

FootNet: Development of a machine learning emulator of atmospheric transport

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1 **FootNet: Development of a machine learning emulator**
2 **of atmospheric transport**

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8 **Key Points:**

- 9 • Simulating atmospheric transport at high resolution is becoming a computational
10 bottleneck for estimating emissions with flux inversions
11 • Trained deep learning models can emulate source-receptor relationships typically
12 constructed with atmospheric transport models
13 • Deep learning emulators can accelerate construction of source-receptor relation-
14 ships by $\sim 7000\%$, increasing the efficiency of flux inversions

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Abstract

There has been a proliferation of dense observing systems to monitor greenhouse gas (GHG) concentrations over the past decade. Estimating emissions with these observations is often done using an atmospheric transport model to characterize the source-receptor relationship, which is commonly termed measurement “footprint”. Computing and storing footprints using full-physics models is becoming expensive due to the requirement of simulating atmospheric transport at high resolution. We present the development of FootNet, a deep learning emulator of footprints at kilometer scale. We train and evaluate the emulator using footprints simulated using a Lagrangian particle dispersion model. FootNet predicts the magnitudes and extents of footprints in near-real-time with high fidelity. We identify the relative importance of inputs to FootNet. Surface winds and a precomputed Gaussian plume from the receptor are identified to be the most important variables for footprint emulation. The emulator helps address the computational bottleneck of flux inversions using dense observations.

Plain Language Summary

It is computationally expensive to infer greenhouse gas emissions using atmospheric observations. This is, in part, due to the detailed model used to represent atmospheric transport. This work demonstrates how a machine learning model can be used to accurately simulate high-resolution transport in the atmosphere. This type of machine learning model will help researchers estimate greenhouse gas emissions using densely spaced observations, which are becoming increasingly common with the proliferation of dense urban monitoring networks and geostationary satellites.

1 Introduction

Monitoring anthropogenic greenhouse gas (GHG) emissions is important for ensuring the success of the Paris Agreement’s long-term goal on mitigating climate change (IPCC, 2022). To that end, there has been a proliferation of dense observing systems over the past decade to better track GHG emissions. There has been a substantial effort to expand observation networks to better quantify urban GHG emissions, as the majority of the world population lives in urban areas and the degree of urbanization is projected to increase in the future (*World Urbanization Prospects: The 2018 Revision*, 2019). The Northeast Corridor GHG observation network was established to quantify emissions of carbon dioxide and methane using tower-based *in situ* measurements in the highly populated region (Karion et al., 2020). The BERkeley Atmospheric CO₂ Observation Network (BEACO₂N; Shusterman et al. (2016)) utilizes low-cost sensors to increase the spatial density of measurements, which could be used to investigate details about urban emissions on intra-city scales. The proliferation of urban GHG observation networks allows for decadal analyses of GHG emissions and provides information to improve the efficiency of GHG reduction policies (Mitchell et al., 2018; Lauvaux et al., 2020). There has been a coincident expansion in satellite GHG observations, which provide similarly dense observations, such as NASA’s Orbiting Carbon Observatory-2 (OCO-2) and OCO-3, the TROPospheric Monitoring Instrument (TROPOMI) onboard the Copernicus Sentinel-5 Precursor (S5P) satellite (Veeffkind et al., 2012) for methane, and a planned constellation of GHG monitoring satellites (e.g., GOSAT-GW and MethaneSat).

The increased volume of observational data sets provide more constraints on estimating GHG emissions. However, current methods do not scale well with the incoming observations. The conventional method of inferring GHG emissions using atmospheric observations is done via atmospheric flux inversions (e.g., Jiang et al. (2017); White et al. (2019); Turner et al. (2020)). The state of the art in atmospheric flux inversions relies on either Eulerian models or Lagrangian particle dispersion models (LPDMs) to simulate atmospheric transport, which provides the linkage to relate observations to

65 surface fluxes. For example, the four-dimensional variational (4D-Var) method uses the
 66 adjoint of Eulerian models to calculate sensitivities of surface fluxes to observations (Baker
 67 et al., 2006; Henze et al., 2007; Jiang et al., 2017; Qu et al., 2022). Kalman filters are
 68 also widely used in flux inversions, which calculate covariance matrices between prior fluxes
 69 and GHG concentrations simulated by Eulerian models to estimate posterior fluxes (Feng
 70 et al., 2009; Kang et al., 2011). Alternatively, LPDMs can be used to calculate sensitiv-
 71 ity of each observation to its upwind sources by simulating the trajectories of an ensem-
 72 ble of particles advected backward in time (Fasoli et al., 2018; Jones et al., 2007; Pisso
 73 et al., 2019). The sensitivity of each receptor to the upwind sources, termed as the re-
 74 ceptor’s “footprint”, can then be used to estimate fluxes inversely (e.g., Turner et al. (2020)).
 75 These methods based on full-physics models are becoming prohibitively expensive due
 76 to the large computational burden of running high-resolution atmospheric transport mod-
 77 els for dense observing systems.

78 Here we present a deep learning-based emulator, FootNet, to efficiently calculate
 79 footprints of ground-based receptors with high fidelity at kilometer-scale spatial reso-
 80 lution. The footprint emulator reduces the computational and storage cost of Lagrangian
 81 model-based flux inversion systems by 2–3 orders of magnitude, which will better accom-
 82 modate the increased volume of GHG observations. We evaluate the performance of the
 83 FootNet model using independent data sets. Finally, we assess the relative importance
 84 of the features in the machine learning emulator using the permute-and-prediction (PaP)
 85 method.

86 2 Method

87 2.1 Footprints simulated by the STILT model

88 Training of the FootNet model is a supervised learning process. This requires ground
 89 truth to guide the optimization of the model parameters. Here, we use a full-physics model
 90 to generate this ground truth. We simulate footprints using the Stochastic Time-Inverted
 91 Lagrangian Transport (STILT) model (Lin et al., 2003; Fasoli et al., 2018), a Lagrangian
 92 particle dispersion model (LPDM). The STILT simulations are conducted for two regions:
 93 the Barnett Shale region in Texas, and the San Francisco (SF) Bay Area in California
 94 (see Figure S1 in Supporting Information). These two regions are chosen because one
 95 has simple topography (the Barnett Shale) whereas the other is topographically com-
 96 plex (SF Bay Area). As such, these regions represent limiting cases for the ML model.
 97 Further, the combination of two regions will help prevent from overfitting the model to
 98 a single location. For the SF Bay Area, STILT simulations are run from 2018 to 2020
 99 with receptors located at realistic sites deployed in the BEACO₂N network (see <http://beacon.berkeley.edu>
 100 and Shusterman et al. (2016)). Footprints for the Barnett Shale region are generated from
 101 a 1-week WRF-STILT simulation in 2013 (Turner et al., 2018). All footprints are sim-
 102 ulated within a 400×400 km² domain at 1×1 km² spatial resolution.

103 2.2 Input variables

104 We use 5 physical parameters from the NOAA High-Resolution Rapid Refresh (HRRR;
 105 Benjamin et al. (2016)) model as the input variables, including the 10-meter zonal wind
 106 speed (U10M), 10-meter meridional speed (V10M), planetary boundary layer height (PBLH),
 107 surface pressure (PRSS), and air density at 850 hPa level (AD850). The FootNet model
 108 receives the input variables from the measurement time (t_0) and t_0 -6h to predict foot-
 109 prints at t_0 . We apply scaling and transformation on the input and output fields to sta-
 110 bilize the training process (see Table S1 in Supporting Information for details). We find
 111 that including Gaussian plumes (see Figure 1), calculated using an simple idealized plume
 112 model and reversed wind fields, as one of the input variables could significantly improve
 113 the performance of FootNet. The Gaussian plume can be efficiently calculated as a Hadamard
 114 product from inputs listed above and, as such, adds minimal computational expense. The

115 Gaussian plume also provides a localization for the ML model in that it tells the ML model
 116 where the observation was made and provides an initial guess for what the spatial struc-
 117 ture should be. The FootNet model is trained to learn the nonlinear transformation from
 118 the idealized Gaussian plumes to footprints using the meteorological fields. The input
 119 variables are interpolated to the 400×400 km² domain and the 1×1 km² spatial reso-
 120 lution of footprints.

121 **2.3 Deep learning model and training details**

122 The model structure underlying the footprint emulator is the U-net model (Ronneberger
 123 et al., 2015), which is now widely applied in the field of Earth Science (Ghorbanzadeh
 124 et al., 2021; He et al., 2022a, 2022b; Zemskova et al., 2022; Tucker et al., 2023). A schematic
 125 diagram of the model architecture is shown in Figure 1. The model consists of 4 con-
 126 volutional blocks and 4 up-convolutional blocks. Each convolutional block includes two
 127 convolutional layers with 3×3 convolutional kernels and one 2×2 max-pooling layer.
 128 Each up-convolutional layer has one 2×2 up-convolutional layer followed by two 3×3
 129 convolutional layers. The convolutional layers are activated by the Rectified Linear Unit
 130 (ReLU) function, and are used to capture the spatial patterns hidden in the data. Out-
 131 puts from the intermediate hidden layers of the model are termed “latent vectors”, which
 132 is a condensed tensor used by the up-convolutional blocks to predict footprints.

133 We train and evaluate the emulator using a combined data set with 10,000 foot-
 134 prints from the Barnett Shale and 10,000 footprints from the SF Bay Area. The com-
 135 bined data set is randomly split to 85% as the training data set and 15% as the test data
 136 set. The test data set is independent of the training process. 15% of the training data
 137 set is used as validation data set to prevent overfitting. We use the mean squared error
 138 as the loss function and the Adam optimization algorithm.

139 **2.4 Performance metrics**

140 We evaluate the performance of FootNet using log-transformed footprints to miti-
 141 gate the impact of the high skewness of the distribution of typical footprint values. The
 142 performance of FootNet is assessed using the Intersection-over-Union (IoU) and the Pear-
 143 son correlation coefficient (r).

144 IoU measures the accuracy of the area of non-zero footprints predicted by Foot-
 145 Net, which is defined as follows:

$$IoU = \frac{|Y \cap \hat{Y}|}{|Y \cup \hat{Y}|} \quad (1)$$

146 Here, Y and \hat{Y} stand for the true footprint and the FootNet prediction, respectively. The
 147 intersection between Y and \hat{Y} represents the overlapping area of the truth and the pre-
 148 diction, whereas the union represents the area covered by either the truth or the predic-
 149 tion. IoU is used widely to evaluate the ability of deep learning models to make accu-
 150 rately localized predictions.

151 We calculate correlation coefficients for footprints in the intersection areas between
 152 truths and the corresponding predictions, which shows the accuracy in magnitudes of
 153 FootNet predictions.

154 **2.5 Permute-and-prediction method**

155 We use the permute-and-prediction (PaP) method to calculate the importance of
 156 input variables for footprint emulation, which improves the interpretability of the Foot-
 157 Net model (Fisher et al., 2019). The PaP method estimates variable importance by per-
 158 muting each input variable with other variables, and the overall accuracy drop represents

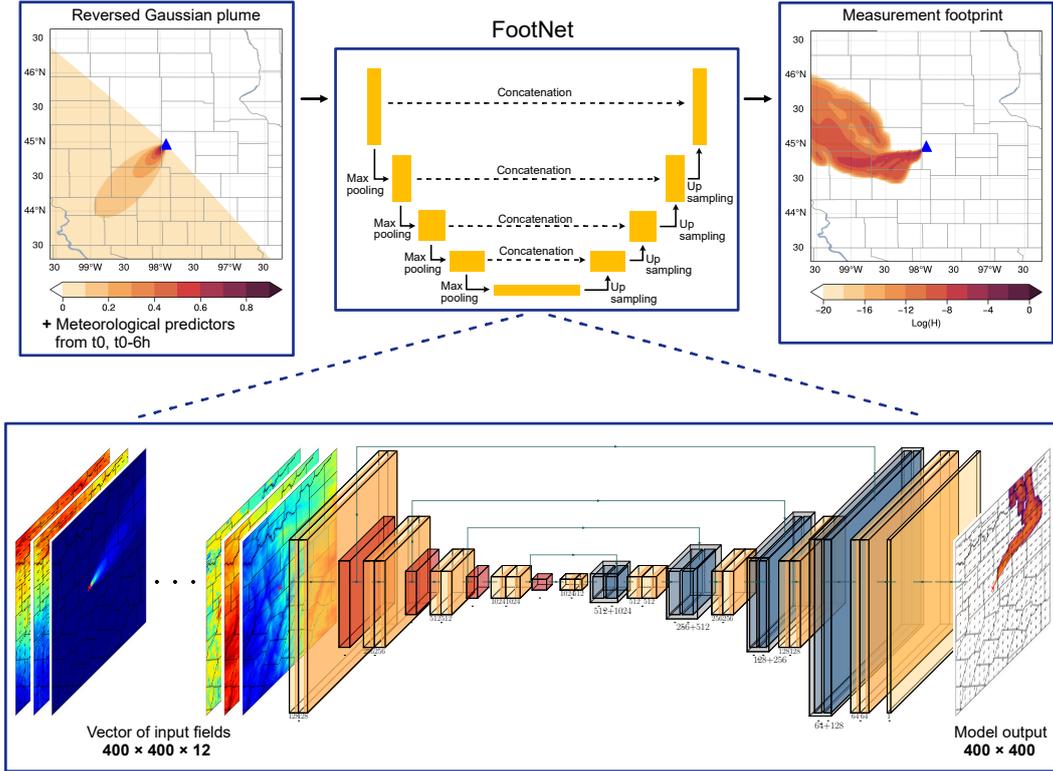


Figure 1. Top row shows the schematic diagram of the FootNet model. Detailed structure of FootNet is shown at the bottom. The orange boxes are 3×3 convolutional layers; the red boxes represent 2×2 max-pooling layers; the light blue boxes are 2×2 transposed convolutional layers. The dark blue boxes represent the latent vectors concatenated from previous layers (shown as the parallel arrows on top).

159 FootNet’s sensitivity to the permuted variable. We estimate variable importance by cal-
 160 culating performance drops in both the IoU and correlation of predicted footprints.

161 3 Results

162 3.1 Evaluating performance of the emulator

163 Figure 2 demonstrates the evolution of FootNet predictions during the training pro-
 164 cess and the overall performance of FootNet after the training converges. Figure 2D shows
 165 a footprint simulated by the STILT model from the test data set, where the footprint
 166 is highly nonlinear with a change in direction near the receptor. The corresponding Foot-
 167 Net predictions are shown in Figures 2 (A-C). After iteration A (shortly after the train-
 168 ing starts), the FootNet predicts measurement footprints around the receptor with a large
 169 negative bias and low correlation coefficient of 0.50. Iteration B is about halfway of the
 170 training process, after which the FootNet prediction better captures the general shape
 171 of the footprint and the correlation is improved to 0.61. The training stops after iter-
 172 ation C. The final FootNet prediction has enriched details and attains a correlation co-
 173 efficient of 0.75. Compared to the test data set (i.e., the true footprints from STILT), the
 174 IoU of FootNet predictions improves from 0.26 after iteration A to 0.58 after iteration
 175 B, and attains a correlation coefficient of 0.76 (see Figure 2A). Figure 2F shows the com-
 176 parison between the truth and FootNet predictions for all footprints in the test data set.

177 FootNet predictions show a slight negative bias compared to footprints simulated using
 178 the full-physics STILT model. The overall correlation between FootNet predictions and
 179 STILT simulations is 0.58.

180 Figure 3 shows footprints from STILT and FootNet for the two regions: the Bar-
 181 nett Shale and the SF Bay Area. Figures 3A and 3E show results from the simple case
 182 (Barnett Shale), where the footprint is similar to an idealized Gaussian plume with time-
 183 reversed winds. FootNet well captures both the magnitudes and spatial patterns of the
 184 footprint, with an IoU of 0.71 and a correlation coefficient of 0.53. Figures 3B and 3F
 185 demonstrate a more complicated meteorological scenario from the Barnett Shale region.
 186 The IoU metric and correlation coefficient between the STILT footprint and the Foot-
 187 Net prediction are 0.74 and 0.59, respectively, for this more complex scenario.

188 Atmospheric transport in the SF Bay Area is decisively more complex as the re-
 189 gion includes steep topography, air-sea interactions, and numerous valleys and deltas;
 190 Figures 3C and 3D show results from the full-physics model for this region. Emulation
 191 of footprints in the SF Bay Area is thus more challenging with an overall degraded fi-
 192 delity as compared to the Barnett Shale region. Figures 3C and 3G show a receptor with
 193 the bulk of the footprint in the Northwest quadrant, these typical meteorological con-
 194 ditions for the SF Bay Area in the summertime with westerly flow bringing airmasses
 195 into the SF Bay Area past the Golden Gate Bridge. The shape and the magnitude of
 196 the footprint is predicted by FootNet with an IoU of 0.44 and the correlation coefficient
 197 to be 0.83. Footprints shown in Figures 3D and 3H show a more complex meteorolog-
 198 ical scenario. Compared to STILT, the FootNet prediction has an IoU of 0.59 and the
 199 correlation is 0.72.

200 There have been other methods developed to improve the efficiency of footprint cal-
 201 culations. For example, Roten et al. (2021) uses nonlinear weighted averaging to inter-
 202 polate footprints from locations near the receptors. Fillola et al. (2023) develops a sim-
 203 ilar footprint emulator based on gradient-boosted regression trees (GBRTs), at a coarse
 204 spatial resolution (20–30 km in mid-latitudes) and 10 grid cells around the measurement
 205 location. The FootNet model reproduces the full-physics model with high fidelity at high-
 206 resolution. This is impressive given the complex topography and meteorology of the re-
 207 gions studied here could complicate the emulation of footprints due to their impact on
 208 transport at kilometer scale. FootNet only takes meteorological fields and the idealized
 209 Gaussian plume as its input. No additional LPDM simulations are needed to generate
 210 footprint predictions after the training process.

211 Using the full-physics STILT model, it takes about 6 months to run 10^8 particle
 212 trajectories for the computation of 1 week of hourly footprints at kilometer scale. The
 213 storage requirement also makes it impractical to use the full-physics model with dense
 214 observations, as the computed 1-week hourly footprints would require 4-terabyte stor-
 215 age space for future re-use. Emulation of footprints using the FootNet model addresses
 216 these two issues and facilitates LPDM-based flux inversion systems with dense observ-
 217 ing systems. The generation of each footprint prediction takes ~ 1 s on central process-
 218 ing units (CPUs), which can be further reduced to 0.08 s on a graphics processing units
 219 (GPU). To analyze a single day of observations made at the 40 BEACO₂N sites in the
 220 SF Bay Area (approx. 650 observations per day), it takes the STILT model 2 hours on
 221 10 compute nodes with 32 CPU cores to generate the required footprints, whereas only
 222 6 min is required for FootNet on one GPU node. This computational efficiency of the
 223 approach mitigates the storage requirement, as footprints could be generated by Foot-
 224 Net in near real-time and there is no need to storage the computed footprints.

225 3.2 Importance of input variables

226 Figure 4 shows the ranking of variable importance for FootNet calculated using the
 227 PaP method. We group variable importance by variable names and time steps. The most

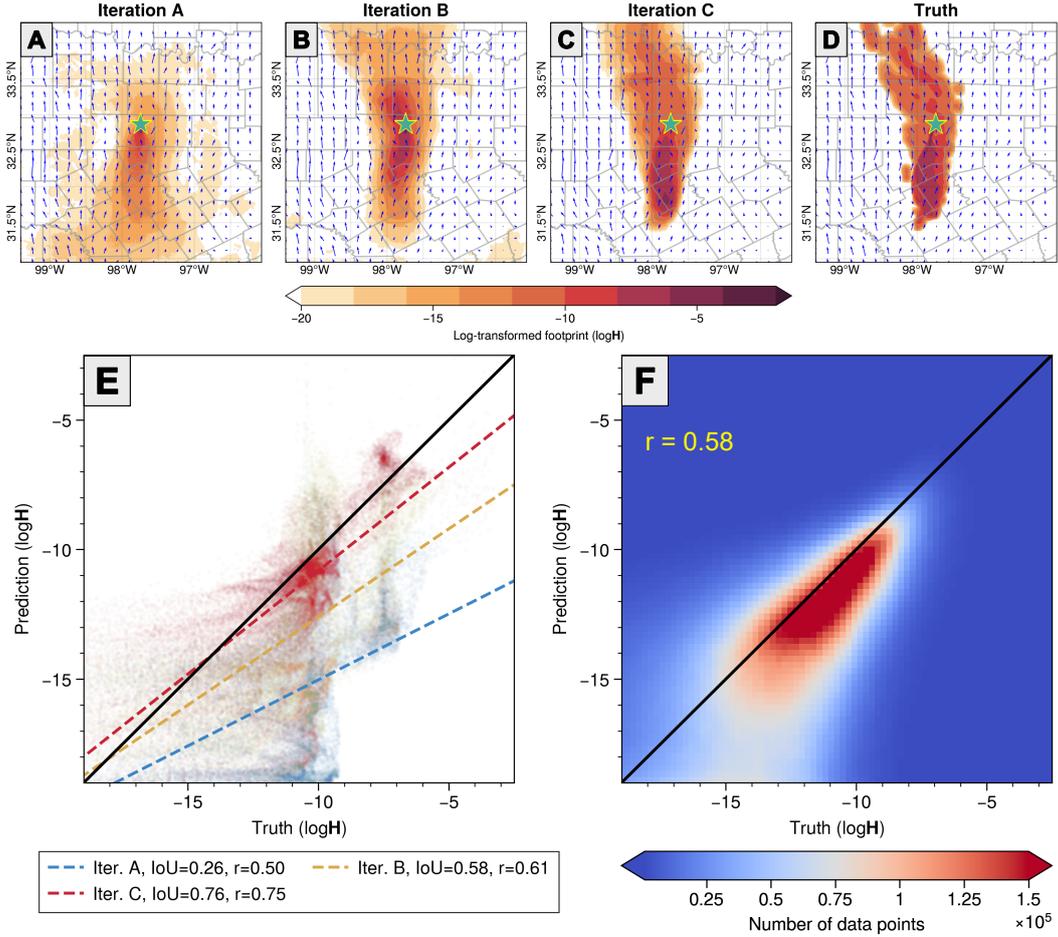


Figure 2. Convergence of the training process and evaluation of the model performance on the independent test data set. (A-C) FootNet predictions from three stages in the training process, corresponding to the truth in (D). The blue arrows represent wind vectors, and the green stars show the location of the receptors. (E) Comparison between footprints simulated by STILT and FootNet predictions in (A-C). (F) Comparison between FootNet and STILT for all footprints in the test data set.

228 important meteorological variables are the 10-meter wind speeds, which lead to a ~ 0.4
 229 decrease in correlation and the IoU drops by ~ 0.16 . Permuting Gaussian plumes degrades
 230 the IoU of correlation of FootNet predictions by 0.25 and 0.1, respectively. FootNet is
 231 less sensitive to surface pressure and air density at 850 hPa than other input variables,
 232 and planetary boundary layer height shows the lowest variable importance. Meteorologi-
 233 cal variables from different time steps show similar importance for footprint emulation.
 234 The IoU is more sensitive to meteorological variables from $t_0 - 6h$, whereas informa-
 235 tion from the measurement time (t_0) is more important for the magnitude accuracy of
 236 FootNet predictions.

237 PaP method provides a rough estimate of variable importance, this is because the
 238 inter-correlation between input variables can lead to an inflation of the feature impor-
 239 tance (Hooker et al., 2021). Nevertheless, the calculated variable importance is in align-
 240 ment with our understanding about the calculation of source-receptor footprints.
 241 Namely, that the computation of footprints with a full-physics model requires advect-

ing particles with the precomputed wind fields, the PaP method indicates the importance of this in the ML model by identifying the 10-m winds as the most important parameters. The Gaussian plume is also identified as highly important. This is, again, because the Gaussian plume is the only input field that provides information about the location of the observational receptor location.

4 Conclusions

Here we described the developed a machine learning emulator of surface measurement footprints, FootNet. This machine learning model can be used to improve the computational efficiency of high-resolution greenhouse gas flux . The FootNet model was trained and evaluated using footprints simulated by the STILT full-physics model for the SF Bay Area and the Barnett Shale region. We show the FootNet prediction evolves and converges to the STILT truth as the training iterates. The overall correlation between FootNet predictions and the STILT simulations is 0.58. The footprint emulator well predicts both the shapes of magnitudes of footprints with a high fidelity. We calculate variable importance for FootNet using the PaP method to improve the interpretability of the FootNet model. 10-meter wind speeds and Gaussian plumes have the greatest importance for the emulation of footprints. The emulation of footprints using FootNet is computationally efficient and mitigates the burden of storing footprints for each measurement location, which makes it feasible to deliver high-resolution estimates of GHG fluxes in near real-time using proliferated dense observing systems in the future.

5 Open Research

We use the full-physics Stochastic Time-Inverted Lagrangian Transport Model (STILT) to simulation footprints for the training of FootNet. The STILT model could be accessed from <https://uataq.github.io/stilt/> (Fasoli et al., 2018). The footprints simulated by the STILT model are available through Turner et al. (2018) and Turner et al. (2020). Examples of the footprint data sets used in the training process could be downloaded from https://hermes.atmos.washington.edu/footnet_training_samples/footprints_data.tar.gz. The meteorological variables are from the High-Resolution Rapid Refresh (HRRR) data product, which is available at <https://rapidrefresh.noaa.gov/hrrr/> (Dowell et al., 2022; James et al., 2022). The repository of the code used in the manuscript is publicly available at https://github.com/taionghe/FootNet_tf/.

Acknowledgments

This work is supported by a NASA Early Career Faculty Grant (80NSSC21K1808) to A.J.T. and NASA FINESST Grant (80NSSC22K1557) to N.D. We acknowledge funding from Environmental Defense Fund, whose work is supported by gifts from Signe Ostby, Scott Cook and Valhalla Foundation. This work is supported in part by the generosity of Eric and Wendy Schmidt by recommendation of Schmidt Futures, as part of its Virtual Earth System Research Institute (VESRI).

The authors declare no conflict of interest.

References

- Baker, D. F., Doney, S. C., & Schimel, D. S. (2006). Variational data assimilation for atmospheric co₂. *Tellus B: Chemical and Physical Meteorology*, 58(5), 359-365. Retrieved from <https://doi.org/10.1111/j.1600-0889.2006.00218.x>
doi: 10.1111/j.1600-0889.2006.00218.x
- Benjamin, S. G., Weygandt, S. S., Brown, J. M., Hu, M., Alexander, C. R., Smirnova, T. G., ... Manikin, G. S. (2016). A north american hourly assimilation

- 288 lation and model forecast cycle: The rapid refresh. *Monthly Weather Review*,
 289 *144*(4), 1669 - 1694. Retrieved from [https://journals.ametsoc.org/view/](https://journals.ametsoc.org/view/journals/mwre/144/4/mwr-d-15-0242.1.xml)
 290 journals/mwre/144/4/mwr-d-15-0242.1.xml doi: [https://doi.org/10.1175/](https://doi.org/10.1175/MWR-D-15-0242.1)
 291 [MWR-D-15-0242.1](https://doi.org/10.1175/MWR-D-15-0242.1)
- 292 Dowell, D. C., Alexander, C. R., James, E. P., Weygandt, S. S., Benjamin, S. G.,
 293 Manikin, G. S., ... Alcott, T. I. (2022). The high-resolution rapid refresh
 294 (hrrr): An hourly updating convection-allowing forecast model. part i: Moti-
 295 vation and system description. *Weather and Forecasting*, *37*(8), 1371 - 1395.
 296 Retrieved from [https://journals.ametsoc.org/view/journals/wefo/37/8/](https://journals.ametsoc.org/view/journals/wefo/37/8/WAF-D-21-0151.1.xml)
 297 [WAF-D-21-0151.1.xml](https://journals/wefo/37/8/WAF-D-21-0151.1.xml) doi: <https://doi.org/10.1175/WAF-D-21-0151.1>
- 298 Fasoli, B., Lin, J. C., Bowling, D. R., Mitchell, L., & Mendoza, D. (2018). Sim-
 299 ulating atmospheric tracer concentrations for spatially distributed receptors:
 300 updates to the stochastic time-inverted lagrangian transport model's r inter-
 301 face (stilt-r version 2). *Geoscientific Model Development*, *11*(7), 2813–2824.
 302 Retrieved from <https://gmd.copernicus.org/articles/11/2813/2018/>
 303 doi: [10.5194/gmd-11-2813-2018](https://doi.org/10.5194/gmd-11-2813-2018)
- 304 Feng, L., Palmer, P. I., Bösch, H., & Dance, S. (2009). Estimating surface co₂
 305 fluxes from space-borne co₂ dry air mole fraction observations using an en-
 306 semble kalman filter. *Atmospheric Chemistry and Physics*, *9*(8), 2619–2633.
 307 Retrieved from <https://acp.copernicus.org/articles/9/2619/2009/> doi:
 308 [10.5194/acp-9-2619-2009](https://doi.org/10.5194/acp-9-2619-2009)
- 309 Fillola, E., Santos-Rodriguez, R., Manning, A., O'Doherty, S., & Rigby, M. (2023).
 310 A machine learning emulator for lagrangian particle dispersion model foot-
 311 prints: a case study using name. *Geoscientific Model Development*, *16*(7),
 312 1997–2009. Retrieved from [https://gmd.copernicus.org/articles/16/](https://gmd.copernicus.org/articles/16/1997/2023/)
 313 [1997/2023/](https://gmd.copernicus.org/articles/16/1997/2023/) doi: [10.5194/gmd-16-1997-2023](https://doi.org/10.5194/gmd-16-1997-2023)
- 314 Fisher, A., Rudin, C., & Dominici, F. (2019, 01). All models are wrong, but many
 315 are useful: Learning a variable's importance by studying an entire class of pre-
 316 diction models simultaneously. *Journal of machine learning research : JMLR*,
 317 *20*.
- 318 Ghorbanzadeh, O., Crivellari, A., Ghamisi, P., Shahabi, H., & Blaschke, T. (2021,
 319 Jul 16). A comprehensive transferability evaluation of u-net and resu-net
 320 for landslide detection from sentinel-2 data (case study areas from taiwan,
 321 china, and japan). *Scientific Reports*, *11*(1), 14629. Retrieved from [https://](https://doi.org/10.1038/s41598-021-94190-9)
 322 doi.org/10.1038/s41598-021-94190-9 doi: [10.1038/s41598-021-94190-9](https://doi.org/10.1038/s41598-021-94190-9)
- 323 He, T.-L., Jones, D. B. A., Miyazaki, K., Bowman, K. W., Jiang, Z., Chen, X.,
 324 ... Li, K. (2022b). Inverse modelling of chinese no_x emissions using deep
 325 learning: integrating in situ observations with a satellite-based chemical re-
 326 analysis. *Atmospheric Chemistry and Physics*, *22*(21), 14059–14074. Re-
 327 trieved from <https://acp.copernicus.org/articles/22/14059/2022/> doi:
 328 [10.5194/acp-22-14059-2022](https://doi.org/10.5194/acp-22-14059-2022)
- 329 He, T.-L., Jones, D. B. A., Miyazaki, K., Huang, B., Liu, Y., Jiang, Z., ... Wor-
 330 den, J. R. (2022a). Deep learning to evaluate us no_x emissions using surface
 331 ozone predictions. *Journal of Geophysical Research: Atmospheres*, *127*(4),
 332 e2021JD035597. Retrieved from [https://agupubs.onlinelibrary.wiley](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2021JD035597)
 333 [.com/doi/abs/10.1029/2021JD035597](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2021JD035597) (e2021JD035597 2021JD035597) doi:
 334 <https://doi.org/10.1029/2021JD035597>
- 335 Henze, D. K., Hakami, A., & Seinfeld, J. H. (2007). Development of the adjoint of
 336 geos-chem. *Atmospheric Chemistry and Physics*, *7*(9), 2413–2433. Retrieved
 337 from <https://acp.copernicus.org/articles/7/2413/2007/> doi: [10.5194/](https://doi.org/10.5194/acp-7-2413-2007)
 338 [acp-7-2413-2007](https://doi.org/10.5194/acp-7-2413-2007)
- 339 Hooker, G., Mentch, L., & Zhou, S. (2021). *Unrestricted permutation forces extrap-*
 340 *olation: Variable importance requires at least one more model, or there is no*
 341 *free variable importance.*
- 342 IPCC. (2022). *Global warming of 1.5°C: Ipcc special report on impacts of global*

- 343 *warming of 1.5°C above pre-industrial levels in context of strengthening re-*
 344 *sponse to climate change, sustainable development, and efforts to eradicate*
 345 *poverty*. Cambridge University Press. doi: 10.1017/9781009157940
- 346 James, E. P., Alexander, C. R., Dowell, D. C., Weygandt, S. S., Benjamin, S. G.,
 347 Manikin, G. S., ... Turner, D. D. (2022). The high-resolution rapid re-
 348 fresh (hrrr): An hourly updating convection-allowing forecast model. part ii:
 349 Forecast performance. *Weather and Forecasting*, 37(8), 1397 - 1417. Re-
 350 trieved from [https://journals.ametsoc.org/view/journals/wefo/37/8/](https://journals.ametsoc.org/view/journals/wefo/37/8/WAF-D-21-0130.1.xml)
 351 [WAF-D-21-0130.1.xml](https://journals.ametsoc.org/view/journals/wefo/37/8/WAF-D-21-0130.1.xml) doi: <https://doi.org/10.1175/WAF-D-21-0130.1>
- 352 Jiang, Z., Worden, J. R., Worden, H., Deeter, M., Jones, D. B. A., Arellano, A. F.,
 353 & Henze, D. K. (2017). A 15-year record of co emissions constrained by mopitt
 354 co observations. *Atmospheric Chemistry and Physics*, 17(7), 4565–4583. Re-
 355 trieved from <https://acp.copernicus.org/articles/17/4565/2017/> doi:
 356 10.5194/acp-17-4565-2017
- 357 Jones, A., Thomson, D., Hort, M., & Devenish, B. (2007). The u.k. met office’s
 358 next-generation atmospheric dispersion model, name iii. In C. Borrego &
 359 A.-L. Norman (Eds.), *Air pollution modeling and its application xvii* (pp. 580–
 360 589). Boston, MA: Springer US.
- 361 Kang, J.-S., Kalnay, E., Liu, J., Fung, I., Miyoshi, T., & Ide, K. (2011). “variable
 362 localization” in an ensemble kalman filter: Application to the carbon cycle
 363 data assimilation. *Journal of Geophysical Research: Atmospheres*, 116(D9).
 364 Retrieved from [https://agupubs.onlinelibrary.wiley.com/doi/abs/](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2010JD014673)
 365 [10.1029/2010JD014673](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2010JD014673) doi: <https://doi.org/10.1029/2010JD014673>
- 366 Karion, A., Callahan, W., Stock, M., Prinzivalli, S., Verhulst, K. R., Kim, J., ...
 367 Whetstone, J. (2020). Greenhouse gas observations from the northeast
 368 corridor tower network. *Earth System Science Data*, 12(1), 699–717. Re-
 369 trieved from <https://essd.copernicus.org/articles/12/699/2020/> doi:
 370 10.5194/essd-12-699-2020
- 371 Lauvaux, T., Gurney, K. R., Miles, N. L., Davis, K. J., Richardson, S. J., Deng,
 372 A., ... Turnbull, J. (2020). Policy-relevant assessment of urban co2 emis-
 373 sions. *Environmental Science & Technology*, 54(16), 10237-10245. Retrieved
 374 from <https://doi.org/10.1021/acs.est.0c00343> (PMID: 32806908) doi:
 375 10.1021/acs.est.0c00343
- 376 Lin, J. C., Gerbig, C., Wofsy, S. C., Andrews, A. E., Daube, B. C., Davis, K. J., &
 377 Grainger, C. A. (2003). A near-field tool for simulating the upstream influence
 378 of atmospheric observations: The stochastic time-inverted lagrangian trans-
 379 port (stilt) model. *Journal of Geophysical Research: Atmospheres*, 108(D16).
 380 Retrieved from [https://agupubs.onlinelibrary.wiley.com/doi/abs/](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2002JD003161)
 381 [10.1029/2002JD003161](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2002JD003161) doi: <https://doi.org/10.1029/2002JD003161>
- 382 Mitchell, L. E., Lin, J. C., Bowling, D. R., Pataki, D. E., Strong, C., Schauer, A. J.,
 383 ... Ehleringer, J. R. (2018). Long-term urban carbon dioxide observations
 384 reveal spatial and temporal dynamics related to urban characteristics and
 385 growth. *Proceedings of the National Academy of Sciences*, 115(12), 2912-2917.
 386 Retrieved from <https://www.pnas.org/doi/abs/10.1073/pnas.1702393115>
 387 doi: 10.1073/pnas.1702393115
- 388 Pisso, I., Sollum, E., Grythe, H., Kristiansen, N. I., Cassiani, M., Eckhardt, S.,
 389 ... Stohl, A. (2019). The lagrangian particle dispersion model flexpart
 390 version 10.4. *Geoscientific Model Development*, 12(12), 4955–4997. Re-
 391 trieved from <https://gmd.copernicus.org/articles/12/4955/2019/> doi:
 392 10.5194/gmd-12-4955-2019
- 393 Qu, Z., Henze, D. K., Worden, H. M., Jiang, Z., Gaubert, B., Theys, N., & Wang,
 394 W. (2022). Sector-based top-down estimates of nox, so2, and co emissions in
 395 east asia. *Geophysical Research Letters*, 49(2), e2021GL096009. Retrieved
 396 from [https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2021GL096009)
 397 [2021GL096009](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2021GL096009) (e2021GL096009 2021GL096009) doi: [https://doi.org/10.1029/](https://doi.org/10.1029/2021GL096009)

2021GL096009

- 398
399 Ronneberger, O., Fischer, P., & Brox, T. (2015). U-Net: Convolutional Networks
400 for Biomedical Image Segmentation. In N. Navab, J. Hornegger, W. M. Wells,
401 & A. F. Frangi (Eds.), *Medical Image Computing and Computer-Assisted In-*
402 *tervention – MICCAI 2015* (pp. 234–241). Cham: Springer International
403 Publishing. doi: 10.1007/978-3-319-24574-4_28
- 404 Roten, D., Wu, D., Fasoli, B., Oda, T., & Lin, J. C. (2021). An interpola-
405 tion method to reduce the computational time in the stochastic lagrangian
406 particle dispersion modeling of spatially dense xco2 retrievals. *Earth*
407 *and Space Science*, 8(4), e2020EA001343. Retrieved from [https://](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020EA001343)
408 agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020EA001343
409 (e2020EA001343 2020EA001343) doi: <https://doi.org/10.1029/2020EA001343>
- 410 Shusterman, A. A., Teige, V. E., Turner, A. J., Newman, C., Kim, J., & Cohen,
411 R. C. (2016). The berkeley atmospheric co₂ observation network: initial
412 evaluation. *Atmospheric Chemistry and Physics*, 16(21), 13449–13463. Re-
413 trieved from <https://acp.copernicus.org/articles/16/13449/2016/> doi:
414 10.5194/acp-16-13449-2016
- 415 Tucker, C., Brandt, M., Hiernaux, P., Kariryaa, A., Rasmussen, K., Small, J.,
416 ... Fensholt, R. (2023, Mar 01). Sub-continental-scale carbon stocks
417 of individual trees in african drylands. *Nature*, 615(7950), 80-86. Re-
418 trieved from <https://doi.org/10.1038/s41586-022-05653-6> doi:
419 10.1038/s41586-022-05653-6
- 420 Turner, A. J., Jacob, D. J., Benmergui, J., Brandman, J., White, L., & Ran-
421 dles, C. A. (2018). Assessing the capability of different satellite observing
422 configurations to resolve the distribution of methane emissions at kilome-
423 ter scales. *Atmospheric Chemistry and Physics*, 18(11), 8265–8278. Re-
424 trieved from <https://acp.copernicus.org/articles/18/8265/2018/> doi:
425 10.5194/acp-18-8265-2018
- 426 Turner, A. J., Kim, J., Fitzmaurice, H., Newman, C., Worthington, K., Chan,
427 K., ... Cohen, R. C. (2020). Observed impacts of covid-19 on urban co₂
428 emissions. *Geophysical Research Letters*, 47(22), e2020GL090037. Re-
429 trieved from [https://agupubs.onlinelibrary.wiley.com/doi/abs/](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020GL090037)
430 [10.1029/2020GL090037](https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020GL090037) (e2020GL090037 10.1029/2020GL090037) doi:
431 <https://doi.org/10.1029/2020GL090037>
- 432 Veefkind, J., Aben, I., McMullan, K., Förster, H., de Vries, J., Otter, G., ... Lev-
433 elt, P. (2012). Tropomi on the esa sentinel-5 precursor: A gmes mission for
434 global observations of the atmospheric composition for climate, air quality
435 and ozone layer applications. *Remote Sensing of Environment*, 120, 70-83.
436 Retrieved from [https://www.sciencedirect.com/science/article/pii/](https://www.sciencedirect.com/science/article/pii/S0034425712000661)
437 [S0034425712000661](https://www.sciencedirect.com/science/article/pii/S0034425712000661) (The Sentinel Missions - New Opportunities for Science)
438 doi: <https://doi.org/10.1016/j.rse.2011.09.027>
- 439 White, E. D., Rigby, M., Lunt, M. F., Smallman, T. L., Comyn-Platt, E., Man-
440 ning, A. J., ... Palmer, P. I. (2019). Quantifying the uk’s carbon dioxide
441 flux: an atmospheric inverse modelling approach using a regional measure-
442 ment network. *Atmospheric Chemistry and Physics*, 19(7), 4345–4365. Re-
443 trieved from <https://acp.copernicus.org/articles/19/4345/2019/> doi:
444 10.5194/acp-19-4345-2019
- 445 *World urbanization prospects: The 2018 revision.* (2019). United Nations.
- 446 Zemskova, V. E., He, T.-L., Wan, Z., & Grisouard, N. (2022, Jul 13). A deep-
447 learning estimate of the decadal trends in the southern ocean carbon storage.
448 *Nature Communications*, 13(1), 4056. Retrieved from [https://doi.org/](https://doi.org/10.1038/s41467-022-31560-5)
449 [10.1038/s41467-022-31560-5](https://doi.org/10.1038/s41467-022-31560-5) doi: 10.1038/s41467-022-31560-5

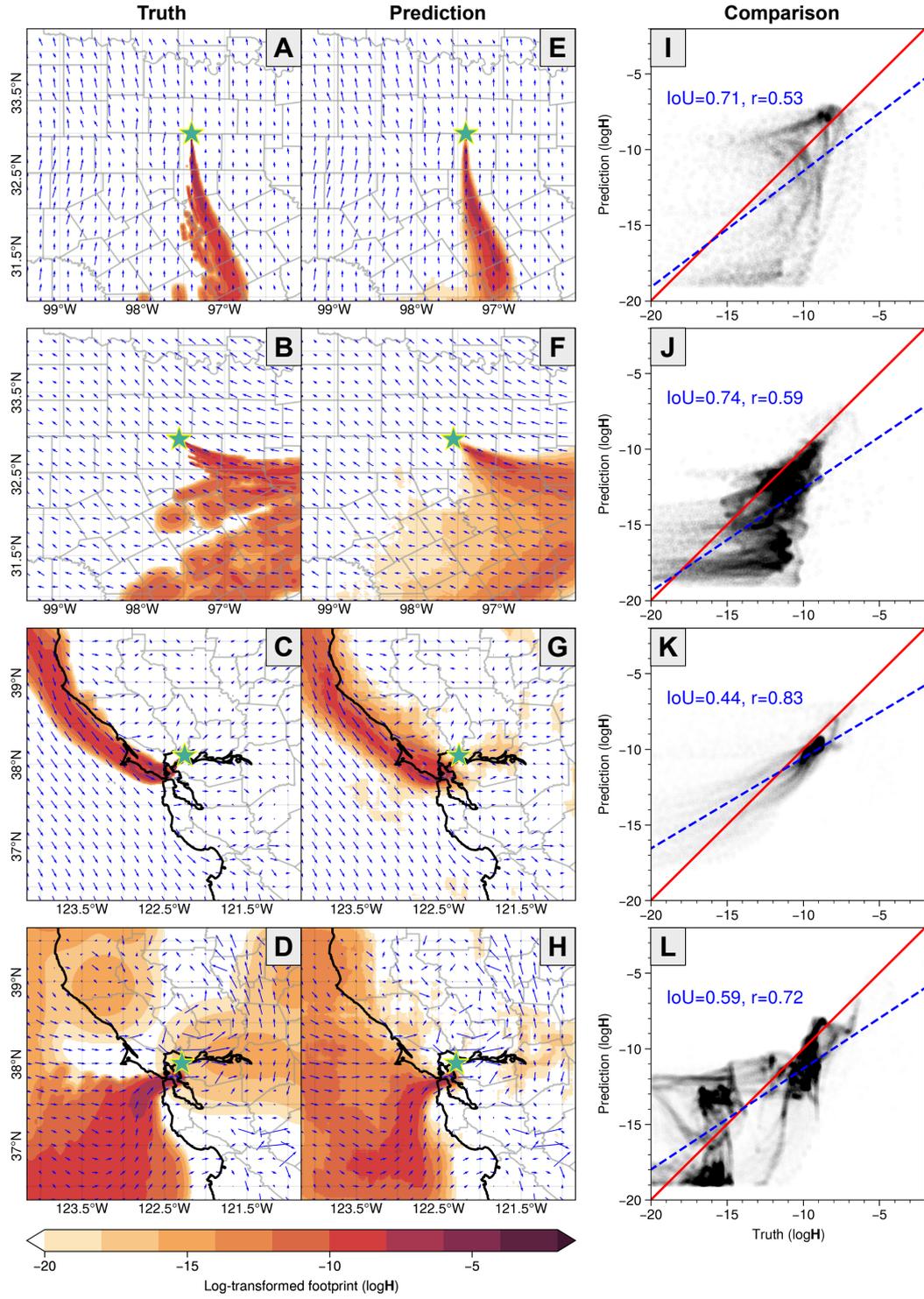


Figure 3. Evaluation of individual FootNet predictions for the test data set. (A-D) Footprints simulated by the full-physics STILT model for the Barnett Shale region and the SF Bay Area, which are treated as the truth in the training process. (E-H) Footprint predictions made by FootNet corresponding to (A-D). The blue arrows represent wind vectors, and the green stars show the location of the receptors. (I-L) Comparison and correlation between the truths and predictions for the four examples.

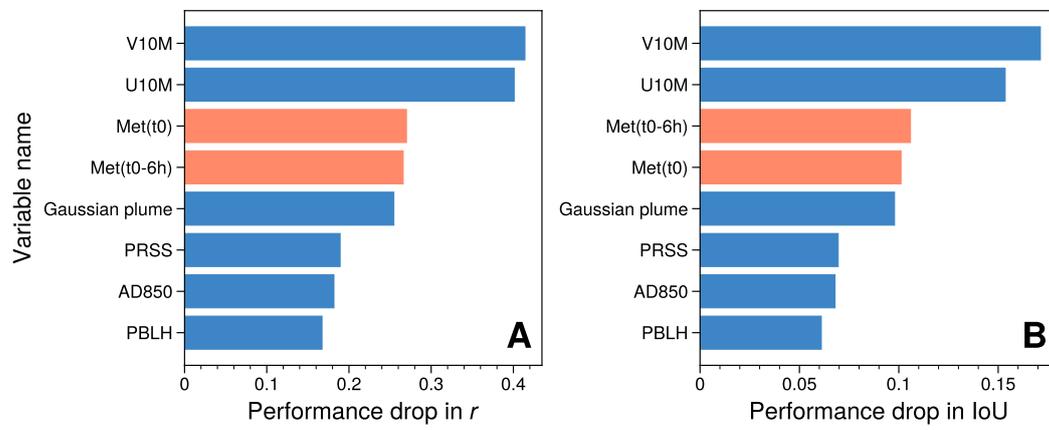


Figure 4. Rankings of importance of the input variables estimated using the permute-and-predict (PaP) method. (A) Performance drop in the correlation coefficients after permuting the input variables.