

# Assessing Precipitation Trends that may inform Aging Dam Overtopping across the USA

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13 **Abstract**

14 In many cases, persistent or recurrent synoptic circulation patterns lead to multiple wet days that  
15 precede an extreme rainfall event. The joint occurrence of high antecedent rainfall and extreme rainfall  
16 defines a compound event that may pose a high risk for overtopping of aging dams. Our novel analysis  
17 assesses whether there are significant trends across the conterminous United States (CONUS) in the  
18 joint and individual occurrence of extreme daily precipitation and  $k$ -day antecedent precipitation  
19 extremes, for  $k=5$  and  $k=30$  days. We find significant trends in the mean and variance of annual  
20 maximum daily rainfall, and in the  $k$ -day antecedent precipitation in certain regions of the CONUS.  
21 However, their mutual dependence as measured through a copula is invariant with time. The probability  
22 of their joint exceedance, i.e., simultaneously experiencing high extremes of daily precipitation and the  
23  $k$ -day precipitation total, is also increasing in many places in the CONUS.

24

25 **Key Points**

- 26 - Annual maximum daily precipitation ( $A$ ) and the associated antecedent precipitation ( $K$ ) are  
27 increasing in many parts of the United States.
- 28 - The probability of the joint extremes of  $A$  and  $K$  is increasing even more than that of their  
29 individual extremes in many parts of the CONUS.
- 30 - The projected flood volume and duration pose concerns for overtopping of dams as they are  
31 likely to be full when extreme rainfall occurs.

32

33 **Plain Summary**

34 Extreme precipitation is becoming more intense and frequent due to global warming, but this does not  
35 always result in more intense and frequent flooding. In some cases, certain climate patterns can lead to  
36 multiple wet days before an extreme rainfall event, which can raise the risk of flooding, and fill up  
37 reservoirs. This study examines the trends in extreme daily precipitation events and in total precipitation  
38 over the 5 and 30 days preceding each event across the contiguous United States. We found that the  
39 average and variance of both annual maximum daily precipitation and its preceding precipitation total  
40 have significant trends in certain parts of the country. The probability for these precipitation variables to  
41 co-occur at their extreme levels is increasing in many parts of the United States. The mutual dependence  
42 between these two precipitation variables is found to be unchanged over time, which may indicate that  
43 the influence of large-scale climate dynamics that create these compound events is not changing, while  
44 the precipitation variables themselves may be changing in certain regions. Wetter conditions before an  
45 extreme rainy day could increase the chance of reservoir being full and the dam failing by overtopping.

46

47 **1. Introduction:**

48 The United States has experienced an average of 0.8 flooding events per year that caused more than \$1  
49 billion in damages since 1980. This led to over \$173 billion in cumulative damage (NOAA National  
50 Centers for Environmental Information, 2022). In October 2015, an extreme rainfall and flooding event  
51 in South Carolina led to the failure of 36 dams. In 2017, a failure of the main and emergency spillways of  
52 the United States' tallest dam, Oroville, in California, led to the evacuation of over 200,000 people and  
53 repairs cost over \$1.2 billion. In 2020, the failure of two Michigan dams led to the destruction of 150  
54 homes and 10,000 people. These are examples of emerging concerns at the intersection of climate  
55 change and aging infrastructure. Of the over 90,000 dams in the USA, at least 1,680 are considered high  
56 hazard and rated as in unsatisfactory condition (Lieb et al., 2019). Nearly 34-36% of the historical dam  
57 failures are attributed to overtopping (Costa, 1985; Foster et al., 2000), and over 190 of the 250 dam  
58 failures during 2010-2019 were classified as hydrologic or flooding failures (Association of State Dam  
59 Safety Officials, 2020). It is interesting that most of these failures do not seem to correspond to an  
60 extreme rainfall event, but to compound extreme rainfall and antecedent rainfall events that led to high  
61 water levels in the reservoir prior to the failure event. The failure of a major dam could have a  
62 catastrophic impact. This motivates an understanding of the trends associated with such compound  
63 events.

64 Most of the existing dams across the nation were constructed more than 50 years ago, and their design  
65 did not account for the nonstationarity of extremes (Lopez-Cantu & Samaras, 2018; Wright et al., 2019).  
66 Increased exposure to overtopping from high flood volumes may increase the chance of catastrophic  
67 dam failure and result in socio-economic impacts (Ho et al., 2017; Larrauri & Lall, 2020). Exploring the  
68 spatial variation of trends in precipitation over different averaging periods that may influence flood  
69 volumes and hence overtopping would help prioritize where to focus risk analysis and mitigation of  
70 aging dams.

71 Potential trends in floods have been assessed based on the observed trends in extreme event  
72 precipitation (Bates et al., 2008; Seneviratne et al., 2012). However, many catchments in the United  
73 States show a weak linkage between extreme event rainfall and streamflow (Mallakpour & Villarini,  
74 2015; Do et al., 2020). Extreme rainfall has been increasing in both intensity and frequency over large  
75 parts of the United States (Trenberth, 2011; Villarini et al., 2011; Kunkel et al., 2013; Rahmani &  
76 Harrington, 2019), and climate projections expect such an increase to continue with global warming  
77 based on the thermodynamic Clausius-Clapeyron relationship (Trenberth, 2011; Papalexiou &  
78 Montanari, 2019). However, despite the increasing trend in extreme precipitation events, there has  
79 been limited evidence of intensification in flooding events over the United States (Archfield et al., 2016;  
80 Hodgkins et al., 2017; Do et al., 2017), suggesting that an extreme rainfall event alone may not be  
81 sufficient to account for extreme floods. This is attributable to the significant influences of other  
82 interactive factors of flooding, such as the catchment's antecedent soil moisture conditions and  
83 hydrological characteristics (Hodgkins et al., 2017; 2019; Tabari 2020). As an example, although the  
84 intensity of rainfall during the Oroville spillway failure in 2017 was relatively moderate (Vahedifard et  
85 al., 2017), high antecedent precipitation (October – January) saturated the basin and filled the reservoir,  
86 promoting a rapid intensification of runoff during the event (White et al., 2019) that led to the use of the  
87 spillway to avoid dam overtopping. The Michigan dam failures in 2020 were also marked by high water  
88 levels behind the dam prior to the failure.

89 The antecedent wetness or soil moisture of a catchment often plays a prominent role in triggering floods  
90 under extreme rainfall in many cases (Ivancic & Shaw, 2015; Berghuijs et al., 2019; Nanditha & Mishra,  
91 2022, Wasko & Nathan, 2019; Wasko et al., 2021). This suggests that even beyond the concern with dam  
92 filling and overtopping, a joint analysis of trends in the extreme daily rainfall and antecedent rainfall  
93 over some averaging period is useful. The decorrelation time scale, as well as the residence time of soil  
94 moisture, is usually less than 30 days. Consequently, we considered the joint occurrence of annual

95 maximum daily rainfall and total antecedent rainfall over the prior  $k$  days ( $k=5, 10, 15, 30$ ) as the  
96 compound event of interest for the analysis of trends across the country. To our knowledge, this is the  
97 first paper to directly take this approach to derive insights into the flood process without an explicit  
98 modeling of continental scale hydrology.

99 Given the risk perspective, we consider trends in the location, scale, and dependence (coupling)  
100 parameters of the annual maximum daily rainfall and the  $k$ -day antecedent rainfall, as well as in the  
101 associated univariate and bivariate return periods of extreme events. Results are reported for  $k=5$  and  
102 30 days, and for return periods  $T=10$  and 100 years. Nonstationary parametric probability distributions  
103 and bivariate copula functions are fit to the data at each location with automatic parameter selection to  
104 derive the results. We find substantial variation in trends deemed statistically significant across the  
105 country, but the resulting trends are still found to be significant from a field significance analysis and are  
106 predominantly increasing.

## 107 **2. Data and Methods:**

### 108 **2.1. Data**

109 The Climate Prediction Center's (CPC) Global Unified Gauge-Based Analysis of Daily Precipitation (CPC-  
110 Global) dataset from the National Oceanic and Atmospheric Administration (NOAA) was used. The CPC-  
111 Global is generated by interpolating gauge reports from multiple information sources available at CPC,  
112 including the Global Telecommunication System (GTS), Cooperative Observer Network (COOP), and  
113 other national and international meteorological agencies. It was shown in an earlier study that the  
114 optimal interpolation objective analysis technique, which is used to create the CPC-Global dataset, is  
115 capable of generating daily precipitation analysis with biases of less than 1% over most parts of the  
116 global and land areas (Chen et al., 2008). The quality of the dataset is assured by performing the quality  
117 control on the collected gauge reports by comparing them to the historical records and independent

118 information from measurements at nearby stations, concurrent radar/satellite observations, as well as  
119 numerical model forecasts, especially focusing on zero and extreme values (Chen & Xie, 2008). Further  
120 detailed information regarding the interpolation algorithm and evaluation processes for generating the  
121 CPC product are described in Xie et al. (2007), Xie & Shi (2010), and Chen et al. (2008).

122 The CPC-Global dataset covers the global land on a daily scale at a  $0.5^\circ \times 0.5^\circ$  spatial resolution for a  
123 period from 1979 to the present. Only using the data that covers the CONUS from 1979 to 2021, we  
124 derived the annual maximum daily precipitation event and its  $k$ -day antecedent precipitation total for  
125 each grid and year.

## 126 2.2. Methods

### 127 2.2.1. Univariate modeling

128 The Generalized Extreme Value (GEV) distribution is the limiting distribution of the block maxima of a  
129 sequence of independent and identically distributed random (i.i.d.) variables based on the extreme  
130 value theorem (see for instance Coles, 2001). It has been a popular choice for analyzing block maxima in  
131 the hydrometeorological field. Accordingly, we use the GEV distribution to model the annual maximum  
132 daily precipitation. For each grid  $i$ , let  $A_{i,t}$  denote the annual maximum daily precipitation for year  $t$ . The  
133 probability distribution for  $A_{i,t}$  is specified as:

$$A_{i,t} \sim \text{GEV}(\mu_{A_i}, \sigma_{A_i}, \gamma_{A_i}) \quad (1)$$

134 where  $\mu_{A_i}$ ,  $\sigma_{A_i}$ , and  $\gamma_{A_i}$  are the location, scale, and shape parameters of the GEV distribution at grid  $i$ ,  
135 respectively. The cumulative distribution function of GEV for  $A_{i,t}$  is given by:

$$F_{A_i}(A_{i,t}) = e^{-\left[1 + \gamma_{A_i} \left(\frac{A_{i,t} - \mu_{A_i}}{\sigma_{A_i}}\right)\right]^{-1/\gamma_{A_i}}} \quad (2)$$

136 Following Katz (2013), nonstationarity of  $A_{i,t}$  is modeled through linear trends in the parameters  $\mu_{A_i}, \sigma_{A_i}$   
 137 while treating  $\gamma_{A_i}$  as time invariant:

$$\begin{aligned}\mu_{A_i}(t) &= \alpha_1 + \beta_1 t \\ \sigma_{A_i}(t) &= \alpha_2 + \beta_2 t\end{aligned}\tag{3}$$

138 To model the  $k$ -day antecedent precipitation, the 2-parameter gamma distribution (G2) is used. The G2  
 139 distribution is considered a reasonable choice for daily or weekly precipitation events (Thom, 1951;  
 140 Buishand, 1978; Geng et al., 1986). Let  $K_{i,t}$  denote the total precipitation over  $k$  days preceding the date  
 141 of the annual maximum precipitation in year  $t$  for grid  $i$ . Then by reparametrizing  $1/\sigma_{K_i}^2$  and  $\sigma_{K_i}^2 \mu_{K_i}$   
 142 into  $\alpha_{K_i}$  and  $\beta_{K_i}$ , respectively, following Johnson et al. (1994),  $K_{i,t}$  can be described by G2 as:

$$K_{i,t} \sim G2(\alpha_{K_i}, \beta_{K_i})\tag{4}$$

143 where  $\alpha_{K_i}$  and  $\beta_{K_i}$  indicate the shape and scale parameters of the G2 distribution at grid  $i$ , respectively.  
 144 The cumulative distribution function of G2 for  $K_{i,t}$  is given by:

$$F_{K_i}(K_{i,t}) = \frac{1}{\Gamma(\alpha_{A_i})} \gamma\left(\alpha_{A_i}, \frac{K_{i,t}}{\beta_{A_i}}\right)\tag{5}$$

145 where  $\Gamma$  is the gamma function and  $\gamma$  is the lower incomplete gamma function. We model the  
 146 nonstationarity of  $K_{i,t}$  through the parameters  $\mu_{K_i}$  and  $\sigma_{K_i}$  by assuming they change linearly over time:

$$\begin{aligned}\mu_{K_i}(t) &= \alpha_3 + \beta_3 t \\ \sigma_{K_i}(t) &= \alpha_4 + \beta_4 t\end{aligned}\tag{6}$$

147 These specifications allow us to explore univariate trends in the location and scale parameters of the  
 148 annual maximum precipitation and  $k$ -day precedent precipitation totals at each site. For inference on  
 149 the parameters of the univariate GEV, we use the package *ismev* in *R* that implements the Maximum  
 150 Likelihood estimators for the parameters as described in Coles (2001). Estimates are provided for each



151 of the parameters, and their standard errors (se) as well. For the analysis, we map all cases where  
 152  $|\hat{\beta}|/se(\hat{\beta}) > 2$ , as an approximate significance test.

153 We define:

$$u_{i,t} = F_{A_i}(A_{i,t} | \mu_{A_i}(t), \sigma_{A_i}(t), \gamma_{A_i}), \quad v_{i,t} = F_{K_i}(K_{i,t} | \mu_{K_i}(t), \sigma_{K_i}(t)) \quad (7)$$

154 The impact of the nonstationarity on each of the univariate extremes of A ( $r_{A_i}$ ) and K ( $r_{K_i}$ ) is assessed by  
 155 computing the ratio of the return level at the end of the given period to the return level at the  
 156 beginning:

$$r_{A_i} = \frac{F_{A_i}^{-1}\left(1 - \frac{1}{T} \mid \mu_{A_i}(e), \sigma_{A_i}(e), \gamma_{A_i}\right)}{F_{A_i}^{-1}\left(1 - \frac{1}{T} \mid \mu_{A_i}(b), \sigma_{A_i}(b), \gamma_{A_i}\right)}, \quad r_{K_i} = \frac{F_{K_i}^{-1}\left(1 - \frac{1}{T} \mid \mu_{K_i}(e), \sigma_{K_i}(e)\right)}{F_{K_i}^{-1}\left(1 - \frac{1}{T} \mid \mu_{K_i}(b), \sigma_{K_i}(b)\right)} \quad (8)$$

157 where  $T$  refers to the recurrence interval (e.g.,  $T=10$  or  $100$  years) and  $e$  and  $b$  refer to the end and  
 158 beginning of period, respectively. Each estimated ratio's statistical significance is tested using bootstrap  
 159 resampling. We focus on this as our test of significance for nonstationarity in the quantiles, rather than  
 160 just the trend coefficients. Recall that only linear trends in the location and scale parameters were  
 161 modeled.

## 162 2.2.2. Bivariate modeling

163 To test whether the dependence between  $A_{i,t}$  and  $K_{i,t}$  is changing with time, we consider whether the  
 164 correlation  $\rho_i$  between  $u_{i,t}$  and  $v_{i,t}$  changes with time. Note that by Equation (7), the temporal trends in  
 165 the mean and variance of  $A_{i,t}$  and  $K_{i,t}$  are effectively addressed in the construction of  $u_{i,t}$  and  $v_{i,t}$ , and  
 166 thus we expect the mean and variance of  $u_{i,t}$  and  $v_{i,t}$  are constant over time. Then an estimate of  $\rho_i$   
 167 would be provided by:

$$\hat{\rho}_i = \frac{\sum(u_{i,t} - m_{u_i})(v_{i,t} - m_{v_i})}{s_{u_i}s_{v_i}} = \frac{\sum(u_{i,t}v_{i,t} - m_{u_i}v_{i,t} - u_{i,t}m_{v_i})}{s_{u_i}s_{v_i}} = \frac{\sum(u_{i,t}v_{i,t}) - 2m_{u_i}m_{v_i}}{s_{u_i}s_{v_i}} \quad (9)$$

168 where  $m_{u_i}$ ,  $m_{v_i}$ ,  $s_{u_i}$ , and  $s_{v_i}$  are the mean and standard deviation of  $u_{i,t}$  and  $v_{i,t}$ , respectively. If the  
 169 dependence between  $u_{i,t}$  and  $v_{i,t}$  is stationary, then the expected value of the cross product  $w_{i,t} =$   
 170  $u_{i,t}v_{i,t}$  should be invariant with time. We explore the stationarity of  $w_{i,t}$  using the Mann-Kendall test, to  
 171 assess whether modeling the nonstationarity in the dependence structure is needed. We found  
 172 significant trends in only a few places (less than 1%) in the CONUS. This was not significant based on a  
 173 field significance test, implying a stationary dependence structure could be considered for bivariate  
 174 models of  $A_{i,y}$  and  $K_{i,y}$ .

175 Copulas have been used extensively for modeling the dependence of multivariate random. Since the  
 176 dependence structure was identified as stationary, the multivariate cumulative distribution function of  
 177  $A_{i,y}$  and  $K_{i,y}$  is represented in terms of their marginal of  $u_{i,t}$  and  $v_{i,t}$ , with a stationary copula function  $C_i$ ,  
 178 defined by a copula parameter  $\theta$ :

$$F_{A_i, K_i}(A_{i,t}, K_{i,t}) = C_i(u_{i,t}, v_{i,t}; \theta) \quad (10)$$

179 There are several parametric copula families available, and the strength of bivariate dependence is  
 180 usually controlled by  $\theta$ . Using the package *VineCopula* in R (Nagler et al., 2022), we determine the  
 181 optimal set of copula family and  $\theta$  that best fits a given bivariate distribution based on the Bayesian  
 182 Information Criterion (BIC) statistics for each grid  $i$ .

183 Since we consider the nonstationarity of  $A_{i,t}$  and  $K_{i,t}$ , their probability distributions are assumed to vary  
 184 with time, and thus the probability of their joint exceedances for a fixed set of thresholds is also  
 185 expected to be time dependent. Here, we measure the probability of joint exceedances for a fixed set of  
 186 thresholds  $A_i^*$  and  $K_i^*$  at time  $t$ , i.e.,  $p(A_{i,t} > A_i^*, K_{i,t} > K_i^*)$ , using copulas (Tilloy et al., 2022):

$$p(A_{i,t} > A_i^*, K_{i,t} > K_i^*) = G_t(A_i^*, K_i^*) = 1 - u_{i,t}^* - v_{i,t}^* + C_i(u_{i,t}^*, v_{i,t}^*; \theta) \quad (11)$$

$$u_{i,t}^* = F_{A_i}(A_i^* | \mu_{A_i}(t), \sigma_{A_i}(t), \gamma_{A_i}), \quad v_{i,t}^* = F_{K_i}(K_i^* | \mu_{K_i}(t), \sigma_{K_i}(t)) \quad (12)$$

187 Then we compute the change in the probability of joint exceedances by calculating  $G_e(A_i^*, K_i^*)/$   
 188  $G_b(A_i^*, K_i^*)$ , where  $e$  and  $b$  refer to the end and beginning of the period. We present the results for the  
 189 joint occurrence of an annual maximum daily precipitation event exceeding its 100-year return level  
 190 following a  $k$ -day antecedent precipitation total greater than its 10-year return level. Consequently,  $A_i^*$   
 191 and  $K_i^*$  are set as the 100-year return level of  $A_{i,t}$  and 10-year return level of  $K_{i,t}$ , respectively, based on  
 192 the probability distributions at  $t=b$ . A significance test was performed for the estimated ratios at the 5%  
 193 level for each grid  $i$  using bootstrap resampling.

194

### 195 3. Results

#### 196 3.1 Spatial patterns of univariate trends

197 During the period of record, the location parameter of  $A$ ,  $\mu_A$ , has increased significantly over the eastern  
 198 half of the CONUS while there are mixed trends in the western half (Figure 1a). Broadly speaking, these  
 199 geographical contrasts are consistent with the findings from earlier studies (Easterling et al., 2017;  
 200 Wright et al., 2019; Harp & Horton, 2022). The scale parameter of  $A$ ,  $\sigma_A$ , has increased across the  
 201 CONUS, in multiple spatial clusters partially covering regions in the northwest, southwest, and the east  
 202 coast (Figure 1b). Areas where both  $\mu_A$  and  $\sigma_A$  show an increasing trend, such as the northeastern  
 203 region, would have an amplified increase in the probability of extreme rainfall (Figure S.1a).

204 However, the location parameter of  $K$ ,  $\mu_K$ , has decreased throughout the CONUS, except for some  
 205 regions including the states of Wyoming, Idaho, and Montana, for both cases of  $k=5$  and  $k=30$  days  
 206 (Figures 1c and 1e). The scale parameter of  $K$ ,  $\sigma_K$ , shows different patterns for  $k=5$  and  $k=30$  days. When

207  $k=5$  days,  $\sigma_K$  shows statistically significant increases in the eastern half of the CONUS relative to the  
208 west, except in some regions in the northwest and near the states of Colorado and Oregon (Figure 1d).  
209 When  $k=30$  days,  $\sigma_K$  shows statistically significant increases mostly in the southwestern regions (Figures  
210 1f). For most locations where trends in  $\mu_K$  and  $\sigma_K$  are both significant,  $\mu_K$  shows a decreasing trend  
211 while  $\sigma_K$  increases, for both cases of  $k=5$  and  $k=30$  days (Figures S.1b and S.1c). This is interesting since  
212 the implications for antecedent precipitation prior to an extreme event are quite mixed. An increase in  
213 the variance, but a decrease in the mean value could still portend a higher risk of an extreme event,  
214 since it would reflect more frequent smaller and less frequent but potentially larger total precipitation.

215 Most cases where both  $\mu_A$  and  $\mu_K$  increase appear scattered in the western half of the CONUS,  
216 especially within the northwestern regions (Figure S.2a). Interestingly,  $\mu_A$  and  $\mu_K$  show negative trends  
217 in regions near the west coast, and many of these cases are in the vicinity of the regions where both  
218 parameters have increased (Figure S.2b). These spatial patterns of simultaneous increases/decreases in  
219  $\mu_A$  and  $\mu_K$  represent where the changing climate is likely to further amplify/damp potential flood risk.

220 Linear trends in the univariate extremes of  $A$  and  $K$  were also explored in terms of their 10-year and 100-  
221 year return levels. The spatial variability of these trends is shown in Figure 2. The 10-year and 100-year  
222 return levels of  $A$  show similar spatial patterns of significant changes across the CONUS, mostly  
223 composed of positive trends (Figure 2a and 2b). It is notable that the northeastern region has significant  
224 increases in the 10-year and 100-year return levels of  $A$ , consistent with the significant increases in the  
225 location parameter of  $A$  observed in Figure 1a.

226 The 10-year and 100-year return levels of  $K$  have changed significantly as well across the CONUS,  
227 regardless of the  $k$  value. Their spatial trends are similar to each other, with low spatial coherence –  
228 significant positive trends often occur close to significant negative trends. For both cases of  $k=5$  and  
229  $k=30$  days, many locations have shown significant changes in the 10-year and 100-year return levels of  $K$

230 but only a few spatial clusters of them are visually detectable. For  $k=5$  days, the 10-year and 100-year  
231 return levels of  $K$  have increased the most in the states of Wyoming and Montana, and eastern Texas. At  
232 the same time, areas near the state of Oklahoma and northern Texas have experienced a significant  
233 decrease in those return levels of  $K$  (Figures 2c and 2d). For  $k=30$  days, the 10-year and 100-year return  
234 levels of  $K$  have increased the most near the states of Montana, Wyoming, and Colorado, and decreased  
235 the most in regions including the states of Arizona, Nevada, northern Texas, and the southeastern  
236 regions (Figures 2e and 2f). In closing, we remind the reader that the 5- and 30-day precipitation totals  
237 ( $K$ ) analyzed here are conditional on the subsequent occurrence of an annual maximum daily rainfall  
238 event ( $A$ ), and do not refer to the 5- or 30-day annual maximum precipitation.

### 239 **3.2 Bivariate trend analyses**

240 When  $k=5$  days, a strong dependence between  $A$  and  $K$  is identified in clusters mainly along the western  
241 coast and in some regions near the states of Montana, Wyoming, and Missouri (Figure S.3a). When  $k=30$   
242 days, such a strong dependence is also observed in other regions as well, particularly over the eastern  
243 half of the CONUS, including the states of Kansas, Missouri, Iowa, Wisconsin, and the southeastern  
244 regions (Figure S.3b). For these locations,  $A$  is expected to have greater magnitudes with a wetter  
245 precedent 30-day period,  $K$ , reflecting a persistent wet weather regime, that would be a concern for  
246 flood generation and dam safety.

247 For both  $k=5$  and  $k=30$  days, in most cases, radially asymmetric copula families, such as Gumbel, Clayton,  
248 and Joe copulas, were identified as best explaining the dependence structure between  $A$  and  $K$  using the  
249 BIC criteria (Figures S.4a and S.4b). Based on the fitted copula model, linear trends in the probability of  
250 joint exceedances were estimated, and their spatial variability is shown in Figure 3. For  $k=5$  days, there  
251 have been significant increases in the joint probability of  $A$  exceeding its 100-year event ( $A_{100}$ ) and  $K$   
252 exceeding its 10-year event ( $K_{10}$ ) across the CONUS, particularly in parts of the states of California,

253 Washington, Idaho, Colorado, Nebraska, Minnesota, and in the northeastern regions (Figure 3a). Similar  
254 spatial patterns of such increases are observed for  $k=30$  days as well, but with denser clusters and  
255 greater magnitudes (Figure 3b).

256

#### 257 **4. Summary and Discussion**

258 We motivated the analysis of the joint trends in annual maximum daily rainfall and the antecedent  $k$ -day  
259 rainfall from the perspective that these two variables jointly determine flood potential. The potential  
260 failure of a large number of aging dams in the United States by overtopping under a changing climate is  
261 the driving practical concern. To address this, one would need an analysis of the daily inflows into each  
262 of the more than 90,000 reservoirs, and information on their flood operating rules, to estimate the flood  
263 volume that could lead to overtopping. Such information is not forthcoming. Consequently, using these  
264 two rainfall variables as a proxy became necessary. The general framework followed was to consider a  
265 nonstationary, probabilistic model of the univariate and joint exceedance probabilities of the annual  
266 maximum daily rainfall and the antecedent  $k$ -day rainfall across the country. Using this analysis, one  
267 could identify regions with increasing trends in the rare events associated with both the annual  
268 maximum daily rainfall event and the antecedent rainfall. Where these are statistically significant, there  
269 may be increasing concern for the potential overtopping of dams. We developed a model for the  
270 purpose, and provide results for selected return periods and durations of antecedent rainfall. The model  
271 includes a consideration of the dependence between the annual maximum daily rainfall and the  
272 antecedent  $k$ -day rainfall. Where this dependence is high, the underlying synoptic meteorology is prone  
273 to persistent periods of rainfall that culminate in an extreme rainfall event. This is an area of concern,  
274 especially where both types of rainfall have positive trends.

275 Our analysis of trends in the annual maximum 1-day precipitation ( $A$ ) and the total precipitation for  $k$   
276 days preceding the annual maximum ( $K$ ) revealed that the average magnitude of  $A$  has been increasing  
277 across the eastern half of the CONUS, while  $K$  has been decreasing, on average, in most places in the  
278 CONUS, except for regions near the states of Wyoming, Idaho, and Montana. These stark differences  
279 between the spatial trends in  $A$  and  $K$  may partially explain why flood magnitudes have shown unclear  
280 trends despite the significant increase in precipitation extremes across the CONUS (Archfield et al.,  
281 2016; Slater & Villarini, 2016). Trends in the univariate extremes of  $A$  and  $K$  were also explored in terms  
282 of the 10-year and 100-year events. The rainfall associated with the 10-year and 100-year return levels  
283 of the daily annual maximum has been increasing in general across the CONUS. For the preceding period  
284 rainfall, the 10-year and 100-year return levels have increased in many places in the CONUS, but their  
285 spatial patterns were more fragmented. The probability of annual maximum daily precipitation event  
286 exceeding its 100-year return level following a  $k$ -day antecedent precipitation total greater than its 10-  
287 year return level has been increasing across multiple areas in the CONUS.

288 The seasonality of precipitation varies across the country, as do the dominant mechanisms of rainfall.  
289 Since our focus was a national scale characterization of the changing risk of the joint increase in  
290 antecedent and annual maximum daily rainfall, we have not explored the details of the changes in  
291 synoptic conditions to see whether the frequency and persistence of the meteorological factors  
292 responsible for extreme rainfall have changed. Since the correlation of the  $k$ -day and the annual  
293 maximum day rainfall does not appear to change with time anywhere in the country, one may speculate  
294 that the mechanism associated with the wet spells that culminate in the annual maximum daily rainfall  
295 event has not changed. However, there are indications that the amount of rain associated with this  
296 mechanism has increased for both types of rainfall in many parts of the country. Even where the  
297 antecedent  $k$ -day rainfall has decreased, its variance has increased. As a result, the trends in the  
298 magnitude of the  $T$ -year event ( $T=10$  and 100) show an increase in most of these locations. There are

299 many more significant trends in the  $k$ -day rainfall than in the annual maximum daily rainfall over the  
300 past 43 years. This is also interesting since the increased antecedent rainfall would correspond to a  
301 higher runoff potential for even a relatively modest rainfall event and lead to reservoir full conditions  
302 that would be a concern for dam overtopping. This observation is consistent with the observed recent  
303 dam failure events that have typically not been associated with catastrophic daily rainfall.

304

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312

### 313 **Data Availability**

314 The Climate Prediction Center's (CPC) Global Unified Gauge-Based Analysis of Daily Precipitation (CPC-  
315 Global) dataset may be obtained from NOAA PSL, Boulder, Colorado, USA, from their website at  
316 <https://psl.noaa.gov/data/gridded/data.cpc.globalprecip.html>.

317

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379 [state-wire-dams-f5f09a300d394900a1a88362238dbf77](https://apnews.com/article/ne-state-wire-us-news-ap-top-news-sc-state-wire-dams-f5f09a300d394900a1a88362238dbf77)

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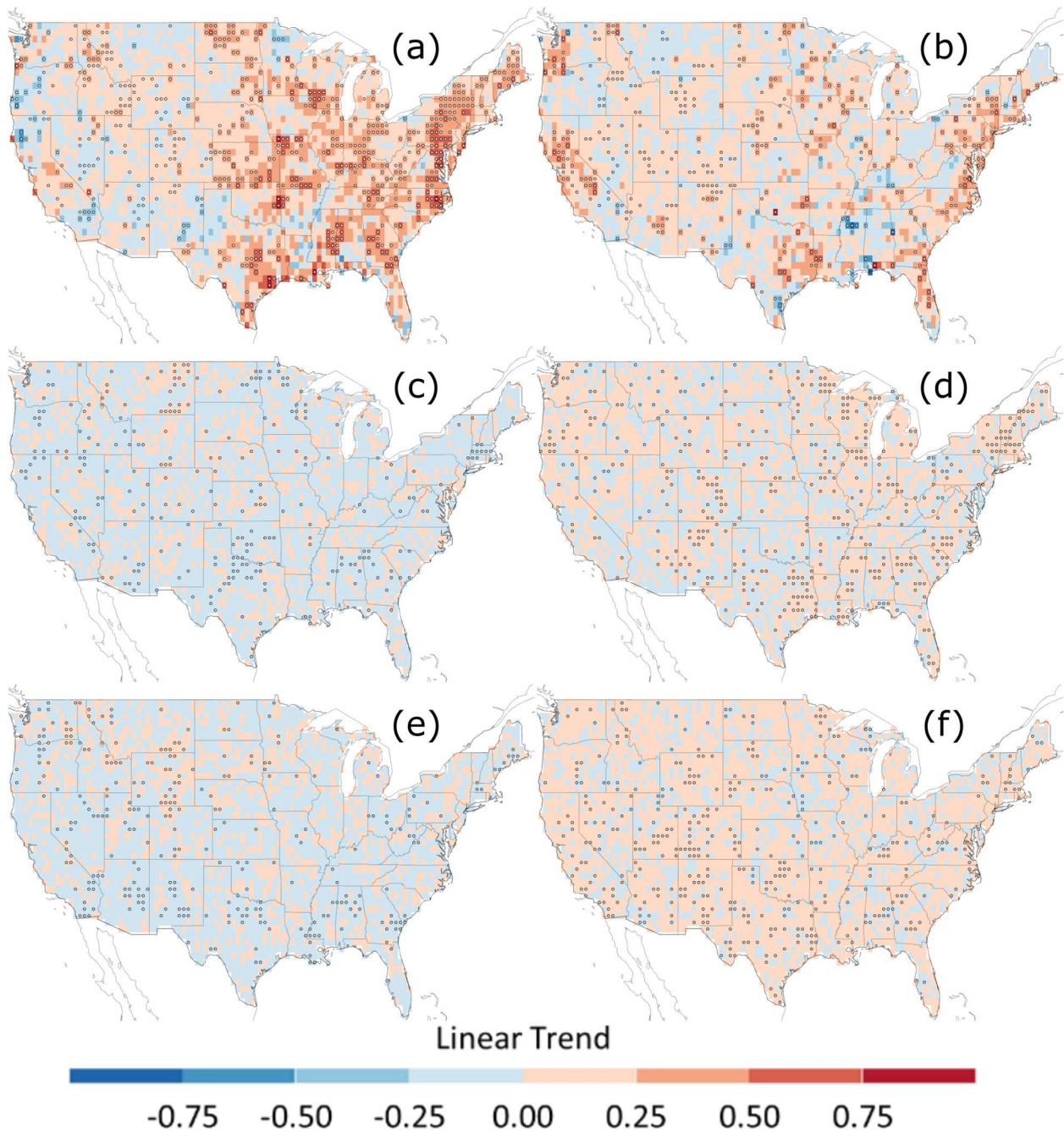
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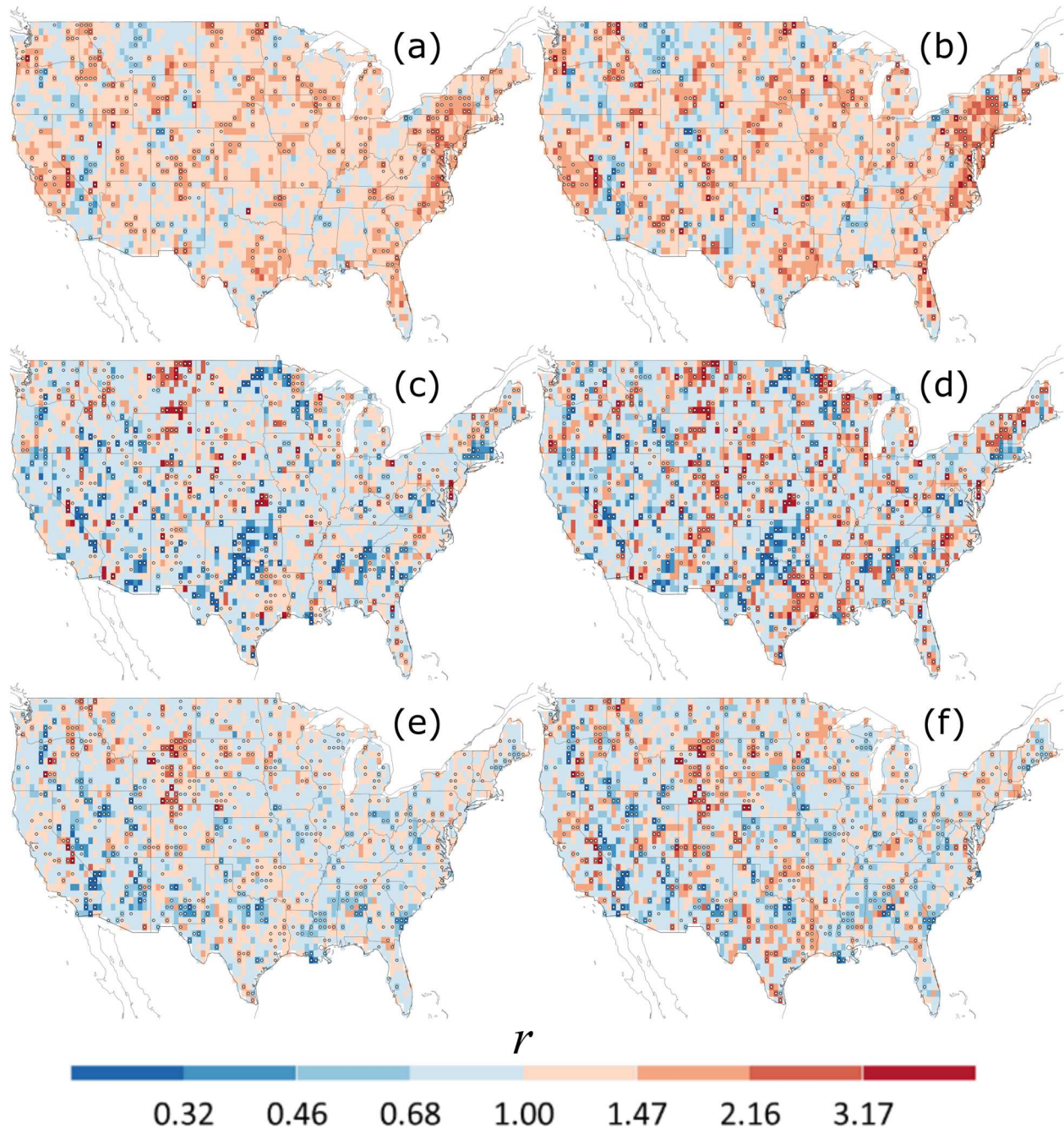


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461 **Figure 1.** Spatial trends in the (a) location parameter of A, (b) scale parameter of A, (c) location  
 462 parameter of 5-day K, (d) scale parameter of 5-day K, (e) location parameter of 30-day K, and (f) scale  
 463 parameter of 30-day K. Statistically significant estimates ( $p$ -value < 0.05) are represented with white  
 464 circles. The colors indicate the linear slope of estimated trends.

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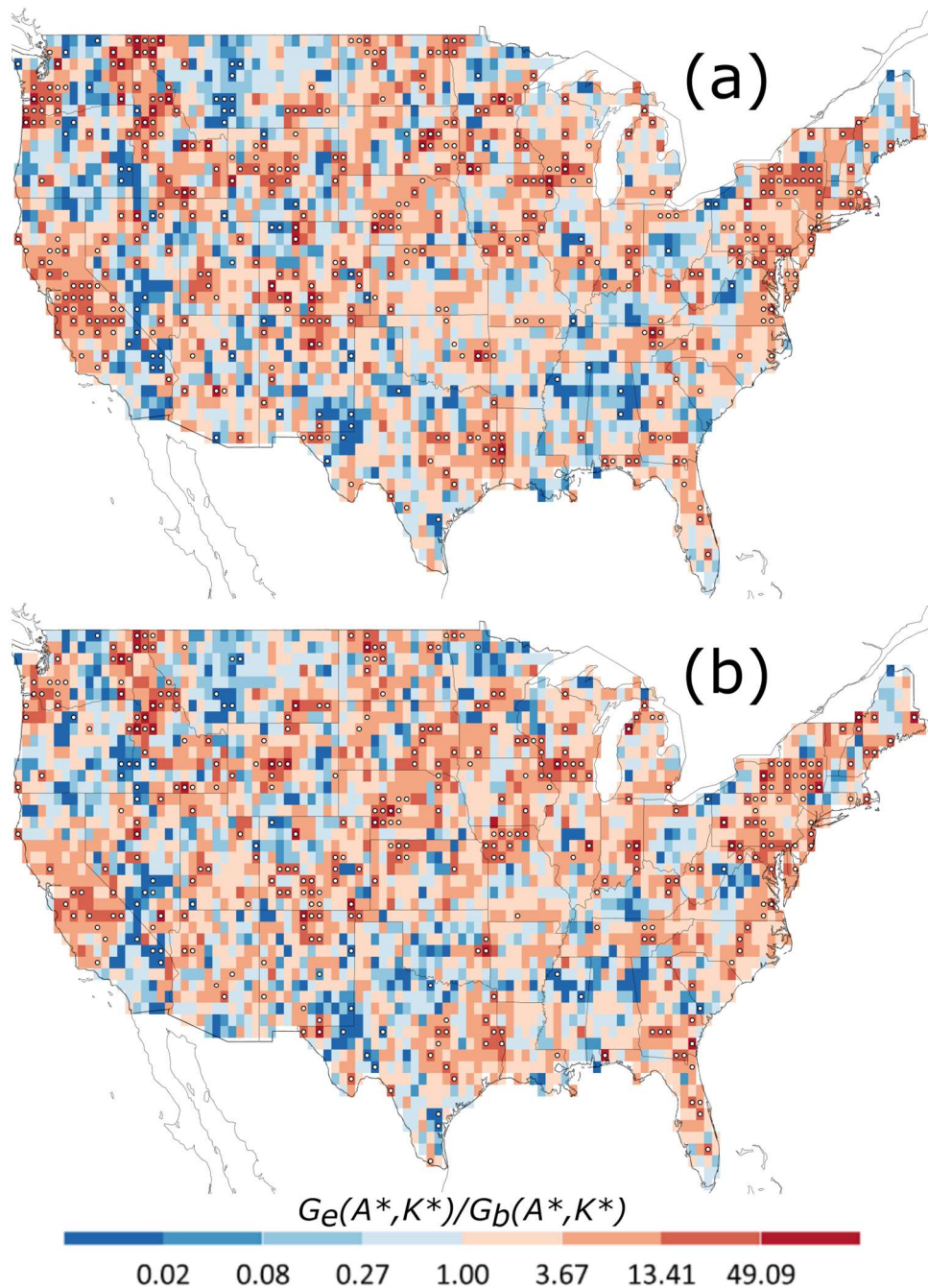
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468 **Figure 2.** Spatial trends in the 10-year return level of (a)  $A$ , (c) 5-day  $K$ , and (e) 30-day  $K$  and 100-year  
 469 return level of (b)  $A$ , (d) 5-day  $K$ , and (f) 30-day  $K$ . Statistically significant estimates ( $p$ -value  $< 0.05$ ) are  
 470 represented with white circles. The color indicates the ratio ( $r$ ) of the return level at the end of the given  
 471 period to the return level at the beginning. Details of  $r$  are presented in Equation (8).

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476 **Figure 3.** Spatial trends in the probability of joint exceedances of  $A$  and  $K$ , i.e., joint occurrence of annual  
 477 maximum daily precipitation event exceeding its 100-year return level following a  $k$ -day precedent  
 478 precipitation total greater than its 10-year return level, for (a)  $k=5$  and (b)  $k=30$ . Statistically significant  
 479 estimates ( $p$ -value  $< 0.05$ ) are represented with white circles. The color indicates the ratio of the  
 480 probability at the end of the given period to the probability at the beginning. Details of the ratio are  
 481 presented in Equation (11).