Journal of Glaciology, Vol. 69, No. 279, 2024

Journal of Glaciology

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# Evidence that seismic anisotropy captures upstream palaeo 1 ice fabric: Implications on present day deformation at 2 Whillans Ice Stream, Antarctica 3 Justin LEUNG,<sup>1</sup> Thomas HUDSON,<sup>1</sup> John-Michael KENDALL,<sup>1</sup> Grace BARCHECK<sup>2</sup> 4 <sup>1</sup>Department of Earth Sciences, University of Oxford, Oxford, UK 5 <sup>2</sup>Department of Earth and Atmospheric Sciences, Cornell University, Ithaca, NY, USA Correspondence: Justin Leung <justin.leung@earth.ox.ac.uk> ABSTRACT. Understanding deformation and slip at ice streams, which are 8 responsible for 90 % of Antarctic ice loss, is vital for accurately modelling largescale ice flow. Ice crystal orientation fabric (COF) has a first-order effect on 10 ice stream deformation. For the first time, we use shear-wave splitting (SWS) 11 measurements of basal icequakes at Whillans Ice Stream (WIS), Antarctica, 12 to determine a shear-wave anisotropy with an average delay time of 7 ms and 13 fast S-wave polarisation ( $\varphi$ ) of 29.3°. The polarisation is expected to align 14 perpendicular to ice flow, whereas our observation is oblique to the current 15 ice flow direction ( $\sim 280^{\circ}$ ). This suggests that ice at WIS preserves upstream 16 fabric caused by palaeo-deformation developed over at least the past 450 years, 17 which provides evidence of the concept of Microstructural Fading Memory. 18 Our results imply that changes in the shape of WIS occur on timescales shorter 19 than COF re-equilibration. The "palaeo-fabric" can somewhat control present-20 day ice flow, which we suggest may somewhat contribute to the long-term 21 slowdown at WIS. Our findings suggest that seismic anisotropy can provide 22 information on past ice sheet dynamics, and how past ice dynamics can play 23 a role in controlling current deformation. 24

# 25 INTRODUCTION

Despite ice streams spanning only 10 % of Antarctica's surface area, they are responsible for 90 % of 26 Antarctic ice loss (Morgan and others, 1982). Therefore, studying ice stream rheology is important for 27 understanding Antarctica's contribution to sea-level rise. One source of uncertainty in ice stream dynamics 28 is the effect of ice fabrics on rheology, where ice with a crystal oriented fabric (COF) can be ten times 29 weaker in shear in a particular direction relative to isotropic ice (Budd and Jacka, 1989; Pimienta and 30 others, 1987). Glacial ice is formed of anisotropic grains with hexagonal crystalline symmetry, such that 31 the viscosity along the basal plane of ice (normal to c-axis) is sixty times less than that perpendicular to 32 it (Duval and others, 1983). Under stress, the c-axes in a bulk polycrystalline ice mass can rotate to form 33 an ice COF over timescales of hundreds of years, which can change in response to the stress it encounters 34 (Azuma, 1994). Hence, understanding ice COF provides insight on past deformation history and how it 35 might influence future ice flow. 36

Most glacial ice COF measurements are taken from microstructural analyses of ice core samples. However, these are usually measured from stable or slow-moving regions of ice sheets, and cannot provide much information of the physical processes in fast-deforming regions (Fan and others, 2021; Llorens and others, 2022). In contrast, seismic anisotropy measurements can be used to deduce ice COF properties over large areas in different ice settings, including ice streams (Smith and others, 2017). Therefore, seismic anisotropy can provide insight in these key fast-flowing regions, which can inform models of ice-sheet dynamics.

Whillans Ice Stream (WIS) is a major ice stream in West Antarctica that flows into the Ross Sea 43 embayment (see Figure 1; Picotti and others, 2015). The downstream portion of WIS is known as Whillans 44 Ice Plain (WIP), and it flows at a speed of over 300 metres per year, with stable sliding of the ice stream 45 punctuated 1-2 times daily by sudden unstable sliding motion during 30-minute slip events that also 46 produce high frequency icequakes and tremor (Barcheck and others, 2018; Bindschadler and others, 2003; 47 Winberry and others, 2013). Long-term slowdown of the ice stream can be seen, with longer periods of 48 quiescence between slip events over time, suggesting possibility of future stagnation (Winberry and others, 49 2014). WIS is an excellent area to study basal seismicity given that seismic and global navigation satellite 50 system data have been collected over recent decades at numerous sites to study its stick-slip cycle (e.g. 51 Barcheck and others, 2020; Pratt and others, 2014; Walter and others, 2011, 2015; Winberry and others, 52 2009, 2011) and basal hydrologic cycle (e.g. Fricker and Scambos, 2009; Siegfried and others, 2016). 53

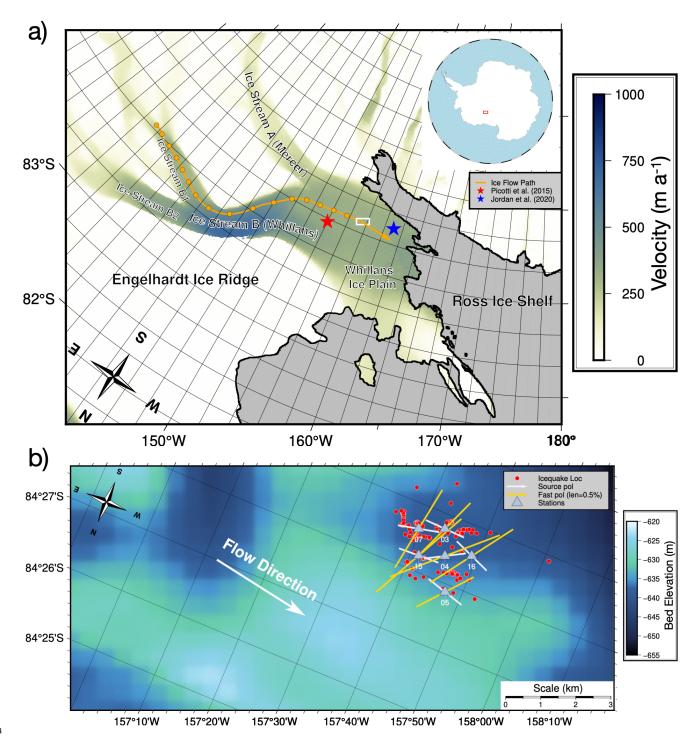


Fig. 1. Stereographic maps showing Whillans Ice Stream (WIS) and study location. (a) Regional map of the WIS. The grounding line is marked in the thick black line, and the grey shaded areas mark regions of floating ice. The blue and red star show the study site locations of Jordan and others (2020) and Picotti and others (2015) respectively. The orange line outlines the upstream flow path of the ice at our study site location, assuming current flow velocities, with orange points marking the locations at intervals of 50 years (see supplementary information for flow path calculation). The background colour map shows the ice flow velocity obtained from MEaSURES InSAR-Based Antarctica Ice Velocity Map, Version 2 (Rignot and others, 2017). The study area in (b) is outlined by the white box. (b) Detailed map of the study region. Stations are marked as blue triangles, and icequake locations are shown by red scatter points. Gold lines show the fast S-wave polarisation direction, with the length of the line representing the strength of anisotropy. White lines show the source polarisations for each event, as estimated from recorded shear waves. Dominant ice flow direction (280°) is indicated by the large white arrow. The background colour map shows the bed elevation Morlighem (2022).

There are currently few ice COF observations for the entire ice column at WIS. Picotti and others (2015) 56 used active seismic sources to suggest an azimuth-independent vertically transverse isotropic fabric (VTI) 57 at WIS, with a focus on the top 200 metres. Conversely, Jordan and others (2020) used electromagnetic 58 methods to argue that the c-axes orient parallel to flow at WIS by polarimetric radar sounding that 59 measured the top 400 metres of WIS (see Figure 1 for locations). Here, we provide the first seismic 60 anisotropy measurements from shear-wave splitting of basal icequakes of the entire ice column at Whillans 61 218 Ice Stream. 62

#### METHODOLOGY 63

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This study uses 319 icequakes recorded between January 20th and February 27th, 2014 by six seismometers 64 at Whillans Ice Plain, Antarctica, part of a network active between 2012 to 2018 (Barcheck and others, 65 2020; Schwartz, 2012). The ice at the study site is between 690 and 710 m thick (Barcheck and others, 2020) 66 and moving at  $\sim 370 \text{ m a}^{-1}$  (Morlighem, 2022). Since horizontal orientation of the instruments is important 67 for studying seismic anisotropy, we verified the orientation of these instruments using a teleseismic event. 68 We performed a manual search for icequakes focused within the duration of bidaily slip events at WIS, 69 described in Barcheck and others (2021). Icequake arrival times are picked manually and are located using 70 NonLinLoc, a probabilistic non-linear earthquake location algorithm (Lomax and others, 2000). Only 71 icequakes originating at the bed of the ice stream are of interest for measuring total anisotropy in the ice 72 column, therefore icequakes with a source depth shallower than 400 metres are removed. Each icequake is 73

<sup>74</sup> filtered by a 10-100 Hz bandpass filter, based on the dominant source spectra of the icequakes (see Figure

S1). Seismic anisotropy is analysed on the horizontal (north and east) components because a ~100 m thick
firn layer refracts the ray path of icequakes to near-vertical incidence at the surface (Picotti and others,
2015).

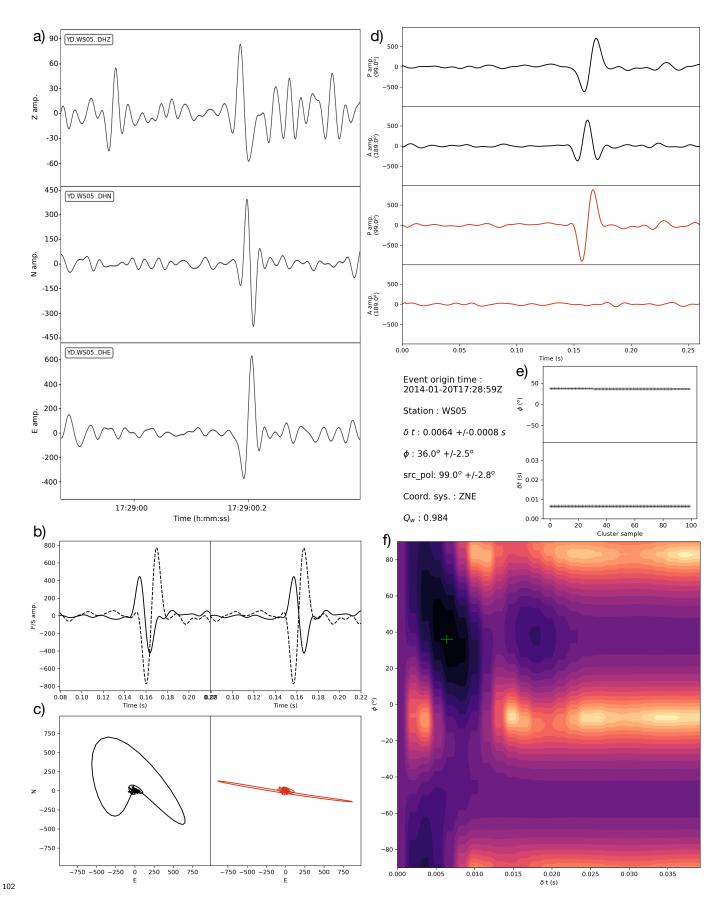
Shear-wave splitting (SWS) analysis is conducted using the python package SWSPy (Hudson and 78 others, 2023), based on the approach of Wuestefeld and others (2010). It can be summarised as follows: 79 First, a range of analysis time windows are defined because SWS measurements are sensitive to window 80 lengths (Teanby and others, 2004). Second, a grid search is performed over fast shear-wave polarisation 81 of -90°<  $\varphi \leq 90^{\circ}$  and delay times between fast and slow S-waves of  $0 \leq \delta t \leq 0.1$  for each window, such 82 that  $\varphi = 0$  represents a fast shear-wave polarisation in the north (and south) direction. The splitting 83 parameters,  $\varphi$  and  $\delta t$ , associated with the minimum second eigenvalue of the S-wave covariance matrix 84 that best linearize particle motion, describe the anisotropy observed along a given source-receiver ray path. 85 Third, density-based cluster analysis is performed on all optimal  $\varphi$  and  $\delta t$  values, such that the optimal 86  $\varphi$  and  $\delta t$  values are obtained from the most stable cluster with minimum variance in  $\varphi$  and  $\delta t$  (Ester and 87 others, 1996; Teanby and others, 2004). The source polarisation is then calculated by taking the azimuth 88 of the largest eigenvalue of the covariance matrix of the linearised waveforms (Walsh and others, 2013). 89

A well-constrained result after SWS correction is defined as satisfying the following four requirements: 90 (1) the particle motion (see Figure 2c) becomes approximately linear after removing splitting using the 91 optimal SWS parameters, (2) the error surface (see Figure 2f) has a unique, well-constrained solution, (3) 92 splitting parameters ( $\varphi$  and  $\delta t$ ) are stable (see Figure 2e) throughout different clusters, and (4) the quality 93 factor  $Q_w$  is larger than 0.7.  $Q_w$  measures the robustness of the splitting measurement, and it is calculated 94 by comparing the results from the eigenvalue method of Silver and Chan (1991) to the cross-correlation 95 method of Menke and Levin (2003). A value of  $Q_w = 1$  signifies a perfect match between the two methods, 96  $Q_w = -1$  a good null result, and  $Q_w = 0$  a poor result (Wuestefeld and others, 2010). 97

The strength of anisotropy  $(\delta V)$ , or the difference between fast and slow S-wave velocities, can be quantified by the change in velocity, derived from the delay time  $(\delta t)$ :

$$\delta V = (V \times \delta t \times 100)/r \tag{1}$$

where V = 1944 m s<sup>-1</sup> is the average isotropic shear-wave speed (Smith and others, 2017) and r the source-receiver distance.



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Fig. 2. An example of a well-constrained shear-wave splitting event. (a) Icequake signal before correction in the vertical, north and east component. (b) The waveforms before (left) and after (right) SWS correction, plotted in the fast (black line) and slow (dotted) directions. (c) Horizontal (north and east) particle motion before (left) and after (right) SWS correction. (d) Particle motion of icequakes in the source polarisation (P) and the perpendicular azimuth (A) before (top two) and after (bottom two) correction. (e) Optimal  $\varphi$  and  $\delta t$  for different cluster sizes. A good splitting measurement should have constant  $\varphi$  and  $\delta t$  values independent of cluster size. (f) Error surface plotted on  $\varphi$  vs  $\delta t$ . Larger errors are represented with brighter colours, and smaller errors with darker colours. The optimal  $\varphi$  and  $\delta t$  and its uncertainties are shown with the green symbol.

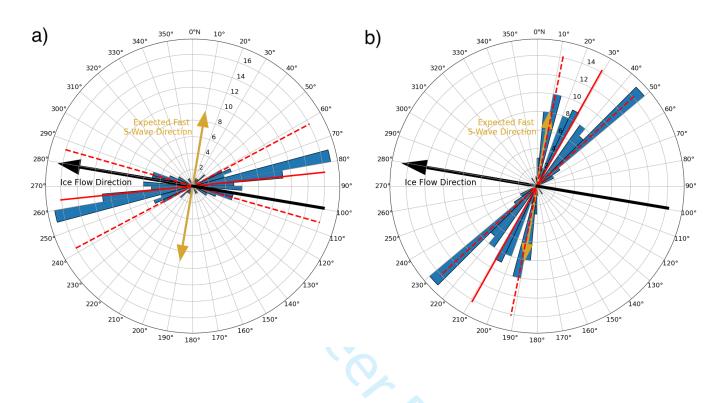
## 104 **RESULTS**

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80 results from 70 events fulfill the aforementioned four criteria, and therefore are chosen for further 105 analysis. The fast S-wave polarisation  $\varphi$  and source polarisation of these events are plotted as polar 106 histograms in Figure 3. For a double-couple icequake source associated with ice slip at the bed, S-wave 107 source polarisation is aligned with the direction of slip (Hudson and others, 2020). One might typically 108 expect the average S-wave source polarisation to align approximately with ice flow direction. Most source 109 polarisation measurements lie approximately in the east-west direction with an average of  $264^{\circ}N \pm 22^{\circ}$ 110 (see Figure 3a), which is in agreement with the Whillans Ice Stream's flow direction of  $280^{\circ}N \pm 2^{\circ}$  (Rignot 111 and others, 2017). 112

The average delay time for these results is 7.1 ms and ranges from 1.6 ms to 19.2 ms. The average strength of anisotropy,  $\delta V$ , is ~1.5 %, with a maximum of 2.8 %. This is below the maximum directional variation in S-wave velocities of single ice crystals of 12 % (Lutz and others, 2020).

The shear-wave splitting measurements have an overall mean fast S-wave direction ( $\varphi$ ) of 29.3°N ± 18° 116 (see Figure 3b). The uncertainty in this result is defined as one standard deviation, likely representing an 117 upper estimate of uncertainty in the result that could be caused by temporal variations in  $\varphi$  (see Figure 118 S2). Individual receivers generally have mean  $\varphi$  that fall within a range of 22.4°N to 47.0°N (see Figure 119 1b), with the exception of station WS07, which has a mean  $\varphi$  of 9.1°N (see label 07, Figure 1b). Ice 120 core studies (Lipenkov and others, 1989; Wang and others, 2002; Weikusat and others, 2017) and seismic 121 anisotropy studies (Kufner and others, 2023; Smith and others, 2017) have found that regions of longitudinal 122 extension, such as ice divides and ice streams, have a vertical girdle fabric. In such fabrics,  $\varphi$  is found to 123 be perpendicular to the ice flow direction (Harland and others, 2013). Based on ice flow direction derived 124 from InSAR (Rignot and others, 2017) and the source polarisation data in Figure 3a, one would expect  $\varphi$ 125



**Fig. 3.** Rose diagrams of (a) source polarisations and (b) fast S-wave directions for all the 80 SWS measurements. The solid and dotted red lines indicate the averages and uncertainties respectively. The gold arrows on both diagrams indicate the expected fast S-wave direction based on ice flow direction, which are shown as black arrows (see main text for further details). Method for estimating uncertainty is included in the supplementary information.

 $\sim 10^{\circ}$ N at the Whillans study site (golden arrow, Figure 3). However, the mean  $\varphi$  we observe of 29.3°N  $\pm 18^{\circ}$  is oblique to this expected fast S-wave direction of  $\sim 10^{\circ}$ N, even after accounting for uncertainty. A t-test shows that the 95 % confidence interval of the fast S-wave directions lies in between 25.3°N and 33.3°N (assuming that the distribution of fast S-wave directions in the data is Gaussian), confirming our confidence in this obliquity.

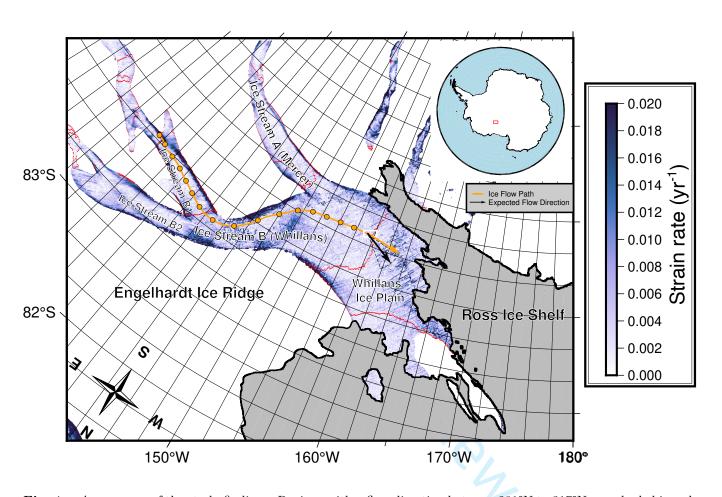
## 131 DISCUSSION

#### <sup>132</sup> Possible origins of an ice COF with an oblique fast S-wave direction

<sup>133</sup> Our results suggest that the ice COF at Whillans Ice Stream (WIS) is oriented oblique, rather than <sup>134</sup> perpendicular, to the ice flow direction. This obliqueness suggests one of two hypotheses: either that the <sup>135</sup> local strain at our study site acts oblique to ice flow; or that the ice COF at WIS is the result of preservation <sup>136</sup> of historic deformation upstream of the study site.

Regarding the first hypothesis, a possible reason for extension oblique to ice flow is the differential ice 137 flux between the two tributaries of Whillans Ice Plain (WIP) across a suture zone. The study site is located 138 downstream of the confluence between the upper WIS and Mercer Ice Stream (MIS), where the faster flow 139 of WIS relative to MIS leads to shear strain across the suture zone, which can reorientate ice crystals (see 140 Figure 4; Beem and others, 2014). However, Bindschadler and others (1987) argue that shear is minimal 141 between WIS and MIS. Additionally, we postulate that this suture zone has a negligible effect on the ice 142 COF at our study site because the significant mixing between the two ice streams in the suture zone would 143 perturb the ice fabric on length scales of the order of hundreds of metres. This mixing would likely yield 144 significant differences in the fast-polarisation S-wave azimuth ( $\varphi$ ) between the different stations, yet the 145 fast-polarisation S-wave azimuths remain constant within uncertainty across the network (see Figure 1b) 146 and a dominant fast polarisation direction can be seen in Figure 3b. Nonetheless, even if our ice COF were 147 to be affected by this shearing, the suture zone is located upstream of our study site (see high strain rates 148 near the intersection of WIS and MIS in Figure 4) and therefore also supports the second hypothesis. 149

We instead favour the second hypothesis: that WIS has a "palaeo-COF" that preserves a record of WIS' 150 upstream palaeo-deformation. Ice core studies and numerical simulations suggest that such preservation 151 of a palaeo COF is possible (Faria, 2018; Llorens and others, 2022). This can be explained by the concept 152 of Microstructural Fading Memory, where polycrystalline ice temporarily inherits signatures from its past 153 microstructure that are progressively erased over a certain relaxation time (Faria, 2018). In the case of 154 WIS, this past microstructure is the remnant of upstream palaeo-deformation, such that the COF still 155 has not reoriented towards or re-equilibrated with the local principal compression direction. Most of the 156 ice deformation at WIP occurs along the shear margins (Truffer and Echelmeyer, 2003) and ice flow is 157 mainly accommodated by basal sliding, so internal deformation at Whillans is low but still existent. In 158 such flow regimes, lattice rotation plays an important role relative to dynamic recrystallisation in ice fabric 159



**Fig. 4.** A summary of the study findings. Regions with a flow direction between 281°N to 317°N, are shaded in red. The orange arrow shows the present-day flow direction. The black arrow indicates the flow direction inferred from the fast S-wave polarisation direction, and the dashed black sector outline shows the range of azimuths expressed by the red shaded regions. The background colour map is the strain rate calculated using Rignot and others (2017)'s velocity map (see supplementary information for calculation). Other features shown in this map are as in Figure 1a. The azimuth of the strain rate is shown in Figure S3.

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evolution (Azuma, 1994; Fan and others, 2021). The c-axes of the ice crystals always rotate towards the 160 principal direction of compression, which in ice streams is the azimuthal direction perpendicular to the flow 161 direction (Smith and others, 2017; Thorsteinsson and others, 2003). The meandering nature of WIS alters 162 the direction of compression, and therefore the ice COF, which we hypothesise in WIS evolves based on c-163 axis rotation, represents an integrated history of upstream strain induced by this changing stress. As such, 164 it is difficult to pinpoint the origin of the fabric formation. However, for the ice COF to have developed 165 the observed oblique  $\varphi$ , part of the integrated strain history must have originated from upstream areas 166 in the ice stream where the flow direction was perpendicular to  $\varphi$ . Considering the present-day westward 167 flow direction only and fast S-wave polarisation uncertainties of 18°, these regions have a flow direction 168 approximately in the west-northwest direction of 281°N to 317°N (see shaded red regions in Figure 4). 169 The nearest region with such a flow direction along the ice flow path is in the southern tributary of WIS, 170 indicating that the ice COF could not have been purely derived from the integrated strain alone over the 171 past 450 years. Consequently, this implies that the entire ice stream flow field of WIS changes on timescales 172 shorter than ice COF re-equilibration. With this observation, we assumed constant flow directions with 173 time because ice-flow chronological studies do not suggest major changes in flow direction at WIS over the 174 past 500 years (Catania and others, 2012). Furthermore, the validity of this assumption does not affect our 175 conclusion of a palaeo-COF at WIS because present-day ice velocity orientations are insufficient to explain 176 the observed  $\varphi$ . 177

Larger strain rates can accelerate the rotation of lattices, which reduces the re-equilibration timescales 178 of ice fabrics and causes the COF to inherit signatures of the local strain field. Therefore, the integrated 179 strain history better preserves the fabric along flow where the strain is greater. From present-day velocities, 180 the largest strain rates are located on the main trunk of WIS before it merges with the MIS (see Figure 181 4). However, these strain rates could have been different in the past because of the dynamic nature of ice 182 streams. Some studies show that ice streams in the Ross Sea sector have variable mass fluxes over the 183 past centuries, in particular the Kamb Ice Stream (Bougamont and others, 2015; Catania and others, 2012; 184 Conway and others, 2002). Further studies of ice anisotropy, in combination with more detailed past ice 185 conditions and flow calculations, would further evidence any dynamic changes in ice anisotropy along WIS. 186 Given that the expected  $\varphi$  based on current ice flow is only just outside the uncertainty of our results, 187

we cannot ignore the possibility of an ice COF derived from the present-day study site. However, there is only a negligible part of the study area that has a flow direction between 281°N and 317°N, with the remainder of this region located downstream of the study site (see red shaded regions in Figure 4). Hence, it is unlikely that enough time elapses for the ice COF to re-equilibrate with the present-day flow direction. We therefore suggest that the ice fabric is most likely derived from upstream palaeo-deformation.

#### <sup>193</sup> Comparison to other COF studies at WIS

Our results of an oblique fast S-wave direction ( $\varphi$ ) differ from previous findings of an azimuth-independent fabric (Picotti and others, 2015) and a fabric with  $\varphi$  parallel to flow between 170 m and 400 m depth (Jordan and others, 2020). We attribute these differences to variations in sampling location and depth (see Figure 1a).

Jordan and others (2020) find two types of vertical girdle fabrics at different depths: a fabric with  $\varphi$ 198 perpendicular to flow for ice up near the surface, and another fabric with  $\varphi$  parallel to flow up to 360 199 m deep. The former fabric agrees with our results, while the latter suggests a longitudinally compressive 200 instead of longitudinally extensional stress regime, where compression and extension is defined as the 201 principal compression axis being parallel and perpendicular to flow respectively. Because their study was 202 conducted near the grounding line (see Figure 1a), we attribute the second girdle fabric ( $\varphi$  parallel to 203 flow) to the influence of longitudinal compression due to stronger interactions between the ice and the bed 204 topography near the grounding zone (Bindschadler and others, 1987; Picotti and others, 2015). If both 205 fabrics are present in the ice column at our study site, then as we only invert for a single anisotropic layer, 206 both fabric orientations would be represented as a single, composite result. If two perpendicular fabrics 207 are present, then any shear-wave splitting measurements would be unable to discriminate between the 208 layers, with the anisotropy amplitude (delay-time) being damped or amplified, but the overall orientation of 209 anisotropy remaining constant. Other studies have suggested that the stress regime at WIP is longitudinally 210 compressive (Bindschadler and others, 1987). However, this likely does not apply to our study site. Firstly, 211 the strain rates at WIS vary massively as little as 20 kilometres (see Figure 9 of Bindschadler and others, 212 1987). Secondly, the ice flow path inferred from present-day velocities indicates that the ice at our study site 213 has travelled along the outer part of the curve at WIP, where we expect the stress regime to be longitudinally 214 extensional (see Figure 4). Because most of the vertical shear needed to accommodate the driving stress 215 at WIS occurs within the basal sediment layer (MacAyeal, 1989), we expect the velocity orientation to 216 be similar across all depths of the ice stream. Thirdly, the ice at our study site is located sufficiently 217 far from the grounding line, such that it should not experience significant longitudinal compression from 218

interactions between the ice and grounding line bed topography (Pattyn, 2000).

Picotti and others (2015) observe an azimuth-independent fabric across the entire ice column, and 220 suggest that ice streams with low basal shear stress and highly-water-saturated sediments have COF 221 profiles similar to ice divides due to the increasing influence of vertical compression relative to transverse 222 compression. However, most of their study is based on surface wave data and travel-time inversions 223 that could only image the fabric up to 200 m at WIS. Furthermore, their study site is located above 224 Subglacial Lake Whillans, which is further inwards of the curve at WIP, where the stress regime is less 225 longitudinally extensional (see Figure 1a). Additionally, their ice COF is likely to have undergone more 226 equilibration caused by higher strain rates and lower flow velocities on the northern side of WIS (see Figure 227 4; Bindschadler and others, 1987). Given this variance in ice COF in WIS, future studies of ice deformation 228 and anisotropy can furthermore reveal the spatial and temporal variability of ice COF at WIS. 229

### <sup>230</sup> Comparison to other ice streams

Shear-wave splitting studies from another Antarctic ice stream, Rutford Ice Stream (RIS), find that the 231 COF at RIS is approximately perpendicular ( $\sim 85^{\circ}$ ) to ice flow (Harland and others, 2013; Smith and others, 232 2017). Unlike the deviatoric nature of WIS stream flow, the flow direction at RIS is approximately linear 233 over COF re-equilibration timescales. As such, it is not possible to discriminate to what extent the COF 234 at RIS represents the current deformation or a preserved upstream deformation state. Kufner and others 235 (2023) suggest that the RIS COF signal is dominated by the latter. The strength of anisotropy, effectively 236 a measure of the strength of the ice COF, at RIS is 3-5 %, while that at WIS is 1.5 %, suggesting that 237 internal deformation is lower at WIS than RIS. This is consistent with findings that ice flow at WIS is 238 mainly accommodated by lateral shearing at the margins and basal sliding, where the vertical shear strain 239 rates required to support the driving stress are mostly confined within a weak basal till layer, and not 240 within the ice itself (Blankenship and others, 1986; MacAyeal, 1989; Truffer and Echelmeyer, 2003). 241

A recent seismic anisotropy study at RIS by Kufner and others (2023) suggested that multi-layer anisotropy can be present in ice streams, where the deepest third of the ice stream is thought to comprise an azimuthally isotropic cluster fabric caused by basal shearing (Azuma, 1994). However, the apparent absence of multiple fast S-wave phase arrivals in our data suggests that the effects of any multi-layer anisotropy at WIS are negligible, to which here we define multi-layer anisotropy as a type of depth-dependent anisotropy with sharper changes in anisotropic signatures with depth. Indeed we did not observe sufficient hints of

multi-layer splitting to invert for multiple layers, even though such an inversion is possible at ice streams (Hudson and others, 2023). Inverting for a multi-layer anisotropic model at WIS would introduce additional parameters on layer thicknesses and fast polarisation directions, which could result in overfitting of the data, compared to a single depth-integrated anisotropy model.

Because most of the vertical shear at WIS is accommodated within the basal sediment layer (MacAyeal, 252 1989), we would expect the surface velocity direction to represent the orientation of maximum strain with 253 depth, except perhaps for a thin (1 to 10s metres) basal shear layer near the ice-bed interface, which could 254 vary somewhat in orientation over short length scales (10s to 100s metres) due to local bed topography 255 variations. The depth of ice affected by shearing will either be too thin to be observed in seismic lengthscales 256 or too weak to affect the overall anisotropic signature of the ice stream (Bindschadler and others, 1987: 257 Blankenship and others, 1986). Additionally, even if the shear zone were to exhibit strong anisotropy, the 258 cluster fabric that would likely result is azimuthally isotropic and therefore has little effect on our results of 259 a preferred c-axis azimuth. In summary, we therefore would expect the dominant anisotropy to be oriented 260 relative to surface ice flow velocity. 261

# <sup>262</sup> Implications of an oblique ice fabric on ice flow

The effective viscosity for compression and extension is higher along the basal plane. As seen in RIS, where 263 the horizontal c-axis is oriented perpendicular to flow, the effective viscosity is higher along flow than across 264 flow (Jordan and others, 2022; Kufner and others, 2023). This hardening along the flow direction, which 265 is perpendicular to the c-axes and parallel to the basal plane, is thought to increase the viscosity by an 266 order of magnitude relative to isotropic ice (Kufner and others, 2023). However, our results at WIS show 267 a c-axis orientation that is not perpendicular, but oblique to ice flow or equivalently a misalignment of 268 the basal plane with the flow direction. Because the basal plane is associated with directions of highest 269 effective viscosity, this misalignment implies that internal deformation will be resisted more at WIS if the 270 c-axis direction re-equilibrates with the local principal stress direction. The internal deformation in WIS 271 might be minimal today, but it may become important in the future. Firstly, the long-term slowdown 272 in WIS has been associated with basal strengthening, especially in the upper portion of the ice stream 273 (Beem and others, 2014). If the driving stress is somehow sustained, then a lower proportion of this stress 274 could be accommodated by the basal till and a higher proportion through internal deformation. Secondly, 275 the deceleration results in increased duration between periods of slip events at WIS, which is expected to 276

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<sup>277</sup> increase the significance of internal viscous deformation (Winberry and others, 2014).

Our observations also suggest that palaeo ice COF can somewhat control present-day ice flow. If 278 the shape of an ice stream deviates on length scales less than the distance ice travels within the COF 279 re-equilibration time, then the COF may not be aligned with ice flow, limiting the effective viscosity of 280 the ice column along the ice flow direction. If an ice stream flows linearly for a duration greater than 281 the re-equilibration time, then the COF should re-equilibrate with the bulk stress, such that the basal 282 plane will rotate closer to the ice flow direction, increase the effective viscosity, and decrease the rate of 283 deformation downstream. The degree of re-equilibration of an ice COF with the surrounding stresses is 284 not only dependent on ice stream shape, but also on flow speed. Slower-flowing ice will have more time 285 to re-equilibrate with the surrounding stress field. The long-term slowdown at WIS can therefore provide 286 more time for its ice COF re-equilibration, which reduces the misalignment of the basal plane with flow 287 direction and increases the effective viscosity along the flow direction of WIS. Despite internal deformation 288 becoming more significant with the long-term slowdown, this higher effective viscosity instead indicates 289 that internal deformation will be more difficult, which has consequences on future predictions of the ice 290 flow at WIS. 291

Most icesheet-scale ice dynamics models assume either that ice is isotropic, or parameterise anisotropy 292 effects via an enhancement factor to account for ice weakening due to COF orientation relative to ice 293 flow. However, recent studies such as Smith and others (2017) and Kufner and others (2023), suggest that 294 enhancement factors should no longer be used to parameterise ice viscosity in fast-deforming regions such 295 as ice streams. Additionally, the effect of anisotropy on the viscosity of ice can differ significantly between 296 different types of ice fabrics. Most results concluding that ice weakens when anisotropy is considered 297 originate from studies based on cluster fabrics. Conversely, radar and seismic observations at RIS (Jordan 298 and others, 2022: Kufner and others, 2023), and numerical simulations (Ma and others, 2010) show that 299 ice with a girdle COF has a higher effective viscosity in relation to isotropic ice. Our findings at WIS 300 further support the importance of characterising COF- and directionally-dependent ice viscosity in ice flow 301 models, and emphasise that understanding ice COF in both space and time is important for producing 302 more realistic deformation in ice dynamics models. 303

# 304 CONCLUSION

This study provides shear-wave splitting (SWS) observations from basal icequakes at Whillans Ice Stream 305 (WIS). From these observations, we infer the ice crystal orientation fabric (COF) anisotropy over the entire 306 ice column. The observations provide insight into past and present deformation at WIS. The results from 307 80 discrete icequakes SWS observations show that WIS has an average fast S-wave direction ( $\varphi$ ) of 29.3°, 308 which is oblique to the expected direction of  $\sim 10^{\circ}$  based on ice flow direction at the study site of around 309 280°. We suggest that the ice COF records an integrated strain history along its flow path for at least the 310 past 450 years to have preserved deformation in the direction of  $\varphi$ , and therefore evidence the concept of 311 Microstructural Fading Memory. The non-perpendicularity of  $\varphi$  to ice flow implies that the shape of an 312 ice stream can affect its flow, such that spatially deviatoric ice streams including WIS can flow slower if 313 they were instead linear. Given the long-term slowdown of WIS, the basal plane will have more time to 314 re-equilibrate with the surrounding stress field, which can further contribute to the long-term slowdown. 315 Our results have implications for ice sheet models, suggesting that historic ice flow can preserve ice fabric 316 and hence directionally-dependent ice viscosity that might play an important role in such models. 317

# 318 SUPPLEMENTARY MATERIAL

The supplementary material for this article can be found in suppl\_mat\_WIS\_anisotropy.pdf, as attached with the submission of this manuscript.

# 321 ACKNOWLEDGEMENTS

<sup>322</sup> We thank Alex Brisbourne for his comments, which have improved the manuscript.

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