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Manuscript details

Title: Mechanisms and seismological signatures of rupture complexity induced by fault damage zones in fully-dynamic earthquake cycle models

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1 **Mechanisms and seismological signatures of rupture**
2 **complexity induced by fault damage zones in**
3 **fully-dynamic earthquake cycle models**

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9 **Key Points:**

- 10 • Reduction of nucleation size and pulse-crack transitions are two distinct damage zone
11 effects that induce back-propagating rupture fronts.
12 • Damage effects can enhance high-frequency radiation and complexity of source time
13 functions, potentially observable in the far field.
14 • Back-propagating fronts have potential signatures in near-field seismograms and can
15 affect peak ground motions.

Abstract

Damage zones are common around faults, but their effects on earthquake mechanics are still incompletely understood. Here, we investigate how damage affects rupture patterns, source time functions and ground motions in 2D fully-dynamic cycle models. We find that back-propagating rupture fronts emerge in large faults and can be triggered by residual stresses left by previous ruptures or by damage-induced pulse-to-crack transitions. Damage-induced back-propagating fronts are modulated by slip rate oscillations, amplify high-frequency radiation, and sharpen the multiple peaks in source time functions even in the absence of frictional heterogeneity or fault segmentation. Near-field ground motion is predominantly controlled by stress heterogeneity left by prior seismicity, and further amplified within the damage zone by trapped waves and outside it by secondary rupture fronts. This study refines our knowledge on damage zone effects on earthquake rupture and identifies their potentially observable signatures in the near and far field.

Plain Language Summary

Faults are surrounded by layers of fractured rocks, known as damage zones, which can affect earthquakes and related hazards, but in ways that are still not well understood. Here, by running computer simulations, we investigate how damage zones influence earthquake ruptures and consequent ground motions. Our models fully account for seismic wave effects, produce multiple earthquake cycles, and span a large range of fault lengths and damage zone properties that are representative of natural faults. We identify characteristic patterns of earthquake rupture produced by damage zones: back-propagating fronts that re-rupture the fault, and oscillatory fault motions that affect ground shaking amplitude and frequency content. We identify which of these effects might be observable in seismograms recorded near and far from the fault. Overall, our computational study highlights significant effects of damage zones on earthquakes and on the shaking they produce. These results can guide us to better interpret earthquake source and ground motion observations, and to predict the potential characteristics of future events.

1 Introduction

Faults are usually surrounded by damage zones which, as increasingly demonstrated in numerical and observational studies, can substantially affect earthquake rupture processes. Fault damage zones are characterised in geological observations by distributed fractures and micro-cracks (e.g., Mitchell & Faulkner, 2009; Savage & Brodsky, 2011) and in geophysical studies by compliant or low velocity fault zones (e.g., Huang & Ampuero, 2011; Yang, 2015). Previous modelling studies show that in the presence of damage zones, fault zone reflected waves, head waves and trapped waves can interact with the rupture and promote a number of source phenomena: pulse-like rupture, premature rupture arrest, periodic modulation of slip rate, periodic patterns of off-fault damage, transition to supershear rupture at relatively low background stress, and rupture speeds that are theoretically unexpected for steady ruptures in homogeneous media (Harris & Day, 1997; Huang & Ampuero, 2011; Huang et al., 2014, 2016; Pelties et al., 2014). Some of these predicted effects of damage on earthquake rupture have been increasingly supported by seismological and geological observations. For example, evidence for unexpectedly fast rupture was found in earthquakes occurring within damage zones in Big Bear, Southern California (Huang et al., 2016). A faster rupture in the direction of increasing fault maturity (Perrin et al., 2016) and the sustained “slow supershear” of the 2018 Indonesia earthquake at a speed between S-wave and Eshelby’s speed (Bao et al., 2019; Oral et al., 2020) have been also attributed to damage effects. Modelling studies also identify damage-induced rupture features that persist across multiple earthquake cycles, in particular back-propagating rupture fronts (Idini & Ampuero, 2020; Thakur et al., 2020; Nie & Barbot, 2022; Abdelmeguid et al., 2019) that resemble rupture patterns observed in real earthquakes (e.g., Beroza & Spudich, 1988; Hicks et al., 2020a; Vallée et al., 2023).

66 However, our understanding of damage zone effects on earthquakes is still incomplete,
 67 partly due to limitations of previous modelling studies. Studies based on single-rupture
 68 simulations (e.g., Harris & Day, 1997; Huang et al., 2014, 2016; Oral et al., 2020) strongly
 69 depend on initial stresses that are prescribed arbitrarily. This limitation is addressed by
 70 seismic cycle modelling, in which the initial fault stresses for each earthquake result from the
 71 previous seismic and aseismic slip on the fault. To keep the computational cost affordable,
 72 the most systematic earthquake cycle studies on damaged faults (Idini & Ampuero, 2020;
 73 Nie & Barbot, 2022) adopt the quasi-dynamic approximation, in which seismic wave effects
 74 are only crudely modelled. Such dynamic effects are known to be important (Thomas et al.,
 75 2014), especially in presence of damage zones, as highlighted in recent fully-dynamic cycle
 76 models (Abdelmeguid et al., 2019; Thakur et al., 2020). On the other hand, due to their
 77 high computational cost, fully-dynamic cycle studies have explored a limited range of model
 78 parameters (e.g., Kaneko et al., 2011). In particular, the ratio of fault length to nucleation
 79 size has not yet been pushed to the high values required in continuum fault models with
 80 homogeneous friction properties to produce realistic statistics of seismicity (Cattania, 2019;
 81 Barbot, 2019) and to promote damage-induced rupture complexity (Idini & Ampuero, 2020).

82 Here we investigate the effects of damage zones on rupture patterns in 2D fully-dynamic
 83 earthquake cycle simulations that span a broad range of parameter values, representative
 84 of natural fault zone properties and fault lengths. To efficiently explore the fully-dynamic
 85 models, we select model parameters based on the insights from previous quasi-dynamic
 86 modelling (Idini & Ampuero, 2020). In the following, we first present our model assumptions
 87 and simulation settings. Next, we analyze the emergence of back-propagating fronts in large
 88 faults with and without damage, and the potential signatures of damage effects in near- and
 89 far-field ground motions.

90 2 Model

91 We consider a fault bisecting a damage zone embedded in a homogeneous elastic
 92 medium. We focus on a 2-D anti-plane problem, which corresponds to a vertical section
 93 across a strike-slip fault (Fig. 1). The damage zone has a thickness $2h$ and a damage level
 94 Δ , defined as the relative contrast of shear modulus between damaged (μ_d) and intact rocks
 95 (μ_h): $\Delta = 1 - \mu_d/\mu_h$. In terms of S-wave speeds of damaged (V_d) and host rocks (V_h), the
 96 damage level is $\Delta = 1 - (V_d/V_h)^2$.

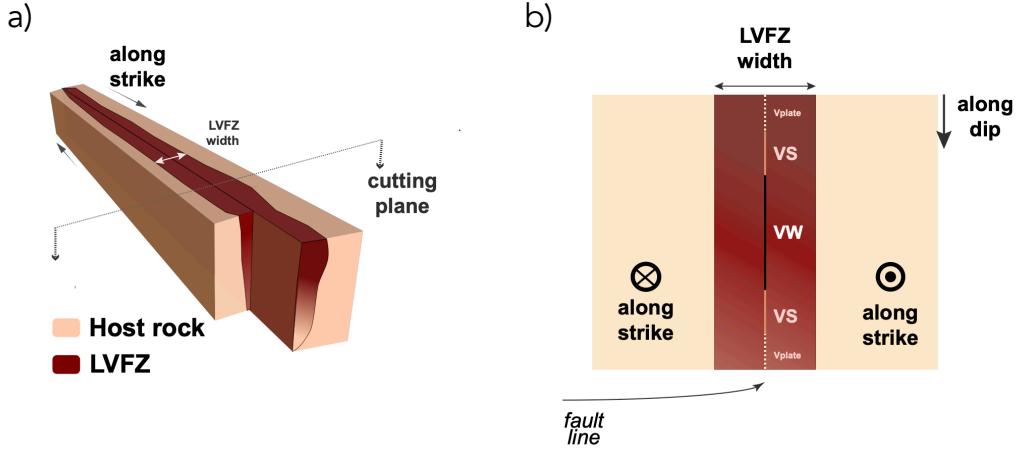


Figure 1: Illustration of damage model. (a) Conceptual, 3D representation of a vertical strike-slip fault with a damage zone, (b) 2D model built on the vertical cross-section in (a). The fault line comprises of a central velocity-weakening (VW) patch that hosts earthquakes, and is surrounded by two velocity-strengthening (VS) regions that host transient aseismic slip, which is, in turn, surrounded by outer segments that slip aseismically at steady plate velocity V_{pl} .

97 The fault shear strength is governed by the conventional rate-and-state friction law
 98 with state evolution following the ageing law (Dieterich, 1979; Ruina, 1983):

$$99 \quad f(V, \theta) = f_0 + a \ln \left(\frac{V}{V_0} \right) + b \ln \left(\frac{V_0 \theta}{D_c} \right) \quad (1)$$

$$100 \quad \dot{\theta} = 1 - \frac{V \theta}{D_c} \quad (2)$$

102 where V is slip velocity, θ the state variable, D_c the characteristic slip distance of state
 103 evolution, f_0 the steady-state friction coefficient at the reference velocity V_0 , and a and b
 104 the coefficients quantifying the direct and evolution effects, respectively.

105 The model comprises spatially variable frictional parameters that represent a seismo-
 106 genic zone surrounded by creeping segments (Fig. 1b). The central segment of length
 107 L_{vw} , referred to as “the fault” hereafter, is seismogenic: its friction is velocity-weakening
 108 at steady state ($a - b < 0$). It is surrounded by two segments of length $L_{vs} = L_{vw}/2$ that
 109 are velocity-strengthening ($a - b > 0$) and host transient aseismic slip. The outermost seg-
 110 ments slip aseismically and steadily at the prescribed plate velocity $V_{pl} = 10^{-9}$ m/s, which
 111 provides the tectonic loading.

112 A characteristic length scale of the problem is the nucleation size, L_{nuc} , which is the
 113 size of the area of aseismic slip that precedes dynamic rupture. For the ageing law and $a/b >$
 114 0.5 , a range of a/b values typically observed in laboratory experiments, in a homogeneous
 115 medium with shear modulus μ (Rubin & Ampuero, 2005):

$$116 \quad L_{nuc} = \frac{2\mu D_c b}{\pi \sigma (b - a)^2} \quad (3)$$

117 A theoretical estimate of the nucleation size in a damage zone was derived and validated
 118 numerically by Kaneko et al. (2011). It depends on damage zone thickness h and damage
 119 level Δ , and ranges between the values given by Eq. 3 with $\mu = \mu_h$ for small h and with
 120 $\mu = \mu_d$ for large h . Here, we evaluate L_{nuc} as Kaneko et al. (2011), and normalize distances
 121 by L_{nuc} and time by L_{nuc}/V_s (V_s standing for S-wave speed).

122 The problem primarily depends on three non-dimensional parameters: damage thick-
 123 ness to fault length ratio ($2h/L_{vw}$), damage level (Δ), and fault length to nucleation size
 124 ratio (L_{vw}/L_{nuc}). We consider values of damage thickness and level within ranges that led
 125 to distinctive rupture patterns in previous work by Idini and Ampuero (2020). We vary Δ
 126 between 30 and 90%, which corresponds to a velocity reduction between 17 and 68%, similar
 127 to the range observed in nature (Huang et al., 2014). We set values of damage thickness
 128 down to $2h/L_{vw} = 1/40$. Large values of L_{vw}/L_{nuc} are found necessary to produce seismic-
 129 ity with a realistic distribution of magnitudes (Cattania, 2019; Barbot, 2019), as mentioned
 130 earlier. We thus consider fault lengths as large as possible, while computationally affordable,
 131 up to $L_{vw}/L_{nuc} = 15$ for damage models and $L_{vw}/L_{nuc} = 40$ for homogeneous cases.

132 We use the spectral element method for 2D fully-dynamic earthquake cycle simula-
 133 tions. The method of Kaneko et al. (2011) was implemented by Liang et al. (2022) in the
 134 software SEM2DPACK with further optimisations and parallelism (see Data Availability
 135 Statement). It handles alternating time periods of quasi-static and dynamic fault slip by
 136 adaptive time stepping. In dynamic periods, the bottom and side boundaries function as ab-
 137 sorbing boundaries. In quasi-static periods, we prescribe on these boundaries displacements
 138 that are consistent with the plate velocity, using a back-slip approach. The simulations re-
 139 produce the fundamental phases of earthquake cycles: interseismic, pre-seismic, co-seismic
 140 and post-seismic slip. Here we focus on the co-seismic phases.

141 3 Results

142 3.1 Back-propagating fronts in large faults with and without damage

143 Back-propagating fronts are one notable form of rupture complexity associated with
 144 damage zone effects (Idini & Ampuero, 2020). They are secondary rupture fronts that
 145 propagate in the opposite direction to the main rupture front. Their possible existence
 146 in real faults was first suggested in a finite source inversion study of the 1984 Morgan
 147 Hills earthquake (Beroza & Spudich, 1988). Since then, to mitigate the non-uniqueness
 148 or ill-posedness of the inverse problem, most finite source inversions have adopted source
 149 parameterisations restricted to a single rupture front, which limits the possible discovery of
 150 more back-propagating fronts. More recently, with the advent of teleseismic back-projection
 151 studies and more flexible source inversion approaches, back-propagating fronts have been
 152 robustly imaged on different events, including the 2010 El Mayor-Cucapah (Meng et al.,
 153 2011), the 2016 Romanche oceanic transform fault (Hicks et al., 2020b), and the 2019
 154 intermediate-depth northern Peru earthquakes (Vallée et al., 2020). Numerical studies point
 155 to damage effects (Idini & Ampuero, 2020) and fault size effects (Barbot, 2019) as possible
 156 origins of back-propagating fronts. In the following, we distinguish these two effects.

157 Regardless of the presence of damage, we find that stress concentrations near the edges
 158 of creeping sections or of previous partial ruptures in a large fault can generate back-
 159 propagating fronts. Faults that are much longer than their nucleation length generate
 160 seismicity with a wide range of rupture sizes (Cattania, 2019), resulting in a heterogeneous
 161 stress state prior to any large rupture. In our simulations, such stress heterogeneity emerges
 162 when $L_{vw}/L_{nuc} \geq 10$. In smaller faults, as those considered by Kaneko et al. (2011), all
 163 events break the entire fault and leave a relatively smooth state of stress. Figures S1-2
 164 show the fault stresses before and after a full rupture, and the spatiotemporal distribution
 165 of slip rate in models without damage zone, for $L_{vw}/L_{nuc} = 10$ and $L_{vw}/L_{nuc} = 40$. In
 166 both cases, rupture nucleates near the bottom edge and propagates bilaterally at average

167 speeds of 50 to 80% of the S-wave speed V_s . Near the stress concentrations in either side of
 168 the fault, upon the arrival of main rupture fronts, new fronts emerge and propagate in the
 169 opposite direction at speeds near V_s . The emergence of such secondary fronts in the absence
 170 of damage supports the previous findings of Fig. 9a in Barbot (2019), Fig. 1e in Cattania
 171 (2019), and Fig. 2d in Idini and Ampuero (2020).

172 The initiation of back-propagating fronts at residual stresses occurs also in the presence
 173 of damage. Indeed, damage favors this mechanism by reducing the nucleation size. The
 174 example in Fig. 2a shows two such back-propagating fronts nucleating near the peaks of
 175 initial stress. They are modulated by damage zone effects: they interact with fault zone
 176 trapped waves and break up into multiple pulses, as further discussed in Section 3.2.

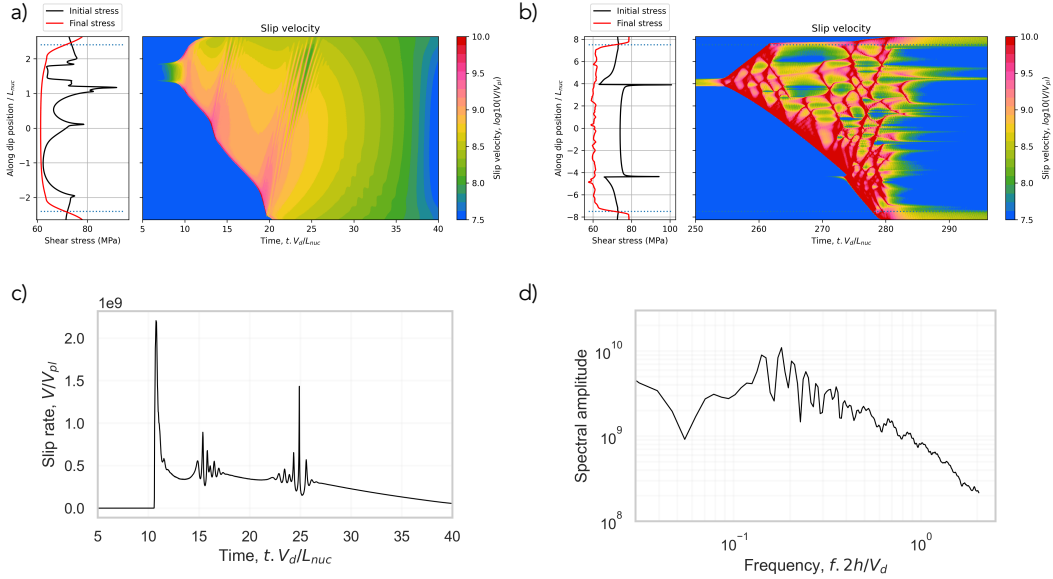


Figure 2: Back-propagating fronts in damaged faults. a) Initial (black) and final (red) stresses along the fault (left) and spatiotemporal evolution of slip rate (right) in the damage model of $L_{vw}/L_{nuc} = 5$, $\Delta = 60\%$, and $L_{vw}/2h = 40$, b) same as (a) but for the damage model of $L_{vw}/L_{nuc} = 15$, $\Delta = 90\%$, and $L_{vw}/2h = 40$, c) Slip rate at the position $2.4L_{nuc}$ in the damage model with $L_{vw}/L_{nuc} = 5$, d) Spectrum of a time window of slip rate containing fault-zone-induced oscillations in (c).

177 The presence of damage produces a separate driving mechanism for back-propagating
 178 fronts, related to transitions between pulse-like and crack-like rupture behavior. This mech-
 179 anism, first identified by Idini and Ampuero (2020) in quasi-dynamic models, can be sum-
 180 marised as follows. In homogeneous media, our models produce crack-like ruptures. Also in
 181 a damage zone, rupture is crack-like initially: since its size is much shorter than the damage
 182 zone thickness $2h$, being far from the host rock, it behaves as in a —uniformly damaged—
 183 homogeneous medium. When its length exceeds $2h$ in a highly-damaged zone, however, the
 184 rupture becomes pulse-like as it would in an elastic slab of thickness $2h$ with rigid bound-
 185 aries (Field & Baker, 1962). As rupture grows much larger than $2h$, it starts losing its
 186 sensitivity to the damage zone and behaves as in a homogeneous intact medium. Therefore,
 187 the pulse front becomes crack-like again. For this new crack propagates bilaterally, two
 188 crack fronts emerge from the pulse front (Fig. 2b, detailed below). One of these secondary
 189 crack fronts propagates in the opposite direction to the pulse: a back-propagating front. As
 190 they keep growing, the new cracks undergo crack-to-pulse and pulse-to-crack transitions;
 191 and the process repeating successively leads to the formation of multiple secondary fronts.

192 A slip budget argument further explains the necessity of multiple fronts: the slip produced
 193 by cracks and damage-induced pulses is largely different, because the former scales with
 194 rupture length whereas the latter scales with h . Even though ruptures much larger than
 195 h eventually become cracks, they pass through a stage of pulse-like rupture which leaves a
 196 slip deficit. A back-propagating front makes up for this deficit, but only partially, because
 197 it also eventually turns into a pulse. To completely fill the slip gap thus requires multiple
 198 secondary fronts.

199 Our fully-dynamic simulations confirm the existence of the damage-induced mechanism
 200 of back-propagating fronts in large faults. Because a sufficiently large $L_{vw}/2h$ and high
 201 damage are required for the crack-to-pulse transition to manifest, we set $L_{vw}/2h = 40$ and
 202 $\Delta = 90\%$. An example is shown in Fig. 2b. Initially, rupture propagates bilaterally at
 203 speeds in the range of 50 – 100% V_d . Secondary fronts nucleate at various locations along
 204 the fault, including multiple fronts that nucleate well after the passage of the main front
 205 and propagate bilaterally at speeds close to V_d . Their nucleation points do not coincide
 206 with the peaks of initial stress, but rather with stress heterogeneities forming during the
 207 previous stages of the rupture. These rich rupture patterns do not occur in models without
 208 damage, even with large L_{vw}/L_{nuc} (see the homogeneous case in Fig. S2); which thus
 209 counters the suggestion of Nie and Barbot (2022) that rupture style in a damage zone is
 210 simply controlled by the ratio of fault size to nucleation size. Moreover, by comparing
 211 quasi-dynamic and fully-dynamic models, we find that dynamic effects tend to increase the
 212 occurrence of secondary fronts and amplify their peak slip rates (Figs. S3-4).

213 3.2 Source modulations caused by fault damage zones

214 We find that interactions between rupture fronts and trapped waves in a damage zone
 215 cause slip rate oscillations, at frequencies that are characteristic of the damage zone. Fig.
 216 2c shows an example of such oscillations. Their spectrum prominently peaks at a frequency
 217 near $V_d/4(2h)$, the fundamental frequency of wave reverberations across the damage zone
 218 which constructively interfere to form trapped waves. Our analyses of cases with different
 219 damage levels confirm this interpretation (Fig. S5).

220 Damage-induced rupture effects can sharpen the complexity of source time functions
 221 (STF). Fig. 3a compares STFs of models with and without damage zone. While the STF
 222 in the homogeneous case has a single peak, the damage model produces multiple sharp
 223 peaks resulting from both back-propagating fronts and slip rate oscillations (as also found
 224 in other cases, Fig. S6). Real STFs often exhibit multiple peaks that are usually interpreted
 225 as sub-events originating from different rupture segments, often associated with structural
 226 segmentation by frictional or geometrical barriers along the fault (e.g., Vallée, 2013; Ross et
 227 al., 2019). Our finding alternatively suggests that multiple peaks in a STF can originate from
 228 damage zone effects, even on faults with uniform frictional properties and simple geometry.

229 Damage-induced rupture complexity also amplifies high-frequency radiation. Compar-
 230 ing STF source spectra of models with and without damage zone (Fig. 3b) reveals a system-
 231 atic amplification above the corner frequency in damage models relative to homogeneous
 232 models, up to a factor of ~ 10 . This highlights the potential significance of damage effects on
 233 far-field observations. The damage-caused excessive high-frequency radiation occurs in the
 234 broad band above the corner frequency — not at a specific frequency that can be associated
 235 with damage zone properties. While this challenges the inference of damage-induced rup-
 236 ture effects from far-field data, in the next section, we investigate the potential signatures of
 237 damage-induced slip rate oscillations and back-propagating fronts in near-field observations.

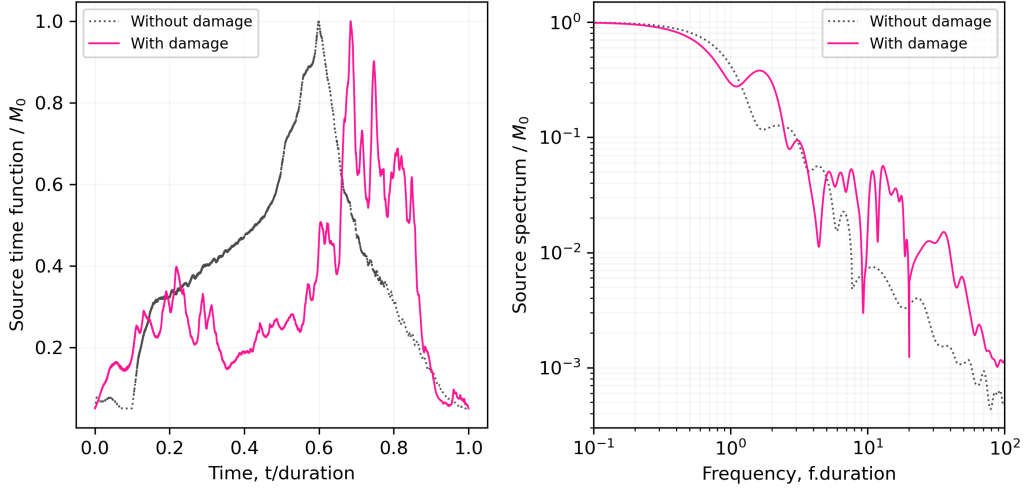


Figure 3: Far-field view of damage-induced source complexity. a) Source time functions of models with damage zone ($L_{vw}/L_{nuc} = 15$, $\Delta = 90\%$, and $L_{vw}/2h = 40$) and without damage zone ($L_{vw}/L_{nuc} = 40$), b) Their spectra. To facilitate the comparison, amplitudes are normalized by seismic moment, and time by rupture duration. The damage model is the same as in Fig. 2b.

3.3 Damage effects on near-field ground motions

The effects of both initial stresses and damage zones on earthquake rupture affect ground motion and its spatial variability. A higher initial stress can result in stronger ground motion by increasing stress drop (e.g. Cotton et al., 2013) and rupture speed (e.g. Aagard and Heaton, 2004), and initial stress heterogeneity can enhance high-frequency strong motion (Madariaga, 1983; Kame & Uchida, 2008). Damage can amplify near-source ground motion by trapped wave modulation of the source (Section 3.2, and e.g., Ben-Zion et al., 2003). Our models produce ground motion amplification by both factors, and here we assess their respective effects on peak ground velocities (PGV).

We find that near-field ground motion is governed by initial stress heterogeneity, and further affected by damage effects. Fig. 4ab shows the initial stresses and spatial distribution of PGVs for two homogeneous and damage models. In the homogeneous model, rupture nucleates near the bottom edge where the initial stress is the largest. Initial stress peaks are also present near the upper edge. In the damage model, the largest stresses are concentrated near both edges, and residual stress peaks are also present in the central portion. The largest PGVs (above 2 and 4 m/s in homogeneous and damage models, respectively) are concentrated near these high-stress areas. This spatial correlation is expected from the radiation of strong motion phases due to abrupt changes in rupture speed when rupture encounters residual stress concentrations (Madariaga, 1983; Kame & Uchida, 2008). Such ground motion amplification due to initial stress heterogeneity manifests as along-fault ground motion variability. Comparing the two cases in Fig. 4c, PGV decreases with distance to the fault as expected. The PGVs in the damage model are smaller than in the homogeneous model outside the damage zone, but larger inside the damage zone, by a factor of ~ 2 . This damage-induced amplification results in a sharp contrast between the regions inside and outside the damage zone all along the fault. In Fig. S7 we show similar findings for a case with smaller nucleation length. Overall, we find that initial stresses are the main control of the spatial variability of peak ground motion along the fault, while damage-induced amplification strongly affects the ground motion variability across the fault.

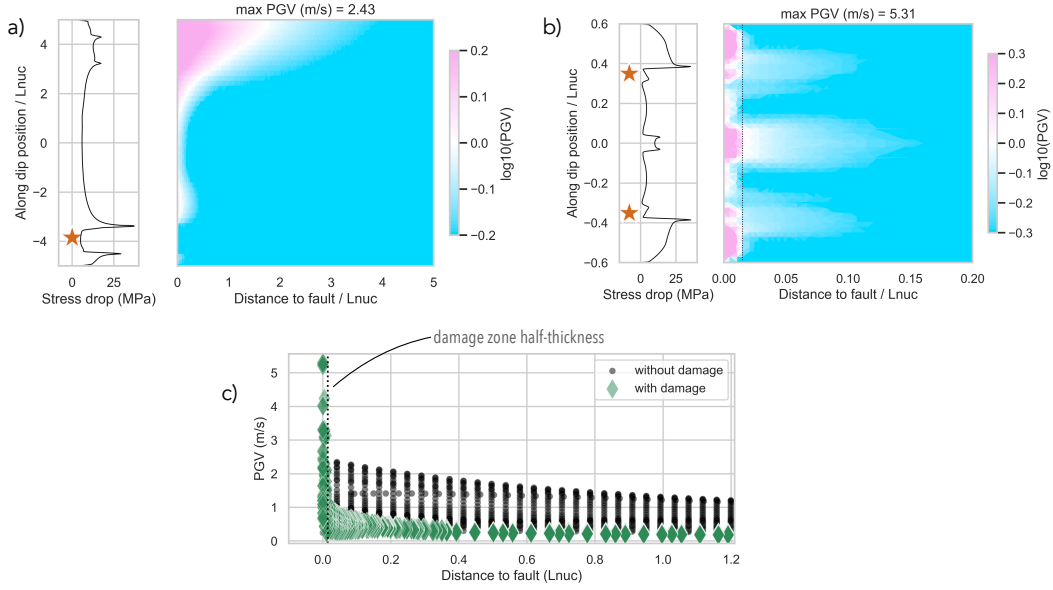


Figure 4: Stress heterogeneity and damage effects on near field ground motion. a) Initial stress and spatiotemporal change of slip rate in the homogeneous model of $L_{vw}/L_{nuc} = 10$, b) same as (a) but for the damage model ($L_{vw}/L_{nuc} = 1.2$, $\Delta = 90\%$, and $L_{vw}/2h = 40$), and c) comparison of peak ground velocities (PGV) as a function of fault distance between homogeneous and damage models.

266 Back-propagating fronts are visible in the near-field seismograms and can locally affect
 267 the peak ground motion. In both homogeneous and damage cases, waves radiated by sec-
 268 ondary fronts are present in the seismograms as later arriving pulses at various distances
 269 (Fig. S8). At some distances (Fig. S9b) the largest peaks are in the first arriving pulses,
 270 which are radiated by the primary rupture front. At other distances (Fig. S9cd), the later
 271 pulses generated by secondary fronts have the largest amplitudes. Considering the recent
 272 advances in near-fault monitoring techniques (e.g., Qiu et al., 2021; Li et al., 2023), our
 273 finding underpins the potential for the discovery of back-propagating fronts in dense arrays
 274 close to faults.

275 4 Conclusions

276 We studied the effects of fault damage zones on rupture dynamics and ground motions
 277 by 2D fully-dynamic earthquake cycle modelling. Our simulations span a relevant range of
 278 fault sizes (relative to nucleation size, L_{nuc}) and damage zone properties, and expand the
 279 insights from previous quasi-dynamic modelling studies.

280 We confirm that both damage zone properties and relative fault size control rupture
 281 complexity, and we identify their respective effects. In particular, we distinguish the mech-
 282 anisms of secondary rupture front generation due to each. On large faults, regardless of the
 283 presence of damage, the emergence of heterogeneous stress states featuring residual stress
 284 concentrations induces back-propagating fronts. In the presence of damage, an additional
 285 mechanism owing to a pulse-to-crack transition (Idini & Ampuero, 2020) operates on faults
 286 that have sufficiently high damage levels and thicknesses, and are relatively large ($15L_{nuc}$
 287 here).

288 Damage-induced rupture complexity potentially imprints seismological signatures both
 289 in the near and far field. Rupture fronts interact with damage zone trapped waves, leading
 290 to oscillations in slip rate at resonance frequencies that are characteristic of the damage
 291 zone. Damage-induced oscillations and secondary fronts amplify high-frequency radiation
 292 and enhance the complexity of source time functions, manifested by multiple moment rate
 293 peaks, which is potentially observable in the far field. Regarding near-field ground motions,
 294 residual stress concentrations predominantly shape the spatial variability of peak ground
 295 velocities along strike, while damage affects the variability across the fault by introducing
 296 a contrast between ground motions inside and outside the damage zone. Additionally,
 297 damage-induced secondary fronts can locally amplify peak ground motions far from the
 298 damage zone, and increase the hazard therein.

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309 Data Availability Statement

310 All data needed to reproduce this work is available online: 2D fully dynamic cycle mod-
 311 eling tools and quasi-dynamic comparison models can be found at [https://github.com/
 312 jpampuero/sem2dpack](https://github.com/jpampuero/sem2dpack), and [https://github.com/elifo/qdyn/tree/master/examples/
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