

Weak phases production and heat generation controls fault friction during seismic slip

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The triggering and magnitude of earthquakes is determined by the friction evolution along faults. Experimental results have revealed a drastic decrease of the friction coefficient for velocities close to the maximum seismic one, independently of the material studied^{1,2}. Due to the extreme loading conditions during seismic slip, many competing physical phenomena are occurring (like mineral decomposition³, nanoparticle lubrication¹, melting⁴ among others) that are typically thermal in origin⁵ and are changing the nature of the material.

Here we show that a large set of experimental data for different rocks can be described by such thermally-activated mechanisms⁶, combined with the production of weak phases. By taking under account the energy balance of all processes during fault movement, we present a framework that reconciles the data, and is capable of explaining the frictional behavior of faults, across the full range of slip velocities (10^{-9} – 10 m/s).

The similarity of microstructures observed in nature and in experiments suggests that energetic frameworks like the one presented could quantitatively link observations across the scales and provide deep, physics-based insight on the physical mechanisms driving seismic slip.

The knowledge of the friction (shear strength) evolution along a pre-existing fault is of major

21 importance, as it allows extracting many characteristics and features of seismic slip. In particular,
22 the decrease of the friction with increasing velocity or displacement (a process called frictional
23 weakening) determines the possible nucleation of earthquakes. If the weakening rate is larger than
24 a critical value, this leads to the triggering of a dynamic slip at the origin of earthquakes⁷. In
25 addition to nucleation, the evolution of the friction coefficient- and thus of the fault's shearing
26 resistance- determines the arrest of the fault slip and governs the form and budget of energy dissi-
27 pation during seismic slip⁸. The latter is essential as it determines the amount of energy produced
28 at the fault, which is radiated on the surface through seismic waves and tremors.

29 During the last 20 years, a large set of experimental works has been devoted to reproducing
30 the extreme conditions of a seismic slip. The development of high velocity shear apparatus al-
31 lowed the research community to perform experiments at the maximum velocity reached during an
32 earthquake event (1 – 10 m/s) and, thus, characterize the behaviour of a fault over the full range of
33 possible slip rates⁹. A drastic decrease of the friction has been observed in most cases for veloc-
34 ities closed to the maximum slip velocity independently of the material considered¹, however the
35 physical mechanisms accompanying this rapid weakening being different for each rock type. Fol-
36 lowing microstructural observations and measurements in the sheared samples, several thermally
37 and mechanically activated weakening mechanisms were proposed to understand the experimental
38 results at seismic slip rates⁶. The common feature of all these weakening mechanisms is phase
39 transformation -like mineral decomposition³, nanoparticle lubrication¹, melting⁴- during which a
40 change in the nature of the material takes place.

41 To describe the effect of such a weak phase on the frictional behaviour of a mixture of a
42 strong/weak phase and constrain the influence of phase change on the mechanical behaviour, we
43 consider first experiments looking at the effect of a weak phase on the frictional response of fault
44 zones. The weak phases used for the tests are talc or saturated clay materials sheared at low
45 velocities (lower than 10^{-5} m/s), so that the mechanisms described above are not triggered. The
46 results are shown in Figure 1, where we may observe that the friction coefficient μ decreases as
47 the weak phase fraction increases. This effect of the weak phase fraction can be captured using
48 an exponential law $\mu = \mu_0 + \Delta\mu e^{-\alpha w}$, where μ_0 is the friction coefficient of the weak phase,
49 $\Delta\mu = \mu_s - \mu_0$ is the difference of the friction coefficient of the strong and weak phases, w is
50 the weak phase fraction and α a weakening coefficient ranging from 0.1 to 15 (see supplementary
51 information). Note that such nonlinear weakening laws are also used in geomechanical engineering
52 to describe the weathering of calcarenite^{10,11}.

53 The derived exponential decrease of the mechanical strength from the experimental data of
54 Figure 1 is then included into a thermo-chemo mechanical model that accounts for the coupled
55 mechanisms activated at higher velocity conditions (see Methods for the mathematical description
56 of the model). In this model, the degradation or creation of a weak phase is induced by the energy
57 input to the system and it is not present before shearing. This unifying approach aims at reconcil-
58 ing observations across a wide spectrum of materials and velocities. The extensive experimental
59 data set used for the comparison corresponds to shear tests performed with rotary shear apparatus
60 that allows to reach high displacements and therefore the steady state (see Figure 2). These exper-
61 iments are realized on either gouge granular samples (usually 1mm thick¹⁷) sandwiched between

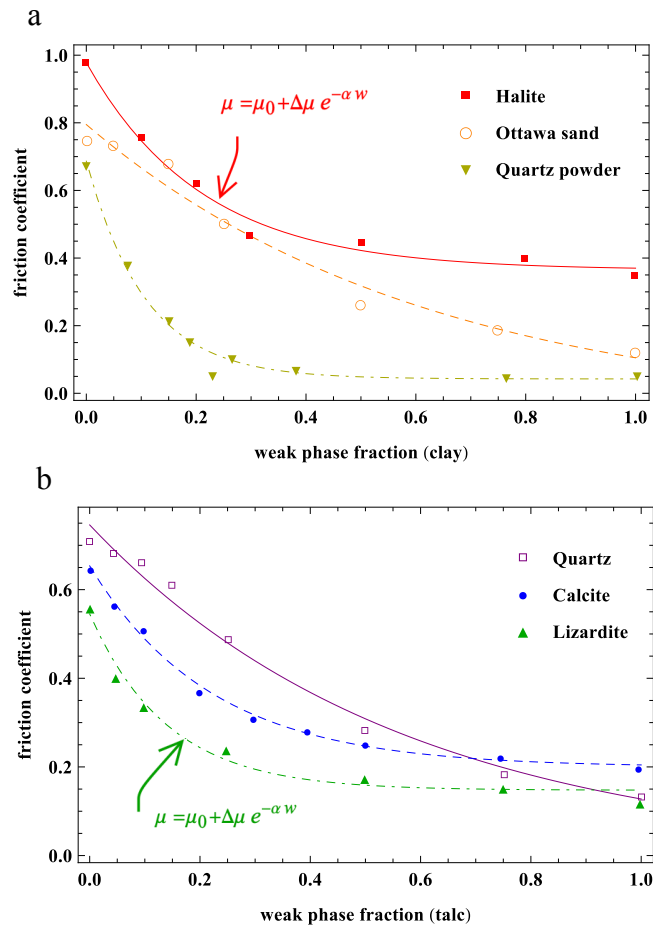


Figure 1: **Effect of the weak phase content on the steady state friction coefficient.** The friction of weak/strong phase binary mixtures is represented as function of the weak phase content in experiments carried out at subseismic sliding velocities and at constant normal stress using triaxial saw cut, double and simple direct shear and rotary shear configurations. **a**, results for clay as weak phase: red corresponds to a muscovite/halite mixture ¹², orange to a crushed Ottawa sand/montmorillonite mixture ¹³, dark yellow to a quartz powder/bentonite mixture ¹⁴. **b**, results for talc as weak phase: purple corresponds to quartz as strong phase ¹⁴, blue to calcite ¹⁶, green to Lizardite ¹⁵. In **a-b**, the points represent the experimental data and the solid or dashed lines represent the interpolation using this exponential function.

62 two blocks or on bare rock samples¹⁸. In the latter, a gouge material is formed after only a few
63 millimetres of displacement² with a thickness of 100 to 300 μm . The data are gathered based on
64 the nature of the material sheared and the physical mechanisms that are inferred to operate during
65 the experiments^{1,19}.

66 The constitutive law for the mechanical behaviour is applied to the gouge material, which ac-
67 commodates all the deformation and is affected by the temperature, the weak phase fraction and the
68 state of stress. The weak phase creation is modelled as an endothermic first order chemical trans-
69 formation affecting the energy balance equation and respecting the mass balance. The geometry
70 of the model chosen is larger of one or two orders of magnitude than the gouge in order to impose
71 far field boundary conditions for the temperature and the extend of the phase transformation (see
72 Figure 2). The steady states of this model can be determined using a continuation algorithm (see
73 Methods), to test the hypothesis that the combination of thermally activated weakening and the
74 creation of a weak phase may account for the observed steady state frictional response over many
75 orders of magnitude of shear velocity.

76 The resulting steady state response of the model, in terms of friction and velocity, is depicted
77 in Fig. 2. We can identify five distinct regimes of the system response to loading velocity: (I)
78 **Static**. At low velocities, the material remains at static friction. Negligible temperature increase
79 or weak phase production is observed. (II) **Thermo-mechanical weakening**. The temperature
80 increase leads the friction coefficient to drop, in the absence of any weak phase production. (III)
81 **Thermo-chemical stabilization**. With increasing velocity and temperature, small fractions of the

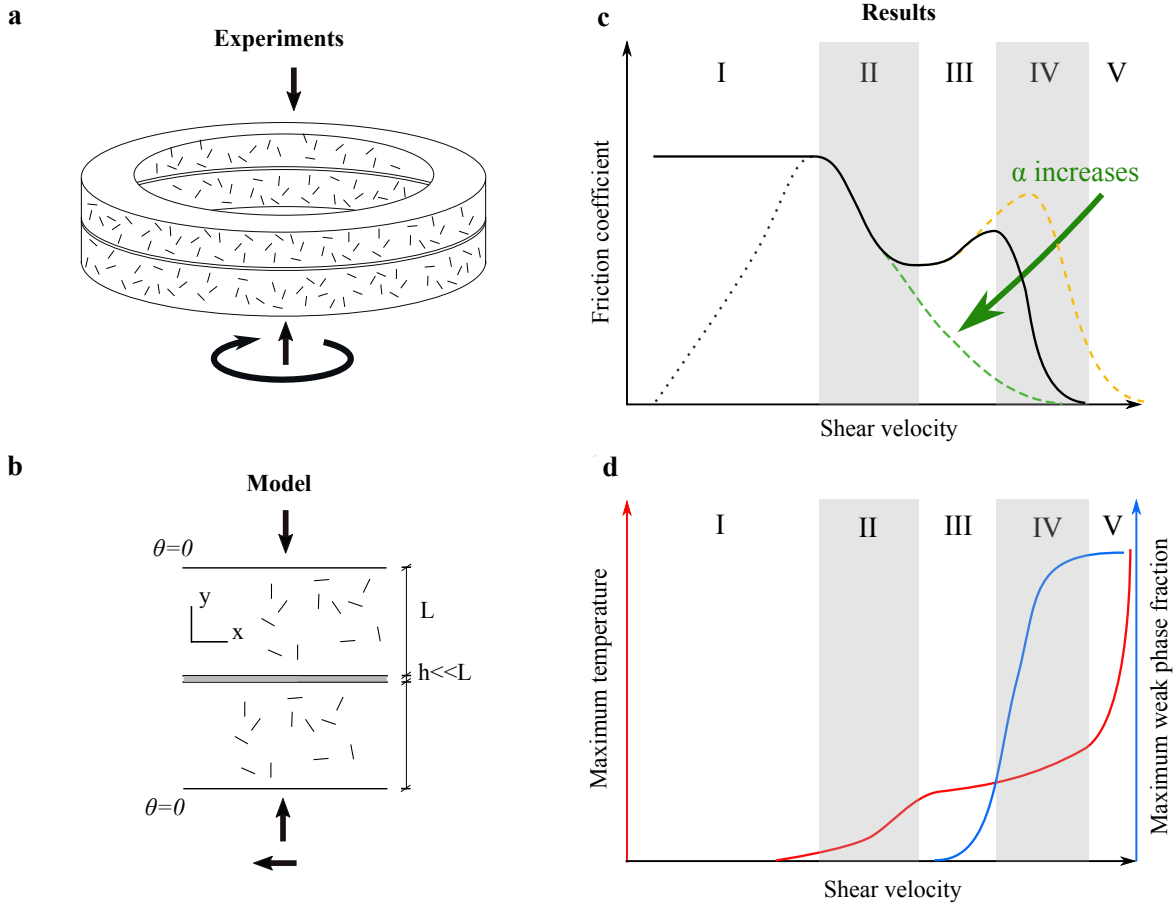


Figure 2: **a-b**, Schematic view of the geometry of the high velocity rotary shear experiments and the model. **c-d**, Steady state of the thermo-chemo mechanical model. Response of the mathematical system of equations (Eqs. 5-6 in Methods) at steady state. **c**, the steady state friction coefficient as a function of velocity, for varying weak phase sensitivity coefficient α . **d**, the steady-state temperature and weak phase content dependency on the velocity, plotted for the black line of **c**. The five regimes (I - V) that can be observed in the response of the friction coefficient are correlated with the temperature and weak phase production processes, as explained in the main text.

82 weak phase are produced, absorbing the excess temperature and reducing the thermal softening
83 effect on the friction coefficient. Depending on the value of the weakening coefficient, the friction
84 coefficient can experience an intermediate increase. (IV) **Chemo-mechanical weakening.** Even-
85 tually, weak phase content will be produced until it reaches a critical value that will dominate the
86 friction coefficient and lead the material to unconstrained weakening. (V) **Runaway instability.**
87 Once the reactants are depleted ($w = 1$), the temperature is increasing uncontrollably and the
88 friction coefficient drops towards zero.

89 After identifying the regimes of the steady frictional response of faults, the model is applied
90 to experimental data. Figure 3 summarizes the results of the model for the steady state friction
91 coefficient as a function of the velocity for six sets of materials^{1,9,18-21}. The experimental data
92 are a collection of several independent studies at different experimental conditions. As shown in
93 the supplementary information, the normal stress shows no clear effect on the value of the friction
94 coefficient reported here and for this reason it is not further investigated in this study. One of
95 the interesting features of the model is the reproduction of strengthening observed experimentally
96 at intermediate velocities (regime III in Figure 2) without supposing any additional hardening
97 mechanism. For each material, the inferred phase transformation and the resulting weak product
98 are highlighted. The model enables to capture accurately the observations and uses as input the
99 material parameters listed in the supplementary information. Moreover, it enables us to retrieve
100 information for the parameters of the different processes such as the activation energies, together
101 with an assessment of the temperature evolution. This can be used as a basis to compare with
102 the microstructural observations of the samples after the experiments. Indeed, in Figure 4 we

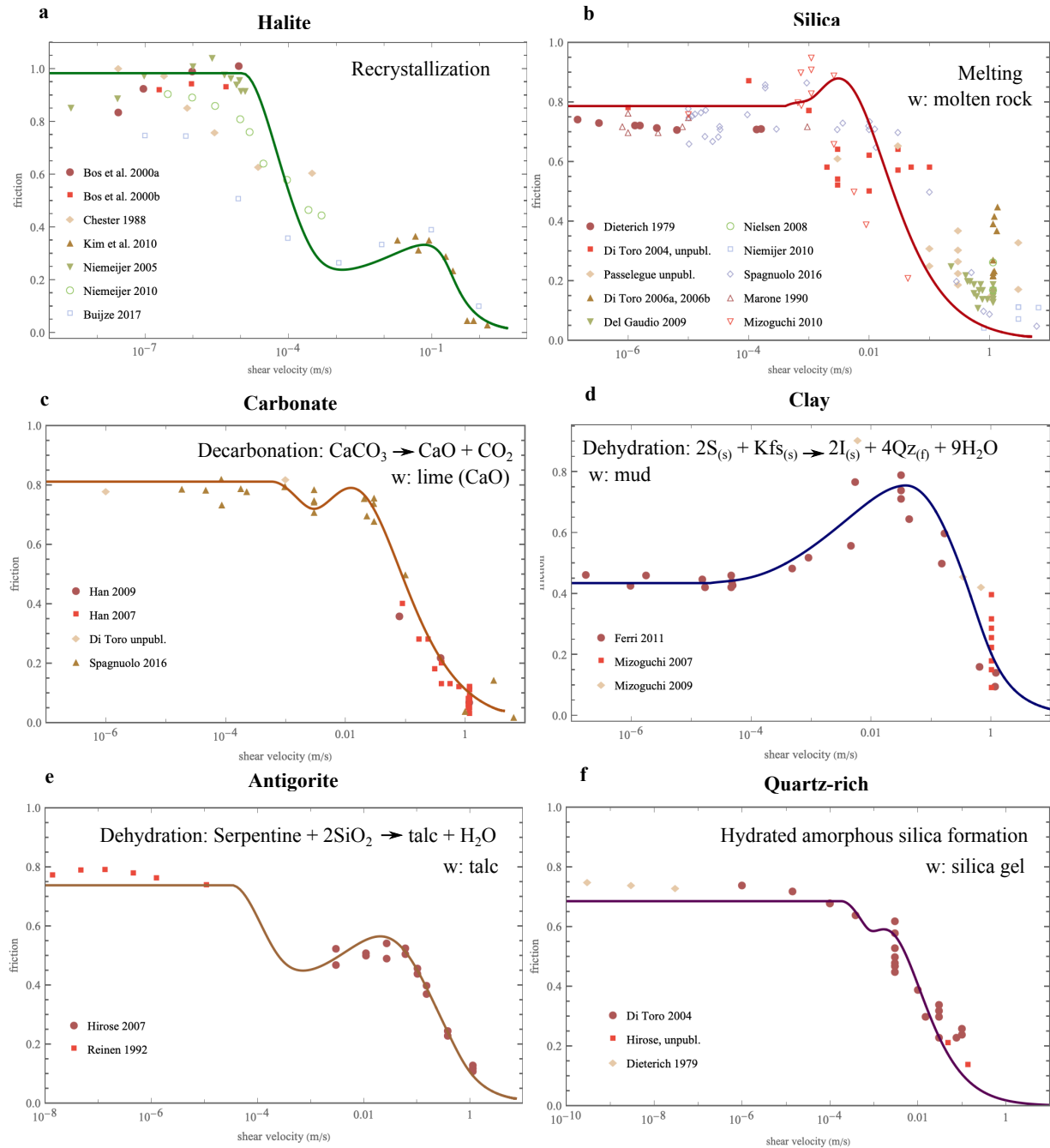


Figure 3: Results of the model for different types of materials. Application of the mathematical model (solid lines) to literature data (dots) of the friction coefficient as a function of the velocity. See the Methods for the mathematical description, Fig. 2 for the qualitative steady-state response and the supplementary information for the references of the experimental data. For each material, the phase transformation and the associated weak phase are indicated. **a**, for halite rocks. The model reproduces the experimental behaviour with $\alpha = 0$. **b**, for silicate rocks ($\alpha = 7.5$). **c**, for carbonate rocks ($\alpha = 5.3$). **d**, for clay-rich rocks ($\alpha = 2$). **e**, for antigorite ($\alpha = 1.5$). **f**, for quartz-rich rocks ($\alpha = 14$).

103 are summarizing the evolution of the Temperature and weak phase ratio w required to obtain the
104 friction coefficient results of Figure 3. Based on these two figures, we can compile the processes
105 underpinning the macroscopic response of the frictional resistance of the different materials.

106 The temperature predicted by the model when the weak phase begins to appear can be
107 compared to the theoretical activation temperature of the phase transformation (decarbonation²²,
108 melting²³, dehydration²⁴ or clay type transition⁹), when available. In all cases, the temperature of
109 the model is lower than the theoretical one (e.g. 530° C against 720° C for carbonates) imply-
110 ing that the phase transition is triggered locally at the contact of the grains where the temperature
111 can be higher than the bulk temperature. Moreover, these local phase changes are hard to detect
112 even though essential for the mechanical behaviour. This also explains why the evidences of the
113 phase transformations from specific sensors or microstructural observations (recrystallized halite
114 grains¹⁷, increase of CO₂²² or humidity next to the tested sample¹⁸, melted asperities²⁵ and white
115 flakes due to silica gel²⁰) are retrieved for higher velocities in experiments than predicted by the
116 model. A notable case is halite, for which the weakening factor is $\alpha = 0$ implying that any weak
117 phase generated during shear does not affect the friction coefficient. As the material undergoes
118 recrystallisation¹⁷ during shearing which is a phase transformation that produces the same mineral
119 with different grain sizes. Despite not producing a weak phase directly though, recrystallisation af-
120 fects the energy budget and, thus the temperature produced (Figure 4) and therefore the mechanical
121 behaviour of the gouge.

122 These results suggest that a thermally activated creep and the transformation of the material

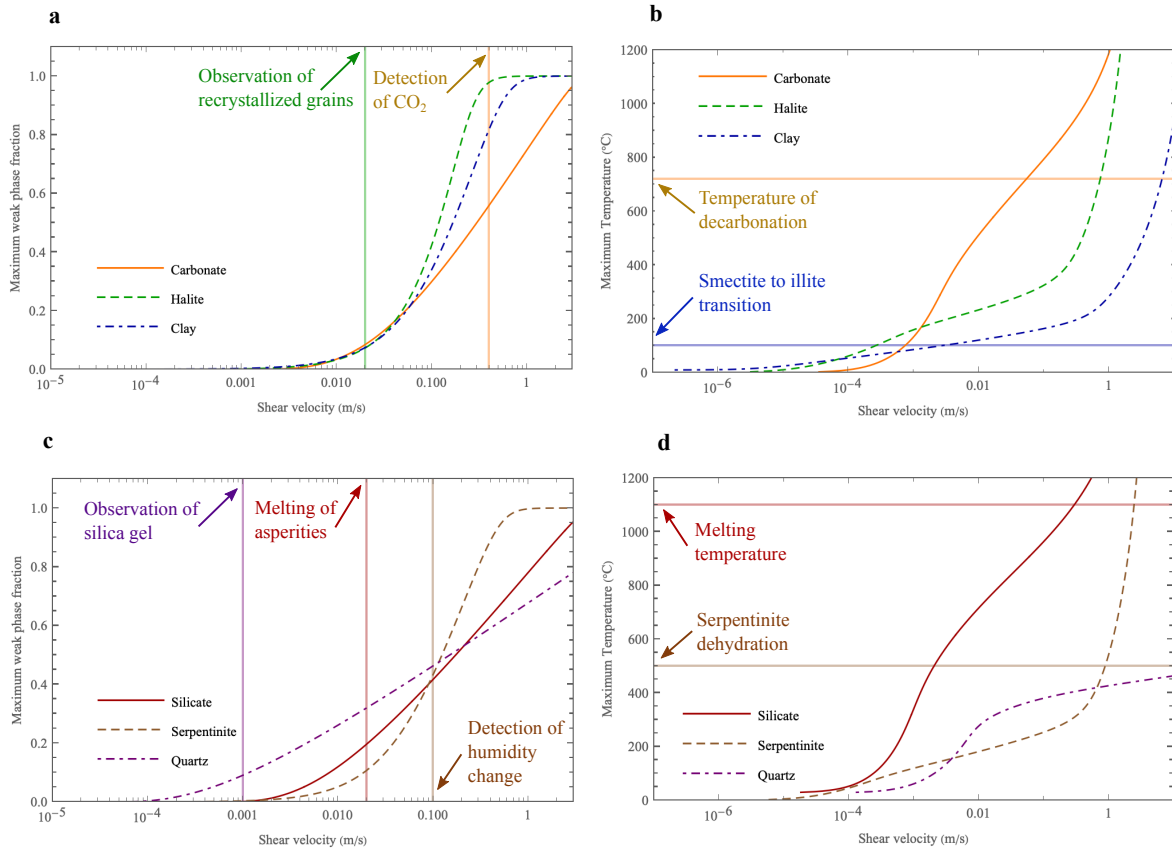


Figure 4: **Temperature and weak phase fraction evolution with the velocity for the experiments of Fig. 3.** **a** and **c**, weak phase fraction in the middle of the sample. Note that weak phase production has been approached as a first order chemical reaction, thus reaching its maximum value of one (100% weak phase present) when the reaction is depleted. **b** and **d**, maximum temperature in the middle of the sample.

123 inside the fault zone may be the dominant mechanisms during seismic slip of dry rocks. In the case
124 where pressurized fluids are present -a scenario difficult to study experimentally- the static friction
125 response⁹ and the transient behaviour through thermal pressurization^{26,27} are likely to be affected.
126 In that case a detailed comparison between phase transition and thermal pressurization needs to be
127 carried, to assess the dominant mechanism of slip ²⁸.

128 **Methods**

129 **Description of the Mathematical Model.** When the shear velocity applied to a rock or a granular
130 sample is increased, thermal effects tend to dominate the frictional response^{5,20,29,30}. A critical
131 velocity is required to activate this mechanism that is related to the processes at asperities or grain
132 contacts⁵. In this paper, we focus on the response of the material for intermediate and high veloc-
133 ities where the thermal and chemical effect are important (other models have been developed for
134 lower velocities and the nucleation of earthquakes^{29,31}). Therefore, we consider here that for low
135 velocities experiments the strength of the material is determined by the static friction of the ma-
136 terials in contact or the internal static friction of the granular assembly. For velocities larger than
137 the critical one, the shear stress of the system is calculated by solving a thermo-chemo-mechanical
138 model inside the deforming zone. The critical velocity is retrieved as a result from this model
139 and can be approximated by an analytical solution (see supplementary information). Physically, it
140 corresponds to the critical velocity for which thermal weakening becomes significant.

141 The mathematical model consists of solving the momentum, mass and energy balance equa-
142 tion at steady state, for an infinite sheared layer. The equations are briefly summarized here for
143 easiness in reproducibility of the results³.

144 The momentum balance equations are considered and we neglect the inertia terms³²:

$$\sigma_{ij,j} = 0 \quad (1)$$

145 where σ_{ij} is the stress tensor. These equations lead in the case of one dimensional shear zone to a
146 constant normal and shear stress in space inside the layer.

147 The constitutive law for the mechanical behaviour is a rigid elastic-viscoplastic law with
 148 the most generic form: an Arrhenius-power law dependency^{3,33}. This law is only considered in
 149 a layer of thickness h , much smaller than the total thickness of the layer L (see Figure 2). This
 150 enables to describe the fact that after only a few millimetres of slip during the shear experiments
 151 on bare rocks, a thin layer of gouge materials forms. This layer composed of crushed grains from
 152 the initially rough surfaces has generally a thickness of 100-300 μm^2 and accommodates all the
 153 deformation. However, as the boundary conditions for the weak phase and the temperature are
 154 not well defined for this gouge layer, a domain of 1 cm is considered in order to apply Dirichlet
 155 boundary conditions for these fields.

$$\dot{\epsilon}^{vp} = \dot{\epsilon}^0 \left(\frac{\tau}{\tau_y} \right)^m e^{-Q/RT} \quad (2)$$

156 where $\dot{\epsilon}^0$ is a reference strain rate, m is the exponent of the power law, τ is the shear stress, τ_y is
 157 the yield stress, Q is an activation enthalpy for the microscopic mechanism inducing a nonlinear
 158 behaviour, R is the perfect gas constant and T is the temperature. This law allows to include more
 159 physics into the hardening evolution as in the theory of plasticity for metals³³. The Arrhenius
 160 dependency of the flow law enables to introduce multi-physical couplings such as the effect of
 161 heat generation on the frictional strength or more generally interface phenomena between the solid
 162 skeleton and the pores^{34,35}.

163 The effect of the non-mechanical state variables on the mechanical behaviour of the system
 164 can be expressed as a single scalar function called the weathering index¹¹, X_d . The strength of the
 165 material depends on both the plastic strain and this weathering index. It is assumed that the two

166 effects are uncoupled^{10,11} and a multiplicative structure of the yield stress is postulated:

$$\tau_y = T_y(\epsilon^p)T_y(X_d) \quad (3)$$

167 In our case, we do not consider any purely mechanical hardening law, so that the function $T_y(\epsilon^p)$ is
 168 constant. Moreover, X_d is considered to be a weak phase volume fraction. As shown in Figure 1,
 169 the presence of a weak phase induces an exponential decrease of the frictional strength along with
 170 the weak phase fraction. Assuming negligible shear strength for the weak phase, the final form of
 171 the constitutive law is therefore:

$$\dot{\epsilon}^{vp} = \dot{\epsilon}^0 \left(\frac{\tau}{\tau_0} \right)^m e^{-Q/RT} e^{\alpha m w} \quad (4)$$

172 where τ_0 is the yield strength of the strong phase and α is the weak phase sensitivity coefficient.

173 For a material consisting of two species: a weak and a strong phase, occupying volumes V_w
 174 and V_s respectively, we may define the volume ratio $w = \frac{V_w}{V_w + V_s}$. Inside a one dimensional shear
 175 zone yield a system of two equations^{3,36} obtained from the mass balance of the weak phase fraction
 176 and the energy balance equations:

$$\frac{\partial T}{\partial t} = c_{th} \frac{\partial^2 T}{\partial y^2} + F(y) \frac{\tau \dot{\epsilon}^{vp}}{\rho C} - \frac{\Delta H r_F}{\rho C} \quad (5)$$

$$\frac{\partial \rho_1}{\partial t} + \frac{\partial J_w}{\partial y} = r_F \quad (6)$$

177 where T is the temperature, c_{th} the thermal diffusivity, ρC the heat capacity of the mixture con-
 178 sidered constant here, J_w the diffusion flux of the weak phase, ΔH the enthalpy of the phase
 179 change reaction considered endothermic, r_F the reaction rate and $\rho_1 = \rho_w w$. $F(y)$ is a function
 180 which value is 1 for $y \in [-h/2, h/2]$ and 0 otherwise. The reaction rate is expressed as first order

181 chemical reaction with an Arrhenius law.

$$r_F = (1 - w) \frac{\rho_s}{M_s} k_F e^{-Q_c/RT} \quad (7)$$

182 where ρ_s and M_s are the density and molar mass of the strong phase. k_F and Q_c are the preexpo-
 183 nential factor and activation energy of the chemical reaction. Using Equations 4, 7, considering a
 184 Fick's law for the diffusion flux (defining a diffusivity c_w) and the steady state of Equations 5 and
 185 6, we obtain a system of two differential equations in space. This system is written in a dimension-
 186 less form for the purpose of reducing the number of parameters to study and to enable a clearer
 187 understanding of the main features of the system:

$$\frac{\partial^2 \theta}{\partial \bar{y}^2} + F(\bar{y}) Gr e^{\frac{Ar \theta}{1+\theta}} e^{\alpha m w} - Da(1 - w) e^{\frac{Arc \theta}{1+\theta}} = 0 \quad (8)$$

$$\frac{\partial w}{\partial \bar{y}^2} + \mu Da(1 - w) e^{\frac{Arc \theta}{1+\theta}} = 0 \quad (9)$$

188 where, θ is the dimensionless temperature. Gr , Da , Ar and Arc are called the Gruntfest, Damköhler,
 189 Arrhenius and chemical Arrhenius numbers respectively. They are defined by:

$$Ar = \frac{Q}{R T_0}, \quad Arc = \frac{Q_c}{R T_0} \quad (10)$$

$$Gr = \frac{\tau_0 \dot{\epsilon}_0 L^2}{\rho C c_{th} T_0} \left(\frac{\tau}{\tau_0} \right)^{m+1} e^{-Ar} \quad (11)$$

$$Da = \frac{\Delta H k_F \rho_s L^2}{\rho C M_s c_{th} T_0} e^{-Arc} \quad (12)$$

$$\mu = \frac{\rho C c_{th} T_0 M_w}{\Delta H \rho_w c_w} \quad (13)$$

190 **Numerical Bifurcation of the Steady State friction coefficient.** The solutions of this nonlinear
 191 system of differential equations are approximated numerically using pseudospectral methods. The
 192 temperature and weak phase fraction fields are interpolated in space using Chebyshev polynomials

193 of the first kind:

$$\theta(\bar{y}) = \sum_{i=1}^N a_i (\phi_{2i}(\bar{y}) - 1) \quad (14)$$

$$w(\bar{y}) = \sum_{i=1}^N b_i (\phi_{2i}(\bar{y}) - 1) \quad (15)$$

194 where ϕ_{2i} are the Chebyshev polynomials of degree $2i$. Note that only the even degree Chebyshev
195 polynomials are kept here as the solution is symmetric about the origin. Moreover, a basis recom-
196 bination is used by considering interpolation functions of the form $\psi_{2i}(y) = \phi_{2i}(y) - 1$, allowing
197 to enforce a zero Dirichlet boundary conditions implicitly³⁸. N is the number of polynomials used
198 to simulate the solutions. A convergence analysis has been conducted in each case to verify that N
199 is high enough to have a negligible error on the solution. a_i and b_i are the interpolation coefficients
200 for the temperature and the weak phase fraction respectively. The interpolation points used for the
201 resolution are the Gauss-Lobato points defined by:

$$x_j = \cos\left(\frac{(2j-1)\pi}{4N}\right), \quad j = 1, \dots, N \quad (16)$$

202 The nonlinear system of algebraic equations obtained is solved using the Newton-Raphson method.
203 In order to capture all the steady state solutions of the system for the different values of the stress, a
204 continuation pseudo-arclength algorithm is used. The continuation parameter chosen is the Grunt-
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