Separating Internal and Forced Contributions to Near Term SST Predictability in the CESM2-LE

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Abstract. An open question in the study of climate prediction is whether internal variability will continue to contribute to prediction skill in the coming decades, or whether predictable signals will be overwhelmed by rising temperatures driven by anthropogenic forcing. We design an interpretable neural network that can be decomposed to examine the relative contributions of external forcing and internal variability to future regional SST trend predictions in the near-term climate (2020-2050). We show that there is additional prediction skill to be garnered from internal variability in the Community Earth System Model version 2 Large Ensemble, even in a relatively high forcing future scenario. This predictability is especially apparent in the North Atlantic, North Pacific and Tropical Pacific Oceans as well as in the Southern Ocean. We further investigate how prediction skill covaries across the ocean and find three regions with distinct coherent prediction skill driven by internal variability. SST trend predictability is found to be associated with consistent patterns of interannual and decadal variability for the grid points within each region.

1. Introduction

Skillfully predicting both global and regional climate change on interannual to decadal timescales is an outstanding problem from both a scientific and societal standpoint [Findell et al., 2023]. Trustworthy forecasts on this timescale can provide actionable information about the future climate for various sectors affected by climate change [Solaraju-Murali et al., 2021; Kushnir et al., 2019; Dunstone et al., 2022]. However, making skillful forecasts on decadal timescales is a challenge because it requires both predicting the climate response to anthropogenic forcings like greenhouse gases and aerosols, as well as skillfully forecasting low frequency internal climate variability [Meehl et al., 2021]. For example, it has been argued that modulations in the rate of global mean surface temperature increase are associated with changes in the internal low frequency variability in the Pacific ocean so that even in the global mean, skillful temperature predictions require comprehensive understanding about internal variability [Trenberth and Fasullo, 2013; Labe and Barnes, 2022]. On regional scales, the amplitude of internal variability can be much larger relative to the forced response than on global scales, providing an even larger source of uncertainty in the range of variability [Lehner et al., 2020; Lehner and Deser, 2023]. Identifying and understanding predictable internal variability on regional scales is therefore an opportunity to provide stakeholders with improved estimations of the future range of variability.

Internal variability on interannual to decadal timescales can be predictable both in model simulations of the pre-industrial climate [Branstator et al., 2012; Gordon et al., 2021; Gordon and Barnes, 2022], and in hindcast simulations of the historical era [Meehl et al., 2016; Smith et al., 2019; Delgado-Torres et al., 2022]. It has been suggested that future, global scale variability may too be predictable for certain initial states [Labe and Barnes, 2022]. This predictability is generally associated with low frequency modes of variability, namely the Pacific decadal oscillation [PDO; Mantua et al., 1997; Newman et al., 2016] and Atlantic multidecadal variability [AMV Enfield et al., 2001]. However, prediction skill associated with internal variability is often sparse and limited to ocean heat predictability in mid-latitude ocean basins [Yeager et al., 2018]. Even with these limitations, it has been demonstrated that skillful sea surface temperature (SST) prediction can constrain predictions of surface climate evolution, for example temperature and precipitation over Europe [Simpson et al., 2019; Borchert et al., 2021a]. Therefore, studies have increasingly suggested studying “windows of opportunity” or state-dependent predictability to better leverage skill in decadal predictions [Merryfield et al., 2020; Mariotti et al., 2020; Brune et al., 2018; Borchert et al., 2018; Gordon and Barnes, 2022]. This framework focuses on identifying initial states or “windows” where the climate is more predictable, inherently acknowledging that predictability depends on the initial state of the system, and these “windows” provide the best opportunity to make skillful decadal predictions.

In the next 30 years, it is expected that forced warming from anthropogenic greenhouse gases will continue to increase. This raises the question of whether sources
of predictability identified in the historical climate will still contribute to skillful decadal predictions, as the large signal of forced warming could overwhelm predictable signals from internal variability. Here, we aim to investigate whether, and to what extent, internal variability contributes to near term decadal prediction skill in a relatively high future forcing scenario. We develop a novel neural network architecture that separately ingests information about the forced response and internal variability to predict the SST trend over the next 10 years. This architecture is then used to diagnose the contribution of internal variability to prediction accuracy, in order to identify regions where internal variability is a significant source of predictability in a near-future climate. We further address the question of where and when we can attribute prediction skill to internal variability in the presence of high anthropogenic forcing.

2. Data & Methods

2.1. Community Earth System Model Version 2 Large Ensemble, CESM2-LE

This study uses output from the Community Earth System Model Version 2 Large Ensemble (CESM2-LE) [Danabasoglu et al., 2020; Rodgers et al., 2021]. The CESM2-LE is a collection of 100 ensemble members of CESM2 run under the specified historical forcing for the Coupled Model Intercomparison Project Phase 6 [CMIP6; Eyring et al., 2016] for years 1850-2014, and the SSP3-7.0 future radiative forcing for 2015-2100 [O’Neill et al., 2016]. Note that ensemble members 1-50 use the biomass burning specified for CMIP6 however members 51-100 use a smoothed version which affects end-of-century warming [Fasullo et al., 2022]. The ensemble members are also designed to sample the phase of the Atlantic Meridional Overturning Circulation (AMOC) by splitting the full ensemble into five groups based on their initialized AMOC. We account for both the biomass forcing and AMOC initialization in our experiment design (see next section). We use sea surface temperature (SST) output bilinearly regridded to $5^\circ \times 5^\circ$ resolution, and coarsened to annual means at each grid point.

The target predictions in this work are classifications of future decadal SST trends, specifically whether a future trend in a particular region will fall in the lower, middle or upper tercile of the 2020-2050 distribution in that region (Figure 1b). We therefore calculate sliding (i.e. starting each year) 10-year linear least-squares trends over the years 2020-2050 in $10^\circ \times 10^\circ$ boxes in the ocean for each ensemble member. Figure 1a demonstrates the annual mean time series for a single ensemble member (blue curve) and the forced response (black curve) in a $10^\circ \times 10^\circ$ boxes in the Southern Ocean ($240^\circ$E - $250^\circ$E, $40^\circ$S - $50^\circ$S) over 1960-2100. SST trends for consecutive 10-year periods (green, orange and red lines) show that even though forced SST increases throughout the 21st century, regional internal variability can still contribute to reduced warming or even cooling in the later part of the 21st century. The distribution of decadal SST trends over 2020-2050 further demonstrates this point (Figure 1b), with trends in this particular grid box ranging from -1°C/decade to over 1.5°C.
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Figure 1. (a) CESM2-LE annual mean SST time series area averaged over 240°E - 250°E, 40°S - 50°S. The blue line is a single ensemble member (member 70) with gray lines indicating all other members. The black line is the forced response, defined as the ensemble mean. The green, orange and red lines are individual 10 year trends in SST in ensemble member 70, plotted every 10 years. (b) Distribution of SST trends (°C/decade) between 2020 and 2050 for all ensemble members at 240°E - 250°E, 40°S - 50°S. Color coding indicates the tercile cut-offs, green are in the lower third (or tercile) of the 2020-2050 distribution, orange in the middle third, and red in the upper third. (c) Schematic of the neural network architecture demonstrating the internal variability network (IV_Network) and external forcing network (EF_Network), and their summation to the Combined Network output.
2.2. Artificial Neural Networks

Artificial neural networks (ANNs) are used here to both make predictions of future decadal SST trend and also to investigate sources of predictability. We use ANNs because they are an established method of identifying sources of predictability on decadal timescales [Gordon and Barnes, 2022] and for predicting future trends in SST [Labe and Barnes, 2022]. In this application, neural networks can be considered a non-linear data driven model, taking information about the current and past state of the climate (the state of global SSTs) to make a prediction about a future quantity (regional decadal SST trends). Unlike some previous studies that use ANNs with post-hoc evaluation methods to examine their predictions and predictability [e.g. Labe and Barnes, 2022; Gordon and Barnes, 2022], we separate the prediction problem into an internal variability component and an external forcing component by designing two separate ANNs and only coupling them at the final prediction step of the network. This design allows for a direct investigation of the relative contributions of internal variability and external forcing to the ANN’s prediction. The external forcing component is defined as the ensemble mean across all ensemble members at each grid point, and the internal variability for a member is defined at each grid point as the full member minus the ensemble mean.

More specifically, we design two neural networks for the prediction task, named the EF Network and the IV Network (Figure 1c), which make predictions using only information about external forcing (EF) and internal variability (IV), respectively. The inputs to the neural networks are maps of global SST at 5° × 5° resolution. For the IV Network, we input two time-lagged maps of internal variability, the first, averaged over the 10 years prior to the prediction (τ = −1 to −10) and the second, averaged over 10 years and lagged by five years (τ = −5 to −14) (Figure 1c). These inputs provide the ANN with information about the current state of internal SST variability, and an earlier state, which gives information about the time evolution of internal variability before a prediction. The input to the EF Network is simply a map of the forced response (i.e., ensemble mean at each grid point) averaged over the 10 years prior to a prediction (τ = −1 to −10)(Figure 1c).

Each of the neural networks outputs a classification of the future SST trend (i.e. lower, middle or upper tercile) at a particular grid point, and these values are summed pair-wise (with no activation, weight or bias) to make the Combined Network prediction. This is demonstrated schematically in Figure 1c. The upper box shows the EF Network, with a single map of the externally forced SST input into an artificial neural network which outputs three values, EFa, EFb and EFc. The lower box is the IV Network, with two time lagged internal variability maps input into an ANN which also outputs three values, IVa, IVb and IVc. The outputs of the individual models are summed pairwise (EFa+IVa, EFb+IVb, EFc+IVc) to make the final predictions of the future SST trend over the next 10 years. We name this full system the Combined Network. The Combined Network’s prediction is taken to be the class with the highest value prediction in the final layer after the softmax activation function is applied. The softmax activation
function converts the raw ANN outputs to probability-like values. The inclusion of
the softmax activation means that higher value predictions correspond to higher ANN
confidence in the prediction such that predictions can then be ranked by their value.
For ease of comprehension, specific examples of predictions by the Combined Network
with contributions from the IV_Network and EF_Network is provided schematically in
Figure S1.

We subset the 100 ensemble members into 60 members for training data for training
the ANNs, 20 members for validation data for selecting the best performing networks,
and 20 members for testing which is “unseen” by the ANNs which is exclusively used
for performance evaluation and final analysis. The training, validation and testing data
is created by grouping individual ensemble members such that each data set equally
samples across the five AMOC initializations, and the two different biomass forcings
in the individual ensemble members. We use model years 1960-2100 for training the
ANNs, but only validate and test on 2020-2050. We use a wider span of model years
for training so the neural networks can “see” more possible internal variability states.
All results presented are from the testing set. We train 10 combined networks for each
10° × 10° grid box in the ocean and present results from the best network at each location,
but results do not qualitatively change if we instead use an average of networks. We
define “best” as the network that achieves the lowest loss on the validation data (not
shown). Further, detailed information about the hyperparameters and training process
is provided in the supporting information.

3. Results

3.1. Identifying Contributions to Prediction Skill

The Combined Networks skillfully predict SST trends over 2020-2050 (Figure 2a),
with the accuracy outperforming random chance (by design 33%) over most of the
globe. Furthermore, the highest neural network accuracy corresponds to regions
that are considered to be more predictable on decadal timescales: the North Pacific,
North Atlantic and Southern Indian Ocean [Meehl et al., 2021]. Recent literature
has emphasized the importance of identifying so-called “windows of opportunity” for
prediction skill on decadal timescales because this provides an indication of when
variability may be at its most predictable [Mariotti et al., 2020; Gordon and Barnes,
2022]. We therefore examine the existence the windows of opportunity in near-future
decadal predictions, adopting a similar method used by Mayer and Barnes [2021; Gordon and Barnes [2022] by designating windows of opportunity as the 20% of samples
that the Combined Networks assigned the highest confidence at each grid point (see
methods). Note that other cutoffs could also be used because neural network accuracy
increases with increasing confidence in prediction (see supplement Figure S2), however,
we choose 20% as this provides the clearest signal of accuracy increase. The 20% most
confident samples as designated by the neural networks generally have higher accuracy
than all predictions (Figure 2b) demonstrating that the neural networks have learned inputs that are more likely to lead to a correct prediction, and hence initial states that are more predictable. Skill improvements are especially evident in the North Pacific PDO region, the North Atlantic Ocean and broadly across the Southern Ocean which aligns with previous work that points to windows of opportunity for enhanced prediction skill existing in these regions [Gordon and Barnes, 2022].

We examine the contribution of internal variability to the Combined Network’s skill by using permutation importance testing [Breiman, 2001; McGovern et al., 2019] in Figure 2c. Permutation importance measures a deep learning model’s dependence on a certain predictor by scrambling that predictor while holding the others fixed and examining how the output is affected by the corrupted input data. Here, we test the sensitivity of the Combined Network’s skill to the internal variability input and assume a null hypothesis that internal variability does not increase prediction skill. We scramble the internal variability input pixel-wise (randomly drawing each pixel individually from its distribution in the testing set) to create a corrupt testing set and calculate the accuracy of the neural network on this data. This process is repeated 500 times for each grid box and we plot the mean accuracy of each neural network on the scrambled data (Figure 2c). The neural networks still perform well in some regions (Indian Ocean, Subtropical North Atlantic) when the internal variability input is scrambled implying that network skill is largely derived from the forced response in these regions. The difference between the total accuracy (Figure 2a) and the accuracy from the permutation importance testing (Figure 2c) provides the contribution of internal variability to the neural network’s skill (Figure 2e). We consider internal variability to significantly increase a network’s skill (reject the null hypothesis) if the network’s accuracy on the true testing set is greater than the 90th percentile of the accuracy on the scrambled data. Internal variability significantly contributes to the Combined Networks’s skill in the northern and eastern edge of the North Pacific and extending into the tropical Pacific (i.e. the PDO “horseshoe”). There is also enhanced prediction skill from internal variability in the subpolar North Atlantic. Internal variability in these regions has previously been shown to be predictable in studies of pre-industrial and historical climate [Gordon and Barnes, 2022; Meehl et al., 2021], but these results further imply that internal variability in these regions can provide predictability in the presence of relatively high anthropogenic forcing.

In conjunction with identifying windows of opportunity for improved prediction skill, studies have underlined the difficulty in attributing prediction skill during windows of opportunity to either internal variability, or time varying changes in anthropogenic forcing in the historical period [Borchert et al., 2021b]. We therefore use permutation importance to decipher to what extent internal variability contributes to prediction skill during windows of opportunity. First we calculate the skill of the 20% most confident predictions in the scrambled internal variability data (Figure 2d). We find skill increases in the Southern Indian and Atlantic Oceans even with scrambled internal variability input implying that internal variability did not contribute to the enhanced
skill during windows of opportunity in these regions. This increased skill is hence likely derived solely from the external forcing input. Notably, skill enhancements in the North Pacific, Tropical Pacific and some of the North Atlantic Ocean during windows of opportunity can likely be attributed to the networks learning predictable internal variability (Figure 2f). Furthermore, in regions where internal variability contributes substantially to prediction skill, enhancements during windows of opportunity are even larger than across all predictions. For example, the general accuracy increase provided by internal variability in the Tropical Pacific is approximately 5-8 percentage points (Figure 2e) but accuracy increases to up to 15 percentage points during windows of opportunity (Figure 2f).
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3.2. Internal Sources of Predictability over 2020-2050

Having identified regions where internal variability provides enhanced skill for SST trend prediction, we now examine how large-scale phenomena can lead to regional prediction skill in a future climate. We first isolate grid points where internal variability contributes significantly to prediction skill in 2020-2050 (i.e. regions un-stippled in Figure 2e). We then classify whether the IV_Network at each grid point was correct or incorrect for each test sample prediction. Four example IV_Network accuracy timeseries are demonstrated schematically in Figure 3a. We use K-means clustering to cluster these prediction outcome lists, resulting in clusters of grid points with correlated prediction skill. That is, where skill within a cluster is more likely to be associated with the same input pattern of variability. We choose six clusters as this number appeared a reasonable choice for this data (Figure S3) and plot the assigned clusters in Figure 3b. Three distinct spatial regions emerge: a Tropical Pacific cluster, a North Pacific cluster and a North Atlantic cluster (clusters 4, 5 and 6 respectively). These grid points are also well described by their respective centroids (Figure S3b and S3c). The remaining three clusters (clusters 1, 2 and 3) are not spatially distinct, and investigation into their sources of predictability are beyond the scope of this study. However, the underlying variability that leads to similar prediction skill within these clusters remains an intriguing avenue for future work. We choose to focus the remainder of this study on clusters 4, 5 and 6.

To investigate patterns of internal variability that correspond to common predictability within each cluster, we first compute the IV_Network accuracy within a cluster for each testing sample (i.e. percentage of grid points in the cluster that were correctly predicted) and isolate samples with cluster accuracy greater than 50% (i.e. more than 50% of grid cells within the cluster are correctly prediction for that sample). For example, Figure 4a and Figure 4d is the composite of input samples for which cluster accuracy in the North Pacific cluster is greater than 50%. We additionally separate the composites based on the predicted tercile within a cluster so that the opposing trend signals are not mixed in the composite. This distinction assumes that due to the spatial proximity of grid points within each cluster, that the correct target prediction will generally be the same.
In the North Pacific cluster (cluster #5), predictable upper tercile SST trends follow slightly positive SSTs in the PDO horseshoe 5-14 years before the prediction (Figure 4a) which appear to become more negative in the 10 years directly preceding the prediction (Figure 4d). This SST evolution likely leads to predictable upper tercile trends because the leading mode of decadal variability in the North Pacific, the PDO, acts on approximately a 10-20 year timescale [Newman et al., 2016]. Increasingly negative SSTs in the horseshoe region over a 15 year period are thus likely followed by warming SSTs in the next decade. Supplement Figure S4a shows the composite annual mean PDO index for the samples in this cluster, demonstrating the evolution of decreasing PDO index transitioning back to increasing PDO index over the input and prediction output window. We also suggest the opposite mechanism for predictions of lower tercile SST trends in the North Pacific cluster (Figure 4g and 4i), with strengthening positive SSTs in the horseshoe region over the input period leading to more predictable lower tercile SST trends. See Figure S4d for composite PDO index over this period. These results provide evidence that some SST trends that are lower than that of the forced response may be predictable in the near future, and predictable trends are associated with the decadal evolution of the PDO.

In the North Atlantic cluster, precursors to predictable positive SST trends appear to be a strengthening SST dipole between the North Atlantic subpolar gyre and subtropical North Atlantic, with subpolar gyre SST anomalies becoming more negative, and the subtropical SST anomalies becoming more positive (Figure 4b and 4e). This SST pattern is likely driven by a similar mechanism to that identified by Borchert et al. [2018], with strengthening positive SST anomalies in the subtropical Atlantic forming a predictable state for positive SST anomalies in the subpolar gyre. Supplement Figure S4b shows the composite SST evolution for the North Atlantic subpolar gyre for these predictions, supporting this theory. Predictable lower tercile SST trends in the subpolar gyre are preceded by strengthening positive SST anomalies in the 15 years before a prediction (Figure 4h and 4k). This positive anomaly is likely followed by a negative anomaly within the 10-year prediction window (Figure S4e), resulting in net negative SST trends following these initial states. Here we find that there are more samples in the upper tercile trend composite (132) than the lower tercile trend composite (38), implying that a warming trend in the subpolar gyre region may be more predictable than a cooling trend which aligns with previous findings [Borchert et al., 2018; Gordon and Barnes, 2022]. Furthermore, though these mechanisms leading to predictability in the North Atlantic have been studied previously, here we provide evidence that it may continue to be a source of predictability in the presence of relatively high anthropogenic forcing in the near future.

Lastly, the initial state that corresponds to correct predictions of upper tercile trends in the Tropical Pacific cluster (Figure 4c and f) appears to coincide with a strengthening El Nino like pattern in the central Pacific Ocean for the 15 year period preceding the prediction of positive trend, as equatorial Pacific SST anomalies strengthen from prediction lead years 5-14 (Fig. 4c) to lead years 1-10 (Fig. 4f). We
hypothesize that the ANN’s are forecasting a shift to La Nina in the early part of the 10-year prediction window as large El Nino events are often followed by a rebound to a La Nina within both observations and CESM2 [Planton et al., 2018; Capotondi et al., 2020]. This La Nina hence results in large negative SST anomalies in the tropical Pacific in the early part of the prediction window. The SSTs will then likely follow the approximate timescale of the El Nino Southern Oscillation (ENSO) cycle by growing into neutral conditions, and then likely another El Nino within the later part of the future 10-year period, resulting in a net positive trend over the forecast period. Supplement Figure S4c demonstrates the composite annual mean Nino3.4 index for the 10 years preceding and following the upper tercile predictions for samples in Fig 4c and 4f, showing a robust Nino3.4 decrease early in the prediction window, followed by a positive trend for the next decade. Conversely, a common initial state for predictable lower tercile SST trends for the ENSO cluster (Figure 4i and 4l) shows a strengthening La Nina-like cooling in the central Pacific over the preceding 15 years. Similar to the positive trend prediction, we hypothesize that the ANNs forecast a substantial El Nino early in the prediction window which dramatically increases tropical SSTs. These positive SST anomalies then decay to neutral conditions and a further La Nina event within the 10 year window (see supplement Figure S4f, like S4c, shows the composite annual mean Nino3.4 index for the preceding and following 10 years of predictions in the composite). This tropical SST evolution therefore results in a net negative trend prediction for grid points in the Tropical Pacific cluster (El Nino to neutral to La Nina).

4. Conclusion

This study demonstrates that internal variability is a source of predictability in the years 2020-2050 in the CESM2-LE, even with the relatively high anthropogenic climate forcing in the SSP3-7.0 scenario [O’Neill et al., 2016]. This result has interesting implications for future projections of regional climate change, as it implies that there may be some periods where SST trend predictions can be more skillful than just predicting the forced response. SST patterns like ENSO and PDO are associated with atmospheric teleconnection which affect temperature and precipitation over land, so any improved predictions of these patterns can potentially couple to improved future estimates of land surface processes [Mankin et al., 2020]. Furthermore, it is becoming clear that identifying windows of opportunity for improved prediction skill will continue to be a crucial method for making skillful near-term climate forecasts [Mariotti et al., 2020]. Our results further suggest that windows of opportunity for increased prediction skill will likely exist in a future with increased anthropogenic greenhouse gas forcing. Interestingly, in places where internal variability is a significant source of skill, correctly forecasting internal variability becomes even more important during windows of opportunity. The importance of internal variability during windows of opportunity reinforces the need to investigate predictable states of internal variability in the climate system as it likely provides the best opportunity for skillful decadal predictions.
Our findings may potentially aid in the communication of climate change and its impacts since internal variability modulates the forced climate change signal, particularly on regional scales. For example, there is still potential for continued warming and extreme events due to internal variability even after aggressive climate change mitigation efforts [Diffenbaugh et al., 2023]. Much of the public perceives climate change based on short-term, regional trends [Shao et al., 2016] so continued warming could harm continued mitigation efforts if previous efforts are perceived to have failed. With improved understanding of predictable internal variability, we can better attribute whether future variability stems from either successful mobilization against climate change, or irreducible internal variability.

**Code & Data Availability**

The CESM2-LE is available at the Climate Data Gateway [https://climatedata.ibs.re.kr/data/cesm2-lens](https://climatedata.ibs.re.kr/data/cesm2-lens). The code for this study is available on GitHub at [https://github.com/emily-gordy/Separating_EFIV_2020-2050.git](https://github.com/emily-gordy/Separating_EFIV_2020-2050.git).
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References


REFERENCES


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S1 Detailed Information About Training ANNs

The IV_Network is two SST maps (5184 pixels) densely connected to a hidden layer of 20 nodes, followed by a hidden layer of 40 nodes. This is densely connected to the output layer of 3 nodes. The hidden layers use rectified linear unit (ReLU) activation while the final layer has no activation. We also remove all bias terms from the IV_Network because this forces a zero input to be mapped to zero output (as we define zero IV input to be zero anomaly from the forced response). The EF_Network consists of an input map of the forced response (2592 pixels) connected to a single hidden layer of 10 nodes with ReLU activation, which is connected to an output layer of three nodes with no activation. The architectures differ between the two networks because we expect the internal variability task to be more complicated, whereas there is limited predictability that can be garnered from the forced response.

The outputs of each network are summed pairwise with no bias term and after summation, the softmax activation is added to convert the predictions to probability-like. We call the fully coupled system the Combined Network. The Combined Network is trained with categorical cross-entropy loss on the final predictions so that each component network must learn to correctly scale its contribution to the output. During training, we implement dropout at a rate of 0.2 between the hidden layers in the IV_Network. We also use ridge regularization of 0.01 on the inputs of the EF_Network and 0.0001 on the inputs to the IV_Network. The Combined Network is trained with Adam optimizer and an initial learning rate of 0.1 which steps down to 0.01 after 30 epochs and 0.001 after a further 30 epochs.

We use class weighting during training because we train on the full 1960-2100 period but the terciles are chosen from 2020-2050, meaning that the classes are not necessarily balanced in the training data. We weight each class by its relative size in the training data i.e. if the number of samples in each of the classes is 100/95/95 then they are weighted 1/1.05/1.05. If the sample weight is greater than 1.1 in this formulation then it is reduced by 10% to prevent any sample weights from becoming too large, e.g. if the classes are 100/95/80 then sample weighting would be 1/1.05/1.13 instead of 1/1.05/1.25 (since 1.25 × 0.9 is 1.13). This was found to be effective to prevent the ANNs from defaulting to a single class on unbalanced data. The neural networks are trained for a maximum of 1000 epochs with early stopping if the validation loss does not decrease for 100 epochs. This combination of inputs, outputs, architecture, and hyperparameters was found to perform flexibly across all grid boxes.
S2 Example ANN predictions

We provide three examples of ANN predictions in Figure S1. These predictions are all real predictions made by networks used in the study. All three examples are correct predictions. In Figure S1a, the IV_Network and EF_Network both predict the upper tercile node, by assigning the highest weight to this node. After the softmax activation (which conserves relative ranking) the upper tercile is therefore the prediction of the ANN.

In Figure S1b, the IV_Network and EF_Network make different predictions, with the IV_Network predicting the lower tercile, and the EF_Network predicting the upper tercile. However, once the networks are combined and softmax applied, the lower tercile has the highest weight meaning that it is the Combined Network’s prediction. In this case, the inclusion internal variability was the reason the Combined Network made the correct prediction, demonstrating how internal variability can provide future predictability, and these networks can be used to examine this.

Lastly (and most complexly, bear with us), in Figure S1c, the IV_Network and EF_Network make different predictions. This time however, the combinations work against each other to such an extent that after summation neither is the highest node, but instead the middle tercile is the winning prediction. In this example, the no single component network made the correct prediction, demonstrating the power of this technique to make synergistic predictions of the future.

S3 ANN confidence levels

Figure S2 demonstrates how neural network accuracy generally increases with increasing confidence in prediction, implying that the ANNs have learned which samples are more predictable than others. In the main text we include only the accuracy across all samples (Figure 2a = Figure S2a) and the accuracy for the 20% most confident (Figure 2b = Figure S2e). Here show the accuracy for three additional confidence cut-offs (80%, 60%, 40% = Fig. S2b, Fig. S2c, Fig. S2d). This indicates that while 80% was chosen in the main text as the cut-off, other confidence levels can be used to show the existence of windows of opportunity.

S4 K-means Robustness

Here we demonstrate several key metrics for checking the robustness of our K-means clustering in Section 3.2. Firstly, we note that the optimal choice of number of clusters can be tricky and vary based on the random state of the K-means algorithm. One way of deciding on choice of cluster number is using the silhouette score, which maximizes for the optimal number of clusters. Figure S3a demonstrates the silhouette score for initial state used in our cluster analysis, showing that six is the optimal number of clusters. Secondly, we note that although six is found to be best for the combination of the data and random state, this does not necessarily mean that all data points are well described by the learned centroids. We therefore plot both the distance from the cluster centroid at each grid point (Figure S3b), and correlation coefficient with the cluster centroid with each grid point (Figure S3). In both panels, lighter colors indicate grid points which are best described to the cluster center, either by closest distance (Figure S3b) or highest
Figure S1: Schematic of three example predictions of future SST trend at 20S-30S 60W-70W. Each panel demonstrates input maps, their predictions by the individual neural networks, and the final prediction before and after the softmax activation is added for actual samples from the testing set. Prediction year and ensemble member is given in each panel title. Grey shading indicates the winning prediction at each step in the neural networks. Pink box indicates the final output by the Combined Network.
correlation (Figure S3c). This demonstrates that the general regions we choose for close analysis in the main text (North Pacific, North Atlantic, and Tropical Pacific) are also best described by their cluster centroids.

S5 Composite Nino3.4, PDO and North Atlantic subpolar gyre evolution

We plot some climate indices to relate states of internal variability in Figure 4 to large scale variability. We calculate the PDO index (Figure S4a and S4d) by first removing the ensemble mean from each member. We then calculate the first EOF of North Pacific (20N-60N, 110E-120W) annual mean SST for the entire ensemble for the entire run (1850-2100). The corresponding principal component timeseries is defined as the PDO index. We define the North Atlantic subpolar gyre SST (Figure S4b and S4e) as the area weighted annual mean SST from 40N-60N, 80W-20W with the ensemble mean removed. Nino3.4 (Figure S4c and S4f) is calculated as the area weighted annual mean SST over 5N-5S, 170W-120W taken from each ensemble member with the ensemble mean removed.
Figure S3: (a) Silhouette score for 2-9 clusters. (b) Euclidean distance from the applicable centroid at each grid point. (c) Pearson correlation coefficient with applicable centroid at each grid point.
Figure S4: a. Annual Mean Nino 3.4 index for 10 years before up to 10 years after predictions of positive SST trend in the Tropical Pacific cluster. b. Annual mean PDO index for predictions of upper tercile SST trend in the North Pacific cluster. c. Annual mean North Atlantic subpolar gyre SST for predictions of upper tercile SST trend in the North Atlantic cluster. d., e. and f. as a, b. and c. but for lower tercile predictions.