PARADOXICAL IMPACT OF SPRAWLING INTRA-URBAN HEAT ISLETS: REDUCING MEAN SURFACE TEMPERATURES WHILE ENHANCING LOCAL EXTREMES

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ABSTRACT

Cities are at the forefront of climate change impacts and face a growing burden of adaptation to 1 ensuing natural hazards. Extreme heat is a particularly challenging hazard as persistent heatwaves 2 are locally exacerbated by the Urban Heat Island (UHI) effect. As a result, there is an increasing sci-3 entific interest in the influence of diverse urban morphologies on UHI. However, as the temperatures 4 within cities are highly spatially heterogeneous, bulk quantification metrics such as UHI Intensity 5 may hamper understanding. Here, we use remotely sensed Land Surface Temperature (LST) data 6 for 78 diverse cities to develop a novel multi-scale framework of quantifying spatial heterogene-7 ity in the Surface UHI. We identify heat clusters emerging within the SUHI using percentile-based 8 thermal thresholds and refer to them collectively as intra-Urban Heat Islets. We first develop a La-9 cunarity based metric (Λ_{score}) to quantify the spatial organization of heat islets at various degrees 10 of sprawl and densification. Using probabilistic models, we condense the size, spacing, and inten-11 sity information about heterogeneous clusters into distributions that can be described using single 12 scaling exponents. This allows for a seamless comparison of the heat islet characteristics across 13 cities at varying spatial scales. From the size distribution analysis, we observe the emergence of two 14 distinct classes wherein the dense cities (positive Λ_{score}) follow a Pareto size distribution, whereas 15 the sprawling cities (negative Λ_{score}) show an exponential tempering of Pareto tail. This indicates a 16 significantly reduced probability of encountering large heat islets for sprawling cities. Contrastingly, 17 however, Heat Islet Intensity modeled as exponential distributions reveal that a sprawling configu-18 ration is favorable for reducing the mean temperature of a city. However, for the same mean SUHI 19 intensity, it also results in higher local thermal extremes. This poses a paradox for urban designers 20 in adopting expansion versus densification as a growth trajectory to mitigate the UHI. 21

22 Introduction

More than 50% of the world's population currently resides in cities, and the number continues to increase rapidly with a 23 projection that 70% of the global population will be urbanized by 2050 (Prudhomme, 2018). Rapid urbanization trends 24 are manifested in expansion and densification of existing cities and the merging of agglomerations to form megacities, 25 particularly in South Asia and sub-Saharan Africa (Seto and Shepherd, 2009). Among the numerous challenges that 26 cities face, a particularly urgent problem due to climate change is that of extreme heat. Urban areas often raise the 27 local temperatures relative to natural and rural surroundings leading to the phenomenon of Urban Heat Island (UHI) 28 effect. A synergistic interaction between UHIs and increasingly persistent heat waves further exacerbates the extreme 29 temperatures within cities (Li and Bou-Zeid, 2013; Zhao et al., 2018). Repercussions of extreme heat include thermal 30 discomfort (Nikolopoulou and Lykoudis, 2006), increased energy consumption (Santamouris, 2014), and a greater 31 number of heat-related casualties during heat waves (Semenza et al., 1996; Uejio et al., 2011). 32 The UHI is typically quantified as UHI Intensity, i.e. the difference between the air temperatures of a represen-33 tative urban area (point measurement or spatial average) and rural area. However, such an estimate is inadequate to 34 address the intra-urban spatial heterogeneity. Commendable efforts to collect spatially resolved thermal data such as 35 the Basel Urban Boundary Layer Experiment (BUBBLE) campaign (Rotach et al., 2005) are rare and often limited to 36 a single city. On the other hand, earth-monitoring satellites such as Landsat and Moderate Resolution Imaging Spec-37 troradiometer (MODIS) enable consistent high spatial resolution characterization across multiple cities. As a result, 38 the Surface UHI (SUHI) estimated using Land Surface Temperatures (LST) has emerged as an alternative approach 39 which we adopt in this study (Roth et al., 1989; Voogt and Oke, 2003). For satellite sensors, urban features such as 40 building roof and wall exteriors, surface materials, albedo, impervious and vegetated fractions, and surface moisture 41 within each pixel determine the resultant LST. Note that while SUHI bears similarity in spatial and temporal patterns 42 to UHI, spatial patterns of SUHI are more coupled with urban form and function, whereas air temperatures are subject 43

to the boundary layer wind profiles as well, therefore, a point-to-point correspondence can not be expected (Panwaret al., 2019).

LST, which is strongly determined by the land use land cover properties, emerges from the underlying self-46 organization of the urban forms. As a result, the role of spatial organization of urban form in reducing SUHI Intensity 47 has been a topic of substantial research spanning multitude of spatial scales. At the micro-scale, i.e. within the urban 48 canyon, the surface temperatures are extremely sensitive to the geometrical details of immediate surroundings, such 49 as street canyon geometry, sky-view factor, vegetative fraction, solar access and shading (Jamei et al., 2016; Taleghani 50 et al., 2015; Andreou, 2013). However, at the local scale, i.e. of the order of few kilometers, consistent thermal patterns 51 emerge due to locally homogeneous patches of urban form and function (Stewart and Oke, 2012; Ching et al., 2018). 52 We do not have a clear understanding of the optimal urban form and function that minimize the urban heat locally 53 as well as at a city-scale. For instance, studies investigating local scale impacts (Sobstyl et al., 2018; Schwarz and 54 Manceur, 2014) report that high-density urban development leads to higher local temperatures, whereas, several others 55 note that sprawling urban development may result in worse thermal conditions (Stone Jr and Rodgers, 2001; Stone 56 et al., 2010). Debbage and Shephard (2015) (Debbage and Shepherd, 2015) show that regardless of the urban density 57 type within a patch, the relative spatial contiguity of the urban land use patches is a critical variable as well. Despite 58 these recent advances on the intra-urban thermal landscape over the last few decades, a comprehensive framework for 59 the characterization of intra-urban thermal heterogeneity for diverse city morphologies is still lacking. 60

We use a multi-scale framework wherein we treat the SUHI not as a single entity, but as a collection of heterogeneous clusters of heat within the city. We refer to these clusters as **intra-urban heat islets**. The objective of this study is to evaluate the impact of spatial organization of these heat islets on their properties such as size and intensity and

determine if there is a favourable spatial structure for reducing surface temperature extremes at intra-urban spatial 64 scales. Urban morphology, and as a result LST, emerges via the processes of densification and expansion, albeit 65 constrained by cultural, geographic and economic factors (Batty, 2013; Mustafa et al., 2018). Different degrees and 66 combinations of these two processes result in diversity of form and function. Dense urban growth occurs when there 67 is increased in-fill construction within existing high-density built-up area. Such a process is often driven by economic 68 and socio-political factors that lead to settlement of new urban regions close to the city center (Andersson et al., 2006). 69 This is akin to the preferential attachment phenomenon observed in complex networks where a new node is more likely 70 to agglomerate at the "hub nodes" with the highest density of edges (Barabási and Albert, 1999). We hypothesize that 71 the densification within urban area results in hot regions getting hotter and larger thereby resulting in a heavy-tailed 72 size distribution of heat islets. Urban expansion in the form of sprawl, on the other hand, occurs at the periphery of 73 urban areas in the form of growing sub-urban regions. We hypothesize that this would lead to the emergence of heat 74 islets that are spread more evenly throughout the city, often interspersed with local heat sinks. This can be detected 75 in the size distribution as a fast decaying tail, often in the form of an exponential tempering (Amaral et al., 2000). 76 Similar effects of urban expansion and densification on the power-law node degree observed is observed in several 77 urban infrastructure systems such as roads and sewage networks (Mohajeri et al., 2015; Yang et al., 2017; Klinkhamer 78 et al., 2017). Note that we don't refer to the spatial organization of urban assets such as buildings or impervious 79 areas. Rather, we directly analyze the LST. We implement the framework for a set of 78 cities sampled globally. 80 Using probabilistic models, we condense the size, spacing, and intensity information about heterogeneous clusters 81 into distributions that can be described using single scaling exponents. This allows for a seamless comparison of the 82 heat islet characteristics across cities that represent varying degrees of sprawl or densification. We then assess how the 83 thermal spatial structure relates to the traditional lumped metric, SUHI Intensity. Lastly, we discuss implications for 84

desirable thermal configurations for cities to minimize the area and intensity of the heat islets.

86 Data acquisition and Clustering technique

A set of 78 cities were sampled encompassing diverse climatological, geographical, and cultural backgrounds as well 87 as different realizations of urban form and function (Figure 1). The cities selected range from megalopolises such as 88 Guangzhou, London, and New York City with a population of over 10 Million and metropolitan areas up to 3000 km², 89 to smaller cities such as Tbilisi, Bern, and Oslo that span less than 100 km². As a globally standardized dataset of 90 urban extent, the Urban Land Use layer of Land Cover product from MODIS was used. The exact definition of urban 91 boundaries and city area plays a significant role in urban scaling laws (Cottineau et al., 2017), therefore, a buffer of 92 5 km in the rural regions was taken to account for the peri-urban settlements. However, as the heat islets occur well 93 within the city boundaries, the results were found to be independent of the buffer width. 94

For each city, we selected a Landsat image of a summertime cloud-free day, and derived the LST in the geospatial 95 computing environment of Google Earth Engine (Gorelick et al., 2017) using the methodology described in Walawen-96 der et al. (2012) (Walawender et al., 2012). A novel aspect of our methodology is the clustering technique used to 97 characterize the LST. The LSTs are treated analogously to topography in Digital Elevation Models (DEM), where the 98 temperatures substitute for elevation (Shreevastava et al., 2018). As the cities belong to diverse climatic backgrounds 99 (and hence, background temperatures) (Zhao et al., 2014), percentile-based thermal thresholds were chosen for identi-100 fying the relative hottest regions within the urban areas. The areas above a given thermal threshold (e.g., corresponding 101 to percentiles of temperatures) were identified, and the connected pixels were grouped into a cluster that we refer to as 102 a heat islet. Supplementary Information provides code and text describing the methods in more detail. 103

104 Size distribution of heat islets

In an exploration of *shapes* of heat islets, we found consistent self-similar, fractal topography across all cities (Shreevastava et al., 2019) (See Supplementary Figure 1). Here, we focus on their *size* distribution by building on the scaling laws known for fractal surfaces. According to Korcak's law, the size distribution of clusters in a fractal topography is expected to follow a power law at the percolation threshold (Imre and Novotnỳ, 2016; Mandelbrot, 1975; Isichenko and Kalda, 1991). This is mathematically represented as: $N(a) \propto a^{-\beta}$ where N is the number of clusters of area, a, and the scaling exponent is β . Expressed as an exceedance probability we can write it as a Pareto distribution:

$$P(A \ge a) \propto a^{1-\beta}, \quad \forall \ a \ge a_{min}$$
 (1)

where, for a given area a, the probability of an islet having an area A larger than a is represented by P, the scaling 111 exponent is represented by β , and the minimum area at or above which the power-law is valid is represented as a_{min} . 112 We use Maximum Likelihood Estimation (MLE) to test for and fit the exceedance probability distributions(Clauset 113 et al., 2009) (See Supplementary Text 3). This process is carried out for multiple thermal thresholds (50^{th} , 60^{th} , \cdots , 114 90th percentiles). We find that the estimated exponents ranged between 1.6 to 2.2 with a mean $\beta = 1.88$. However, 115 for the smaller cities ($A_{city} \leq 650 \text{ km}^2$), the variability in exponents was much larger (Supplementary Figure 2). 116 One explanation for this is statistical, wherein for small cities there are not enough islets obtained at 90 m resolution 117 which results higher statistical fluctuations about the mean are observed. As the number of islets increases with city 118 size, steady averaging is achieved that results in convergence towards the mean. However, from an urban growth 119 perspective, this behavior is consistent with several other complex systems that operate within cities (Klinkhamer 120 et al., 2017; Barthelemy, 2016). For smaller cities, the variability due to factors unrelated to city size result in more 121 detectable fluctuations and it simply indicates that they have not grown in size enough to display self-organization yet 122 (Batty, 2008). We, therefore, excluded those from any further analysis and proceed with 49 cities where the internal 123 thermal structure could be reliably quantified. For the larger cities, the distributions were well described by Equation 124 1 with the same mean exponent and a narrow variability (std. dev. = 0.026) (Shreevastava et al., 2019). 125

The impact of a dense or sprawling spatial organization becomes apparent in how the exceedance probability dis-126 tributions change as the threshold increases. The large metropolitan regions of Lagos and Jakarta are selected as 127 representatives of dense cities, where Chicago and Guangzhou are chosen to represent sprawling cities (Figure 2a,b). 128 The Pareto size distribution is consistent at lower thresholds for all cities. At 90th percentile threshold, however, Lagos 129 and Jakarta show a pronounced aggregation of heat islets indicative of dominance of a dense urban center, whereas 130 Chicago and Guangzhou are more dispersed (Figure 2c,d). In agreement with our initial hypothesis, Lagos and Jakarta, 131 display a Pareto heat islet size distribution across all the thresholds (Figure 2e). However, for Chicago and Guangzhou, 132 the heat islet size distributions deviate significantly from the Pareto in the form of an exponential tempering (Figure 133 2f), such that their distributions more closely follow: 134

$$P(A \ge a) \propto a^{1-\beta} \cdot e^{-c \cdot a}, \quad \forall \ a \ge a_{min}$$
⁽²⁾

where c represents the exponential tempering coefficient (Supplementary Table 3).

Such behavior is explained by invoking percolation theory (Isichenko, 1992; Sahimi and Sahimi, 2014). Percolation theory is the study of random clusters and their spatial connectivity at a given threshold. The coagulation of dispersed clusters into a contiguous component is referred to as percolation, and the largest cluster is identified as the percolating cluster. In fractal landscapes, the Pareto size distribution of clusters holds within a finite range (Percolation Transition Range) of thresholds, i.e., until the percolating cluster retains its identity. We computed the percolation transition range by identifying the inflection points in the size of the largest cluster as a function of temperature threshold (Figure 2g,h).

142 The range was then normalized using the minimum and maximum temperatures for each city such that the range is

restricted to 0 and 1. We refer to this as the Normalized Percolation Range (NPR) (Supplementary Figure 3). In case

of the aggregated cities (e.g. Jakarta and Lagos) as the temperature threshold is increased, the largest connected islet

decreases in size gradually, and the resulting NPR is large (Figure 2g). Conversely, in the case of sprawling cities

146 (e.g., Chicago and Guangzhou) there is a much sharper decrease in the size of the percolating cluster (Figure 2h)

resulting in a narrow NPR (Figure 2i,j). As the 90th percentile thresholds in these cases fall outside the NPR (Figure

148 2j), exponential tempering is observed.

From the perspective of the size distribution of heat islets alone, as the thermal threshold is increased, fewer and smaller heat islets are captured. Therefore, an exponential tempering presents a reduced probability of encountering large heat islets of higher temperatures. This suggests that a sprawling spatial structure is favourable for reducing the size of extreme heat islets. Thus far, we have characterized the size distribution of these islets, not their spatial organization. We now introduce a metric to quantify and analyze the relationship between the spacing of the urban heat islets and the characteristics we observed in their size distributions.

155 Quantifying Aggregated vs Dispersed heat islets: Lacunarity

A built-up patch in a city acts as a source of increased sensible heat flux, as well as anthropogenic heat flux due to 156 human activities such as air-conditioning. Likewise, the gaps between the patches (also referred to as spacing in this 157 work), often water or vegetation, act as heat sinks that absorb the excess heat generated. Therefore, characterizing this 158 spacing between the urban patches is an essential step towards ameliorating heat stress (Debbage and Shepherd, 2015). 159 Particularly, the impact of the relative sizes and strengths of such sources and sinks on the overall thermal landscape 160 has been relatively understudied and requires further investigation. Since the present study focuses on the thermal 161 landscape characterized by LST, we can directly quantify the spacing between the identified heat islets. Popular 162 metrics such as root mean square distances work well for Gaussian systems, but for fractal landscapes, lacunarity is 163 a better-suited metric of spatial structure (Plotnick et al., 1996). Lacunarity (Λ) is a scale-dependent measure of the 164 aggregation of spaces between the heat islets (Mandelbrot, 1982; Plotnick et al., 1996). A 'gliding box' algorithm for 165 the calculation of Λ as a function of box size (r), as described in Plotnick et al. (1993), was adopted here (Methods 166 section). While the absolute values of Λ offer little insight, the appropriate way to interpret lacunarity is in the context 167 of the rate of change of Λ as a function of r. If the value of $log(\Lambda(r))$ decreases at any scale (quantified with log(r)), 168 the presence of spacing corresponding to that length scale is indicated. The two extremes of lacunarity curvature can 169 be best conceptualized as a chessboard-type homogeneous distribution of small-scale spacing, and a single contiguous 170 cluster. Essentially, the length scales corresponding the steepest slopes should be interpreted as the dominant scale of 171 spacing. 172

As the differences in the spatial organization of heat islets are most apparent at higher temperature thresholds, here, we characterized the spatial structure obtained at the 90th percentile of LST for all cities. By extension, the total *islet area* under consideration corresponds to the hottest 10% of the total city area. Lacunarity curves for the four representative cities investigated in the previous section are highlighted in Figure 3. The cities that have a dominance of larger spacing between the islets lay above the diagonal. Conversely, a dispersed spatial structure of the heat islets manifests as smaller spacing, fall under the diagonal. We assign a single score (Λ_{score}) to the convexity of the curves in Figure 3a such that positive scores indicate larger spacing and vice-versa. This is achieved using the followingempirical equation:

$$log_{10}(\Lambda(r)) = \left(1 - \frac{log_{10}(r)}{2}\right)^{2^{\Lambda_{score}}}$$
(3)

where constants 1 and 2 are used to fix the end points of the curve at $log(\Lambda(r)) = 1$ and log(r) = 2, and the exponent, Λ_{score} is scale-independent measure of the shape of the lacunarity curve (See Methods section). The 49 cities have Λ_{score} ranging between -0.9 to 0.6, and distributed normally (Figure 3b; See Supplementary Table 4).

Using Λ_{score} , we compare the relationship between the islet spacing and their NPR (and by extension, likely expo-184 nential tempering at higher thresholds). We find that the dense cities associated with an aggregated heat islet structure 185 (positive Λ_{score}) display a larger NPR (≥ 0.25 ; Figure 3c). Whereas, sprawling and disaggregated cities (negative 186 Λ_{score}) have a smaller NPR (< 0.25; Figure 3c) and consequently an exponential tempering of the power law tail 187 (Figure 2f). An exception to this pattern are cities with a negative Λ_{score} despite having an NPR ≥ 0.25 (shown in 188 yellow in Figure 3c). Upon examination, we found these to have a significant river flowing right through them. Under 189 such a scenario, the percolating heat cluster is divided structurally into two halves by a heat sink, irrespective of the 190 threshold (Supplementary Figure 4). This results in a negative Λ_{score} due to the spacing introduced by the river despite 191 an aggregation of heat islets on either side of the river. Thus, Figure 3c serves to quantitatively affirm the correlation 192 between the spatial configuration of cities (dense and/or sprawling) and the 2 classes of size distributions of the heat 193 islets. 194

Note that for any given size distribution, the islets can be spatially arranged in several ways. In order to examine 195 the variability in islet size and spacing of the various cities, we define two scale-independent metrics to characterize 196 size: Mean (A_M) and Largest (A_L) Relative Heat Islet Sizes, calculated as a percentage of the total city area. First, 197 we observe that there is a weak positive correlation ($R^2 = 0.4$) between A_M and spacing of the heat-islets (Figure 198 3d). This is expected because a positive Λ_{score} as well as a high A_M corresponds to dense cities, and a negative 199 Λ_{score} and low A_M corresponds to sprawling cities. More noteworthy is the horizontal spread about the diagonal in 200 Figure 3d which reflects the different spatial configurations (characterized by Λ_{score}) that are possible for any given 201 size distribution. This spread may be explained by A_L , which increases with Λ_{score} (illustrated using marker size in 202 Figure 3d; Supplementary Figure 5). In the bottom-left, both A_M and A_L are small. This is because negative Λ_{score} 203 corresponds to sprawling cities where large clusters were absent in the islet-size distribution (as inferred from the 204 exponential tempering of Pareto). In the bottom-right, however, the dominance of the largest aggregated islet results 205 in a positive Λ_{score} despite a low A_M value. A schematic diagram drawn to represent each of the vertices of this 206 plot is given as Supplementary Figure 6. The phase plot of A_M and Λ_{score} may be useful for city planners to gauge 207 the current spatial structure of the thermal landscape of their cities and to determine mitigation strategies to achieve a 208 more desirable state. 209

Islet Intensity distribution

Apart from the size and spacing of heat islets, we now focus on the temperatures obtained within the heat islets. To address this, we first use the well-known indicator of excess heat in urban areas, the SUHI Intensity in the traditional sense i.e., the difference between the mean urban and rural temperatures (Schwarz et al., 2011) to evaluate the average excess heat within cities. We find that larger Λ_{score} values (representative of aggregated heat islets) tend to be associ-

ated with higher SUHI Intensity (Figure 4b). This suggests that sprawling cities, with a larger number of heat sinks to

match the heat sources, are a better configuration for reducing the *overall* SUHI Intensity. This is in agreement with our
findings based on the size distribution of extreme heat islets as well as Debbage and Shephard (2015) findings based
on discontiguity of urban patches calculated using National Land Cover Dataset (NLCD) (Debbage and Shepherd,
2015). Traditional estimates of the UHI Intensity that simply use the difference between the **mean** temperatures over
an urban area and the surrounding non-urban environment fail to address the intra-urban heterogeneity adequately.

For a more comprehensive assessment of the thermal variability within cities, we introduce a novel *Heat Islet Intensity* distribution metric. First, we compute the excess heat (ΔT) for each islet as the difference between the mean *islet* temperature and the *threshold* temperature. We refer to this term as the *Islet Intensity*. We find that the mean and standard deviation of ΔT were equal (Supplementary Figure 7) which, along with the shape of its distribution (Figure 4a), were indicative that ΔT is exponentially distributed, i.e:

$$P(\Delta T \ge x) \propto 1 - e^{-\lambda x} \tag{4}$$

where, for a given islet intensity x, the probability of an islet having a temperature ΔT larger than x is represented by P, an exponential distribution characterized by λ . By extension, $1/\lambda$ is the mean islet intensity. Lower values of λ correspond to an increased probability of higher temperatures within the islets. Therefore, a single metric, λ can be used as an indicator to capture the intra-urban thermal variability across islets. This is represented as the color bar in Figure 4b.

We find that while cities with a higher degree of sprawl have a lower mean temperature, for the same SUHI (Y-axis in 231 Figure 4b), cities with lower Λ_{score} also experience higher likelihood of encountering thermal extremes. For example, 232 dense cities such as Lagos and Jakarta have a steeper exponential decaying rate than Chicago and Guangzhou, which 233 drastically reduces the probability of local thermal extremes within their heat islets. While the probability of a heat 234 islet being hotter than the mean by 1° C is almost zero for the first two, the likelihood increases to roughly 20% for the 235 latter two (Figure 4a). As the larger heat islets are often associated with the highest islet intensity as well, this can result 236 in a significantly large areas of extreme heat especially for megacities like Guangzhou and Chicago. Such a finding 237 reveals that while mean SUHI Intensity decreases with sprawling cities, for the same mean, they also experience higher 238 local thermal extremes. As a result, in addition to the mean SUHI Intensity, it is essential to characterize the thermal 239 heterogeneity within the cities, and the islet intensity distribution can be adopted as a complementary metric. 240

241 Summary and Conclusions

Cities grow through a combination of parallel and sequential episodes of expansion and densification at different rates. 242 Depending on local preferences and constraints, neighborhoods adopt different spatial patterns, for example, from 243 dense downtowns to sprawling suburbs. Factors like geographical topography, coastline, and intra-urban commuting 244 time constrain expansion, whereas other factors such as local building laws limit densification. While there are several 245 objective functions such as commuting travel time distribution, net carbon emissions, and socio-economical factors 246 which urban form and functions are optimized for, here, we focus on the aspect of urban heat. More specifically, 247 the spatial heterogeneity of extreme heat islets within urban areas. Towards that, we present a novel multi-scale 248 framework that allows us to identify intra-urban heat islets for several thermal thresholds. Using this framework, 249 we evaluate the impact of spatial organization, characterized by a Lacunarity-based metric, Λ_{score} . We do not find 250 a bi-modal distribution of Λ_{score} into two classes of sprawl or dense cities only. Rather, the Λ_{score} was normally 251 distributed around a mean value close to zero indicating that most cities display a balance between sprawl and dense 252

heat islet structure. Different realizations and degrees of expansion and densification yield a diverse array of spatial
 structures.

We condense the size, spacing, and intensity information about heterogeneous clusters into probabilistic distribu-255 tions that can be described using single scaling exponents. This allows for a seamless comparison of the intra-urban 256 heat islet characteristics across cities at several spatial scales ranging from 90 meters (resolution of Landsat 8 and 257 corresponding to several urban blocks) up to few thousand sq km (total area of large cities). We implement this frame-258 work for 78 globally representative cities to answer the following key questions. First, how many and how big are the 259 emergent heat islets at multiple thermal thresholds? Second, how much hotter than the threshold are these heat islets? 260 From the size distribution analysis, we demonstrate that islet sizes in dense cities follow and maintain a power law 261 tail across all temperature thresholds, whereas the sprawling cities show an exponential tempering of tails at higher 262 thresholds. Such a tempering is favourable as it indicates a reduced emergence of large heat islets in sprawling and 263 dispersed spatial configurations. Additionally, a dispersed configurations results in lower mean SUHI Intensity over 264 the city. However, from the islet intensity distribution analysis, we find that heat islet intensities (ΔT) can be mod-265 elled as exponential distributions, where dispersed configurations result in higher rate parameters, λ . This implies a 266 significantly higher probability of encountering extreme temperatures within the islets. As a result, while a sprawling 267 configuration is favorable for reducing the mean temperature of a city, for the same mean SUHI intensity, it results in 268 higher local thermal extremes. Therefore, from a design decision perspective, a trade-off between mean versus local 269 thermal extremes depending on other climatological and demographic factors will be required. In cities set in hotter 270 background climates, for instance, it maybe more desirable to reduce local extremes to avoid extreme heat hazards es-271 pecially if the local extremes occur where most vulnerable populations reside, such as densely populated downtowns, 272 or areas without access to air-conditioning such as urban slums. 273

Our analysis here is limited to the structural heterogeneity of heat sources and sinks, and not the functional hetero-274 geneity. If we assume a uniform heat capacity of land use, the sizes of heat islets are then indicative of the strength of 275 the sources, and the length-scale of spacing is indicative of the sink strengths. Consideration of the functional hetero-276 geneity will require a treatment of the variability in heat capacities and thermal conductivities of the land use which 277 jointly determine heat dissipation from sources, which is possible using models such as Weather Research Forecast 278 (WRF) (Chen et al., 2011; Salamanca et al., 2011). In such a scenario, instead of LST, heat fluxes can be treated as 279 DEM for such an analysis. It may also then be beneficial to study the spatial correlation between source strength and 280 sink strength to evaluate thermal dissipation. 281

We recognize that the spatial patterns of air temperatures (at 2 meters for example) might differ from those based on 282 SUHI derived from LST, as determined by a higher influence of atmospheric turbulence and boundary layer conditions 283 (Panwar et al., 2019). For example, a larger thermal gradient can result in turbulent eddies of larger length-scales in-284 ducing more overturning circulation which can, in turn, reduce the temperatures in dense urban areas. An investigation 285 of the spatio-temporal dynamics of air temperatures is beyond the scope of the present study but it certainly warrants 286 further research to study the persistence of these spatial patterns. Lastly, while the spatial characterization of temper-287 ature is informative for urban heat assessments, it does not inform the overall risk map to the concerned population. 288 Risk is a combination of hazard (extreme heat-stress, a combination of air temperature and humidity (Oleson et al., 289 2015)), time period of exposure, and vulnerability factors such as old age, low educational attainment, high poverty 290 levels, poor health, and lack of air conditioning (Cutter et al., 2009; Uejio et al., 2011; Bradford et al., 2015). In the 291 future, we seek to characterize the spatial variability in risk through joint probability distribution analysis of each of 292 the three dimensions of risk. 293

294 Methods

295 Study area and data sources

Land surface temperature (LST) data was derived using a Single Channel Algorithm as detailed in (Walawender et al., 2012) from Landsat 8 at a resolution of 90 m. The geo-spatial analysis environment of Google Earth Engine (GEE) was used to filter out cloud free summer time days with an incident solar angle of at least 60 degrees (Gorelick et al., 2017). See Supplementary Text S1 and S2 for algorithms, and Table S1 for list of cities and information on Landsat scenes used. For coastal cities the Large Scale International Boundary (LSIB) dataset provided by United States Office of the Geographer was used to crop out the oceans and delineate urban boundaries within GEE environment. Urban area was estimated using MODIS's Land Cover Type dataset - MCD12Q1.

303 Statistical modelling of size and intensity distributions

For fitting probability distribution functions (pdfs) to cluster size and intensity distributions, a combination of maximum-likelihood estimation (mle) with goodness-of-fit tests based on the Kolmogorov-Smirnov (KS) statistic and likelihood ratios were used (Clauset et al., 2009). See Supplementary Text S3 for details and Table S2 for results.

307 Lacunarity

First, the landscape was sliced at a thermal threshold and an islets map was obtained. For each box size $(1 < r < A_{city})$, the number of occupied pixels (islets) was measured. The number of occupied sites was referred to as the box mass. The box was then moved one column to the right and the box mass was again counted. This process was repeated over all rows and columns producing a frequency distribution of the box masses. The number of boxes of size r containing S occupied sites was designated by n(S,r) and the total number of boxes of size r by N(r). This frequency distribution was converted into a probability distribution: $Q(S,r) = \frac{n(S,r)}{N(r)}$. Lacunarity was a measure of variability

in the calculated occupancy for each box size.

$$\Lambda(r) = \frac{VarianceQ(S,r)}{MeanQ(S,r)^2} + 1$$
(5)

For all cities, Lacunarity score was calculated only for the 90th percentile thermal threshold. As a result, 90% of the total area in all cases comprised of spaces and the $\Lambda(r)$ value for box size = 1 was the same for all cities. The largest box size taken under consideration is normalized from 0 to 100 in order to account for the variable sizes of cities. Note that the curvature of Lacunarity curve was unaffected by these transformations.

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438 Figures



Figure 1: World map showing the locations of 78 cities considered in this study. The marker size is representative of the city size, and the colour represents their Koppen-Geiger climate classification Peel et al. (2007). Description of Koppen-Geiger climate types are given in Supplementary Table 1.



Figure 2: Two groups of cities emerge based on the size distributions of heat islets at incremental thermal thresholds. Two representative cities for each group - Jakarta, Indonesia and Lagos, Nigeria for dense cities, and Chicago, USA, and Guangzhou, China for sprawling cities - are shown. (a,b) Land Surface Temperature map (in °C), (c,d) Heat islets that emerge at the 90th percentile thermal threshold, (e,f) Exceedance probability plots for heat islets at several thermal thresholds (50th, ..., 90th). Note the leftward shift in size distribution as the thresholds increase, especially the exponential tempering evident in sprawling cities, (g,h) Largest islet size, and (i,j) sum of remaining islets (as a % of total city area), as a function of thermal threshold. The vertical dashed coloured lines mark the temperatures corresponding to the percentiles used in (e,f).



Figure 3: (a) Lacunarity curves of 49 cities (in grey) and the four archetype cities (in colour) shown on a $log(\Lambda)$ vs log(r) plot. The cities with a concave downwards shape in the upper side of the diagonal indicate larger and more aggregated gaps, whereas cities underneath the curve indicate a more uniform dispersed pattern of islets and smaller gaps. (b) Histogram of Λ_{score} of 49 cities (mean = 0.04, s.d. = 0.38). (c) Scatter plot of percolation transition range and Lacunarity score. This figure illustrates the classification of cities into the 2 classes based on Lacunarity Score and the type of transition. (d) Scatter plot of Mean Relative Heat Islet Size (A_M) versus Λ_{score} . Additionally, since the islet-size distribution is heavy tailed, in addition to the A_M , the largest islet size (as a percentage of the total city area) is indicated using the marker size. The A_M and the largest-heat islet size (A_L) serve to illustrate the size distribution of the city area.



Figure 4: (a) Empirical pdf of ΔT for the 4 archetype cities shown on at their 90th percentile thermal thresholds respectively. The same for all 49 cities is shown in grey in the background. Each ΔT distribution was well described as an exponential distribution characterized by the parameter: λ . (b) Scatter plot of mean SUHI Intensity, defined as the difference between mean urban and rural temperatures, versus Lacunarity Score (Λ_{score}) is shown. A weak positive correlation ($R^2 = 0.344$) is detected shown as dashed regression line. The color as well as size of the marker indicates the inverse of rate parameter (λ) from Equation 4 which is equal to the mean Heat Islet Intensity for each distribution. Increasing size indicates higher temperatures within the heat islets.