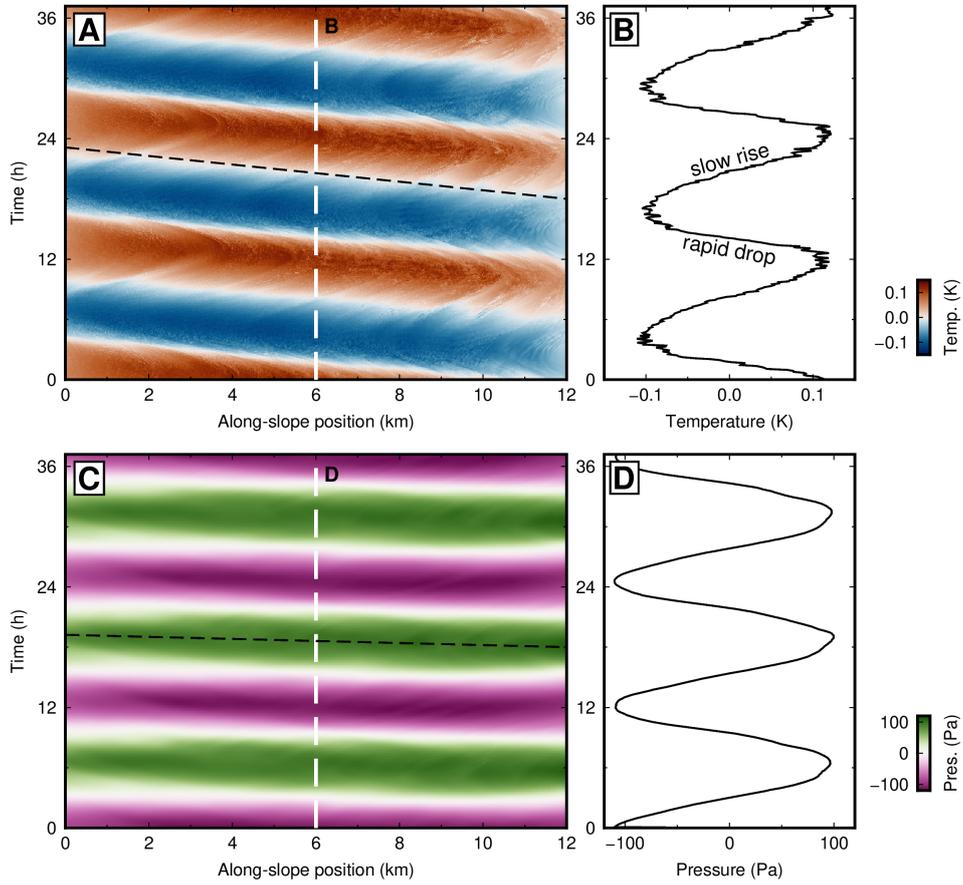
479 A schematic of the simulation is shown in Figure S3. The computational domain  
 480 is tilted to align with the sloping bottom. The domain extends laterally over 21 km to

481 a maximum depth of 2160 m using a spatial resolution of 4.5 m in the tilted coordinate  
 482 system. The ocean is initialized at rest having a background  $N$  value of  $1.3 \times 10^{-3} \text{ s}^{-1}$ ,  
 483 within the range estimated using WOA18 (Boyer et al., 2018) over 1-2.5 km depths along  
 484 the submarine cable ( $1\text{-}3 \times 10^{-3} \text{ s}^{-2}$ ). The incident internal tide is forced at the right  
 485 boundary at the  $M_2$  frequency with an amplitude of  $0.2 \text{ m s}^{-1}$  (Figure S3A). The sim-  
 486 ulation was performed in stages. First, a two-dimensional spin-up run allowed the in-  
 487 cident and reflected waves to come into balance near the slope. A snapshot of the flow  
 488 was then slightly perturbed and extended into three dimensions. The subsequent three-  
 489 dimensional run allowed for the excitation and evolution of small-scale turbulence in the  
 490 oscillating boundary layer (Figure S3B). The time series in the schematic shows the  $x$   
 491 velocity component taken from a point within the boundary layer throughout the sim-  
 492 ulation stages (Figure S3C). The yellow shading indicates the three tidal periods ana-  
 493 lyzed in Figure S4. Since this modeling scenario was designed as a laboratory scale ex-  
 494 periment, modeling results were re-scaled to be representative of the Gran Canaria DAS  
 495 observation site using a bottom temperature of 279.3 K, estimated from the WOA18 Septem-  
 496 ber climatology extracted for the region.

#### 497 *Implications for interpretation of DAS observations*

498 This idealized modeling scenario yields a pattern of near-bottom temperature that  
 499 is remarkably similar to that inferred from DAS observations (Figures 3 and 4). Figure  
 500 S4 plots simulated near-bottom temperature and pressure perturbations (the simulated  
 501 absolute temperature/pressure with the temporal mean subtracted at each point) along  
 502 with a representative time series from a fixed location at 6 km (black dashed line). This  
 503 is the same location plotted in Figure 3E of the main text.

504 The dominant oscillation is at the  $M_2$  tidal frequency. The slopes of the lines of  
 505 constant phase (dashed lines) in Figure S4 indicate propagation speeds up the slope. The  
 506 speed inferred from the pressure signal is about 2.7 m/s, which corresponds to an inter-  
 507 nal wave at  $M_2$  frequency with a horizontal wavelength of about 120 km. The fixed-point  
 508 pressure time series is sinusoidal, and the rise and fall of the signal are symmetrical. The  
 509 bottom pressure is a vertically integrated quantity that is sensitive primarily to the am-  
 510 bient, nearly linear, large-scale internal tide well above the thin bottom boundary layer.  
 511 In contrast, the temperature signal is dominated by local, nonlinear dynamics within the  
 512 boundary layer. The slope of the temperature phase lines corresponds to the speed of



**Figure S4.** (A) Plot of temperature change as a function of time for a near-bottom slice of the model, indicated with a red line in Figure S3B. (B) Time series of temperature change for a single point from A. (C) Plot of pressure perturbation as a function of time and position, as in A. (D) Time series of pressure perturbation for the same point from C. White dashed lines indicate the position shown in panels B,D and in main text Figure 3E. Black dashed lines indicate the along-slope moveout, with a velocity of about 0.65 m/s for the temperature perturbations in panel A and a velocity of about 2.7 m/s for the pressure perturbations in panel C.

513 the near-bottom bores as they sweep water up and down the slope. Characteristic of these  
 514 bores is temporal asymmetry: temperature at a point drops rapidly as the sharp nose  
 515 of an up-slope bore sweeps cold water upward each tidal cycle. The relaxation phase is  
 516 significantly slower. The speed of these features inferred from sloping phase is about 0.65  
 517 m/s, significantly slower than the phase speed of the internal tide itself. The modeled  
 518 bore speed is consistent with the estimates of van Haren (2006), who reported signifi-  
 519 cant temporal asymmetry and bore speeds of 0.4–0.5 m/s in the Bay of Biscay. It is also  
 520 consistent with the DAS estimate (0.5 m/s, shown in Figure 4B of the main text) from  
 521 a slightly supercritical portion of the Gran Canaria slope.

### 522 **Text S3. Simple thermal models for the attenuation of temperature** 523 **by cable construction and burial**

524 To represent the effect of sediment cover or burial on the temperature measured  
 525 within a cable by DAS, consider heat conduction in a semi-infinite solid  $u_t = \kappa u_{zz}$  with  
 526 uniform thermal diffusivity  $\kappa$  and time-harmonic temperature forcing at the free surface  
 527  $u(z = 0, t) = Ae^{i\omega t}$ . This has solution  $u(z, t) = Ae^{-z\sqrt{i\omega/\kappa}}e^{i\omega t}$ , which is well-known.  
 528 Treating this as a filter, the temperature response of a point at depth  $z = z_0$  relative  
 529 to the free surface is simply:

$$H(z = z_0, \omega) = \frac{u(z = z_0, \omega)}{u(z = 0, \omega)} = e^{-z_0\sqrt{i\omega/\kappa}}.$$

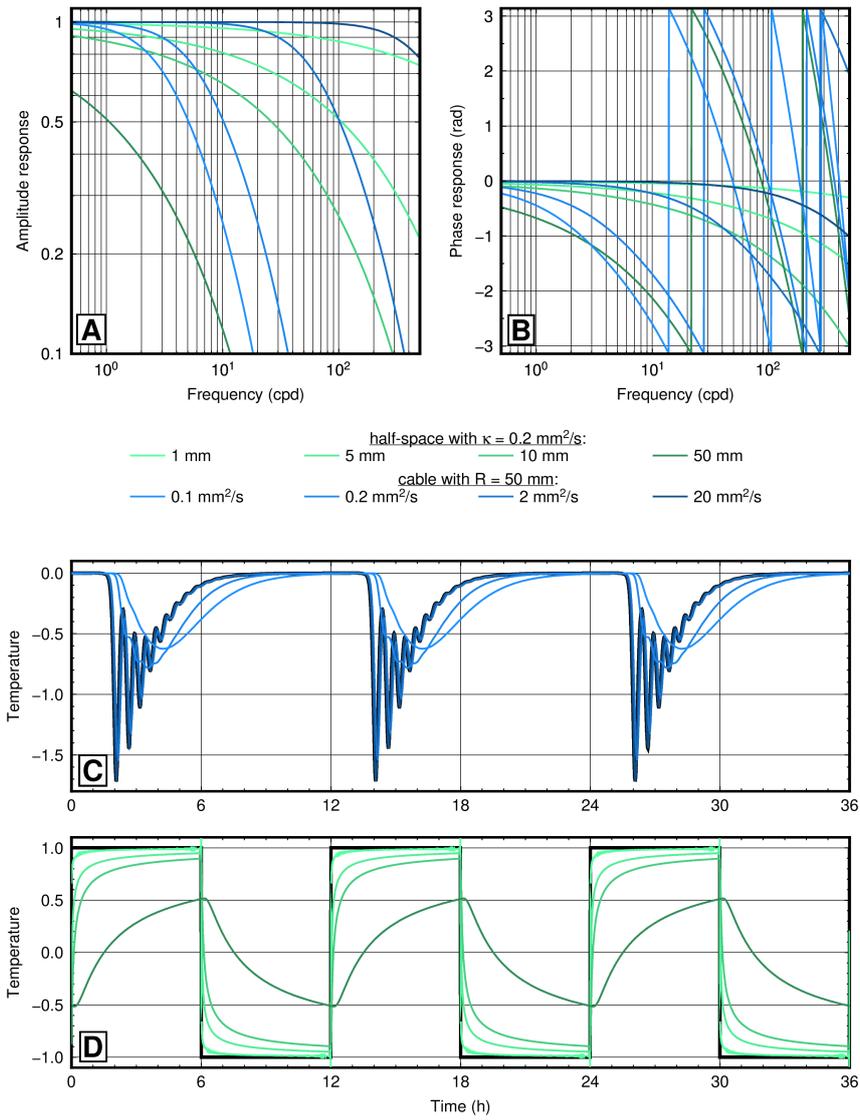
530 Similarly, to represent the effect of finite cable thickness on the temperature mea-  
 531 sured internally by DAS, consider heat conduction in a uniform disk  $\frac{1}{\kappa}u_t = \frac{1}{r}u_r + u_{rr}$   
 532 with time-harmonic temperature forcing at the surface  $u(r = R, t) = Ae^{i\omega t}$ . This has  
 533 solution

$$u(r, t) = A \frac{J_0(r\sqrt{-i\omega/\kappa})}{J_0(R\sqrt{-i\omega/\kappa})} e^{i\omega t}$$

534 for  $r \in [0, R]$ , where  $J_0$  is a Bessel function of the first kind. The temperature response  
 535 of a fiber at the center of the cable relative to the exterior is then:

$$H(r = 0, \omega) = \frac{u(r = 0, \omega)}{u(r = R, \omega)} = \frac{1}{J_0(R\sqrt{-i\omega/\kappa})}.$$

536 These two models are plotted in Figure S5 for various parameters. Burial beyond a few  
 537 centimeters strongly attenuates temperature across the internal wave continuum band  
 538 and tidal periods, using a typical value of thermal diffusivity for marine sediments of 0.2  
 539 mm<sup>2</sup>/s. For a 50-mm radius cable, a thermal diffusivity similar to common polymers used



**Figure S5.** (A) Amplitude and (B) phase response to harmonic temperature forcing at the free surface for a point in a half-space (green) and at the center of a disk (blue) with uniform thermal diffusivity, which are simple models of sediment burial and cable thickness. (C) Example temperature response of a cable with 50-mm radius to internal solitons generated with the “dnoidal” model for different values of thermal diffusivity, analogous to the power cable in the Strait of Gibraltar. (D) Example temperature response of a non-insulating cable to a square wave with burial at various depths in sediment with thermal diffusivity of  $0.2 \text{ mm}^2/\text{s}$ , analogous to the telecommunication cable offshore Gran Canaria.

540 in cable construction (e.g. rubber, polypropylene, nylon) around  $0.1 \text{ mm}^2/\text{s}$  strongly at-  
 541 tenuates temperature across the internal wave continuum band, whereas a value simi-  
 542 lar to steel or aluminum commonly used for cable armoring around  $20 \text{ mm}^2/\text{s}$  has no ef-  
 543 fect. Consequently, the exact construction will greatly influence the thermal sensitivity  
 544 of any cable, though the reduction in sensitivity between armored and unarmored ca-  
 545 ble is mostly a result of differing thickness.

546 The difference in response between two cables of identical thermal diffusivity but  
 547 different diameter to the same forcing is:

$$H(R_1, R_2, \omega) = \frac{J_0(R_1 \sqrt{-i\omega/\kappa})}{J_0(R_2 \sqrt{-i\omega/\kappa})}$$

548 as plotted in Figure 4G, comparing the difference in response between single-armored  
 549 and light-weight protected cable.

## 550 **Movie S1.**

551 Animation to aid in visualization of along-slope variation in temperature fluctu-  
 552 ations associated with nonlinear internal tide dynamics on the slope of Gran Canaria.  
 553 (Top) Data as shown in Figure 3 of the main text. (Bottom) Along-cable slice in tem-  
 554 perature corresponding to the black dashed line above, smoothed with a spatial median  
 555 filter to suppress small differences in amplitude between adjacent channels. Note that  
 556 the temperature at each point is the relative temperature with the mean value over a  
 557 3-day period subtracted for every channel.

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