

The effects of precursory velocity changes on earthquake nucleation and stress evolution in dynamic earthquake cycle simulations

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This is a non peer-reviewed preprint submitted to Earth and Planetary Science Letters.

EarthArXiv Preprint

Highlights

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- Earthquake cycles are simulated with precursory velocity change in fault damage zone
- Earlier onset of precursors reduces nucleation size and causes earlier nucleation
- Such precursors affect the occurrence of slow-slip events between large earthquakes

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The effects of precursory velocity changes on earthquake nucleation and stress evolution in dynamic earthquake cycle simulations

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Abstract

Seismic velocity changes in earthquake cycles have been observed over a wide range of timescales and may be a good indicator of the onset of future earthquakes. Understanding the effects of precursory velocity changes right before seismic and slow-slip events could potentially elucidate the onset and timing of fault failure. We use numerical models to simulate fully dynamic earthquake cycles in 2D strike-slip fault systems with antiplane geometry, surrounded by a narrow fault-parallel damage zone. By imposing S-wave velocity changes inside fault damage zones, we investigate the effects of these precursors on multiple stages of the seismic cycle, including nucleation, co-seismic, postseismic, and interseismic stages. Our modeling results show a wide spectrum of fault slip behaviors including fast earthquakes, slow-slip events, and variable creep. One primary effect of the imposed velocity precursor is on the earthquake nucleation phase, and earlier onset of precursors causes earthquakes to nucleate sooner with a smaller nucleation size that is not predicted by theoretical equations. Furthermore, such precursors affect the nucleation of dynamic earthquakes and slow-slip events. Our results highlight the importance of short- and long-term monitoring of fault zone structures for better assessment of regional seismic hazard.

Keywords: Earthquake cycles, velocity precursors, fault damage zone, slow-slip

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1 **1. Introduction**

2 Earthquakes are a complex phenomenon occurring over a wide range of
3 spatial and temporal scales. They are believed to result from a sudden re-
4 lease of accumulated energy manifested either as failure in intact rocks or
5 sudden stick-slip motion on preexisting faults. Understanding the onset and
6 timing of fault failure leading to earthquakes is one of the ultimate goals of
7 seismology. The seismic cycle consists of several distinct phases: preseismic,
8 seismic, and postseismic, and interseismic. The preseismic phase refers to
9 the period leading up to an earthquake, characterized by the acceleration
10 of creep, build-up to earthquake nucleation, and the subsequent failure re-
11 sulting in dynamic ruptures, i.e., the seismic phase. The postseismic phase
12 follows the earthquake with a period of stress relaxation and inelastic defor-
13 mation. The interseismic phase is primarily associated with a locked fault,
14 where the tectonic plate loading results in gradual stress buildup. Earth-
15 quake nucleation refers to the initial stage of an earthquake's development,
16 starting with the gradual accumulation of stress along a fault line or within
17 the Earth's crust. During nucleation, the stress within the Earth's crust
18 surpasses the strength of the rocks restraining it, leading to the initiation of
19 fault movement. As the fault slips and seismic energy is released, this marks
20 the beginning of the earthquake rupture. Nucleation is a critical phase in
21 understanding earthquake processes, and studying it provides insights into
22 the factors that influence the timing, location, and magnitude of earthquakes.
23 However, our current understanding of the earthquake preparation processes,
24 including the nucleation phase that leads to the start of earthquake rupture
25 acceleration, is still limited. By investigating the factors that contribute to
26 earthquake nucleation, such as precursor phenomena, fault properties, and
27 stress changes, we can gain insights into the fundamental processes that
28 control earthquake initiation and propagation. In this context, earthquake
29 precursor phenomena are unusual events or changes in the fault zone's prop-
30 erties, including the fault's geometry, rigidity, composition, and the presence
31 of fluids. Their changes can be manifested as stress changes, opening and
32 closure of microcracks, and fluid variations that occur before an earthquake.
33 In this study, we focus on the precursory velocity changes resulting from
34 change in fault zone rigidity and how they affect earthquake nucleation and
35 stressing history in seismic cycles.

36 The observations of preseismic signals in natural faults include the reduc-
37 tion in b-values prior to large earthquakes and slow-slip events leading up to
38 large earthquakes, e.g., the 2011 Mw 9.0 Tohoku-Oki earthquake (Kato et al.,
39 2012; Nanjo et al., 2012; Ito et al., 2015), and the 2014 Mw 8.1 Iquique, Chile
40 earthquake (Kato and Nakagawa, 2014). b-values are a measure of number of
41 large earthquakes in relation to number of smaller earthquakes along a given
42 fault. (Kato et al., 2012) identified a large number of very small, repeat-
43 ing earthquakes prior to the Tohoku earthquake that migrated through time
44 slowly towards the mainshock hypocenter. This study suggests that two slow-
45 slip transient sequences propagated towards the initial rupture point of the
46 large Tohoku earthquake. Similar observations were documented prior to the
47 large Chile earthquake (Kato and Nakagawa, 2014). Additionally, changes in
48 seismic wave velocity have been observed along natural faults prior to earth-
49 quakes (Whitcomb et al., 1973; Niu et al., 2008; Chiarabba et al., 2020).
50 Whitcomb et al. (1973) found that both the P- and S-wave velocities sig-
51 nificantly decreased, with $\frac{V_p}{V_s}$ decreasing by 10%, about 3.5 years before the
52 1971 San Fernando earthquake followed by a slower recovery period. Niu
53 et al. (2008) observed precursory velocity changes approximately 10 and 2
54 hours prior to two earthquakes using the travel time data from active source
55 experiments in the SAFOD drill site.

56 Scuderi et al. (2016) have studied such robust precursory signals in lab-
57 oratory fault experiments and found systematic reduction in seismic wave
58 velocities by 1% during fast earthquakes and 3% during slow earthquakes,
59 which are both believed to start via the same nucleation process (Kato et al.,
60 2012; Bouchon et al., 2013; Hulbert et al., 2019). The mechanisms for these
61 precursory seismic velocity changes are primarily attributed to the acceler-
62 ating fault deformation, fluid effects, and opening and closure of microcracks
63 due to stress changes (Scuderi et al., 2016; Page and Felzer, 2015; Stanchits
64 et al., 2003; Rivet et al., 2016). Scuderi et al. (2016) showed that during the
65 preseismic phase, creep begins to accelerate and marks the onset of nonlinear
66 elastic deformation, in which the material response to stress is nonlinear with
67 respect to strain, but the material still returns to its original shape. Such
68 nonlinear elastic deformation is commonly used to model fault-slip while pre-
69 serving the elasticity of the host rock. Fault creep and V_p reduction in lab
70 experiments indicate that asperity contacts within the fault zone begin to
71 fail before macroscopic frictional sliding. However, how such velocity pre-
72 cursors may impact the earthquake rupture and nucleation process is largely
73 unknown. Here, we aim to investigate the potential of precursory velocity

74 changes as an indicator of earthquake size, onset, and duration. Specifically,
75 we aim to explore how the duration of such velocity precursors may impact
76 the earthquake nucleation and rupture process.

77 Observations of preseismic signals in natural faults reveal distinctive fea-
78 tures related to both precursory fault slip behavior and variations in physical
79 rock properties. For instance, reductions in b-values before large earthquakes
80 and occurrences of slow-slip events leading up to seismic events, such as
81 the 2011 Mw 9.0 Tohoku-Oki earthquake, and the 2014 Mw 8.1 Iquique,
82 Chile earthquake, signify precursory fault slip behavior. Changes in seismic
83 wave velocity along natural faults prior to earthquakes represent variations in
84 physical rock properties. Laboratory experiments on earthquake cycles, such
85 as those conducted by Scuderi et al. (2016), also show pre-seismic velocity
86 changes in fault rocks, indicating the presence of both types of phenomena.

87 Natural faults are often surrounded by a network of fractures with multi-
88 scale localization of deformation, and referred to as a fault damage zone
89 (Lewis and Ben-Zion, 2010; Wesnousky, 1994; Niu et al., 2008). Numerical
90 models of earthquakes in fault damage zones approximated as elastic
91 low-velocity layers suggested that they can influence dynamic rupture styles
92 (Huang and Ampuero, 2011; Huang et al., 2014) as well as long-term seis-
93 mic cycle behaviors (Abdelmeguid et al., 2019; Thakur et al., 2020; Nie and
94 Barbot, 2021). Additionally, these fault damage zones may change in elastic
95 strength throughout the earthquake cycle due to coseismic damage accu-
96 mulation and interseismic healing (Thakur and Huang, 2021, and references
97 therein), which give rise to variability in earthquake size, location, and in-
98 terevent times in immature and mature fault zones.

99 The fault-slip behavior over multiple earthquake cycles is also governed
100 by other factors including the variation of initial stress at different scales (An-
101 drews and Ma, 2016) as well as the earthquake nucleation size and duration
102 (Lapusta and Rice, 2003; Cattania, 2019). The distribution of initial shear
103 stress plays a crucial role in determining the static and dynamic stress change
104 on the fault plane and the associated energy release and seismic radiation
105 during an earthquake. Dynamic rupture models with heterogeneous power-
106 law stress distribution, i.e., non-uniform self-similar distribution along depth,
107 have partially explained the observed scaling of stress drop, moment, and ra-
108 diated motion (Ripperger et al., 2007; Andrews and Barall, 2011; Dalguer and
109 Mai, 2011). Models simulating the whole earthquake cycle (Tal and Hager,
110 2018; Tal et al., 2018; Ozawa et al., 2019) also utilize the spatial roughness
111 of faults to induce stress heterogeneities. Therefore, it is evident that both

112 stress and material heterogeneities play important roles in the generation
113 mechanisms of earthquakes in natural fault zones.

114 Permanent deformation can occur in fault zones via a suite of other mech-
115 anisms (Sibson, 1977). One such mechanism is the development of localized
116 shear bands or faults that result from the accumulation of strain and stress
117 concentration within the damage zone. These localized faults can propa-
118 gate through the rock mass, resulting in slip and displacement across the
119 fault zone. Another mechanism is the formation of compaction bands, which
120 are narrow zones of high deformation within the damage zone. Compaction
121 bands result from the localized compression of the rock mass and can lead
122 to significant permanent deformation and reduction in the permeability of
123 the rock (Cox and Scholz, 1995). Fracture propagation and coalescence can
124 also contribute to permanent deformation in earthquake fault damage zones
125 (Mendecki and Chester, 2000). This occurs when fractures in the rock mass
126 grow and merge, resulting in the formation of larger and interconnected frac-
127 tures. The propagation and coalescence of fractures can lead to significant
128 displacement and deformation in the rock mass. Overall, the mechanisms
129 for internal faulting and permanent deformation in earthquake fault damage
130 zones are complex and can be influenced by a variety of factors, including
131 rock properties, stress conditions, and the nature and intensity of seismic
132 activity. We have chosen to model the fault zone deformation in a purely
133 elastic sense, with time-dependent healing only occurring during quasi-static
134 phase.

135 Understanding the interplay between these complexities is crucial for
136 gaining insights into fault behavior and earthquake dynamics. While our
137 modeling approach simplifies the fault zone deformation to a purely elastic
138 sense, we discuss the effects of precursory velocity changes on earthquake
139 cycle dynamics in this study. We model the precursory velocity changes as
140 transient, interseismic changes in damage zone rigidity to study its effects
141 on nucleation and dynamics of subsequent ruptures. Since a natural fault
142 rarely has uniform background stresses, we also show the effects of such pre-
143 cursory velocity changes in earthquake cycles on a fault with a self-similar
144 distribution of initial normal stress with depth, which may manifest due to
145 a priori stress heterogeneities, local geologic structures, or stress transfer from
146 surrounding faults. Our results show that the onset of precursory shear wave
147 velocity-drop causes a reduction in earthquake nucleation size, with earlier
148 precursors showing smaller nucleation size. We also see that such precursory
149 velocity changes cause earlier nucleation of earthquakes, therefore causing a

150 reduction in recurrence intervals over the seismic cycle. Additionally, precu-
151 sory velocity changes allow some intermediate magnitude earthquakes, that
152 do not break through the entire fault asperity, to grow into full ruptures
153 spanning the entire fault width. We also discuss how the heterogeneities in
154 shear stress after multiple earthquakes along a fault are manifested due to
155 fault damage zones, precursors, as well as initial self-similar normal stress.

156 2. Methods

157 We use physics-based numerical models to simulate dynamic earthquake
158 cycles in a two-dimensional vertical strike-slip fault with antiplane geometry.
159 Our modeling covers all stages, employing a 2D spectral element method
160 (Kaneko et al., 2011, and references therein). For simplicity, we represent
161 the fault-parallel damage zone with a constant-geometry layer. The ma-
162 terial is purely elastic, with the damage zone having a lower shear mod-
163 ulus. Initial conditions are depth-dependent on an antiplane fault, with-
164 out along-strike variable properties. Full inertial effects with explicit time-
165 stepping are considered during dynamic ruptures, while a quasi-static algo-
166 rithm with implicit adaptive time-stepping is used during the interseismic
167 period (Lapusta et al., 2000).

168 2.1. Model Setup

169 Our model domain extends to 48 km in depth and 30 km in width (Fig.
170 1b). Since this setup is symmetric across the fault, we only consider one
171 half of the domain to save computational cost. The top boundary represents
172 the earth’s free-surface and is therefore imposed to be stress-free. The fault
173 zone boundary is divided into two parts: the top 24 km of the boundary
174 is the active fault governed by rate- and state-dependent friction laws, and
175 the bottom 24 km loads the fault with a constant velocity of 35 mm yr^{-1} .
176 The other boundaries are absorbing boundaries that allow seismic waves to
177 pass through. The seismogenic zone, a segment of the fault that accumu-
178 lates stress during the interseismic period to eventually host earthquakes,
179 extends from 2 km to 17 km along the fault as in typical strike-slip fault
180 systems. The rest of the fault creeps aseismically. The characterization of
181 faults into seismic failure or aseismic creep is done based on the rate- and
182 state-dependent friction parameter ($a - b$), with a negative value specifying a
183 seismically active locked fault, and a positive value specifying aseismic stable

184 sliding (Blanpied et al., 1991) . Mature fault damage zones in our simula-
 185 tions are approximated as elastic layers parallel to the fault with lower shear
 186 moduli than the surrounding host rock. The damage zone is 1 km wide and
 187 extends throughout the domain of the simulation. The host rock has a den-
 188 sity of 2670 kg/m^3 and an S-wave velocity of 3464 m s^{-1} . The damage zone
 189 has a density of 2670 kg/m^3 and an S-wave velocity of 2425 m s^{-1} , implying
 190 a 30 % velocity reduction, similar to what is observed in nature for mature
 191 strike-slip fault zones (Huang et al., 2014; Perrin et al., 2016; Thakur et al.,
 192 2020).

193 The nucleation phase typically involves a gradual increase in slip rate,
 194 reflecting the accumulation of stress on the fault until it reaches a critical
 195 point, leading to rapid slip and the onset of an earthquake. In the context
 196 of numerical models of seismic cycles, we switch ‘on’ inertial effects as the
 197 maximum fault slip-rate increases after certain threshold, 1 mm/sec in this
 198 case (Lapusta and Rice, 2003). The onset of earthquakes in our models is
 199 captured when the peak slip-rate of the fault exceeds 1 mm/sec. We prescribe
 200 the precursory velocity drop δV_s during the nucleation phase when the fault-
 201 slip starts accelerating. This is in-part due to the scope of this article to
 202 understand the effects of such δV_s change on earthquake nucleation, but also
 203 to make our purely elastic models thermodynamically consistent by only
 204 prescribing δV_s during the quasi-static phase, i.e., the absence of inertial
 205 effects.

206 2.2. Friction Laws

207 The laboratory-derived rate- and state-dependent friction laws determine
 208 how fast the fault is slipping in relation to the shear strength (Dieterich, 1979;
 209 Ruina, 1983; Blanpied et al., 1991). We use a regularized version of the classic
 210 rate- and state-dependent friction, wherein the regularization is interpreted
 211 as a thermally activated creep model that relates the shear strength (T) to
 212 the slip rate ($\dot{\delta}$) as follows:

$$213 \quad T = a\bar{\sigma} \operatorname{arcsinh} \left[\frac{\dot{\delta}}{2\dot{\delta}_o} e^{\frac{f_0 + b \ln(\dot{\delta}\theta/L)}{a}} \right] \quad (1)$$

214 where $\bar{\sigma}$ is the effective normal stress (the difference between lithostatic
 215 stress and the pore fluid pressure), f_0 is a reference friction coefficient corre-
 216 sponding to a reference slip-rate $\dot{\delta}_o$, and a and b are empirical constants that
 217 depend on the mechanical and thermal properties of the interface in contact.

218 The parameter θ is a state variable interpreted as the average lifetime of the
219 surface in contact and L_c is the characteristic length scale over which the
220 contact surface slips. The evolution of the state variable is governed by the
221 aging law (Ruina, 1983):

$$222 \quad \frac{d\theta}{dt} = 1 - \frac{\dot{\delta}\theta}{L} \quad (2)$$

223 The frictional stability on the fault is determined by the parameter $(a - b)$.
224 Fig. 1c shows the depth profile for the friction parameter $(a-b)$. The seismo-
225 genic zone (2 km to 17 km) is prescribed to be velocity weakening at steady
226 state, which means it has potential to develop unstable slip. The rest of the
227 fault is prescribed to be velocity strengthening at steady state, implying a
228 stable sliding behavior. This profile is similar to what is expected at equiv-
229 alent depths from laboratory and numerical experiments (Blanpied et al.,
230 1991; Lapusta et al., 2000). Earthquake dynamics are determined by the pa-
231 rameters a/b and L_c . A lower value of L_c relative to the size of the velocity
232 weakening asperity results in more chaotic rupture styles (Cattania, 2019;
233 Barbot, 2019), whereas a/b controls the relative importance of strengthening
234 and weakening effects and the ratio of static to dynamic stress drops (Barbot,
235 2019).

236 The region where the shear resistance breaks down at the rupture front
237 is described as the cohesive zone (Rubin and Ampuero, 2005). The nucle-
238 ation length and the cohesive zone size can have important effects on the
239 spatiotemporal patterns of fault-slip behavior and need to be well resolved
240 (Rubin and Ampuero, 2005; Erickson et al., 2020). We set $L_c = 2$ mm in our
241 first set of results (Sections 3.1-3.3) which implies an approximate nucleation
242 size of 500 m within the damage zone. We use an average spatial resolu-
243 tion of 33 m, which ensures that we have more than 15 elements within the
244 nucleating region and that the simulations are well resolved (Thakur et al.,
245 2020). Additionally, we show another set of results in Section 3.4 with $L_c =$
246 8 mm in order to understand the effects of precursory velocity changes in
247 earthquake cycles with full, periodic ruptures. All the parameters used for
248 our simulations are described in Table 1.

249 **3. Results**

250 *3.1. Precursory Velocity Change and its Effects on Nucleation Size*

251 We model the velocity precursor as changes in the S-wave velocity of the
252 fault damage zone surrounding a strike-slip fault. While the laboratory ex-

253 periments have documented a change in the P-wave velocity (Scuderi et al.,
 254 2016), natural faults often show equivalent changes in P- and S-wave veloc-
 255 ities in the absence of fluid effects (Whitcomb et al., 1973; Thurber et al.,
 256 2003). Our models are two-dimensional and under antiplane strain approx-
 257 imation, and therefore the models only have SH waves and we assume that
 258 similar changes in material properties during the nucleation phase would lead
 259 to SH wave velocity reduction as well. Since fully dynamic earthquake cycle
 260 models do not provide any constraint on the earthquake location and tim-
 261 ing except the initial stress and friction values, we use the maximum slip
 262 velocity on the fault as a threshold for prescribing the precursory velocity-
 263 drop (Fig. 2). Once the on-fault slip-rate exceeds the threshold, the S-wave
 264 velocity drops instantaneously by 0.5%. It is imperative to note that this
 265 drop happens only within the fault damage zone, where the S- wave velocity
 266 is already 30% lower than the surrounding host rock. Once the earthquake
 267 has completely ruptured and the on-fault acceleration reaches 0, the fault
 268 zone is set up to heal back to its original value logarithmically with time.
 269 Such logarithmic healing has been observed in natural fault zones (Niu et al.,
 270 2008; Vidale and Li, 2003) and laboratory experiments (Shreedharan et al.,
 271 2020). This healing happens over 21 days in our models, which is chosen to
 272 be short enough so that it does not affect the subsequent earthquakes in the
 273 sequence (Fig. 2a). Hereafter, we refer to the shear wave velocity change
 274 as δV_s , with increase referring to damage reduction and decrease referring
 275 to healing. The evolution of the shear wave velocity, and hence the shear
 276 modulus in the fault damage zone (μ_D) with respect to the shear modulus
 277 of the host rock (μ) is given as follows:

$$\frac{\mu_D}{\mu} = \begin{cases} \frac{\mu_{D0}}{\mu_0}, & \text{if } V_{max} \geq V_{threshold} \\ (1 - \exp(-r(t - t_{start}))) + A_0, & \text{if } \frac{\mu_D}{\mu} < A_0 \end{cases} \quad (3)$$

279 where A_0 is the specified amplitude of the shear modulus change corre-
 280 sponding to δV_s , r is the healing rate, and $t - t_{start}$ is the timestep relative
 281 to the previous earthquake. δV_s increase starts after the current earthquake
 282 is over, while t_{start} refers to the start time of that earthquake.

283 The evolution of on-fault peak slip-rate with time is indicative of the
 284 precursor onset duration (Fig. 2b). We can observe a sharp log-linear ac-
 285 celeration of fault-slip rate due to this δV_s . It is important to note that the
 286 actual duration of precursor prior to an earthquake does not have a strict
 287 relation to the slip-rate threshold we use, and the duration needs to be cal-

288 culated after running the simulations. A lower slip-rate threshold leads to a
289 longer precursor duration because in an ideal, homogeneous material, slip-
290 rate increases logarithmically with time as a rupture nucleates (Lapusta and
291 Rice, 2003). The measured precursor durations suggest a logarithmic re-
292 lationship with the precursor slip-rate threshold for $L_c = 2$ mm and $L_c =$
293 8 mm (Fig. 2c), but more data points are needed to establish a quantitative
294 relationship.

295 We also observe a significant reduction in earthquake nucleation size due
296 to δV_s . The theoretical equation for nucleation size in a layered medium
297 (Kaneko et al., 2011) predicts that it should depend only on the shear mod-
298 ulus of the near-fault material given that other parameters are constant.
299 This theoretical relationship overestimates the nucleation size observed in
300 our models with precursors. We measure the nucleation size using the patch
301 of the fault having higher slip-rate than the threshold velocity of 1 mm s^{-1}
302 at the start of the earthquakes. Fig. 2d shows that the nucleation size can be
303 reduced by more than a half with increasing precursor duration for a constant
304 0.5% precursory velocity drop. This is seen across both $L_c = 2$ mm and $L_c =$
305 8 mm simulations. Additionally, since the slip-rate threshold used for setting
306 up the precursor onset duration cannot be lower than the background creep
307 rate of $1 \times 10^{-9} \text{ m s}^{-1}$, the decrease in nucleation size will plateau as the pre-
308 cursor onset duration increases. Our results suggest that the nucleation size
309 is also a function of precursory onset time, with a longer precursor duration
310 leading to a smaller nucleation size.

311 *3.2. Reference Model: Fully Dynamic Earthquake Cycles with a Fault Dam-* 312 *age Zone*

313 Our reference model consists of a fault-parallel damage zone extending
314 throughout the depth of the domain, and a characteristic slip distance of
315 $L_c = 2$ mm. This reference model does not have any δV_s . However, the
316 presence of damage zone, along with the prescribed nucleation size, gives
317 rise to complexities in the earthquake sequence such as variability in earth-
318 quake magnitudes and hypocenter location as well as the presence of slow-slip
319 events. These complexities result from a combination of stress heterogeneities
320 generated by fault zone reflected waves during dynamic rupture (Harris and
321 Day, 1997; Thakur et al., 2020) as well as multi-sized earthquake ruptures
322 due to relatively small nucleation compared to the size of the fault asperity
323 (Cattania, 2019; Barbot, 2019). The cumulative slip contours show that dy-
324 namic wave reflections affect seismic slip in large and small earthquakes (Fig.

325 3a). The spatiotemporal slip-rate of a representative earthquake (marked in
326 yellow star) shown in Fig. 3b highlights multiple dynamic wave reflections,
327 where parts of the fault have sub-seismic slip-rate ($< 1 \text{ mm s}^{-1}$) and other
328 parts have seismic slip-rate. The rupture also propagates as slip pulses at
329 any given depth. Additionally, our reference model has abundant slow-slip
330 events between large earthquakes, as shown by the peak slip-rate along the
331 fault in Fig. 3c. Fig. 3d shows the shear stress along the fault before and
332 after the same earthquake. The shear stress before the earthquake highlights
333 the overstressed nucleating region near 14 km depth. Furthermore, the shear
334 stress after the earthquake is very heterogeneous in space, primarily because
335 of dynamic wave reflections.

336 3.3. Effects of Precursory Velocity Changes on Earthquake Cycles

337 We present four models with different precursory durations for $L_c =$
338 2 mm (Fig. 4a-d). The parameters used are listed in Table 1, under Sec-
339 tion 3.3. Increasing the precursory duration results in a higher number of
340 large, surface-reaching events compared to our reference simulations. In Fig.
341 3a, the reference simulation shows one surface-reaching event between 5-8m
342 slip, averaging one such event every 3m of accumulated slip. Conversely,
343 simulations with δV_s exhibit two or more surface-reaching events for every
344 3m of accumulated slip (Fig. 4a-d). This surge in surface-reaching events is
345 attributed to the introduction of δV_s , leading to faster and earlier nucleation
346 of earthquakes.

347 Analyzing peak slip-rate in these simulations reveals that an earlier onset
348 of δV_s corresponds to an earlier onset of earthquakes (Fig. 4e and f). The
349 first earthquake in the reference model initiates at 55 years, while δV_s models
350 exhibit earlier nucleation, synchronized with the precursor duration. Fig. 4f
351 illustrates the onset of earthquakes and transient slow-slip events over time.
352 The 30-day precursor model depicts two large earthquakes between 25 and
353 70 years, while the 1-hour, 2-day, and 20-day precursor models each feature
354 one large earthquake in the same period. All simulations include one or more
355 slow-slip transients during this time frame.

356 Both the 30-day precursor and the reference model experience fewer slow-
357 slip transients between earthquakes than other precursor simulations. This
358 indicates that if the precursor duration is sufficiently long, earthquake dy-
359 namics are closer to the reference model. The incorporation of precursory
360 δV_s still influences earthquake onset, resulting in earlier nucleation in the

361 30-day precursor compared to the reference model. Simulations with precursors exhibit larger surface-reaching events and fewer small earthquakes due to accelerated earthquake nucleation triggered by precursory velocity-drops in the fault zone, leading to faster ruptures.

365 The size of earthquakes is also influenced by friction parameters L_c , as discussed in Section 3.4. Notably, the onset timing of the precursor does not directly correspond to how early the earthquake will nucleate. This is because we specify the duration of the velocity-drop in terms of the peak slip-rate, and fault slip begins accelerating as soon as the velocity-drop is specified.

371 We further examine the magnitude-frequency distribution and the depth distribution of earthquake hypocenters (Fig. 5). The earthquake magnitude is calculated by integrating fault slip over the rupture length for a given shear modulus within the fault zone, assuming the rupture width is equivalent to the rupture length in the 2D approximation. The cumulative magnitude-frequency distribution exhibits a sharp decline in the number of earthquakes beyond magnitude 6 and a log-linear trend for smaller ($M_w < 4$) earthquakes across all simulations. However, the reference simulation displays several intermediate magnitude earthquakes (M_w 4-6), with a log-linear decrease in the number of events as magnitude increases, characterized by a distinct slope from smaller earthquakes. The gap in the intermediate magnitude earthquakes is present in all the precursor simulations, where the intermediate magnitude earthquakes happen as often as the reference simulation. This is also corroborated by the similarity in the depth distribution of earthquakes between the reference simulation and the 30-day precursor (Fig. 5b). The median hypocenter is closer to 15 km in the reference simulation and the simulation with δV_s of 1-hour, 20-day, and 30-day. The absolute deviation is however the largest for the reference simulation followed by the 30-day precursor. The δV_s for the other simulations have a very small absolute deviation of hypocenters. The simulation with 2-day precursor also has fewer total number of earthquakes compared to the other simulations (Fig. 5a), but the gap in intermediate magnitude earthquakes is still prevalent. This is because most earthquakes in this simulation occur at shallower depths, where it is harder for ruptures to stop without breaking through to the surface due to low fault strength at depths shallower than 5 km (Fig. 5b). Overall, this suggests that the impact of precursors on earthquake dynamics is stronger for shorter durations, and longer precursor durations may not significantly affect the occurrence of intermediate magnitude earthquakes. Despite these quan-

399 titative differences, our models are qualitatively similar in the sense that the
400 incorporation of precursors causes a clock advance of earthquake nucleation,
401 and disrupts the interplay between aseismic creep and dynamic earthquakes.

402 The earthquake hypocenter locations in the 20-day and 30-day precursor
403 simulations show a higher degree of similarity to the reference simulation,
404 with only a small difference in the distribution of hypocenters along depth
405 (Fig. 5b). Specifically, the percentage of hypocenters located within a 5 km
406 radius of the reference simulation increase from 65% in the 1-hour precursor
407 simulation to 95% in the 20-day precursor simulation. Conversely, the 1-
408 hour and 2-day precursors display a significant deviation from the reference
409 simulation, with a noticeably different distribution of hypocenter depths. In
410 particular, the shallow earthquakes in the 2-day precursor simulation result
411 in a lower overall earthquake count compared to the other simulations (Fig.
412 5a). This observation is consistent with the fact that larger earthquakes are
413 more likely to nucleate at the base of the seismogenic zone, which is not the
414 case in the 2-day precursor simulation. Specifically, the percentage of large
415 earthquakes (magnitude greater than 5) located within a 5 km radius of the
416 reference simulation is only 20% in the 2-day precursor simulation, compared
417 to 85% in the 30-day precursor simulation.

418 To understand the nucleation phase of these events with δV_s , we com-
419 pare the spatiotemporal slip-rate history in our 20-day precursor simulation
420 with our reference simulation. A comparison between Fig. 6a and Fig. 6b
421 shows that we have fewer slow-slip events in the presence of velocity precurs-
422 sors. In other words, there is a lower number of earthquakes but a higher
423 number of slow-slip events when there are no precursors. By zooming in to
424 the nucleation phase, we find the incorporation of precursory velocity-drop
425 results in a much shorter duration for the nucleation of earthquakes (Fig.
426 6c-d). In our simulation without precursors (Fig. 6c), the fault accelerates
427 for 21 hours with peak fault slip-rate oscillating within the slow-slip regime
428 ($< 1 \times 10^{-4} \text{ m s}^{-1}$) before growing into seismic event. In contrast, our simu-
429 lation with δV_s (Fig. 6d) shows the nucleation phase acceleration for 3 hours
430 before the seismic event, and the peak slip-rate oscillations are also fewer
431 and restricted to less than 1 hour before the event. We see that while the
432 largest magnitude surface-reaching earthquakes are comparable across the
433 two simulations with the major difference being time-delay, there is a dearth
434 of certain slow-slip events and we have more number of larger earthquakes
435 in our simulation with precursors (Fig. 6b).

436 *3.4. Heterogeneous Stress with and without Precursors*

437 Natural faults exhibit structural complexity, characterized by features like
438 fault interface roughness, stress transfer from nearby faults, and background
439 stress heterogeneity (Smith and Heaton, 2011). Fault segments with varying
440 shear stresses act as asperities facilitating rupture nucleation and propaga-
441 tion, while those with lower shear stresses act as barriers hindering rupture.
442 The evolution of fault stress state, influenced by fault friction, geometry, and
443 material properties, occurs through earthquake cycles and long-term inter-
444 seismic slip.

445 To explore the persistence of δV_s effects in faults with prior stress het-
446 erogeneities, we simulate earthquake cycles incorporating self-similar normal
447 stress distribution along depth, termed heterogeneous normal stress. Self-
448 similarity refers to a property where a structure or phenomenon exhibits
449 similar patterns or characteristics at different scales. Self-similarity is often
450 observed in the patterns of stress changes within fault systems (e.g., Smith
451 and Heaton, 2010). This means that the stress changes at various scales
452 within the fault exhibit similarities, allowing researchers to apply consistent
453 modeling principles across different magnitudes and stages of earthquakes.
454 The concept of self-similarity is valuable in understanding and predicting
455 earthquake behaviors, aiding in the development of models that can capture
456 the complexity of seismic processes across a range of scales. Using a one-
457 dimensional stochastic, fractal-like model for heterogeneous stress (Smith
458 and Heaton, 2011), we analyze its impact alongside velocity precursors and
459 a fault damage zone.

460 The incorporation of self-similar normal stress affects earthquake nucle-
461 ation size (Rubin and Ampuero, 2005; Kaneko et al., 2011), introducing
462 variability with depth. The simulation with heterogeneous normal stress dis-
463 plays a rough slip profile for the aseismic part, in contrast to the reference
464 model showing a rough coseismic slip profile (Fig. 7a). While the hetero-
465 geneous normal stress model delays earthquake nucleation compared to the
466 reference model (Fig. 7c), the introduction of δV_s (20 days prior to the
467 earthquake) leads to earlier nucleation, akin to results in Fig. 4. Figures
468 7b and d illustrate the magnitude-frequency distribution and depth distri-
469 bution of earthquake hypocenters for simulations with heterogeneous normal
470 stress. While more earthquakes nucleate near the base of the seismogenic
471 zone compared to the reference model (Fig. 4), the overall distribution ap-
472 pears similar between models with and without δV_s . This suggests that,
473 although δV_s strongly influences earthquake nucleation onset, its impact on

474 earthquake size and depth distribution is weaker than the effects of the fault
475 damage zone structure, heterogeneous normal stress, and frictional param-
476 eters.

477 Comparing shear stresses before and after a representative earthquake
478 between simulations with and without δV_s and initial heterogeneous normal
479 stress (Fig. 8), the reference simulation with the fault damage zone exhibits
480 post-earthquake heterogeneous shear stress within the seismogenic zone (2 km
481 to 17 km in Fig. 8a). Stress heterogeneities are caused by dynamic wave
482 reflections, limited to the region of rupture propagation. The shear stress
483 before an earthquake lacks heterogeneities, except for stress peaks near the
484 nucleation region and the frictional transition boundary. While the location
485 and number of these peaks in the reference simulation are influenced by stress
486 heterogeneities from previous earthquakes, they are not present at every point
487 along the fault, unlike subsequent simulations.

488 With the inclusion of δV_s (Fig. 8b), shear stress before the earthquake
489 becomes heterogeneous within the seismogenic zone. Additional initial het-
490 erogeneous normal stress results in creeping regions of the fault exhibiting
491 shear stress heterogeneities, amplified in the presence of velocity precursors
492 (Figs. 8c and d).

493 3.5. δV_s Change with a Larger Nucleation Size ($L_c = 8$ mm)

494 In this section, we carry out more simulations using $L_c = 8$ mm while
495 keeping the other parameters similar as the above sections. The larger L_c
496 results in a proportionately larger nucleation size and therefore periodic, full
497 ruptures are exclusively observed in these simulations. The parameters used
498 are listed in Table 1, under Section 3.5. Fig. 9a shows the cumulative slip for
499 four simulations with different precursor duration. We see a clear reduction
500 in nucleation size as the precursor duration increases and thus earlier earth-
501 quake rupture onsets (Figs. 9b and d). The incorporation of such δV_s also
502 results in a log-linear acceleration of slip-rate as discussed previously (Fig.
503 9d). However, the reduction in nucleation size for $L_c = 8$ mm does not cause
504 additional earthquake complexities such as small earthquakes and variable
505 hypocenter locations. We note that the material and frictional properties are
506 the same across these simulations, therefore the reduction in nucleation size
507 is caused solely due to the onset of precursory velocity-drop. The simulation
508 with δV_s 1 second before the earthquake also shows a very slow rupture prop-
509 agation during the start of rupture, demonstrated by very dense cumulative
510 slip contours during the seismic event (Fig. 9a). Additionally, across all these

511 simulations, the earthquake magnitude remains unchanged for these large,
512 periodic events. Since our models are two-dimensional, the earthquake mag-
513 nitude predominantly depends on the rupture length along the dip-direction.
514 Our results show that δV_s does not contribute to any change in rupture length
515 for large periodic events, however, the magnitude of earthquakes along natu-
516 ral faults may be affected by the rupture width along the strike direction. An
517 analysis of the average recurrence interval against the precursor duration is
518 shown in Fig. 9c. We see a direct decrease in the recurrence interval between
519 two large earthquakes as the precursor onset duration increases. If there is
520 a long period of precursor activity before a large earthquake, then the time
521 between that earthquake and the next one is likely to be shorter than if there
522 was a shorter precursor period. This suggests that the length and intensity of
523 the precursor activity can be used to estimate the onset of subsequent large
524 earthquake.

525 4. Discussion and Conclusions

526 In this study, we have explored the impact of precursory velocity changes
527 on earthquake dynamics, particularly focusing on their influence on earth-
528 quake nucleation size, surface-reaching events, hypocenter distribution, and
529 recurrence intervals. Notably, we observed a significant reduction in earth-
530 quake nucleation size, independent of substantial alterations in elastic mate-
531 rial properties in section 3.5. This reduction manifested in changes to the oc-
532 currence of surface-rupturing large events and the distribution of earthquake
533 hypocenters. Furthermore, we delved into the temporal aspects, investigat-
534 ing how varying the precursor onset duration affects earthquake onset time
535 and recurrence.

536 Fig. 10 shows the earthquake magnitudes for our simulations with dif-
537 ferent precursor durations with $L_c = 2$ mm. We can see how the earthquake
538 magnitude changes through time, and that the reference model has the most
539 variability. The largest magnitude events are surface-rupturing and extend
540 through the entire fault width. There is a gap in intermediate magnitude
541 earthquakes and we have some smaller earthquakes in all these simulations.
542 The 2-day precursor has a lack of smaller magnitude earthquakes. As the pre-
543 cursor duration increases and reaches the 30-day duration, we see that there
544 are more intermediate magnitude earthquakes and the catalog is in close
545 resemblance to the reference model. The magnitude-frequency distribution
546 of earthquakes usually follows a power-law relationship, best described by

547 the Gutenberg-Richter (G-R) distribution. Most observations of global and
548 regional seismicity agree with the G-R distribution (Page and Felzer, 2015;
549 Rundle, 1989). However, certain observations of magnitude-frequency distri-
550 butions along more planar faults (e.g., the San Andreas Fault) have shown a
551 “characteristic earthquake” distribution, wherein the largest earthquake of a
552 characteristic size recurs with an approximately regular interval. The period
553 between two such characteristic earthquakes is generally quiescent except
554 for low-level seismic activity (Schwartz and Coppersmith, 1984; Wesnousky,
555 1994). While our reference simulation shows a more log-linear decrease of
556 earthquake size, the simulations with precursory velocity changes are more
557 akin to a characteristic distribution with a dearth of intermediate magnitude
558 earthquakes (Fig. 5a, 7d). Despite the similarities, the slope of the dis-
559 tribution is different from what is observed in nature, primarily due to our
560 choice of friction parameters and the two-dimensional model approximations.
561 Since the effective normal stress and hence the fault strength is low at depths
562 shallower depths, it is harder to stop dynamic ruptures once they reach this
563 shallow depth. When the rupture breaks through the free surface, the magni-
564 tude of the earthquakes tend to be much larger, which, in combination with
565 a lock of along-strike rupture termination, may explain the lack of certain
566 range of intermediate magnitude earthquakes (Thakur et al., 2020). Despite
567 these shortcomings, our models can be potentially linked to well monitored
568 strike slip fault systems like the Parkfield segment, where the current con-
569 sensus of delay of cyclic earthquakes is attributed to the creeping segments
570 acting as barriers and the local stress heterogeneities from surrounding fault
571 systems (Bakun et al., 2005; Barbot et al., 2009).

572 Our study has focused on imposing precursors and self-similar stresses
573 under an elastic approximation to study their effects on earthquake cycles.
574 However, we have not considered the physical mechanisms that may be re-
575 sponsible for such material properties and stress changes through the earth-
576 quake cycle, e.g., incorporating plasticity (Erickson and Dunham, 2014; Mia
577 et al., 2022) or continuum damage rheology (Lyakhovsky et al., 1997; Thomas
578 and Bhat, 2018) within the fault damage zone. Incorporation of inelastic be-
579 havior in the fault zone promotes the accumulation of permanent deformation
580 throughout the fault zone evolution. Such deformation may lead to a com-
581 plex feedback between the evolving fault zone medium and seismic events,
582 generating unique off-fault rupture patterns (Thomas and Bhat, 2018) and
583 self-consistent healing and damage accumulation (Lyakhovsky et al., 1997).
584 Mia et al. (2022) have shown that the off-fault plastic accumulation may

585 lead to partial ruptures and clustering of seismic events in time. In our sim-
586 ulations, these mechanisms will likely affect the slow-slip generation during
587 the aseismic phase and modulate the shear stress evolution throughout the
588 seismic cycle. Additionally, due to the huge computational costs, we have
589 not explored the detailed parameter space for the choice of damage zone ge-
590 ometry as well as precursory velocity onset and amplitude, which are likely
591 to reveal additional fault zone physics in relation to the velocity precursors.
592 Despite these approximations in our study, our simulations with prescribed
593 precursory velocity drop before the earthquake highlights the importance of
594 monitoring such velocity changes in natural faults, which can potentially aid
595 in seismic hazard assessment.

596 In conclusion, we present two-dimensional, fully dynamic earthquake cy-
597 cle simulations with an elastic fault damage zone and analyze the effects
598 of precursory velocity changes with variable onset durations. We further
599 investigate the effects of additional apriori stress heterogeneities with and
600 without such precursory velocity changes. Our models demonstrate that the
601 earthquake nucleation size is reduced by more than half due to a precursory
602 velocity change of 0.5%, depending on how early this change occurs prior
603 to the earthquake. This implies that the earthquake nucleation size can be
604 significantly smaller than those predicted from theoretical equations (Rubin
605 and Ampuero, 2005) if the shear modulus, effective normal stress, and fric-
606 tional parameters vary temporally during the earthquake preparation phase.
607 Furthermore, compared to a reference scenario without any precursory ve-
608 locity drop, earthquakes can nucleate earlier in the seismic cycle, with earlier
609 precursor onset resulting in earlier earthquake onset. Despite this signifi-
610 cant reduction in earthquake nucleation time, we find that the magnitude of
611 earthquakes are comparable across different models for our simulations with
612 $L_c = 8$ mm, whereas they can be highly variable for simulations with $L_c =$
613 2 mm, suggesting that the complexities in earthquake sequences also depend
614 on fault frictional parameters such as the characteristic slip distance L_c . Our
615 models also highlight the relative effects of heterogeneous stress evolution in
616 the presence of fault damage zones and precursory velocity reductions. Fault
617 stress heterogeneities generated by rupture in fault damage zones can af-
618 fect the rupture nucleation and propagation of future earthquakes. However,
619 the incorporation of preexisting self-similar stresses promotes the heteroge-
620 neous distribution of stresses during both rupture propagation and aseis-
621 mic creep. For homogeneous initial stress conditions, precursory velocity
622 changes affect earthquake statistics like the magnitude-frequency distribu-

623 tion and the hypocenter location, while for a heterogeneous initial stress
624 condition, earthquake statistics are not affected significantly. Studies like
625 Scuderi et al. (2016) have shown that precursory change in seismic veloc-
626 ity has been observed in a spectrum of earthquake failure modes, including
627 tremor and low-frequency earthquakes. We have modeled the precursory
628 changes prior to large earthquakes, and shown that it can lead to a dis-
629 ruption in the recurrence of large earthquakes, favoring an advance in the
630 earthquake onset. Subsequently, a delay in the onset of earthquakes can
631 be caused by such disruption if slow-slip and accelerated creep events occur
632 on fault between such large earthquakes. Seismicity observations along the
633 Parkfield segment of San Andreas fault has shown such disruption in periodic
634 seismicity of the regular recurring events (Bakun et al., 2005), attributed to
635 the unique creeping segment along the fault and to the local stress changes
636 from the surrounding fault systems. Our study can provide additional mech-
637 anisms, in a purely elastic assumption, for such disruptions. By exploring
638 a range of complexities due to precursory velocity drop and heterogeneous
639 normal stresses, our dynamic earthquake cycle models suggest that more de-
640 tailed and frequent observations of natural fault zones can help us better
641 understand the aperiodicity of earthquakes along strike-slip fault systems.

642 **Acknowledgements**

643 This study was supported by the National Science Foundation (Grant
644 Award EAR-1943742) and Southern California Earthquake Center (Contri-
645 bution number 20091).

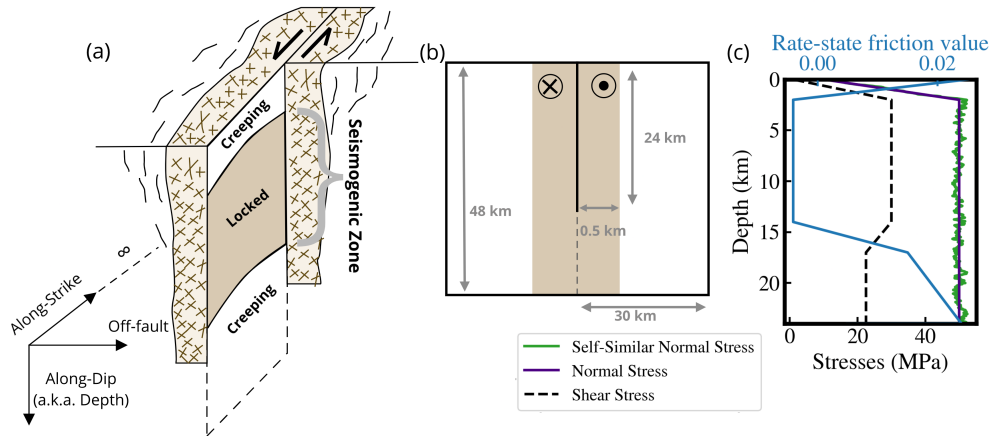


Figure 1: Model description and setup. (a) A schematic fault damage zone along a strike-slip fault. (b) The model geometry for our numerical simulation. It represents a vertical cross-section across the fault zone schematic in Fig. 1a, with a fixed fault damage zone width. The model is infinite along strike. (c) The initial stresses and friction parameters along the fault depth.

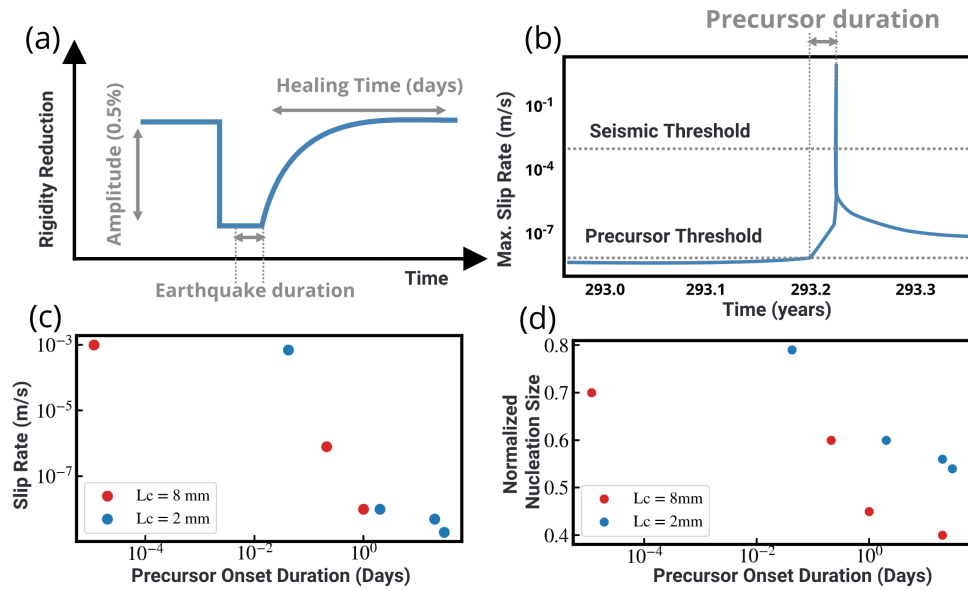


Figure 2: Precursor setup and simulation parameters. (a) The rigidity evolution with time showing the setup of precursory velocity change. (b) A representative earthquake from our simulations highlighting the onset of precursory velocity reduction given a seismic slip-rate threshold. (c) Slip-rate thresholds used in our simulations to set up precursor durations. (d) Observed nucleation size which is normalized against the theoretical estimates is shown for the different precursor onset duration.

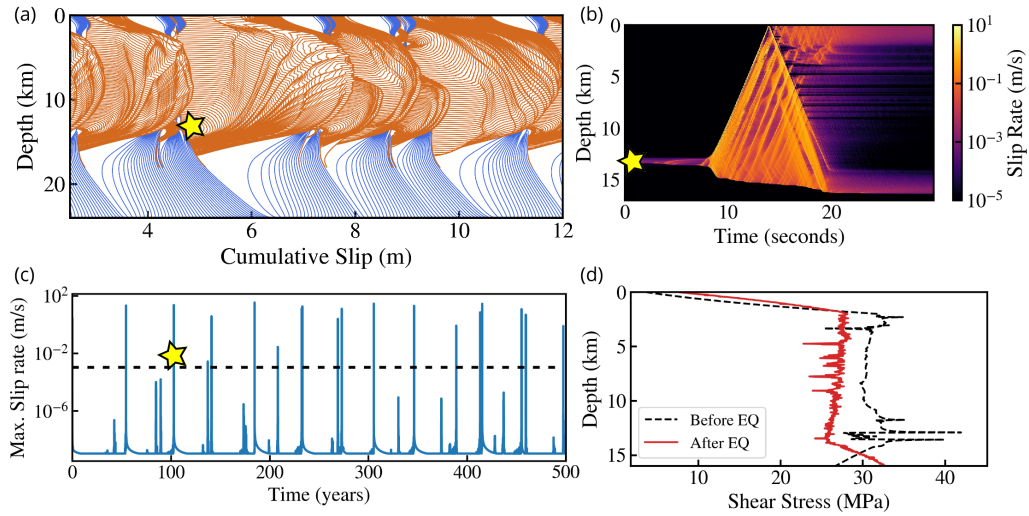


Figure 3: Reference model with fault damage zone. (a) Cumulative slip through earthquake sequences shown along depth. The orange lines are plotted every 0.1 s during earthquakes, and the blue lines are plotted every two years during interseismic periods. (b) Spatiotemporal slip-rate for one representative large earthquake along depth and time. (c) The peak slip-rate on fault is shown in time, demonstrating a range of fast and slow events. The dashed line shows the seismic threshold. (d) The shear stress along depth before and after a representative earthquake. The yellow star shows the location of the representative earthquake highlighted in (b) and (d).

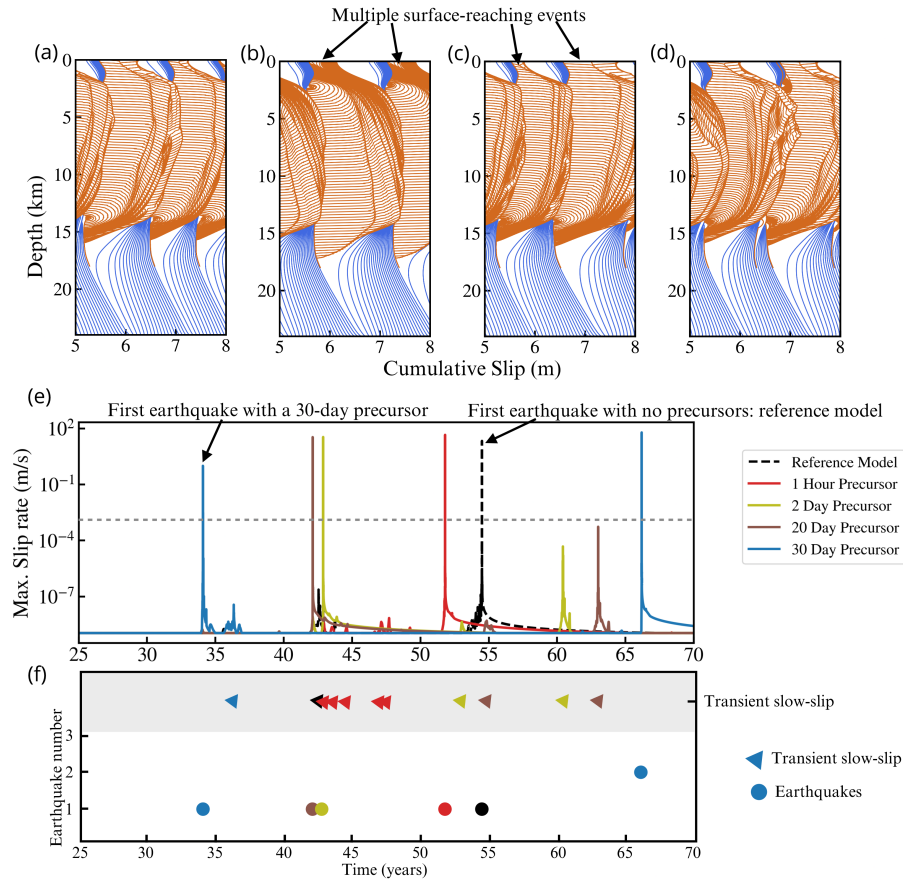


Figure 4: A comparison of earthquake cycle models with different precursory velocity onset. (a-d) Cumulative slip for a section of the earthquake sequence for precursor onsets of (a) 1 hour, (b) 2 days, (c) 20 days, and (d) 30 days before earthquakes. The orange lines are plotted every 0.1 seconds and the blue lines are plotted every 1 year. (e) Peak slip-rate on the fault shown in time for different precursor onsets and the reference simulation. The dashed grey line shows the seismic threshold. (f) Earthquakes and transient slow-slip against time shown for the set of simulations.

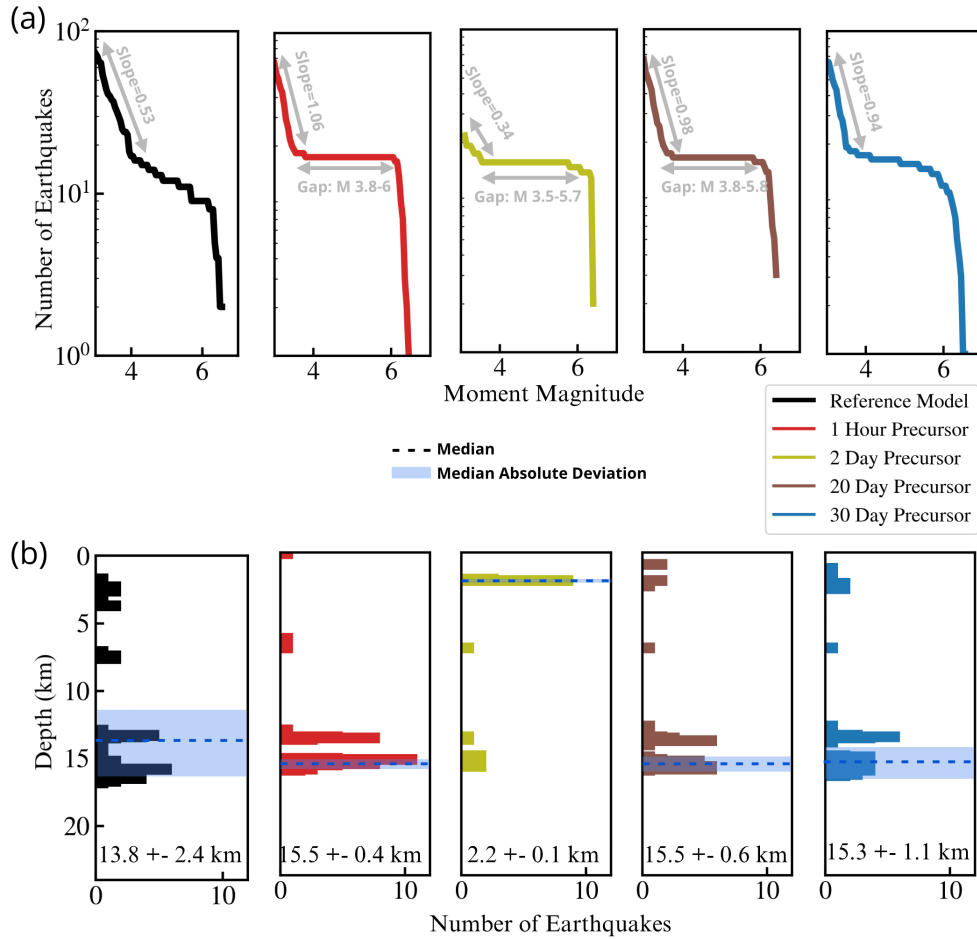


Figure 5: (a) Magnitude-frequency distribution for our reference simulation and different precursor onset durations. (b) Depth distribution of earthquake hypocenters for the same simulations. The median and absolute deviation for the earthquakes is shown in dashed line and shaded region. The values are written at the bottom of the plot.

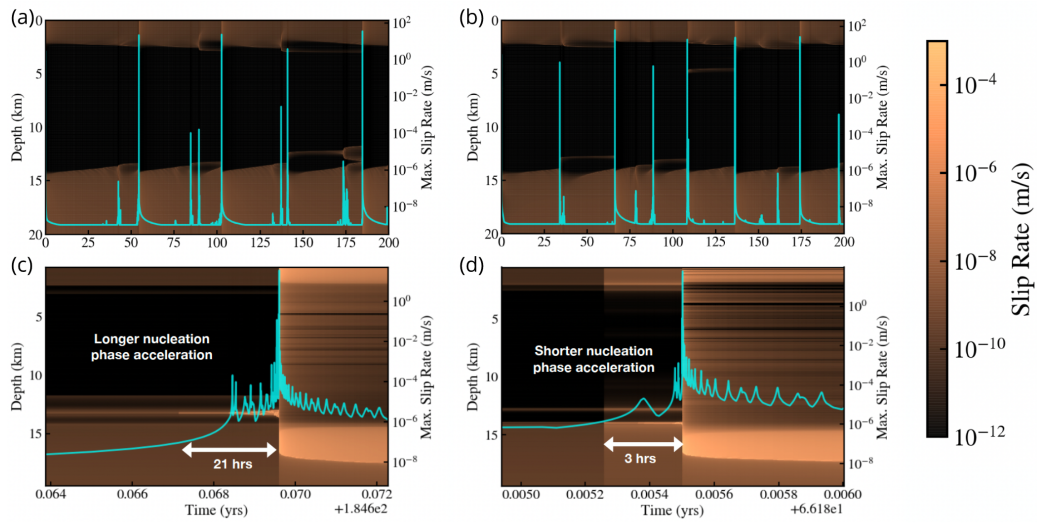


Figure 6: a-c) Spatiotemporal slip-rate history of the reference simulation. (b-d) Spatiotemporal slip-rate history of the 20-day precursor. The bottom figures show the zoom-in of one representative earthquake from each simulation.

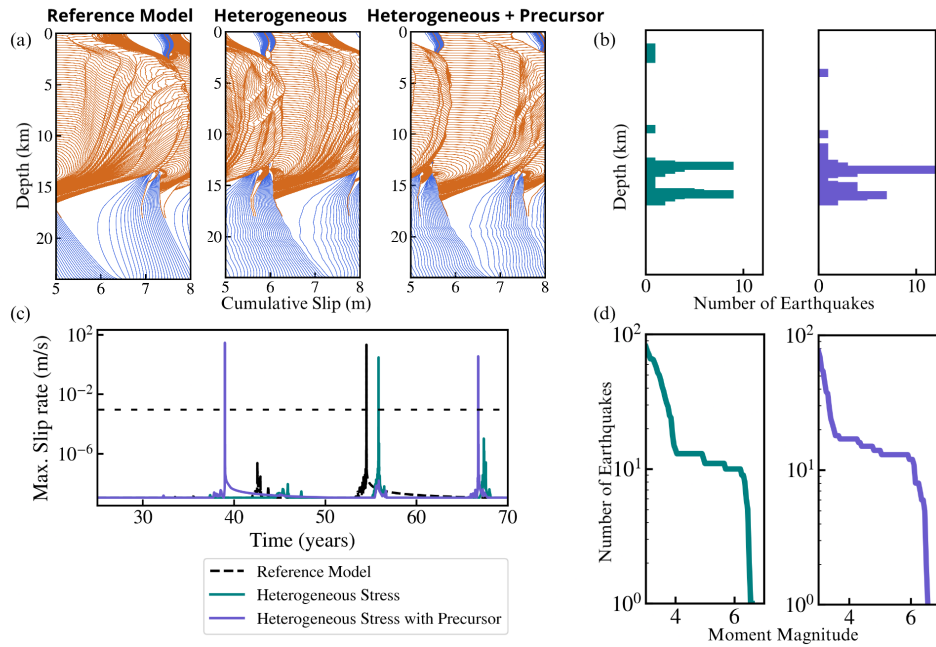


Figure 7: Earthquake cycle simulations with self-similar (heterogeneous) initial normal stress. (a) A comparison of cumulative slip contours for three simulations: the reference model, the heterogeneous stress without precursors, and the heterogeneous stress with precursors. The orange lines are plotted every 0.1 seconds and the blue lines are plotted every 1 year. (b) Depth distribution of earthquake hypocenters. (c) A comparison of peak slip-rate on the fault. The dashed line shows the seismic threshold. (d) Depth distribution of earthquake hypocenters. The magnitude-frequency and depth distribution of reference model are discussed in Fig. 4.

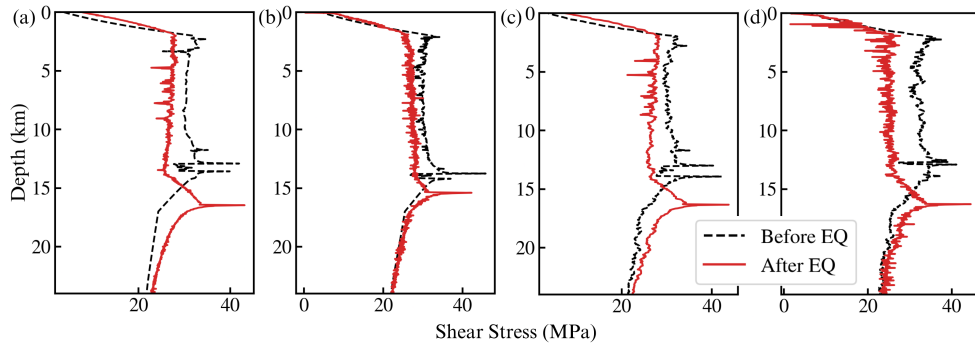


Figure 8: Shear stress before and after one large earthquake. (a) Reference Simulation. (b) 20-Day Precursor. (c) Heterogeneous initial normal stress without precursor. (d) Heterogeneous initial normal stress with 20-day precursor.

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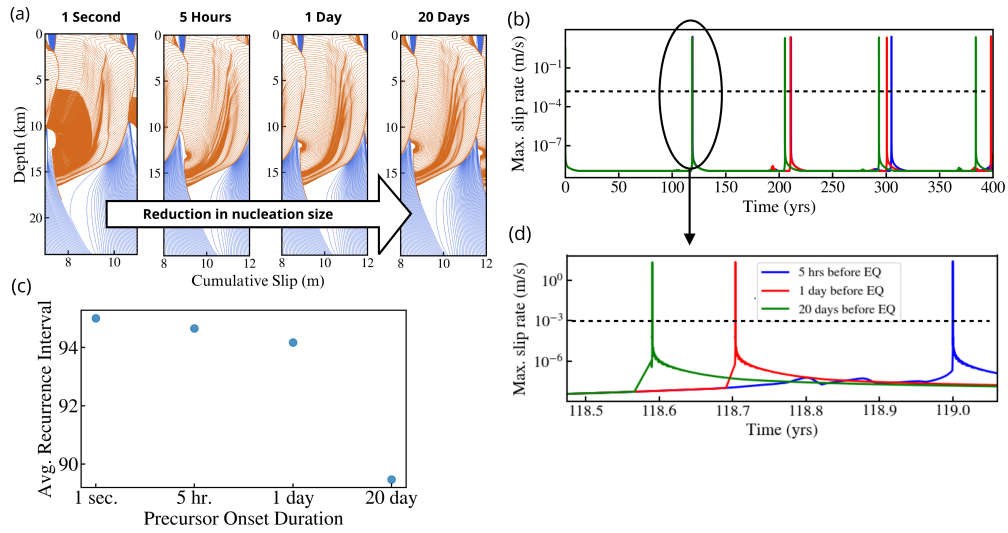


Figure 9: (a) Cumulative slip profiles for simulations with different precursor onset durations. The orange lines are plotted every 0.1 seconds and the blue lines are plotted every 1 year. (b) A comparison of peak slip-rate on the fault for three precursor durations. (c) Precursor onset duration shown against average recurrence intervals. (d) Zoom-in of Fig. 9b showing the earlier nucleation of earthquakes with earlier precursor onset times. The dashed lines show the seismic threshold.

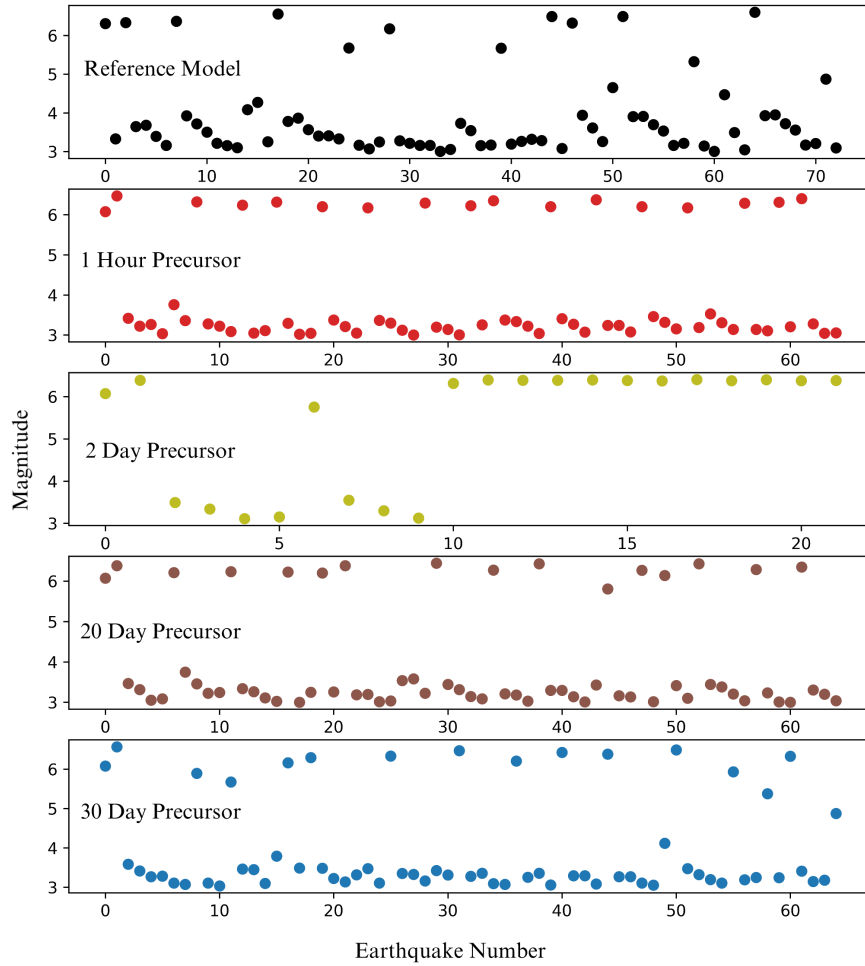


Figure 10: Magnitude and event number of earthquakes for precursor models with $L_c = 2$ mm, shown for different precursor durations.

Table A.1: Parameters Used in Numerical Simulations of Earthquake Cycles

Parameter	Symbol	Value
Static friction coefficient	μ_0	0.6
Reference velocity	V_0	$1 \times 10^{-6} \text{ m s}^{-1}$
Plate loading rate	V_{pl}	35 mm yr^{-1}
Evolution effect	b	0.019
Effective normal stress	σ	50 MPa
Initial shear stress	τ_0	30 MPa
Steady-state velocity dependence	$(b - a)$	-0.004
Width of seismogenic zone	W	10 km
Fault damage zone width	W_d	0.5 km
Average node spacing	dx	20 m
Seismic slip rate threshold	V_{th}	1 mm s^{-1}
Shear modulus of host rock	μ	32 GPa
Shear modulus of damage zone	μ_D	15.7 GPa
Shear modulus after the velocity drop	$\mu_{\delta V_s}$	14.9 GPa
Section 3.3		
Characteristic weakening distance	L_c	2 mm
Precursory velocity threshold (onset duration 1 hr)	$V f_{thresh}$	$8 \times 10^{-4} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 2 day)	$V f_{thresh}$	$1 \times 10^{-8} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 20 day)	$V f_{thresh}$	$5 \times 10^{-9} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 30 day)	$V f_{thresh}$	$2 \times 10^{-9} \text{ m s}^{-1}$
Section 3.5		
Characteristic weakening distance	L_c	8 mm
Precursory velocity threshold (onset duration 1 sec)	$V f_{thresh}$	$9.9 \times 10^{-4} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 5 hrs)	$V f_{thresh}$	$9 \times 10^{-7} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 1 day)	$V f_{thresh}$	$1 \times 10^{-8} \text{ m s}^{-1}$
Precursory velocity threshold (onset duration 20 day)	$V f_{thresh}$	$5 \times 10^{-9} \text{ m s}^{-1}$

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