

1 **The effect of remote sensing resolution limits on aeolian sandstone measurements and the**
2 **reconstruction of ancient dune fields on Mars: Numerical experiment using the Page**
3 **Sandstone, Earth**

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24 **KEY POINTS**

25 Field-gathered aeolian cross-set thicknesses are altered to mimic measurement error from remote
26 sensing pixel resolution limits.

27 Remote sensing resolution limits can severely alter interpretations of aeolian sandstones, even at
28 HiRISE resolution.

29 Accurate measurements require outcrop slopes less than 13° steep, such that the thinnest sets are
30 exposed over detectable distances.

31

32 **PLAIN LANGUAGE SUMMARY**

33 The thickness of wind-blow sand dune deposits are called cross sets. Cross sets can be
34 preserved for long amounts of time as sedimentary rocks, where they act as a record of the
35 ancient surface. A collection of many cross-set thickness measurements can be organized into a
36 distribution of thinner and thicker sets with a particular shape. The shape of the distribution can
37 be analyzed to understand the motion of ancient sand dunes, and in turn the conditions of ancient
38 planetary surfaces. On Earth, we can measure cross-set thicknesses in the field and collect
39 accurate measurements, but for Mars we are mostly limited to satellite images. Here, we perform
40 a numerical experiment on Earth-collected cross-sets from the Page Sandstone. The experiment
41 mimics alters the Earth measurements to become less accurate, as if detected from satellite. The
42 altered distribution is checked for changes which might affect our understanding of the ancient
43 dune fields. Our results show that there is a significant risk of misinterpretation, but that good
44 measurements can be made if the slope of the rock outcrop is shallow, less than 13° from
45 horizontal, such that the thinnest cross sets are exposed over long distances, making them
46 detectable from satellite.

47 **ABSTRACT**

48 The distribution of cross-set thicknesses is important field-collected data for
49 reconstructing ancient aeolian dune fields from the strata they accumulated, but most aeolian
50 strata on Mars must be observed with remote sensing. We hypothesize that remote sensing
51 resolution limits will affect cross-set thickness measurements and the dune field reconstructions
52 that follow. Here, we test this hypothesis using a numerical experiment mimicking the effects of
53 remote sensing resolution limits performed on a distribution of aeolian cross-set thicknesses
54 measured in the field from the Page Sandstone, Arizona, USA. Page set thicknesses are
55 exponentially distributed, representing the accumulations of dry (no water table) dune fields in a
56 state of net-sediment bypass. Set-thickness measurements are progressively blended into
57 adjacent sets based on the map-view distance between their upper and lower bounding surfaces
58 on exposures with different dips. This is termed the “exposure distance” of a cross set, and in this
59 experiment is a function of (1) set thickness, (2) the dip of the outcrop surface, and (3)
60 assumptions of the number of remote sensing image pixels required to detect a set (detection
61 limit). Using outcrop dips from 1° to 60° and detection limits from 3 to 10 HiRISE pixels, gently
62 sloping surfaces (< 13°) allow most of the Page Sandstone sets to be measured, conserving the
63 bypass interpretation made from the true set thicknesses at all detection limits. Although these
64 results are specific to the Page, they can be used as a rule of thumb for future Mars work.

65

66 **1. INTRODUCTION**

67 The distribution of aeolian cross-set thickness is among the easiest stratigraphic data to
68 collect, and the shape of the distribution, as well as its statistical moments, records the
69 aggradation, migration, and the size of dunes in a field (Cardenas et al., 2019; Swanson et al.,

70 2019). Wind is the dominant driver of sediment transport on modern Mars (Ewing et al., 2010;
71 Fenton and Haywall, 2010; Silvestro et al., 2011; Silvestro et al., 2013; Chojnacki et al., 2015;
72 Day and Kocurek, 2016; Lapotre et al., 2016; Cornwall et al., 2018a and b; Chojnacki et al.,
73 2019) and likely been significant throughout the planet's history (e.g., Grotzinger et al., 2005;
74 Lewis et al., 2008a and b; Kite et al., 2013; Milliken et al., 2014; Banham et al., 2018; Anderson
75 et al., 2018; Day and Catling, 2018 and 2019). Even on Earth, where a more diverse set of
76 processes have shaped the planet's surface, the aeolian rock record dates back at least as far as
77 the Archean (3.2 Ga; Rodríguez-López et al., 2014). Therefore, aeolian strata are likely to
78 provide a rich source of information about autogenic processes and paleo-environmental
79 boundary conditions at the ancient surface of Mars, as martian bedform dynamics are controlled
80 by environmental conditions and autogenic processes. Measuring set thicknesses of aeolian
81 sandstones on Mars has the potential to increase our understanding of these ancient conditions on
82 Mars through time. Cross-set thicknesses are observable from remote sensing images and digital
83 elevation models (DEMs; e.g., Milliken et al., 2014; Anderson et al., 2018; Day and Catling,
84 2019). However, resolution limits may lead to remotely-measured thickness distributions that are
85 not representative of the true distribution. This may, in turn, lead to mis-interpretations of the
86 stratigraphy and the ancient martian surface environment. The best currently-available remote
87 sensing images and stereo-derived DEMs of Mars come from the High Resolution Imaging
88 Science Experiment (HiRISE) camera, and have a spatial resolution of 0.25 m/pixel (images) and
89 1 m/pixel (DEMs) (McEwen et al., 2007; Kirk et al., 2008). However, this is still coarse relative
90 to field observations. We hypothesize that this resolution limit has an effect on measurements of
91 set thicknesses and the dune field reconstructions based on them.

92 Here, we perform a numerical experiment using a field-acquired distribution of aeolian
93 cross-set thicknesses from the middle Page Sandstone, Arizona, USA (Cardenas et al., 2019). In
94 this experiment, the population of cross-set thicknesses is modified through the blending of
95 thinner sets into thicker sets on the basis of outcrop dip, the size of a remote sensing image pixel,
96 and the number of pixels needed to identify a unique set of cross strata. The aim is to blend
97 thinner, undetected sets into thicker sets, such that the original dataset is altered in a way that
98 mimics the sub-pixel mixing of a remote sensing image. The ancient environment recorded by
99 the Page Sandstone and its dynamics are well studied (Cardenas et al., 2019; Swanson et al.,
100 2019), and we compare these to re-interpretations of the ancient dune field based on the
101 experimental, resolution-filtered distributions. The distributions are compared using statistical
102 moments (mean, standard deviation, and products thereof), distribution shapes, and the number
103 of measurements remaining in a filtered dataset. The goal of this contribution is to enable
104 quantitative measurements of aeolian strata on Mars that take appropriate caution during
105 interpretation, and providing guidance on minimizing this potential source of error.

106

107 **1.1 Reconstruction of dune-field kinematics from cross-set-thickness distributions**

108 In aeolian dune fields, the controls on dune aggradation are important representations of
109 surface conditions. These autogenic processes include dune interactions (Ewing and Kocurek,
110 2010a and b; Day and Kocurek, 2018) and natural variation in dune scour depths (Paola and
111 Borgman, 1991; Jerolmack and Mohrig, 2005; Cardenas et al., 2019; Swanson et al., 2019).
112 Environmental boundary conditions include wind regime, sediment availability and source
113 geometry, basin geometry, the proximity of the water table to the surface, and antecedent

114 topography (Kocurek et al., 2010; Ewing et al., 2015; Chojnacki et al., 2019; Cardenas et al.,
115 2019; Swanson et al., 2019).

116 Bypassing dune fields are able to accumulate and preserve cross sets via the filling of
117 their own variably deep dune trough scours that form as the dunes migrate, without the need for
118 net-bed aggradation (Paola and Borgman, 1991). These cross sets are laterally discontinuous, as
119 they primarily represent the fill of the deepest local scours. This favors the preservation of thin,
120 heavily scoured sets and thick, scour-filling sets. As such, the variability in set thickness is
121 greater than the variability in dune scour depths. In contrast, laterally continuous, climbing cross
122 sets record steady bed aggradation and will not favor the preservation of cross sets filling the
123 deepest scours as strongly, meaning a greater percentage of dunes have preserved cross sets
124 (Allen, 1973; Rubin and Hunter, 1982; Bridge and Best, 1997; Leclair et al., 1997; Jerolmack
125 and Mohrig, 2005; Swanson, 2019). As a result, the variability in cross-set thickness is closer to
126 the variability in dune scour depths.

127 To better understand the relative contributions of scour depth and bed aggradation, and
128 therefore the forcings upon the dune field, the distribution of cross-set thicknesses can be
129 analyzed quantitatively (Bridge and Best, 1997; Leclair et al., 1997; Jerolmack and Mohrig,
130 2005; Swanson et al., 2019; Cardenas et al., 2019). A primary metric used for such analysis is the
131 coefficient of variation of cross-set thicknesses, c_v ,

$$132 \quad c_v = s_\sigma / s_m \quad (1)$$

133 where s_m and s_σ are the mean and standard deviation of set thicknesses. The value of c_v for a
134 given dune field is controlled by the ratio of dune migration rate to bed aggradation rate (Paola
135 and Borgman, 1991; Bridge and Best, 1997; Leclair et al., 1997; Jerolmack and Mohrig, 2005;
136 Cardenas et al., 2019). Dune heights are commonly gamma distributed, independent of setting -

137 i.e., fluvial, Paola and Borgman (1991); natural and experimental fluvial, van der Mark et al.
138 (2008); experimental fluvial, Ganti et al., 2013; aeolian, Swanson et al. (2016). With gamma
139 distributed dune heights, a dune field undergoing net bypass will have a set thickness $c_v = 0.88 (\pm$
140 $0.03)$ (Paola and Borgman, 1991; Bridge, 1997; Jerolmack and Mohrig, 2005). The distribution
141 of set thicknesses resulting from such a net bypass dune field will be exponentially distributed
142 (Paola and Borgman, 1991; Jerolmack and Mohrig, 2005; Cardenas et al., 2019; Swanson et al.,
143 2019). With a higher aggradation rate relative to the dune migration rate, the set thickness c_v will
144 decrease until it reaches the coefficient of variation of the original bedform heights (Jerolmack
145 and Mohrig, 2005) in the range of 0.29-0.60 (White Sands = 0.29, Swanson et al., 2016;
146 Algodones = 0.45; Cardenas et al., 2019; fluvial dunes in the Trinity River = 0.60; Mason and
147 Mohrig, in review). As the c_v decreases, the best-fit distribution of set thicknesses will also
148 change to a gamma distribution. As the rate of bed aggradation approaches the rate of dune
149 migration, this curve will also better represent the formative bedform heights (Jerolmack and
150 Mohrig, 2005).

151

152 **1.2 The Page and Entrada Sandstones, Earth**

153 We use the Page and Entrada Sandstones, described below, as end-member aeolian dune-
154 field strata, representing dry bypass (no water table; Page) and wet aggradation (water table;
155 Entrada). The Jurassic middle middle Page Sandstone (hereafter, middle Page) is the record of at
156 least six stacked aeolian dune fields, each in a state of near bypass (i.e., low sediment-
157 accumulation rates/low aggradation) during which there was not a near-surface water table. Each
158 bypass accumulation is separated from the others by formation-scale erosional surfaces
159 (Havholm et al., 1993; Havholm and Kocurek, 1994; Blakey et al., 1996; Cardenas et al., 2019).

160 Episodic highstands in dune field water table, driven by highstands in the adjacent Carmel sea,
161 helped preserve these bypass accumulations through subsidence sufficient for the strata to
162 generally not be completely reworked during the following episode of aeolian sedimentation
163 (Havholm et al., 1993; Blakey et al., 1996; Cardenas et al., 2019). The bypass state of the middle
164 Page is recorded by the set thickness c_v of 0.90 and the exponential distribution of set thicknesses
165 (Cardenas et al., 2019). Additionally, the distribution of dune heights has been reconstructed for
166 the middle Page and can be reconstructed from any set of bypass strata with reasonable
167 assumptions about the standard deviation of the population (Cardenas et al., 2019). In contrast
168 with the Page, in the Entrada Sandstone, a rising near-surface water table drove significant
169 aggradation even after antecedent topography was filled (Carr-Crabaugh et al., Kocurek and
170 Day, 2018). This is represented by the set thickness c_v of 0.46, well within an aggradational
171 limits and plausibly representing the c_v of formative dune heights, as well as the gamma
172 distribution of set thicknesses (Cardenas et al., 2019).

173

174 2. METHODS

175 We began with a population of field-acquired set thicknesses from the middle Page
176 Sandstone (set thickness $n = 402$; data from Cardenas et al., 2019). The c_v of middle Page sets is
177 0.90 (Eq. 1; $s_m = 2.44$ m, $s_\sigma = 2.20$ m). The distribution is not rejected as exponential or gamma
178 by a two-sample Kolmogorov-Smirnov tests comparing the distribution to randomly generated
179 distributions of size $n = 100$ (Fig. 1). Both the c_v and the exponential distribution data are
180 diagnostic of the bypass dynamics of the ancient Page dune fields. We tracked the change in
181 these properties as we modified the distribution of set thicknesses to represent limitation imposed
182 on the measurements by hypothetical measurement from remote sensing data.

183 This population of Page set thicknesses was modified by removing measurements below
184 detectable thresholds in remote sensing images, and adding their thickness into adjacent sets. To
185 do this, a value is calculated for each set called exposure distance, D_E , such that

$$186 \quad D_E = s / \tan (\theta). \quad (2)$$

187 This represents the projection of the true vertical set thickness into a surface of dip θ in degrees
188 from horizontal. For a given set thickness s , D_E increases as the outcrop dip θ approaches zero.
189 That is, a set of s thickness is exposed across a longer horizontal distance D_E where the dip of the
190 outcrop is shallower (Fig. 1). One thing to note is that s , as it is used in Eq. 2 and defined in
191 Figure 1, is the apparent thickness of a set. In the experiments presented here, we assumed all
192 strata are horizontal and so the apparent and true thicknesses are equal. If the strata are inclined
193 at an angle Φ below the horizontal, Eq. 2 must be modified to use a true thickness that is
194 different from the apparent thickness:

$$195 \quad D_E = s_{TRUE} \sin (\theta) / \tan (\theta) \cos (90 - \Phi - \theta). \quad (2a)$$

196 With sufficient exposure, Φ can be measured using a DEM (e.g., Kite et al., 2016; Goudge et al.,
197 2017; Hughes et al., 2019), in addition to the readily measured surface slope, θ . Equation 2 was
198 run with a range from 1° to 60° at 1° intervals. Then, we defined a detection limit, D_L , such that

$$199 \quad D_L = xR \quad (3)$$

200 where R is the resolution of an image pixel (set here as the maximum resolution of HiRISE 0.25
201 m) and x is an assumed number of pixels required to identify a unique set. Although D_L shares
202 units of distance with R for purposes of running the code, we will also refer to D_L as the
203 associated number of pixels in the text. We set x to a range from 3 to 10 pixels at 1 pixel
204 intervals, leading to D_L values of ranging from 0.75 m to 2.50 m at 0.25 m intervals. The length
205 of three pixels is a typical rule of thumb for image detection limits, a reasonable lower bound to

206 begin exploration of results. With 8 detection limits and 60 dips, 480 unique experiments were
207 run.

208 Forty-five vertical sections composed of the thicknesses of stacked sets (Cardenas et al.,
209 2019) were organized as columns in a matrix. For each section, the sets were tested for detection
210 in order. For any given set, If $D_E \geq D_L$, that set that set was not modified. If $D_E < D_L$, then the
211 set's thickness was added to adjacent sets depending upon its position, and then removed. If the
212 first set was not detected, its thickness was added to the second. If the final set was not detected,
213 its thickness was added to the previous set. If the set was between other sets, half of its thickness
214 was added to the two adjacent sets. If the set was the only set in the section, it was labeled an
215 automatic detection. One change was allowed to each section before another detection test was
216 performed, until all sets passed the detection test. This process is analogous to the loss of sub-
217 resolution data, as set thicknesses are blended together while overall section thickness is
218 maintained. Finally, although HiRISE DEM resolution is four times coarser than visible images,
219 this experiment assumed sub-pixel interpolations of elevation are reasonable so that DEM
220 resolution would not be the limiting factor in the collection of set thickness measurements.

221

222 3. RESULTS

223 As outcrop dip (θ) increases, D_E for all sets decreases, dropping many sets below D_L .
224 This leads to a decrease in the total number of sets, n , resulting from any experiment (Fig. 2).
225 Note that because the thickness of each of the 45 vertical sections is preserved, a decrease in n is
226 concurrent with a thickening of some sets. In the $D_L = 3$ pixels scenario, the first set is lost at $\theta =$
227 13° , and the number of measurements n , drops as low as 249 (62% of original measurements) at
228 60° (Fig. 2). The loss of the first set occurs at only $\theta = 4^\circ$ in the $D_L = 10$ pixels scenario, and n is

229 reduced to only 66 sets (16% of original measurements) in the $\theta = 60^\circ$ experiment. The loss of
230 sets preferentially drives an underrepresentation of the thinner side of the distributions,
231 represented by the shrinking of thinner histogram bars in Figure 3, as well as an increase in the
232 mean set thickness. The loss of sets eventually leads to a significant reshaping of the distribution,
233 seen clearly in the histograms (Fig. 3) and cumulative distribution functions (CDFs; Fig. 4) both
234 as outcrop dip and detection limit increase. At any given detection limit, the loss of
235 measurements and distribution reshaping occurs progressively from shallow to steeper surface
236 dips (Figs. 3 and 4). In addition to the visual comparison, the similarity of the filtered dataset to
237 the original is reported with a p-value produced by a two-sample Kolmogorov-Smirnov test. This
238 is shown across the entire experimental domain in Figure 5, which contours the p-value results of
239 all experiments at common critical p-values (0.001, 0.01, and 0.1).

240 The filtered histograms become increasingly gamma shaped with decreasing n , driven by
241 the reduction in the thinnest end of the distribution, the increase in the mean and mode, and the
242 thickening tails (Fig. 3). The comparison of the filtered datasets to the fitted distributions is more
243 clearly made in the CDFs (Fig. 4). The progressive filtering and loss of sets reduces the quality
244 of the exponential fit, seen visually and with p-values, but maintains and even increases the
245 quality of the gamma fit (Fig. 4). The filtering also causes s_m to increase by as much as 610% in
246 the most filtered dataset (Fig. 3L), while s_σ only increases by 249% (Figs. 3A vs 3L, and 6). The
247 difference in sensitivity of these two parameters to the applied filtering has significant
248 implications for c_v values (Eq. 1). The rapid increase in s_m relative to the slow increase in s_σ
249 creates a steady decrease in c_v with decreasing n (Fig. 6). Figure 7 shows c_v as a function of the
250 detection limit (D_L) for a number of outcrop dips (θ) ranging from 10° to 60° . These curves are
251 compared to horizontal lines representing field measurements from the middle Page (Cardenas et

252 al., 2019), and the Entrada (Crabaugh and Kocurek, 1993; Kocurek and Day, 2018). As D_L and θ
253 increase, steeper outcrop dips deviate from Page values towards Entrada values, while shallow
254 outcrop dips buffer the amount of data loss and change in c_v .

255

256 4. DISCUSSION

257 The results show that there is a significant risk of remote sensing cross-set thickness
258 measurements not representing the actual stratigraphy, but also that there is a clear range of
259 reasonable conditions for measurement of aeolian cross strata from HiRISE images (Fig. 5).
260 Even at 10 pixel detection limits (Eq. 3), 10° dips (θ) do little to alter the original dataset, losing
261 only up to the finest 4% of measurements (Figs. 2 and 3A-C). The preservation of measurements
262 leads to the preservation of reconstructions of dune-field kinematics and dune heights, as the c_v
263 of all filtered Page datasets at $\theta = 10^\circ$ remain within bypass range (Fig. 7), consistent with
264 interpretations of the original dataset (Cardenas et al., 2019; Swanson et al., 2019). A 30° dip is
265 able to provide a meaningful measurement at a 3 pixel detection limit, with $n = 96\%$ of the
266 original dataset (Figs. 3 and 7), but not beyond; at $D_L = 4$, the 30° dip moves beyond bypass (Fig.
267 7), only maintains $n = 82\%$ of the original data. This degree of blending has significantly altered
268 the shape of the fitted distribution, leading to the rejection of an exponential fit (Figs. 4G and H).
269 In terms of statistical similarity to the original dataset, only $\theta \leq 13^\circ$ can produce accurate
270 measurements at all D_L (Fig. 5). Given the difficulty in truly knowing a detection limit, focusing
271 on outcrops sloping $\leq 13^\circ$, or at least as shallowly as possible, is likely to result in the dataset
272 most accurately representing the actual strata.

273 The effect of resolution filtering on Page dune field reconstructions becomes increasingly
274 destructive with the increasing loss of thin sets. Much of this stems from the difference in

275 response to the filtering by s_m and s_σ (Fig. 5). This indicates that the loss of data alters the shape
276 of the fitted distribution, rather than simply translating it towards thicker measurements (Figs. 3
277 and 4). At worst, the low c_v values and the well-fit gamma curves would lead to the incorrect
278 reconstruction of the middle Page dune fields as highly aggradational (Fig. 7), which would in
279 turn lead to discussion regarding the environmental forcings driving aggradation instead of
280 bypass (e.g., local topography, water table, changing wind regime; Kocurek and Day, 2018;
281 Swanson et al., 2019; Cardenas et al., 2019). In the most filtered examples, the 30°, 45°, and 60°
282 exposures have c_v values approaching that of parts of the Entrada sandstone ($c_v = 0.46$; Fig. 7), a
283 wet, aggradational dune field which represents the end-member of aeolian dune field
284 accumulation styles completely opposite to the dry bypass of the Page (Havholm et al., 1993;
285 Crabaugh and Kocurek, 1993; Havholm and Kocurek, 1994). The reconstruction of the Page as
286 an Entrada-type dune field represents the complete loss of an accurate dataset. Additionally, with
287 a c_v well below 0.88, the ability to reconstruct the distribution of dune heights following the
288 methodology of Cardenas et al. (2019) is lost.

289 Stack et al. (2013), in their Figure 14, show several examples of bed-thickness
290 distributions from sedimentary outcrop on Mars. These distributions have shapes similar to our
291 high- θ experimental results. Namely, exponential fits underestimate of the number of thin beds
292 and overestimate of the number of thick beds (Fig. 3I-L). This is particularly apparent in several
293 of their distributions measured in Holden crater, particularly those labeled H1, H3, H4-H8, and
294 H10 in their Figure 14. Some of the local mean bed thicknesses in Holden crater reported in both
295 Stack et al. (2013) and Day and Catling (2019) are within the D_L values tested here. Although
296 these beds have distribution shapes similar to the filtered datasets reported here, it is not

297 definitive enough to constrain whether or not these beds in Holden crater are aeolian cross sets, a
298 hypothesis still being tested (Day and Catling, 2019).

299 The experiments performed here have additional implications for constraining the
300 depositional environment of strata on Mars. Gamma and exponentially distributed cross set
301 thicknesses, which should represent most aeolian cross sets, have been shown here to increase in
302 mean set thickness (s_m) more rapidly than in standard deviation (s_σ) as filtering increases and the
303 number of sets, n , decreases. This is not a characteristic shared by all distributions. Figure 8A
304 shows the CDF of a normal distribution, generated randomly with $n = 720$, $s_m = 2.98$ m and $s_\sigma =$
305 1.02 m, such that it did not produce negative values and is in range to be modified by the
306 previously used θ and D_L . Figure 8A compares this original distribution to the filtered
307 distribution at $\theta = 60^\circ$ and $D_L = 6$ pixels. The comparisons are qualitatively similar to the filtered
308 Page datasets, and the p-values from a two-sample Kolmogorov-Smirnov test would similarly
309 lead to rejection an exponential fit but do not reject a gamma fit (Fig. 4). A fit to a normal
310 distribution is rejected as well using the same test ($p < 0.001$). The most distinctive departure of
311 the normal distribution from the Page Sandstone results is that s_m and s_σ increase at a much more
312 similar rate with decreasing n , leading to a c_v that starts low and increases with decreasing n
313 (Figure 8B). By beginning with remote sensing set thicknesses rather than field measurements,
314 this experiment could presumably be picked up somewhere at a middling n value to test the
315 response of s_m , s_σ , and c_v to decreasing n . An increasing or steady c_v would then be diagnostic of
316 an originally normal distribution, which would likely rule out aeolian origin, although a
317 decreasing c_v pointing towards an original gamma or exponential distribution would not be
318 unique to aeolian cross sets.

319 This method and these numerical experiments assume individual cross sets are uniform in
320 thickness. This assumption is likely to be valid for dune accumulations in wet systems. However,
321 in a dry aeolian system, during deposition, dune scour depth may vary, and thus cause set
322 thickness to vary spatially. If such variation set thickness is present, the possible error associated
323 with the presented workflow is correlated with both the magnitude of set thickness variability
324 and the surface dip used to calculate the excursion distance. However, in this study, selected
325 sections exhibited very low lateral variation in set thickness, which would be exaggerated for any
326 outcrop dip less than vertical. Similarly, this method would be optimally applicable for either
327 higher-dip exposures of cross sets, or regions with strata that approximate tabular cross sets.
328 Future work is planned to explore the sensitivity of set thickness measurement to the three
329 dimensionality of dune deposits with variable scour depths a numerical model, however, for
330 large-scale dune cross sets, this effect is hypothesized to be minimal.

331

332 **5. CONCLUSION**

333 As a community, we are in a good technological position to significantly improve our
334 understanding of Mars' aeolian history, as aeolian deposits are far more likely to have bed
335 thicknesses measurable with remote observations than fluvial or submarine strata. An
336 understanding of the sedimentology down to the scale of individual beds, regardless of
337 depositional setting, is fundamental to paleo-environmental reconstructions. The results of the
338 numerical experiment conducted here are specific to the Page Sandstone, but offer a general
339 framework to address problems surrounding the finite size of pixels in remotely collected raster
340 images and irregular outcrop topography when measuring strata thicknesses on Mars. Where
341 possible, measurements should be made from shallow-sloping ($\leq 13^\circ$) outcrops, such that thin

342 sets are fully represented because they are exposed over long distances. The experiments here
343 may also prove useful in reconstructing the original distribution of sets by testing the response of
344 a remotely measured dataset to further filtering. Finally, with many considering that aeolian
345 strata may compose more of Mars' rock record than previously recognized (e.g., Anderson et al.,
346 2018; Day and Catling, 2019), this work provides strong quantitative tools with which to
347 interpret these strata and to understand possible sources of error.

348

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354

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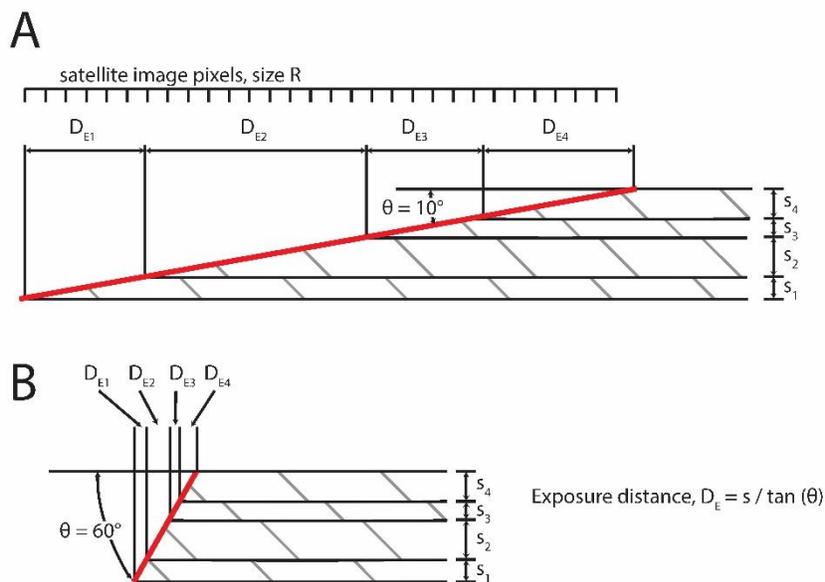
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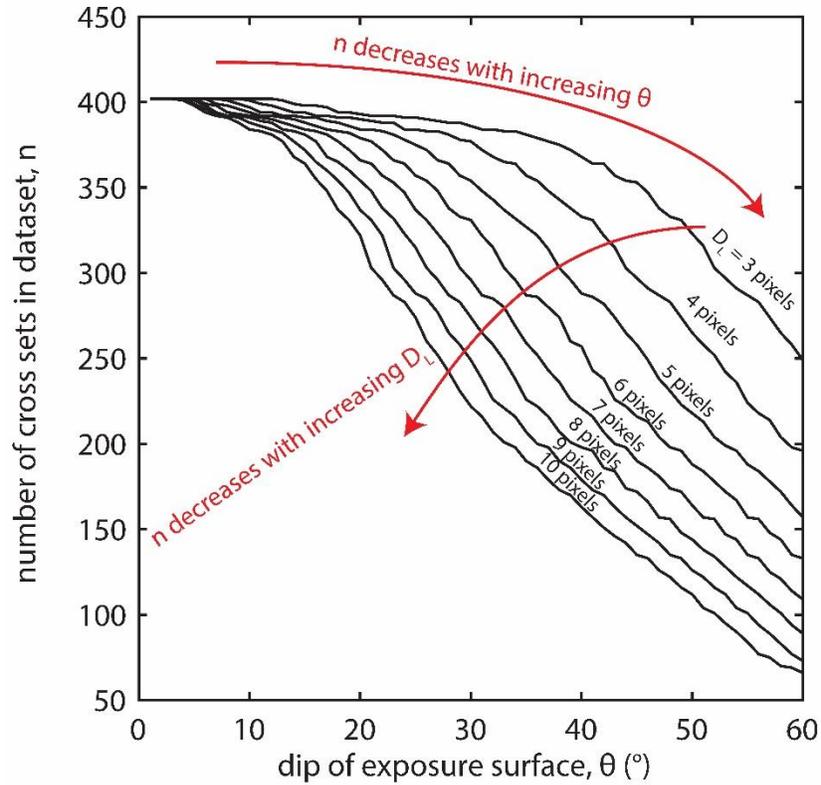
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507 **8. FIGURES AND CAPTIONS**



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 509 Figure 1 – A: Experiment schematic showing why exposure distance, D_E , is a function of outcrop
 510 dip (red surface, $\theta = 10^\circ$) and cross-set thickness, s . Satellite resolution, R , is shown in relation to
 511 D_E . B: An increased outcrop dip ($\theta = 60^\circ$) results in decreased D_E for the same s values as panel
 512 A. The formula to calculate D_L and D_E are shown, assuming horizontal strata.
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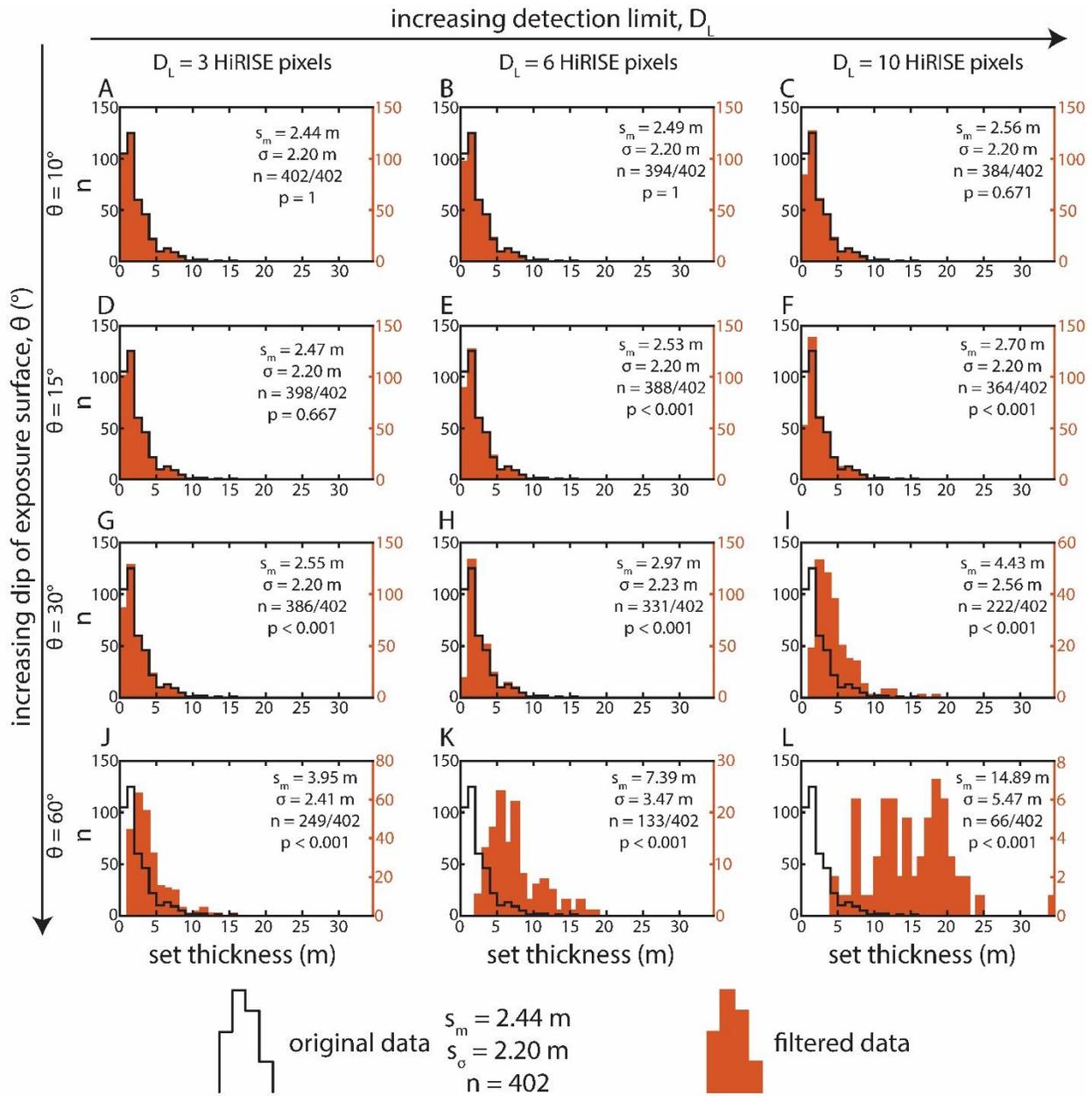


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515 Figure 2 – The effect of blending sets (Fig. 1) on the number of sets in the filtered dataset, as a
 516 function of the dip of the exposure surface (θ) and the detection limit (D_L). The number of sets
 517 (n), and thus the degree of change from the original dataset, is largely controlled by θ , which also
 518 amplifies the effect of D_L at high θ . Wiggles in the lines are due to the threshold nature of the
 519 resolution-based set length filtering.

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Figure 3 – A-L: Histograms comparing the original distribution of Page set thicknesses (black line) to 12 filtered distributions (red filled). All histograms have two y axes showing n for the original data (left) and filtered data (right), and 1 m bins. The filtering of thin sets is performed as a function of outcrop dip and assumed detection limits (Fig. 1). Each panel shows the filtered data's mean, standard deviation, n , and p -value in comparison to the original dataset, calculated using a two-sample Kolmogorov-Smirnov test. Columns represent experimental results at

529 detection limits (D_L) = 3, 6, and 10 HiRISE pixels. Rows represents results at exposure dips (θ)
530 of 10° , 15° , 30° , and 60° . In general, increases in D_L and θ create filtered datasets of decreasing
531 similarity to the original, both in terms of shape, statistical moments, and number of
532 measurements.

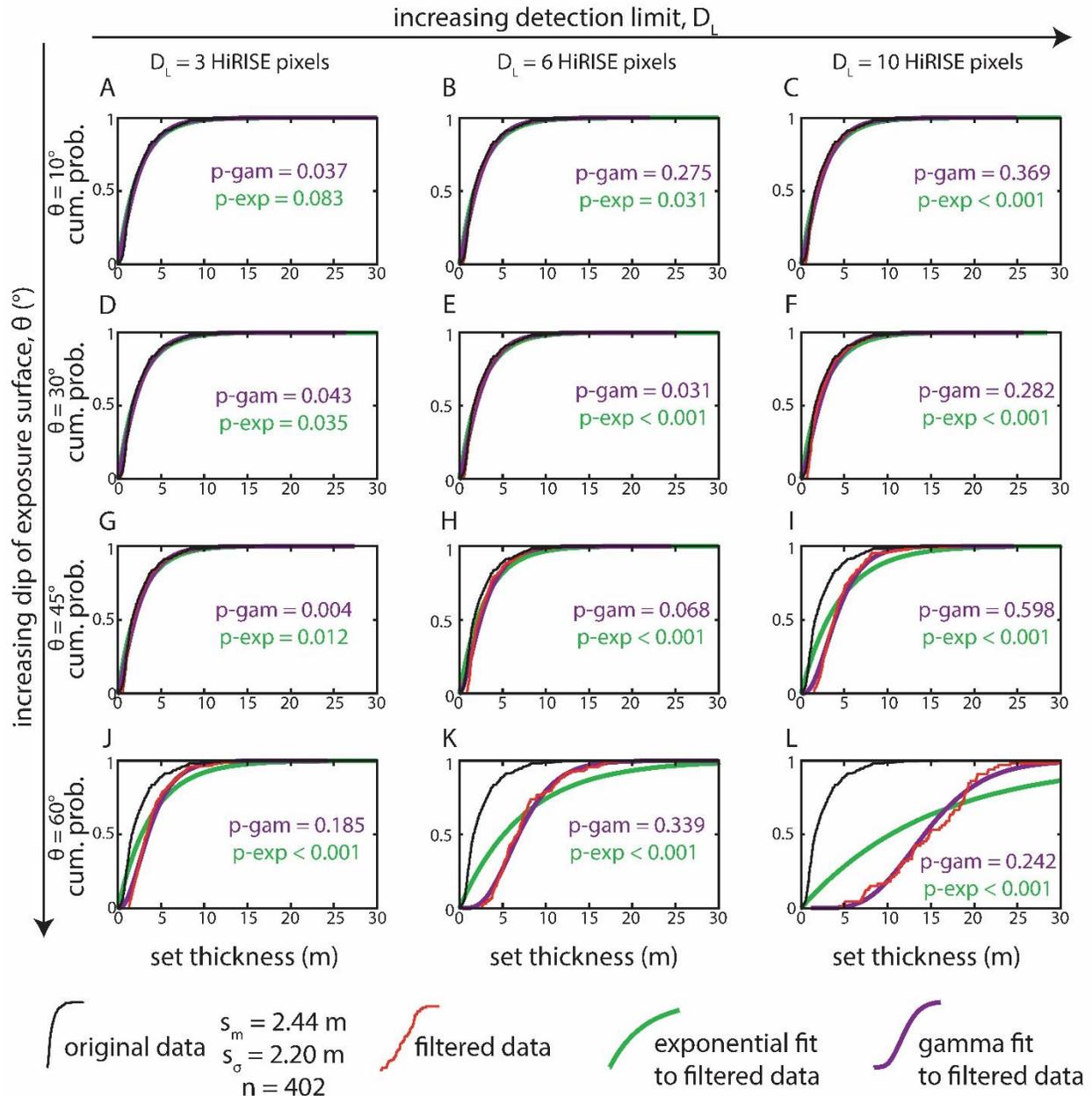
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Figure 4 – A-L: Cumulative distribution functions (CDFs) comparing filtered data to fitted

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exponential and gamma curves, as well as the original dataset (each panel shows the same data

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shown in Fig. 2). The filtering of sets was performed as a function of outcrop dip and assumed

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detection limits (Fig. 1). Shown in these panels are the p-values from the two-sample

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Kolmogorov-Smirnov test of similarity between the filtered data and the fitted gamma and

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exponential distributions. The filtered data's mean, standard deviation, and n values are shown in

545 the associated panels of Figure 2. Columns represent experimental results at detection limits (D_L)
546 = 3, 6, and 10 HiRISE pixels. Rows represents results at exposure dips (θ) of 10°, 15°, 30°, and
547 60°. The progressive filtering of sets coincides with the continued departure from the statistical
548 moments of the original data, as well as the change in shape to gamma distributed, which was
549 maintained in all the experiments.

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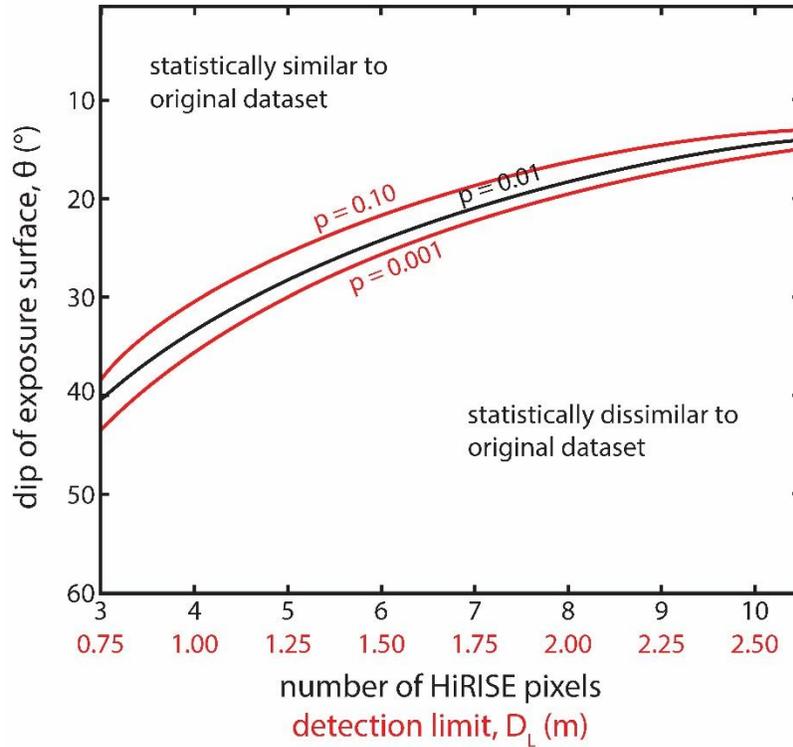
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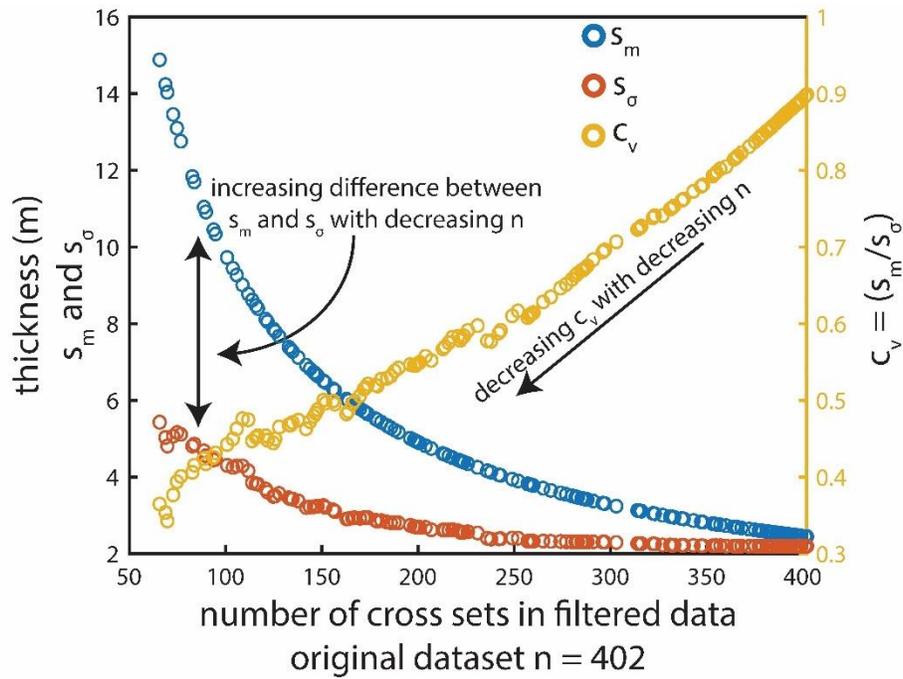


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560 Figure 5 – The detection limit (D_L) and the dip of the exposure surface (θ) as controls on the
 561 statistical similarity of filtered datasets to the original. The red and black lines are contours at p-
 562 values of 0.10, 0.01, and 0.001 calculated from a two-sample Kolmogorov-Smirnov test. These
 563 p-values are commonly used as critical p-values for rejecting the similarity of two datasets or
 564 not.

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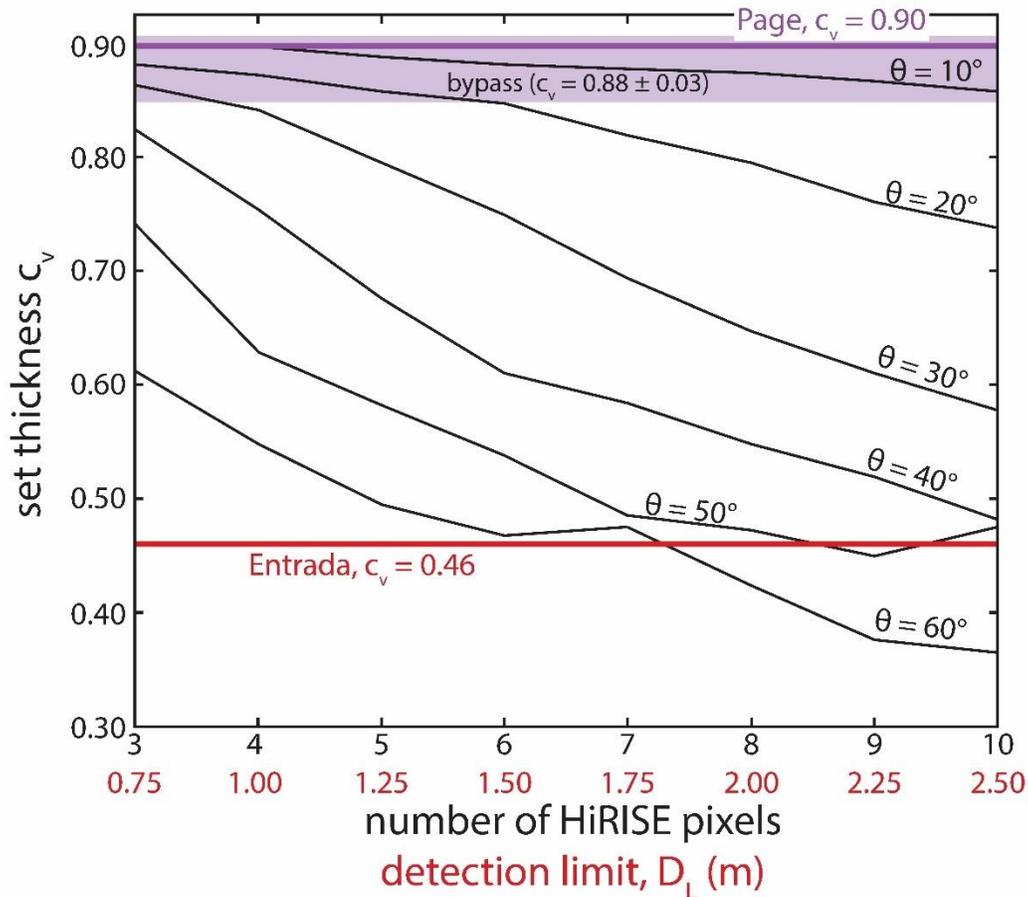
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568 Figure 6 – Change in mean set thickness (s_m), standard deviation of set thickness (s_σ), and
 569 coefficient of variation of set thickness ($c_v = s_m / s_\sigma$) as a function of the number of cross sets (n)
 570 in the filtered datasets. As n decreases with increased filtering, s_m increases more rapidly than s_σ ,
 571 causing a drop in c_v . The c_v is an important value for reconstructing the history of aeolian dune
 572 fields from preserved cross sets, and the change in c_v seen over this plot is significant enough to
 573 alter that reconstruction.

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 576 Figure 7 – The detection limit, D_L (Eq. 2), vs. the coefficient of variation, c_v (Eq. 1), of filtered
 577 and original datasets. The c_v of the unfiltered Page and Entrada data (Kocurek and Day, 2018;
 578 Cardenas et al., 2019) are shown with bold colored lines. A range of c_v values representing
 579 bypass is shown in the purple area (0.88 ± 0.03 ; Paola and Borgman, 1991; Bridge, 1997). Lower
 580 c_v values are increasingly interpreted as aggradational dune fields (Bridge and Best, 1997;
 581 Jerolmack and Mohrig, 2005). The Page and Entrada represent opposite types of dune field
 582 accumulations (dry and bypassing vs. wet and aggrading). This is represented by their different
 583 c_v values. Black lines represent the c_v of the filtered Page datasets at different outcrop dips (θ)
 584 and D_L values. Increasing detection limits decrease the filtered c_v only slightly at $\theta = 10^\circ$, and in
 585 fact does not leave the range of bypass. The effect is more significant at all higher dips. The c_v of
 586 $\theta = 20^\circ$ and 30° are within the range of bypass at $D_L = 3$ and 5 pixels, but move beyond bypass

587 range at higher D_L . At $\theta = 40^\circ$ to 60° , c_v values are lower than bypass, even at $D_L = 3$ pixels. The
588 c_v of $\theta = 50^\circ$ and 60° is equal to or less than the Entrada c_v at $D_L = 8$ and 9 pixels, representing
589 the complete loss of data quality which would lead to the end-member misinterpretation of the
590 Page accumulation history.

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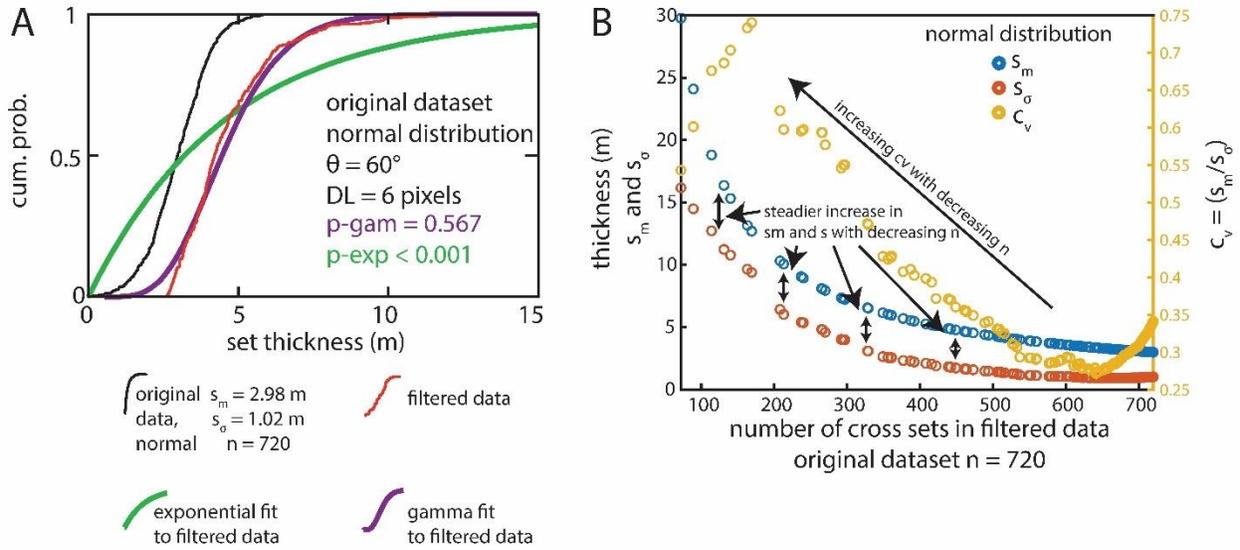
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601 Figure 8 – A normal distribution of cross sets run through the same experiments as the Page sets,
 602 with the intention of looking for unique responses to the filtering process. A: CDF plot
 603 comparing the original normal dataset to a filtered dataset and the filtered dataset's fitted
 604 exponential and gamma distributions. P values are shown for the fits to the filtered data. Similar
 605 to the Page sets, filtering produces a dataset that is gamma shaped rather than exponential. B:
 606 Plot comparing the mean set thickness (s_m), standard deviation of set thickness (s_σ), and
 607 coefficient of variation of set thickness ($c_v = s_m / s_\sigma$) of the normal distribution in panel A as
 608 functions of the number of sets in an experiment, n . Unlike the exponentially distributed Page
 609 sets (Fig. 6), the normal sets show a steady increase in both s_m and s_σ , which creates a steady
 610 increase in c_v .