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ABSTRACT

Turbulent mixing is vital for water transformation in the ocean and sustains the global thermohaline circulation. Despite decades of global observations using different platforms, our understanding of ocean turbulence is still limited. More observations are needed to better characterize the spatio-temporal distribution of mixing to reduce uncertainties in climate models. Marine seismic reflection surveys are an untapped data resource for high-resolution ocean turbulence observation. Turbulent mixing can be extracted from seismic data through horizontal internal wave slope spectra. However, to date, a standardized approach to prepare seismic data for this spectral analysis is still lacking, leading to insufficient consideration of the impact of noise on the resulting diffusivities. To address these issues, we perform a full-wavefield synthetic modeling and processing to reveal noise-induced overestimation of diffusivities. We further propose a widely applicable workflow and apply it to three field seismic surveys with increasing noise levels conducted in regions of different turbulence environments: ocean ridges, open ocean interior, and continental slope. The derived diffusivities are benchmarked against direct measurements around the region to show the fidelity of this seismic method. The extended observation records by seismic data across the Kauai Channel and away from Mid-Atlantic Ridges reveal the importance of topography in modifying the propagation of internal tides and the distribution of turbulent mixing in both near and far fields. Our proposed workflow marks a key advancement towards standardization of seismic-derived ocean mixing rates and holds the potential to unlock massive marine seismic reflection dataset worldwide for ocean mixing characterization.

1. Introduction

Ocean turbulence is a fundamental process in transferring momentum and energy between different water masses, facilitating exchanges between the ocean's surface and its depths, thereby maintaining the global overturning circulation. The breaking of internal waves, which irreversibly mixes water across density gradients, serves as the primary driver of turbulence. Observing, analyzing, and modeling turbulent mixing is crucial to understand and predict regional and global climate (MacKinnon et al., 2017). It is widely accepted that an average diapycnal diffusivity (K_ρ) of $10^{-4} \text{ m}^2 \text{ s}^{-1}$ is required to close the global mixing budget (Munk and Wunsch, 1998), yet observations in the open ocean thermocline suggest values one order of magnitude lower (Waterhouse et al., 2014), implying the existence of mixing hotspots elsewhere. Through decades of observations, studies have discovered that enhanced mixing is

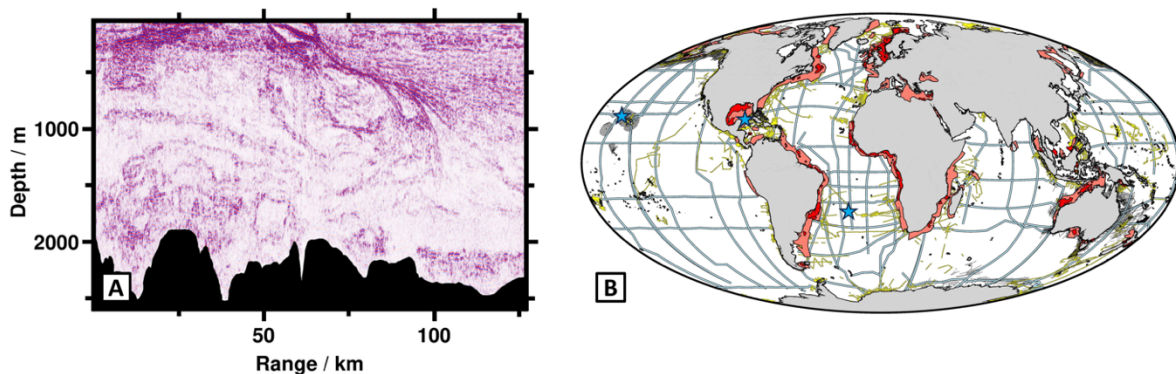
53 mostly concentrated under storm tracks (Whalen et al., 2018), along continental margins
54 (Moum et al., 2002; Alford and Munk, 2019), and in the vicinity of complex topography (Polzin
55 et al., 1997; Ledwell et al., 2000). The geography of mixing hotspots reveals that the energy
56 input into the internal wave field primarily comes from tides and winds (Waterhouse et al.,
57 2014).

58 The conversion of external energy into the internal wave continuum is a complex process.
59 Internal tides are transformed from barotropic tidal currents as they flow over topography (St.
60 Laurent et al., 2001); ocean currents or eddies impinging on small-scale topographic features
61 generates lee waves (Bell Jr, 1975); storms disturbing the base of mixed layer excites near-
62 inertial waves (Gill, 1984; D'Asaro, 1985). All these processes produce internal waves with a
63 wide spectrum of spatial scales and frequencies that can be decomposed into orthogonal modes
64 (Gill, 1982). Low mode internal waves that have larger vertical scales can propagate across
65 ocean basins with larger group velocities (Alford, 2003), whereas high mode internal waves
66 with smaller vertical scales tend to transfer energy near their generation sites (Polzin et al.,
67 1997). The interaction among waves of different modes and their interactions with topography
68 can cascade energy to smaller scales, ultimately leading to energy dissipation through shear
69 and convective instabilities (Whalen et al., 2020). This continually evolving internal wave field
70 leads to prominent spatio-temporal variability of ocean turbulence, which poses a substantial
71 challenge for existing observation efforts to picture a comprehensive, global mixing pattern
72 (Waterhouse et al., 2014; Whalen et al., 2020). In the meantime, climate research calls for
73 increasing observations on the intermittency of turbulence to reduce uncertainties during
74 simulations (Melet et al., 2016; MacKinnon et al., 2017).

75 The past several decades has witnessed significant progress in observing ocean turbulence,
76 yet further advancements are needed. Vertical microstructure profilers equipped with fast-
77 response thermistors and shear probes are used to directly sample isotropic turbulence on length
78 scales as small as $\sim O(1)$ mm (Schmit et al., 1988; Lueck et al., 2002). Such instruments require
79 sophisticated ship-based operations. To complement existing platforms, microstructure sensors
80 have been installed on autonomous underwater gliders (Peterson and Fer, 2014; Palmer et al.,
81 2015; Rainville et al., 2017), and technological development is paving the way for their
82 potential installation on Argo floats (Roemmich et al., 2019). Nevertheless, direct
83 measurements of mixing remain scarce and are insufficient to constrain the global distribution
84 of turbulence. To address this challenge, fine-scale parametrization has been proposed, which

85 infers the strength of turbulence from internal wave shear or strain spectra on larger vertical
86 length scales of $\sim O(1-10)$ m (Gregg, 1989; Polzin et al., 2014). Using conductivity-
87 temperature-depth (CTD) profilers and Argo floats, fine-scale parametrization has revealed
88 reasonable global distribution of turbulent mixing (Whalen et al., 2012; Kunze, 2017; Whalen
89 et al., 2018). However, it has been difficult to benchmark the results of fine-scale
90 parametrization against direct measurements of turbulence due to inconsistent spatio-temporal
91 scales between the two methods (Whalen, 2021). Additionally, more assumptions being
92 adopted by the fine-scale parametrization also lead to larger uncertainties (Polzin et al., 2014).

93 Recently, mixing rates have been derived from seismic reflection images by analyzing
94 horizontal internal wave spectra on scales of $> O(10)$ m, either directly from the turbulence
95 subrange, or from the internal wave subrange through fine-scale parametrization (Sheen et al.,
96 2009; Holbrook et al., 2013). This method, usually referred to as reflection slope spectra, is
97 one of the research branches of a nascent field known as Seismic Oceanography (SO). SO is
98 an acoustic technique that uses marine seismic reflection surveys to remotely sense the small
99 fluctuations of temperature and salinity, whereby producing high-resolution thermohaline fine
100 structures across the entire water column at spatial resolutions of $\sim O(10)$ m (Fig. 1A)
101 (Holbrook et al., 2003). The current development of SO and its distinctive features compared
102 to other observations have been comprehensively reviewed by Dickinson and Gunn (2022).



103

104 Fig. 1. (A) An example of seismic oceanographic image showing oceanic front at Brazil-
105 Malvinas Confluence. Red colors = positive acoustic amplitudes; blue colors = negative
106 acoustic amplitudes; black region = seafloor. (B) Global coverage of legacy marine reflection
107 seismic data. Dark red polygons = regions covered by three-dimensional surveys acquired by
108 seismic exploration companies; thin black lines = publicly available two-dimensional surveys
109 acquired by seismic exploration companies in other regions; yellow lines = publicly available
110 two-dimensional surveys acquired by research institutions; light blue lines = hydrographic
111 transects of World Ocean Circulation Experiment; blue stars = locations of seismic data used
112 in this study. (A) and (B) are adapted from Fig. 2D and Fig. 4A of Dickinson and Gunn (2022),
113 respectively.

114

115 SO has been used to map the spatial distribution of turbulent mixing in diverse
116 environments, including continental margins (Falder et al., 2016; Fortin et al., 2016; Dickinson
117 et al., 2017); ocean ridges (Tang et al., 2021; Tang et al., 2022), oceanic fronts and mesoscale
118 eddies (Tang et al., 2020; Gunn et al., 2021), open ocean interior (Wei et al., 2022) and the
119 Arctic Ocean (Yang et al., 2023). All these studies utilized legacy seismic data acquired by
120 energy industries and academic institutes over the past several decades (Here, we define
121 “legacy” as seismic surveys designed to image the solid Earth instead of the water column).
122 These data exist in abundance, spread across the globe, and can be utilized without incurring
123 additional acquisition expenses (Fig. 1B). For example, Dickinson and Gunn (2022) estimated
124 > 6.3 million km^2 of two-dimensional seismic data and > 5.5 million km^2 of three-dimensional
125 seismic data from five major exploration companies. Exploring legacy seismic data has the
126 potential to yield an unparalleled catalogue of horizontal wavenumber spectra, offering an
127 opportunity to address some fundamental knowledge gaps in downscale energy cascade (Falder
128 et al., 2016; Sallares et al., 2016).

129 Despite SO’s huge potential, several challenges have prevented the method from being
130 accepted by the broader oceanographic community. First, the method lacks a consistent and
131 reliable way to process seismic data, which introduces uncertainties to subsequent analysis.
132 Second, the derived diffusivities have not been benchmarked against direct measurements. To
133 address these problems, a deeper understanding of how seismic data processing impacts
134 spectral analyses and the derived diffusivities is imperative.

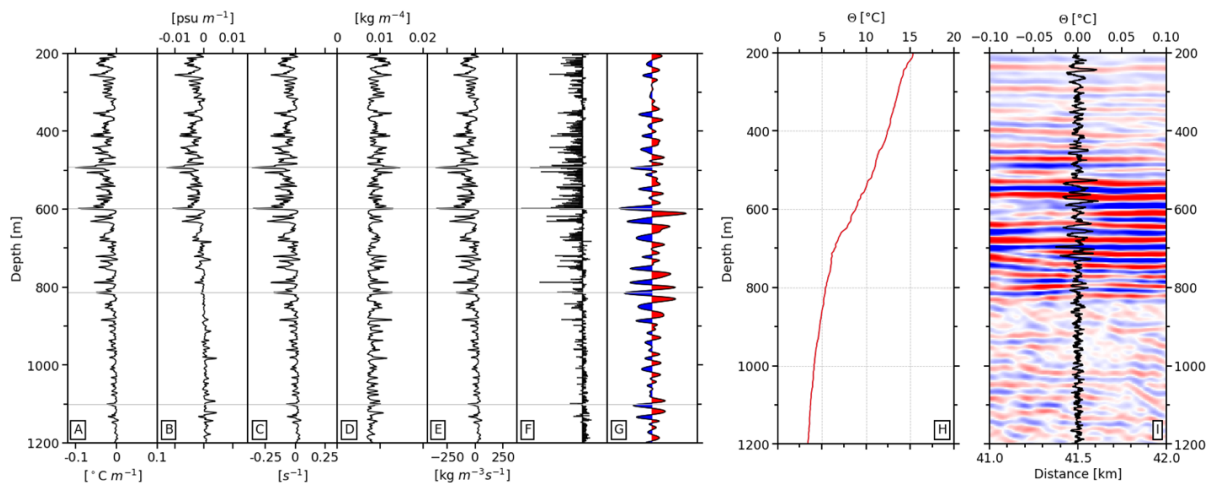
135 Here, we begin by briefly reviewing the principles and current practices used in deriving
136 diapycnal diffusivities from seismic reflection data. We then delve into the immediate
137 challenges encountered in seismic data processing of water column reflections, particularly
138 discussing the issue of low signal-to-noise (S/N) ratios of legacy seismic data. We further
139 demonstrate the susceptibility of reflection slope spectra to noise contamination using a full-
140 wavefield synthetic modeling dataset and propose a workflow to mitigate the low S/N ratio
141 problem. To validate this workflow, we conduct tests on three seismic field datasets
142 characterized by increasing noise levels. These datasets were acquired using different
143 acquisition systems and collected from regions of different turbulence environments: ocean
144 ridges, open ocean interior, and continental slope. The derived diapycnal diffusivities are
145 benchmarked against direct measurements from the Brazil Basin Tracer Release Experiment

146 (BBTRE) and the Hawaii Ocean Mixing Experiment (HOME) (Polzin et al., 1997; Rudnick et
 147 al., 2003). Through these efforts, our work marks a key advancement toward standardization
 148 of the reflection slope spectra method, and thereby holds the potential to unlock massive marine
 149 seismic dataset worldwide for ocean mixing research.

150 2. Overview of seismic-derived turbulence mixing rates

151 a. Seismic images of the ocean

152 Ocean thermohaline fine-structures can be detected by repeat sampling of consecutive
 153 spatial points, e.g., common midpoints (CMP), in the water column by an acoustic source at
 154 the ocean surface, e.g., an air-gun. As the emitted signals travel downward and encounter
 155 acoustic impedance interfaces, they are reflected, traveling back upward, and are received by
 156 a linear array of hydrophones, e.g., a streamer. Acoustic impedance is defined as a product of
 157 density with sound speed in a subsurface medium, which is related to the changes of
 158 temperature and salinity between water masses. Vertical gradients of temperature and salinity
 159 cause vertical contrasts in acoustic impedance which produce reflection coefficients, and the
 160 recorded signals are the reflection coefficients convolved with the acoustic source (Fig. 2).
 161 Thus, seismic reflection surveying provides maps of the vertical gradients of temperature and
 162 salinity, at a scale smoothed by the wavelength of the acoustic source (Ruddick et al., 2009),
 163 which is usually around $O(10)$ m. Holbrook et al. (2013) show that seismic reflections can
 164 faithfully reproduce isopycnal displacements in a turbulent ocean.



165

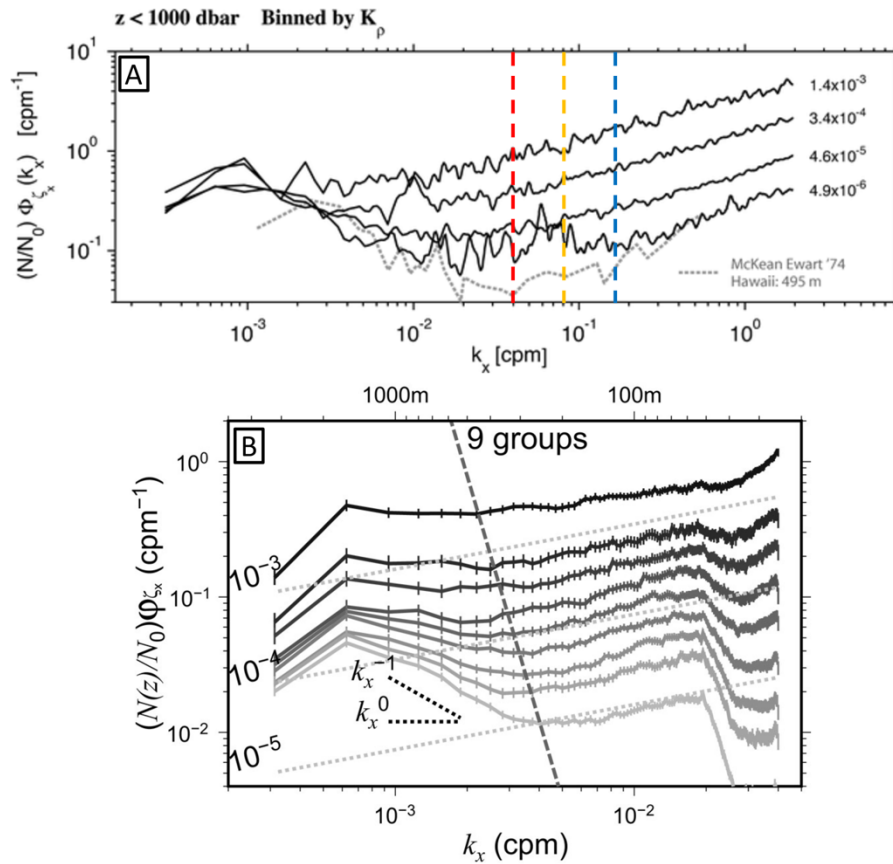
166 Fig. 2. Vertical gradients of (A) temperature, (B) salinity, (C) sound speed, (D) density, (E)
 167 acoustic impedance, and their corresponding reflection coefficients (F). A synthetic
 168 seismogram (G) is produced by convolving (F) with a Ricker wavelet. Horizontal grey lines
 169 mark the similarities between gradients and synthetic seismogram. The last two panels show

170 correlation between concurrent XBT and seismic data from the South Atlantic. (H) XBT
171 measured temperature, (I) short wavelength temperature gradients (black line) of the profile in
172 (H) overlie on the seismic section surrounding the collection location of the XBT. Note the
173 correspondence between seismic amplitudes and temperature gradients.

174

175 *b. Reflection slope spectra*

176 The reflection slope spectra refer to the spectral analysis of vertical displacements of
177 tracked seismic reflections, based on the assumption that seismic reflections follow isopycnals
178 (Krahmann et al., 2009; Holbrook et al., 2013). The basis of this technique is rooted from the
179 horizontal thermistor tow experiments by (Klymak and Moum, 2007a, 2007b), who showed
180 that horizontal isopycnal slope spectra exhibit two distinct subranges that correspond to internal
181 wave and turbulence, each has a slope of $-1/2$ and $+1/3$ in log-log space, respectively (Fig. 3A).
182 Moreover, turbulence subrange can extend to surprisingly low wavenumbers, equivalent to
183 horizontal scales exceeding ~ 500 m (Klymak and Moum, 2007b), far beyond the Ozmidov
184 length scale (10^{-2} - 10^0 m) where isotropic turbulence starts to dominate (Kolmogorov, 1941;
185 Corrsin, 1951; Batchelor et al., 1959). This discovery can be explained by observations and
186 simulations indicating the existence of a regime known as layered anisotropic stratified
187 turbulence (LAST) (Falder et al., 2016). LAST shares the same nonlinear downscale energy
188 cascade as isotropic turbulence and occupies the horizontal scales between internal waves (10^2 -
189 10^3 m) and the Ozmidov length scale (Lindborg, 2006; Klymak and Moum, 2007b; Riley and
190 Lindborg, 2008; Kunze, 2019; Caulfield, 2021).



191

192 Fig. 3. Slope spectra produced by microstructure and seismic measurements. (A) Average
 193 isopycnal slope spectra derived from the Hawaii Ocean Mixing Experiment (HOME). Spectra
 194 are binned in one-decade bins of the turbulent diffusivity estimated from shear probe (adapted
 195 from Fig. 3 of Klymak and Moum (2007b)). Red, yellow, and blue dashed lines mark the
 196 Nyquist wavenumbers of 0.04, 0.08 and 0.16 that are visible to seismic reflection surveys using
 197 receiver spacings of 25 m, 12.5 m, and 6.25 m, respectively (corresponding to CMP spacings
 198 of 12.5 m, 6.25 m, and 3.125 m). The observable wavenumber ranges suggest that the LAST
 199 regime is easily resolved by modern seismic acquisition systems. (B) Average seismic
 200 reflection slope spectra derived from seismic data using receiver spacing of 25 m around the
 201 Island of Taiwan. Spectra are decomposed by energy level in the turbulence subrange for
 202 increments of 0.15 logarithmic units. Vertical black bars represent 95% confidence interval.
 203 The dashed gray line shows the migration of the crossover between internal wave and
 204 turbulence subrange with respect to spectra energy level. Dotted gray lines in show spectral
 205 levels for K_ρ of 10^{-3} , 10^{-4} , and 10^{-5} $\text{m}^2 \text{s}^{-1}$ (after Fig. 5d of Tang et al. (2022)).

206

207 As the horizontal scales of internal waves and LAST are easily resolved by seismic
 208 reflection images (Fig. 3), Sheen et al. (2009) presented the first study to estimate turbulent
 209 mixing rates from both internal wave and turbulence subranges of reflection slope spectra. The
 210 inference of turbulence from the internal wave subrange follows a modified fine-scale
 211 parametrization approach which is an indirect estimate of turbulence and is not discussed in
 212 this study (e.g., Klymak and Moum (2007a); Dickinson et al. (2017)). In contrast, the

213 turbulence subrange that represents LAST is related to isotropic turbulence through energy
 214 cascade and provides an opportunity to directly measure turbulent dissipation ε by fitting to the
 215 Batchelor model (Batchelor et al., 1959):

$$216 \quad \varphi_{\zeta_x}^T = \frac{4\pi\Gamma}{N^2} C_T \varepsilon^{2/3} (2\pi k_x)^{1/3} \quad (1)$$

217 where $\Gamma = 0.2$ is the empirical mixing efficiency (Osborn and Cox, 1972), N is buoyancy
 218 frequency, $C_T = 0.4$ is the Kolmogorov constant, and k_x is horizontal wavenumber. Diapycnal
 219 diffusivity, K_ρ , is then calculated using the Osborn relationship (Osborn, 1980):

$$220 \quad K_\rho = \Gamma \varepsilon / N^2 \quad (2)$$

221 Dickinson et al. (2020) and Tang et al. (2021) have assessed the uncertainties of seismically
 222 derived diffusivities. The major uncertainty comes from the fitting of the slope spectrum to the
 223 Batchelor model, which can be represented by the following relations:

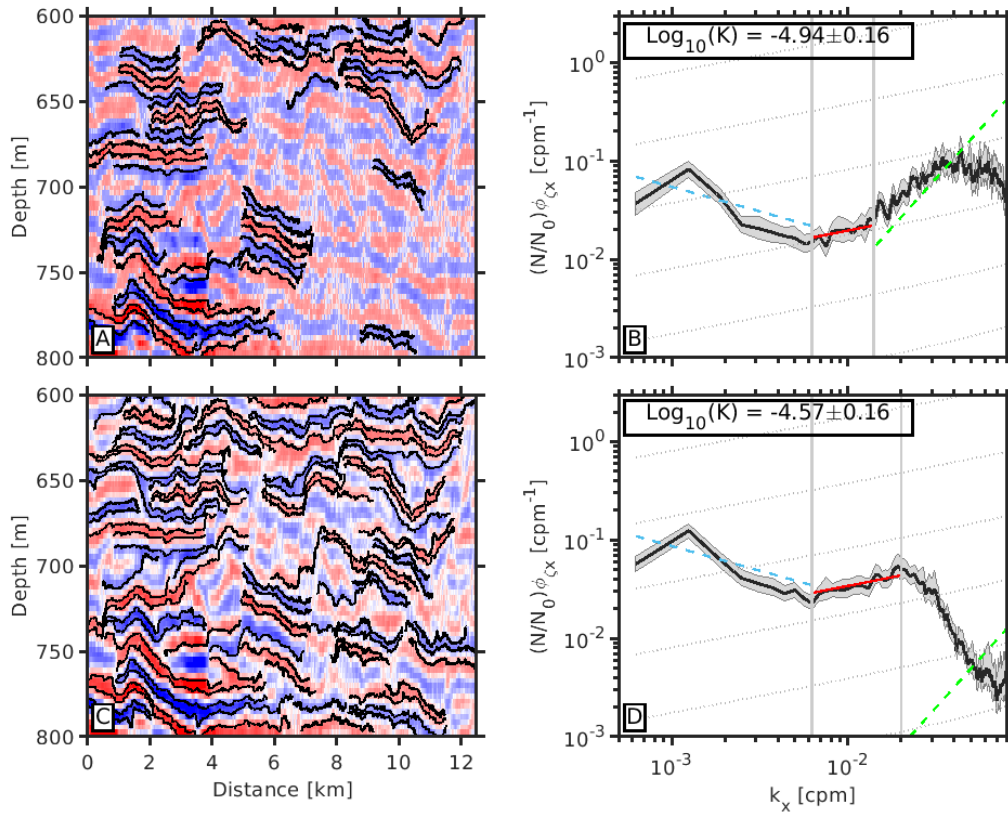
$$224 \quad \begin{cases} b = \frac{1}{M} \sum_{i=1}^M \left(\log_{10} \varphi_{\zeta_x,i}^T - \frac{1}{3} \log_{10} k_{x,i} \right) \\ \varepsilon(b) = \frac{N^3}{4\pi^2} \left(\frac{10^b}{2C_T\Gamma} \right)^{3/2} \\ \sigma_b = \left[\frac{1}{M} \sum_{i=1}^M \left(\log_{10} \varphi_{\zeta_x,i}^T - \frac{1}{3} \log_{10} k_{x,i} - b \right)^2 \right]^{1/2} \\ \varepsilon^\pm = \varepsilon(b \pm \sigma_b) \end{cases} \quad (3)$$

225 Where $\varphi_{\zeta_x,i}^T$ is the slope spectrum value corresponding to wavenumber $k_{x,i}$ within the
 226 turbulence subrange, M is the number of $k_{x,i}$ in the turbulence subrange, b is the intercept of
 227 the fitted straight line in $\log_{10}(k_x) - \log_{10}(\varphi_{\zeta_x,i}^T)$ space, σ_b is the standard deviation of the
 228 residual fitting, $\varepsilon(b)$ represents dissipation rates as a function of b , and ε^\pm means the upper and
 229 lower bounds of dissipation rates corresponding to $b \pm \sigma_b$. Other uncertainties come from the
 230 choices of N , C_T , and Γ . Both the Kolmogorov constant $C_T = 0.4$ and the mixing coefficient Γ
 231 $= 0.2$ will introduce uncertainties of ~ 0.15 logarithmic units in $\log_{10}(K_\rho)$ by taking the upper
 232 and lower bounds of their observed ranges of $C_T \in [0.3, 0.5]$ and $\Gamma \in [0.1, 0.4]$, respectively.
 233 The uncertainties introduced by N are minor and subject to change dependent on local
 234 hydrographic conditions. In this study, we follow this criterion and uncertainties from each
 235 contributing factors are specified in section 5.1.

236 The isopycnal slope spectra of Klymak and Moum (2007b) and reflection slope spectra
237 share similar characteristics. First, the rise and fall of spectra energy levels with respect to
238 turbulent mixing rates is evident in both spectra (Fig. 3). Second, the crossovers between
239 internal wave and turbulence subranges in both spectra migrate to lower wavenumbers as
240 spectra energy increase, indicating LAST extending to greater horizontal scales where stronger
241 internal waves propagate (Fig. 3). These similarities support the reliability of reflection slope
242 spectra in capturing the intensity of internal waves and turbulence. Therefore, this technique
243 has been frequently used to study turbulent mixing in various environments (Song et al., 2021).
244 However, different from thermistor tow measurements, seismic imaging does not directly
245 measure temperature variations. It requires a series of data processing to convert the acoustic
246 signals to final seismic images. Uncertainties can rise from noise contamination and different
247 seismic processing techniques being used, and eventually propagate into the derived turbulent
248 mixing rates. Here we examine this long-standing issue and propose a generic solution for
249 future applications.

250 *c. Data preparation*

251 Seismic Oceanography needs meticulous data processing as the seismic reflectivity of the
252 water column is about 10^2 - 10^3 times weaker than the solid Earth. Therefore, special care is
253 needed to minimize the effect of noise in modifying the shapes and energy levels of the
254 reflection slope spectra. For example, Holbrook et al. (2013) systematically explored how noise
255 can affect slope spectra analysis. First, they found that the harmonic noise, stemming from the
256 periodic change of seismic amplitudes due to the move-up rate of the seismic acquisition, i.e.,
257 the number CMPs generated per shot, can create a spurious turbulence subrange. Second, they
258 discussed the significance of S/N ratio and proposed the application of a band-pass filter for
259 random noise attenuation. Subsequent studies have generally followed this workflow to derive
260 diapycnal diffusivities (Falder et al., 2016; Fortin et al., 2016; Dickinson et al., 2020; Tang et
261 al., 2020). Yet, band-pass filter is usually insufficient for effectively suppressing random noise
262 (Fig. 4A). Noise that shares the same frequency range with reflections can persist. In particular,
263 this workflow overlooks an important source of noise in seismic oceanography: previous shot
264 multiples.



265

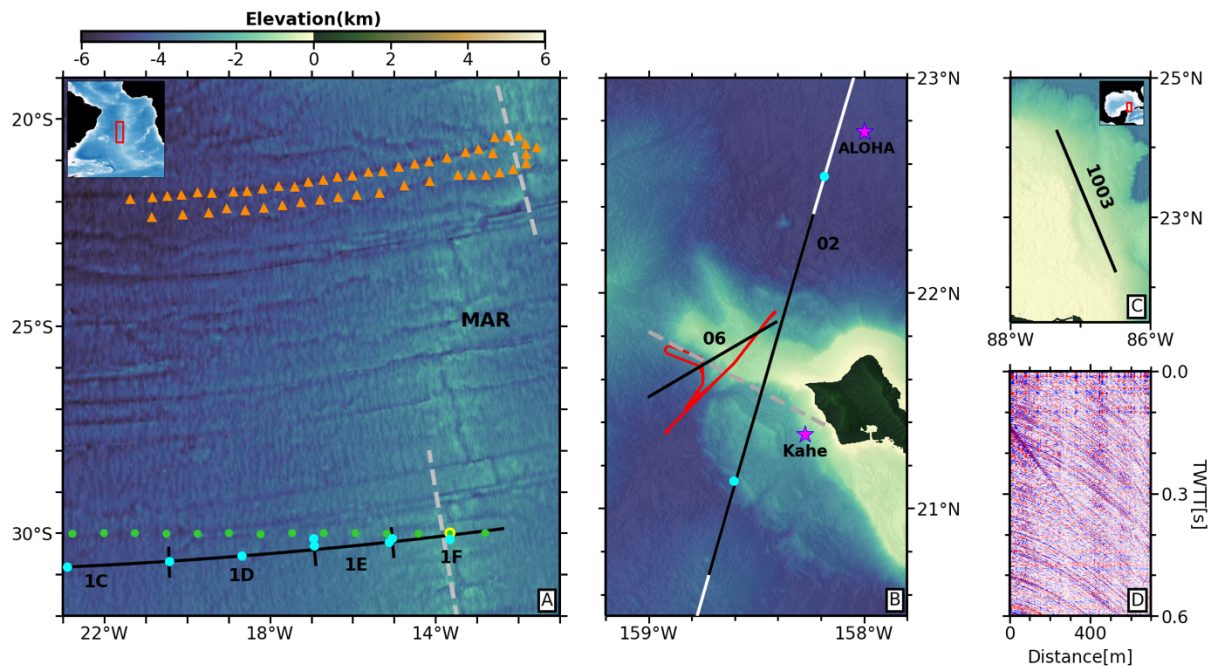
266 Fig. 4. Example spectra analysis of legacy marine seismic data at the Hawaiian Ridge (Fig.
 267 5B). (A) Tracked reflections overlay on band-pass filtered seismic data with S/N ratio of 5.5,
 268 satisfied the criterion of S/N ratio of 4 by Holbrook et al. (2013). (B) Average reflection slope
 269 spectrum calculated from tracked reflections in (A). (C) Same data in (A) but smoothed by a
 270 Gaussian filter with standard deviation of 1. (D) Average reflection slope spectrum calculated
 271 from tracked reflections in (C). Shaded gray area = 95% bootstrap confidence intervals. Dashed
 272 blue lines ($k_x^{-1/2}$), solid red lines ($k_x^{1/3}$) and dashed green lines (k_x^2) = the internal wave subrange,
 273 turbulence subrange and white noise, respectively (Garrett and Munk, 1975; Klymak and
 274 Moum, 2007b; Holbrook et al., 2013). Dashed gray lines = slopes of +1/3 corresponding to
 275 diffusivities increasing by one order of magnitude from 10⁻⁷ to 10⁻² m² s⁻¹. Two vertical gray
 276 lines bound the turbulent subrange used to calculate diffusivity. The calculated diffusivities
 277 and their uncertainties are shown in the upper left corner. In this example, uncertainties only
 278 account for errors in buoyancy frequency and straight-line fitting.

279

280 Previous shot multiples are strong reverberations bouncing between the seafloor and the
 281 sea surface generated by previous shots. Their appearances in the acoustic records are functions
 282 of ocean depth, shot spacing and seafloor composition. Deeper ocean depths, smaller shot
 283 spacing, and harder seafloors (higher reflection coefficient) favor the generation of previous
 284 shot multiples (Fig. 5D). They overprint water column reflections as coherent noise with
 285 inconsistent arrival times across shot gathers but become “random” after CMP sorting and
 286 stacking. However, due to their strong amplitudes relative to reflections from water column
 287 arrivals, stacking is not sufficient to suppress them. This issue is particularly problematic for

12

288 legacy marine seismic data whose acquisition geometry were originally designed to image the
289 solid Earth.



290

291 Fig. 5. (A) Bathymetric map of the central South Atlantic where the CREST seismic survey
292 and the BBTRE microstructure profilers were collected. Black lines = CREST seismic lines;
293 green dots = CTD casts from GO-SHIP survey, the one with yellow edge is used to build the
294 synthetic turbulence model in section 4.1; cyan dots = XBTs collected during the seismic
295 survey; orange triangles = locations of BBTRE profilers; dashed grey lines = mean axes of the
296 local mid-ocean ridges. (B) Bathymetry map of the Kauai Channel. Black lines = seismic lines
297 02 and 06 acquired by the Hawaii Experiment, white line = remaining portion of line 02 (not
298 used); red line = trajectory of the Marlin tow by HOME; cyan dots = XBTs coincident with the
299 seismic survey; purple stars = Kahe and ALOHA stations maintained by the Hawaii Ocean
300 Time-series project; dashed grey lines = along ridge direction by Klymak et al. (2006). (C)
301 Bathymetry map of the eastern Campeche Bank. Black line = seismic line 1003 acquired by
302 the Campeche Experiment. (D) Example of a band-pass filtered shot gather from the (C)
303 showing a series of strong, successive previous shot multiples. Insets show large scale
304 geography, with red boxes marking the locations of the study areas. Bathymetry data is from
305 the Global Multi-Resolution Topography Synthesis (Ryan et al., 2009).

306

307 Without proper noise attenuation, the turbulence subrange of the slope spectra will be
308 dominated by noise (Fig. 4A, 4B), some might not exhibit a turbulence subrange at all. For
309 legacy seismic data, this implies that certain sections of a seismic line may be suitable for slope
310 spectra analysis while others may not (Holbrook et al., 2013). This issue is usually mitigated
311 by applying a smoothing filter on the final seismic image before slope spectra analysis (Fig.
312 4C, 4D), as adopted by Holbrook et al. (2013), Fortin et al. (2017), and Tang et al. (2020).
313 Although smoothing can recover turbulence subrange, it is a crude approach that affects the

314 true amplitudes of the seismic reflections and remove the high wavenumber contents of the
315 slope spectra, creating spectra roll-off that adversely affect the fitting accuracy of turbulence
316 subrange (Figs. 3B, 4B). Most importantly, the derived diffusivities are subjected to change
317 before and after smoothing (Fig. 4B, 4D), implying uncontrollable uncertainties are introduced
318 during this process. Therefore, it is vital to investigate this problem and develop a standard way
319 to derive turbulent mixing rates, minimizing uncertainties during seismic data processing.

320 **3. Data**

321 *a. Seismic data and processing*

322 A standardized strategy requires universal application to different types of datasets. In this
323 study, we explore two popular seismic acquisition systems that are widely used in both
324 academic and industry. The first system comprises a low frequency (e.g., 5-120 Hz) air-gun
325 array as the acoustic source and a long hydrophone streamer (e.g., 6-15 km), usually with 12.5-
326 m receiver spacing, as the recording cable. The powerful source and wide recording aperture
327 enable imaging of deep subsurface structures such as ocean crust, ridges, seamounts and
328 subduction zones (Gulick et al., 2008; Gulick et al., 2013; Shillington et al., 2015; Estep et al.,
329 2019; Carbotte et al., 2020). These types of surveys are carried out on specialized research
330 vessels equipped with this kind of system, like the R/V *Marcus G. Langseth* in the US
331 Academic Research Fleet who has been collecting high-quality seismic data around the globe.

332 The second system uses high frequency (e.g., 40-300 Hz) Generator-Injector (GI) air-gun
333 and a relatively short hydrophone streamer (e.g., 75-2000 m) with 3.125- or 6.25-m receiver
334 spacing depending on different configurations. The high frequency bandwidth produces high-
335 resolution images of the subsurface that can be used to study the detail stratigraphy of
336 sediments (Lowery et al., 2024b) or storage of methane hydrates (Serov et al., 2017). The
337 portability of the GI gun system facilitates its deployment across vessels of different sizes and
338 alongside with other oceanographic sensors, making it a promising system for future dedicated
339 seismic oceanographic cruises (Ruddick, 2018).

340 In this study, we derive diapycnal diffusivities from three seismic datasets collected by the
341 acquisition systems mentioned above during three independent scientific cruises in regions of
342 different turbulence levels:

- 343 1) The Crustal Reflectivity Experiment Southern Transect (CREST) experiment, conducted
344 between January and February of 2016 aboard the R/V *Marcus G. Langseth* (Reece and

345 Christeson, 2017). The primary goal of the CREST survey was to investigate the
 346 evolution of oceanic crust at 30° S. The survey spans the eastern edge of the Rio Grande
 347 Ridge to the Mid-Atlantic Ridge, including a 1,600-km-long continuous east-west data
 348 transect (Fig. 5A). Diffusivities derived from this dataset are compared with the Brazil
 349 Basin Tracer Release Experiment (BBTRE) as they both span from the Mid-Atlantic
 350 Ridge to the ocean interior (Polzin et al., 1997) (Fig. 5A).

351 2) The Hawaiian-Emperor Seamount Chain Seismic Experiment (Part 1) (hereafter, Hawaii
 352 Experiment), also carried out by R/V *Marcus G. Langseth* from September to October
 353 2018 around the Hawaiian Islands (Shillington et al., 2019) (Fig. 5B). The cruise
 354 objective was to examine controls on magmatic addition along the Hawaiian-Emperor
 355 seamount chain, to provide fundamental constraints on rheological properties of oceanic
 356 lithosphere (Watts et al., 2021). We only use two seismic lines from this survey collected
 357 within the Kauai Channel because they were collocated with the Marlin tow
 358 microstructure measurements by the Hawaii Ocean Mixing Experiment (HOME)
 359 (Klymak et al., 2006) (Fig. 5B).

360 3) The Campeche Bank Stratigraphy Seismic Experiment (hereafter, Campeche Experiment)
 361 took place onboard the R/V *Justo Sierra* in July 2022 (Lowery et al., 2024a), using the
 362 Scripps Institute of Oceanography’s high-resolution portable multichannel seismic
 363 system (Fig. 5C). Its purpose was to map the history of the sediment drift on the eastern
 364 Campeche Bank to study the stratigraphic expression of the Loop Current (Lowery et al.,
 365 2024b). The water column data of this survey were severely contaminated by previous
 366 shot multiples due to short shot spacing (Fig. 5D). Thus, these data provide an opportunity
 367 to test the applicability of the proposed processing sequence on very noisy dataset.

368 Seismic data were processed following a traditional seismic oceanographic procedure for
 369 turbulence analysis (Holbrook et al., 2013): geometry definition, direct arrival removal, noise
 370 attenuation, CMP sorting, velocity analysis, stacking, amplitude correction, migration, and
 371 harmonic noise suppression. As will show in the following sections, this processing flow is not
 372 sufficient to accurately derive diffusivities from seismic data and so an additional processing
 373 step, the F-K filter, was applied. Detailed acquisition and processing parameters of the three
 374 surveys are shown in Table 1.

Survey	CREST Experiment	Hawaii Experiment	Campeche Experiment
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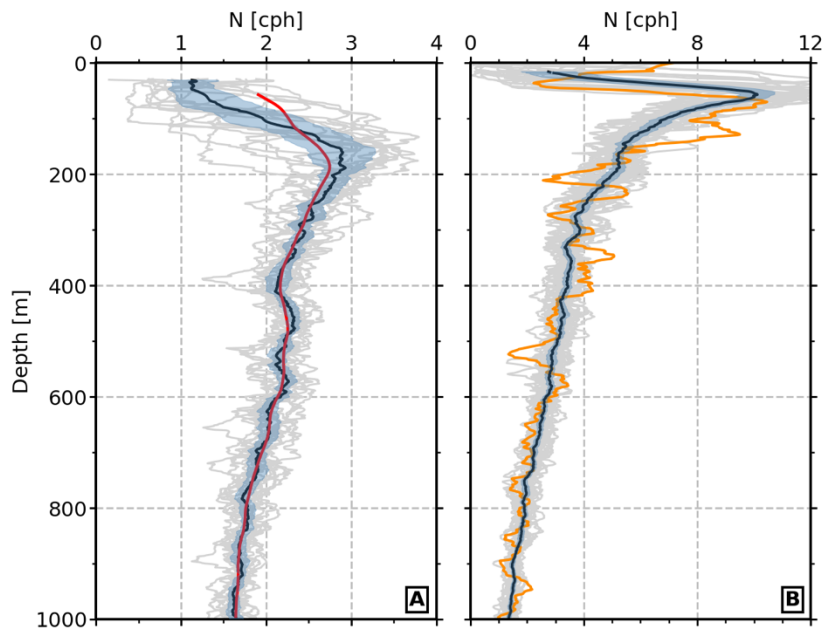
Acoustic source	36 bolt air-gun array with a total volume of 6,600 in ³	36 bolt air-gun array with a total volume of 6,600 in ³	2 GI air-gun array with a total volume of 90 in ³
Shot spacing	37.5 m	62.5 m	12.5 m
Number of receiver channels	1008	1200	120
Channel group spacing	12.5 m	12.5 m	6.25 m
CMP spacing	6.25 m	6.25 m	3.125 m
Channel used	600	600	120
Bandpass filter	30-80 Hz	30-80 Hz	40-320 Hz

375 Table 1. Acquisition and processing parameters of the CREST, Hawaii, and Campeche
376 experiments.

377

378 *b. Hydrographic data*

379 The derivation of diapycnal diffusivity requires measurements of buoyancy frequency. In
380 the central South Atlantic, the GO-SHIP program collected CTD measurements along the 30°
381 S transect in October 2011 (CCHDO, 2023), which is collocated but not concurrent with the
382 CREST seismic survey (Fig. 5A). From these CTD profiles, we selected 14 profiles that are
383 within the region of analysis and calculate a local mean buoyancy frequency profile for this
384 region using the adiabatic leveling method (Bray and Fofonoff, 1981) (Fig. 6A). Near Oahu,
385 the Hawaii Ocean Time-series (HOT) project maintained by University of Hawaii has been
386 acquiring continuous hydrographic data over the years at stations Kahe and ALOHA (Fig. 5B).
387 We used 26 CTD profiles that were concurrent with the Hawaii seismic experiment collected
388 from September to October 2018 to calculate in-situ buoyancy frequency profiles (Fig. 6B).
389 These depth varying buoyancy profiles, $N(z)$, are used to estimate diapycnal diffusivity for
390 each reflection. We used a constant buoyancy profile of 2.5 cph for the Campeche data because
391 it is used as a test set and there are no direct measurements of turbulence to serve as
392 benchmarks.



393

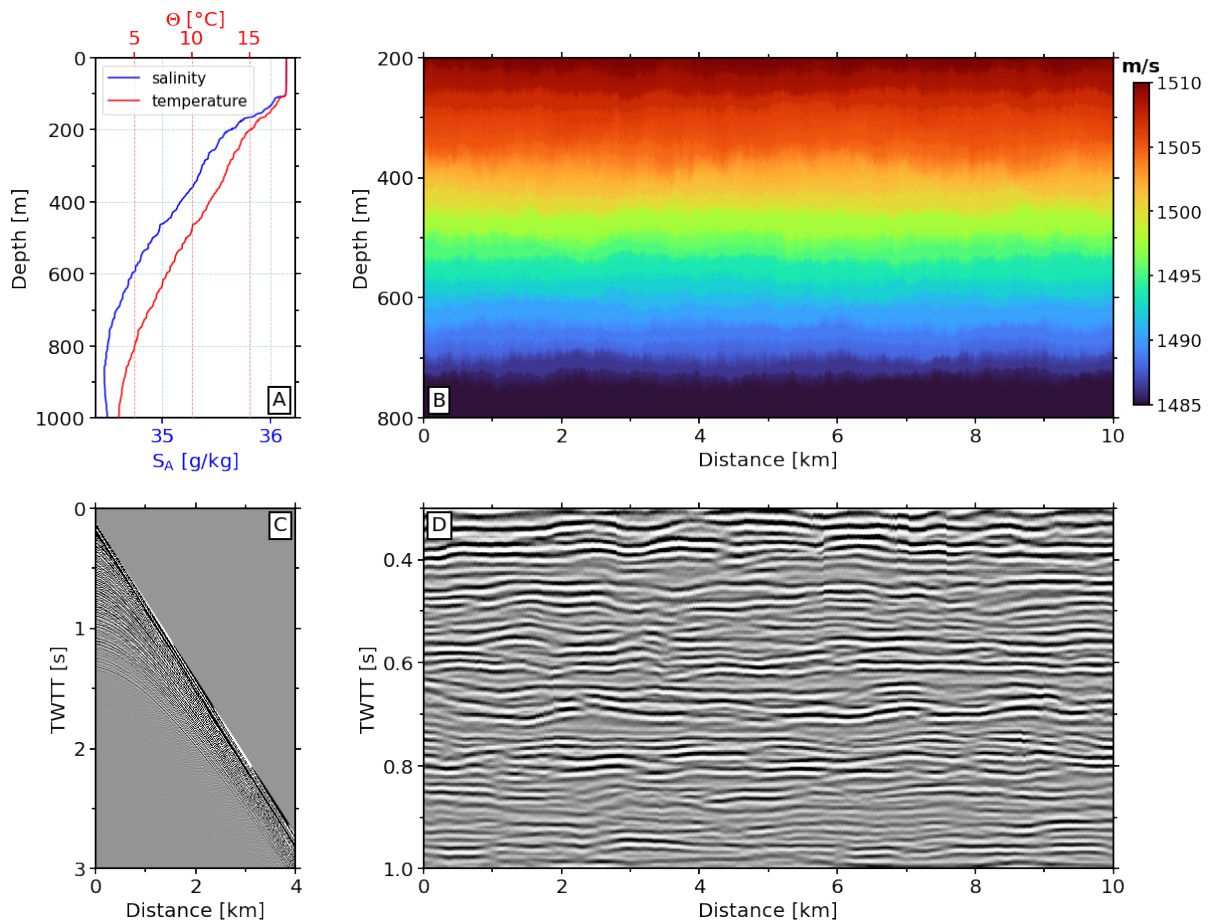
394 Fig. 6. Buoyancy frequency (N) profiles calculated from GO-SHIP CTDs (A) and HOT
 395 CTDs (B). Black lines = average profiles; grey lines = individual profiles; blue shades = 95%
 396 confident interval; red line = local mean profile calculated using the adiabatic leveling method
 397 (Bray and Fofonoff, 1981); orange line = an example profile from station Kahe showing
 398 stratification close to the Oahu Island.

399

400 **4. Susceptibility of reflection slope spectra**

401 *a. Synthetic modeling*

402 To assess how noise and seismic data processing affects the derived diffusivities, we
 403 performed a full-wavefield simulation across a synthetic sound speed and density model
 404 containing spectra characteristics of internal waves and turbulence. The model was created the
 405 same way as Holbrook et al. (2013) by using vertical displacements instead of physical
 406 modeling of fluid dynamics. Internal wave displacements that governed by Garrett-Munk (GM)
 407 spectrum and turbulence that represented by the Batchelor spectrum are independently
 408 programmed into the model (Batchelor et al., 1959; Garrett and Munk, 1975). Sound speed and
 409 density data is calculated from one of the CTD casts of the GO-SHIP A10 survey (Figs. 5A,
 410 7A). We repeated this sound speed and density profile at 2-m intervals for 20 km and displaced
 411 each value by a vertical displacement specified by the GM and Batchelor model. Lastly, the
 412 displaced sound speed and density sections are interpolated onto a constant depth interval of 1
 413 m (Fig. 7B).



414

415 Fig. 7. Full wavefield synthetic modeling. (A) Temperature and salinity profiles from the
 416 GO-SHIP CTD above the Mid-Atlantic Ridge as shown in Fig. 5A. (B) Sound speed section
 417 created using (A) by applying displacement that simulate the spectra characteristics of internal
 418 waves and turbulence. (C) Example of a synthetic shot gather. (D) Final synthetic seismic
 419 section.

420

421 Different from Holbrook et al. (2013) who used “exploding reflector” sources, we did a full
 422 wavefield simulation where seismic waves propagate across the model space. A variable
 423 density and velocity seismic forward modeling engine was used to perform the simulation. We
 424 employed a set of first order differential equations for particle velocity and stress components
 425 (Graves, 1996); and staggered-grid finite difference method was used to numerically solve the
 426 wave propagation with 6th order spatial derivatives and 2nd order temporal derivative.

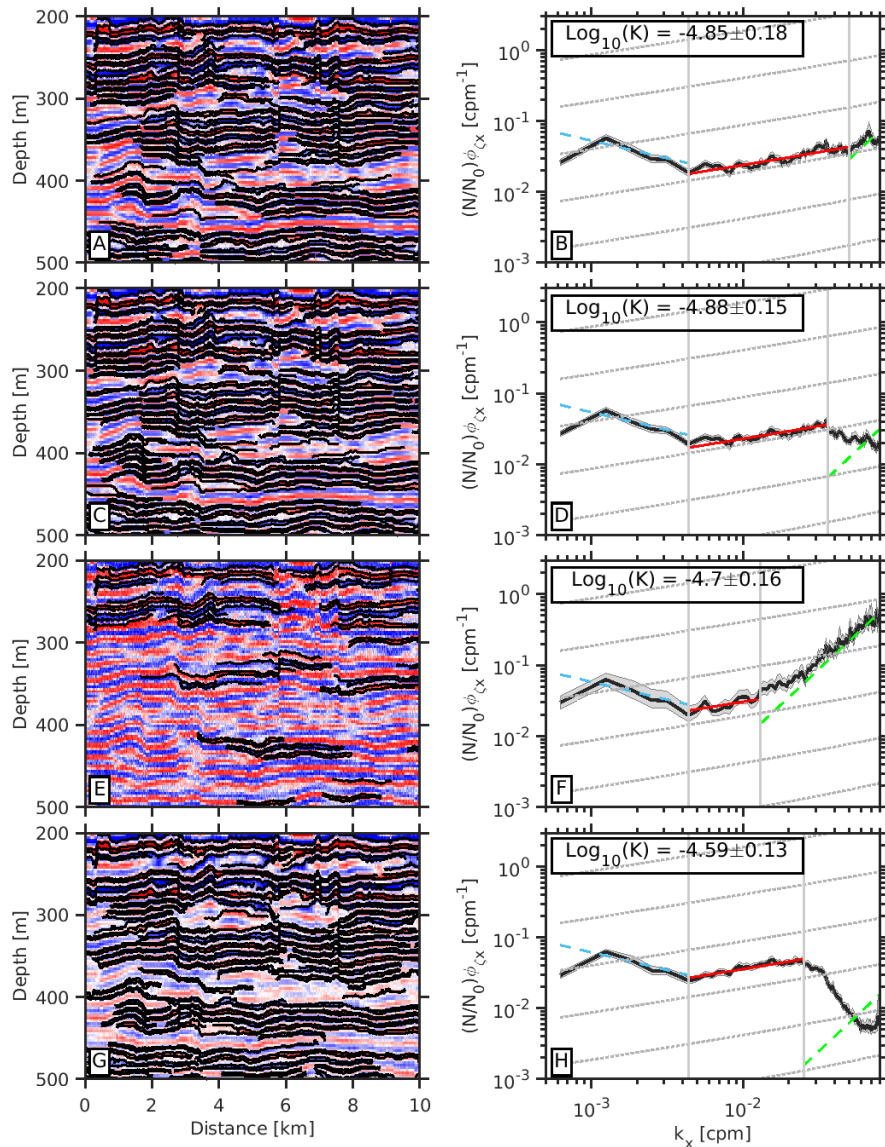
427 We simulated a marine seismic acquisition system with 600 receivers spaced 12.5 m apart
 428 towed on the left side of the shot positions. A very small shot spacing of 6.25 m was used to
 429 increase the horizontal sample rate to capture the non-physical displacements of internal waves
 430 and turbulence in the model space. More realistic physical modeling is needed in the future to
 431 examine the capabilities of normal shot spacing (e.g., 37.5 m in the CREST survey) in detecting

18

432 internal waves and turbulence signatures. A Ricker wavelet with 50 Hz main frequency is used
433 for the wave propagation. Both source and receivers are placed at a depth of 12m below the
434 horizontal sea surface. A total of 1965 shots were simulated with recording length of 4 s and
435 sample interval of 0.5 ms (Fig. 7C). We then carried out pre-stack and post-stack processing to
436 produce a noise free synthetic seismic section. Processing steps includes CMP sorting, velocity
437 analysis, stacking and migration. Velocity analysis was performed on each CMP gather to
438 capture the artificial displacements of internal waves and turbulence. The final seismic section
439 is 10 km long and contains equal levels of turbulence everywhere (Fig. 7D). The synthetic
440 seismic section and shot gathers are used to investigate the effect of noise and data processing
441 on reflection slope spectra.

442 *b. Impact of noise and smoothing filter*

443 As discussed above, noise is an unresolved issue for reflection slope spectra. Moreover, the
444 side-effects of the frequently used smoothing filter have not been well studied. Here, we use
445 the synthetic seismic section (Fig. 7D) to explore these issues by testing four scenarios: (a) the
446 original noise-free synthetic section; (b) smoothed noise-free section: data in (a) are smoothed
447 by a Gaussian smoothing kernel with standard deviation of 0.5; (c) noise-added section, random
448 noise generated by the MATLAB randn function is added to data in (a). (d) smoothed noise-
449 added section, the data in (c) are smoothed using the Gaussian smoothing kernel with standard
450 deviation of 1. We derived diapycnal diffusivities using the average slope spectrum calculated
451 from the tracked reflections of each section (Fig. 8). The results of each scenario are listed
452 below:



453

454 Fig. 8. Demonstration of the noise test on the synthetic seismic section. (A) Noise-free
 455 section with tracked reflections. (B) Average slope spectrum calculated from tracked
 456 reflections in (A). (C-D), (E-F), (G-H) Same as (A-B) but for smoothed noise-free section,
 457 noise-added section, and smoothed noise-added section, respectively. Uncertainties of
 458 diffusivities only account for errors in buoyancy frequency and straight-line fitting. Color
 459 scheme same as in Fig. 4.

460

- 461 a) Noise-free section: the average slope spectrum shows an interval wave subrange with -
 462 1/2 slope and a turbulence subrange with +1/3 slope, the crossover between the two is at
 463 wavenumber 0.004375 cpm (Fig. 8B). A pseudo noise subrange appears at wavenumbers
 464 higher than 0.05 cpm which is caused by the modeling artifact (Fig. 8B).
 465 b) Smoothed noise-free section: The smoothing causes a spectrum roll-off after 0.036 cpm
 466 and slightly lowered the diffusivity by 0.03 logarithmic units from -4.85 to -4.88,

467 comparing with the first scenario (Fig. 8D). Stronger smoothing (e.g., using higher
468 standard deviation) can further erode the turbulence subrange but do not significantly
469 alter the diffusivity values.

470 c) Noise-added section: It is evident that noise disrupts the continuity of seismic
471 reflections, resulting in fewer reflections being tracked and used when calculating the
472 average spectrum (Fig. 8E). In the spectrum, a large portion of turbulence subrange is
473 dominated by noise, creating a noise subrange with +2 slope after 0.013 cpm (Fig. 8F).
474 Notably, the derived diffusivity increased significantly by 0.18 logarithmic units
475 compared with the first case, which is also reflected in the elevation of the energy level
476 of the spectrum.

477 d) Smoothed noise-added section: Smoothing increases S/N ratio and enabled tracking of
478 more reflections (Fig. 8G). A longer turbulence subrange is recovered in the
479 wavenumber range of 0.004375-0.025 cpm (Fig. 8H). The derived diffusivity increases
480 by 0.11 logarithmic units from -4.7 to -4.59 compared with the third case.

481 By comparing results between the four scenarios, the following conclusions can be drawn.
482 First, smoothing filter itself does not significantly change the derived diffusivities except
483 eroding away turbulence subrange at higher wavenumbers. Second, the presence of noise
484 increases the energy level of the spectrum at wavenumbers pertained to turbulence subrange
485 and can lead to overestimation of the derived diffusivity. Lastly, smoothing a noisy dataset
486 worsen the overestimation, likely due to the superposition of spectrum energy that comes from
487 noise onto the spectrum energy from vertical displacements. Therefore, to accurately derive
488 mixing rates from seismic data, it is advisable to suppress noise as much as possible.

489 **5. A spectral solution**

490 *a. F-K filter*

491 Through our investigation into the impact of noise, we find that the weaker the noise the
492 more accurate the derived diffusivities. One of the strongest sources of noise comes from
493 previous shots multiples that have usually been neglected due to their random distribution of
494 arrival times across shot gathers. Although they are added de-constructively during stacking,
495 their high amplitudes relative to water column reflections leave considerable residual noise in
496 the final seismic section. Furthermore, simple frequency filtering failed to remove these

497 multiples since they share the same frequency range with reflections. However, it is possible
498 to separate them in shot gathers prior to stacking.

499 In a geometric sense, without considering higher accuracy at far offsets, a single reflection
500 in a shot gather (time-distance domain) is approximated as a hyperbola:

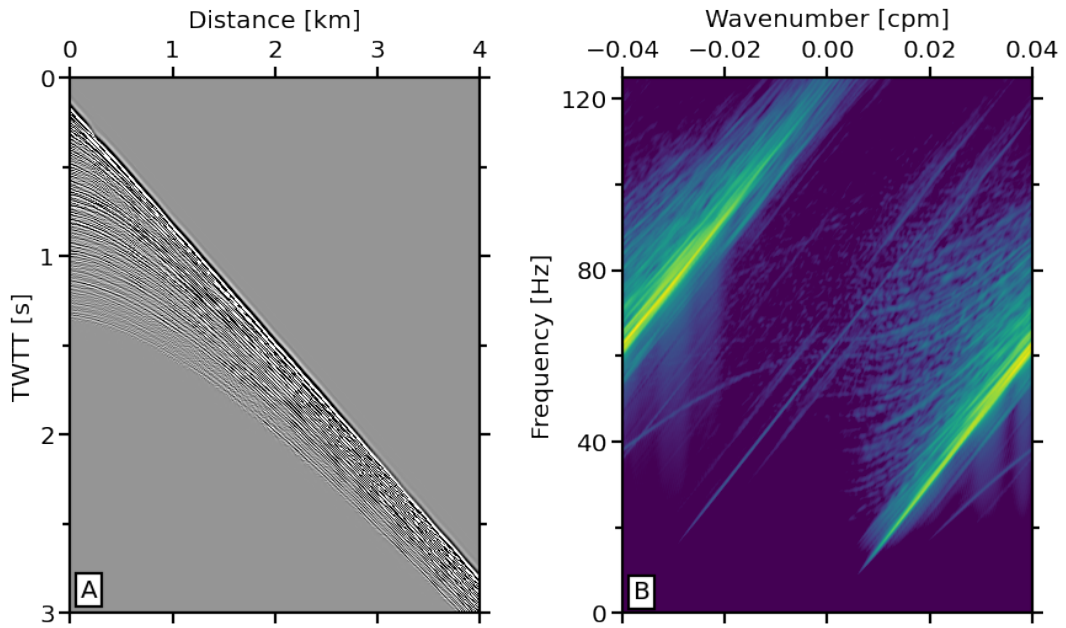
501
$$t^2 = t_0^2 + \frac{x^2}{v^2} \quad (4)$$

502 where t is the reflection traveltime, t_0 is the two-way-traveltime at normal incidence, x is
503 the distance (offset) between the source and receivers, v is the velocity of the medium above
504 the reflecting interface (Yilmaz, 2001). In the meantime, the entire recorded wavefield in a shot
505 gather can be treated as a synthesis of many plane waves with different dips and are separable
506 through two-dimensional Fourier transform:

507
$$F(f, k) = \iint f(t, x) \exp[-j2\pi(ft + kx)] dt dx \quad (5)$$

$$f(t, x) = \iint F(f, k) \exp[j2\pi(ft + kx)] df dk$$

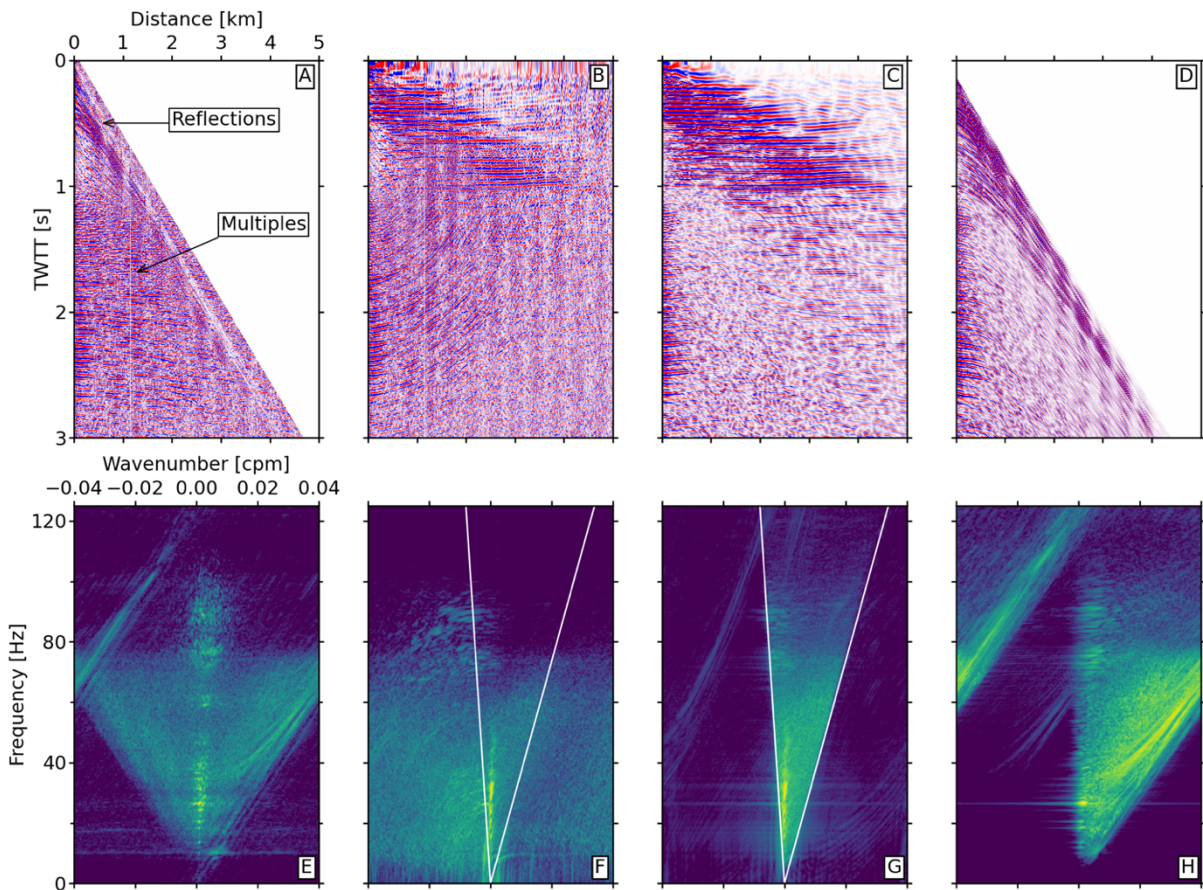
508 where $f(t, x)$ represents time-space domain and $F(f, k)$ represents frequency-wavenumber
509 domain. Seismic events in the two domains can be related through apparent velocities (dips),
510 $V_{app} = dx/dt = df/dk$. In other words, events with the same dip in the $t - x$ domain, regardless
511 of location, are mapped onto a single line in the radial direction in the $f - k$ spectrum (Fig. 9)
512 (Details of 2D Fourier transform in seismic data can be found in Chapter 3 of Yilmaz (2001)).
513 Since previous shot multiples do not exhibit the same hyperbolic shapes as they are reflected
514 multiple times between the seafloor and sea surface, resulting in significantly smaller
515 curvatures compared to reflections (Fig. 10A). Therefore, we can separate reflections from
516 multiples based on their curvature differences (dip differences).



517

518 Fig. 9. A synthetic shot gather with direct arrival removed (A) and its F-K spectrum (B).

519



520

521 Fig. 10. Steps of F-K filter on a shot gather with direct arrival removed from the Hawaii
 522 Experiment. (A) Input shot gather, note the overprint of multiples onto reflections at distance
 523 > 1 km. (B) NMO correction applied. (C) F-K filter applied. (D) NMO correction removed. (E-

524 H) Corresponding F-K spectra of data in (A-D). White lines in (F) and (G) represent the fan-
525 shape dip filter.

526

527 F-K filter, or dip filter, is a proven technique in reflection seismology to remove coherent
528 noise such as ground rolls and guided waves in the $f-k$ domain (Yilmaz, 2001). With proper
529 data preparation, we design a processing sequence that utilizes F-K filter to remove previous
530 shot multiples from the water column. Taking a band-pass filtered (30-80 Hz) shot gather from
531 the CREST survey as a demonstration (Fig. 10), the processing sequence includes four steps:

532 1) Determine a velocity model for shot gathers. The model can be built through the same
533 interactive velocity analysis applied to CMP gathers. However, unlike the velocity model
534 used for stacking, it does not require the same level of detail since it is only used to
535 roughly flatten reflections. For instance, velocities can be picked every 1000 shots. If the
536 hydrographic properties remain relatively consistent along the seismic transect, a 1D
537 velocity model may suffice. In this study, we used the velocities measured by coincident
538 XBTs (Fig. 5).

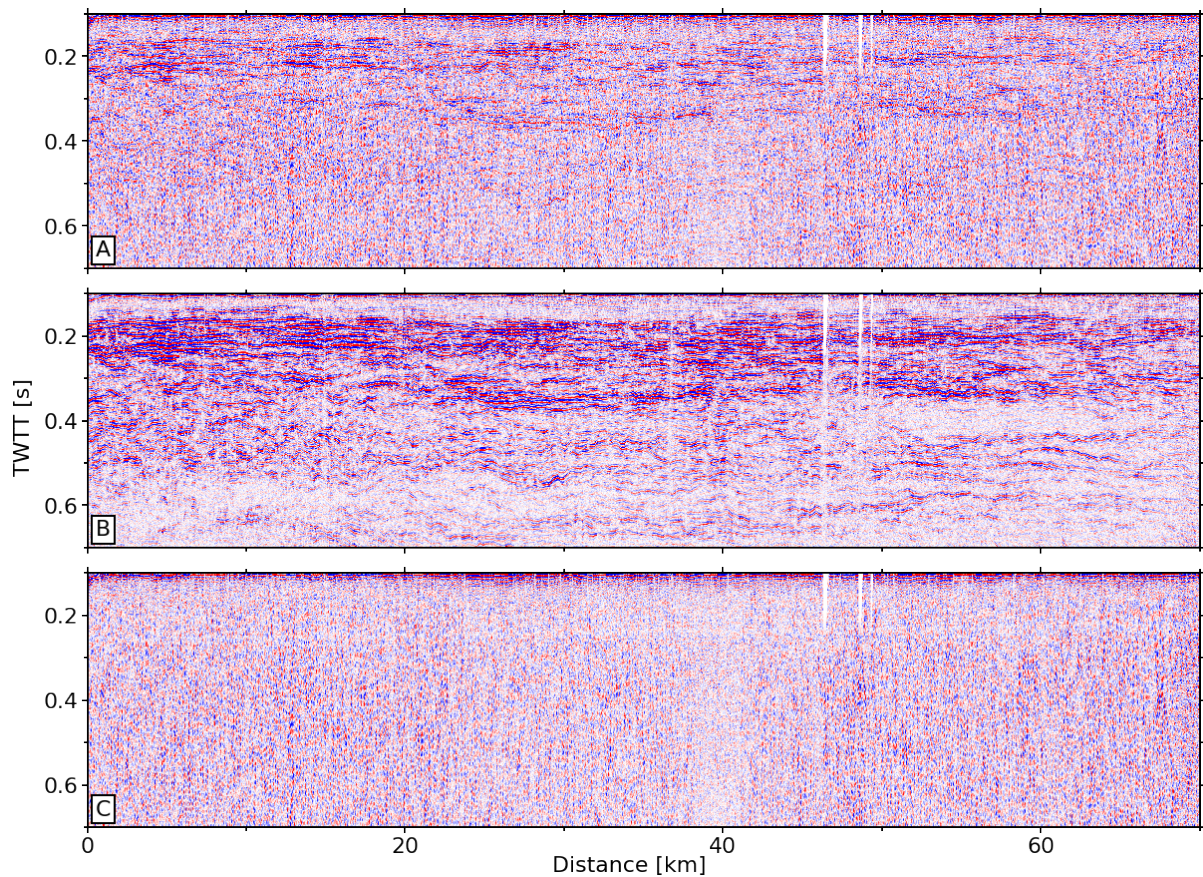
539 2) Apply normal-moveout (NMO) correction using the created velocity model to flatten
540 water column reflections while over-correcting previous shots multiples, causing them to
541 dip/curve upward (Fig. 10B). Through this process, multiples are mapped onto the
542 negative wavenumber quadrant in the F-K spectrum while reflections gather around 0
543 wavenumber along the frequency axis, forming a vertical stripe of high spectra energy
544 (Fig. 10F). The application of NMO on shot gathers assumes that reflectors in the water
545 column have gentle dipping angles, which this is usually true as the thermohaline
546 structures rarely dip greater than 10° (Sheen et al., 2011).

547 3) Design a F-K filter to remove coherent noise. Because of the redundancy inherent in the
548 Fourier transform, it is permissible to eliminate much of the spectra energy in the negative
549 wavenumber quadrant that corresponds to previous shot multiples, retaining only the
550 energy centered around zero wavenumber. Here, we follow Yilmaz (2001) to define the
551 F-K filter in ms/trace. As shown in Fig. 10G, a fan-shape dip filter starting from the origin,
552 spanning between -1 and 3.5 ms/trace is applied to remove multiples and further reduce
553 random noise. The reason to partially remove energy in the positive wavenumber
554 quadrant is discussed in the next section.

555 4) Apply inverse NMO correction with the same velocity model in step (1) to restore
556 reflections to original positions. It is recommended to follow up with a band-pass filter

557 to remove artifacts resulted from the inverse transform of spectra discontinuities in the F-
558 K domain.

559 We applied this processing strategy to the Campeche experiment which is severely
560 contaminated by multiples due to fine shot spacing (Fig. 5D). As shown in Fig. 11, previous
561 shot multiples are effectively removed without harming the amplitudes of water column
562 reflections. Additionally, a substantial amount of water column structure, previously obscured
563 or masked by noise, have now been recovered, suggesting the advantages of noise attenuation
564 in pre-stack processing stages.

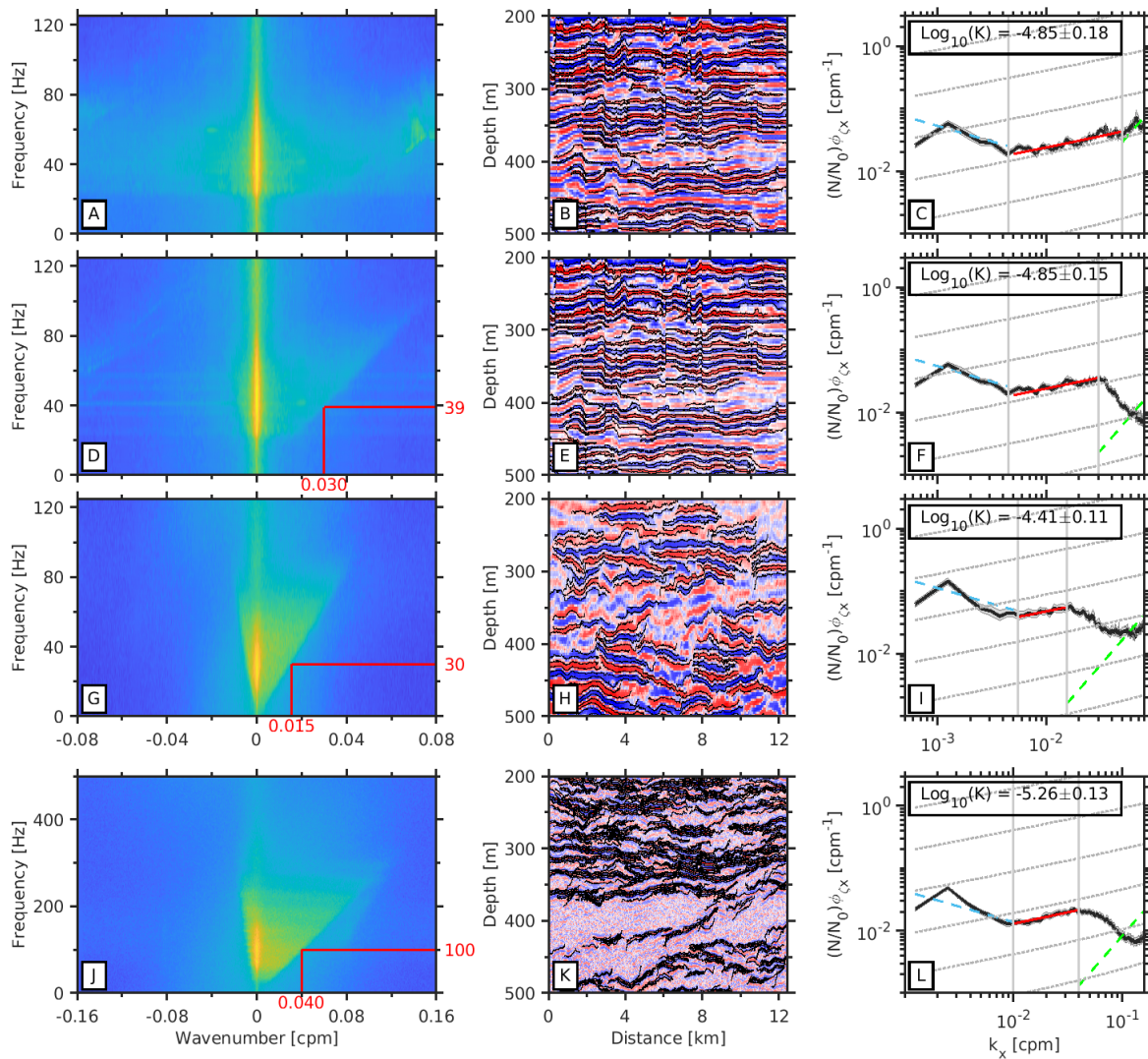


565
566 Fig. 11. Sections of seismic line 1003 of the Campeche Experiment without (A) and with
567 (B) F-K filter applied. (C) Differences between (A) and (B) showing the removed noise.

568
569 *b. Trade-off between S/N ratio and wavenumbers*

570 Ideally, during F-K filtering, the positive wavenumber quadrant of the F-K spectrum should
571 remain intact as it contains the entire wavenumber range needed to estimate turbulence.
572 Although our proposed F-K filter is effective in removing previous shot multiples, other
573 sources of noise that cannot be separated in the F-K domain such as strong ambient noise and

574 diffractions can persist and distort the slope spectra. Under these circumstances, we have the
 575 choice to apply a fan-shape F-K filter to further remove high-wavenumber noise by sacrificing
 576 a portion of high wavenumbers in the positive wavenumber quadrant, thereby improving the
 577 S/N ratio (Fig. 10G). To illustrate its effectiveness, we applied this method to the noise-free
 578 synthetic, CREST, and Campeche seismic data (Fig. 12).



579

580 Fig. 12. The relationships between F-K filters and roll-off wavenumbers in slope spectra.
 581 (A) F-K spectrum of the synthetic seismic section in (B). (C) Average slope spectrum
 582 calculated from tracked reflections in (B). (D-F) Same for F-K filtered synthetic seismic section
 583 (F-K filter: -1, 4.8 ms/trace). Red annotations in (D) showing the correspondence between the
 584 central frequency of data in (B, E) and the roll-off wavenumber in (F) along the edge of the F-
 585 K filter in the positive wavenumber quadrant. (G-I) Same for the CREST data (F-K filter: -1,
 586 3.5 ms/trace). (J-L) Same for the Campeche data (F-K filter: -0.5, 1.25 ms/trace). Note the
 587 change of axes in (J-L) due to different frequency bandwidth and CMP spacing of the
 588 Campeche Experiment. Also note the significant increase of resolution in (K) compared to (B),

589 (E), and (H). Color scheme for slope spectra is the same as in Fig. 4. Uncertainties of
 590 diffusivities only account for errors in buoyancy frequency and straight-line fitting.

591

592 First, applying a fan-shape F-K filter on the synthetic section (Fig. 12A, 12D) demonstrates
 593 the superiority of this method over a smoothing filter as it maintains the correct energy level
 594 of the spectrum, ensuring that the derived turbulent diffusivity remains unchanged (comparing
 595 diffusivities in Fig. 12C and 12F). Although this trade-off method also induces a spectrum roll-
 596 off in the reflection slope spectrum (Fig. 12F), the remaining turbulence subrange is still long
 597 enough to estimate turbulence with high fitting accuracy because LAST extends to relatively
 598 low wavenumbers. Furthermore, since the F-K filter was applied on NMO-corrected shot
 599 gathers, the form of the retained F-K spectrum naturally transfers to the post-stack data which
 600 also underwent NMO correction before stacking. This characteristic offers the flexibility to
 601 control the roll-off wavenumber of the turbulence subrange based on the dominant frequency
 602 of the post-stack data. Take the synthetic section as an example, the roll-off wavenumber (0.03
 603 cpm) in the reflection slope spectrum (Fig. 12F) is related to the central frequency (39 Hz) of
 604 the seismic data (Fig. 13A) along the slope of the F-K filter in the positive wavenumber
 605 quadrant (Fig. 12D). Critically, this relationship holds true for field seismic data (Figs. 12, 13).
 606 The following equations show how the slopes of the F-K filter can be derived from the central
 607 frequency of the data and a user-defined roll-off wavenumber, for both the synthetic
 608 experiment and Campeche data, which have 6.25 m and 3.125 m receiver spacing, respectively:

609 Synthetic:

$$610 \quad \frac{k_r}{f_c} = \frac{0.03 \text{ cycles/m}}{39 \text{ cycles/s}} = \frac{0.03 \times 6.25 / \text{trace}}{39 / 1000 \text{ ms}} = \frac{0.1875 / \text{trace}}{0.039 / \text{ms}} = 4.8 \text{ ms / trace} \quad (6)$$

611 Campeche:

$$612 \quad \frac{k_r}{f_c} = \frac{0.04 \text{ cycles/m}}{100 \text{ cycles/s}} = \frac{0.04 \times 3.125 / \text{trace}}{100 / 1000 \text{ ms}} = \frac{0.125 / \text{trace}}{0.1 / \text{ms}} = 1.25 \text{ ms / trace} \quad (7)$$

613 where k_r represents roll-off wavenumber, f_c is the central frequency of the data. In this way,
 614 we can quantitatively determine the length of the retained turbulence subrange.



615

616 Fig. 13. Frequency spectra of the synthetic (red), the CREST (orange), and the Campeche
 617 (blue) seismic sections shown in Fig. 12. Annotations mark the central frequencies of each
 618 dataset.

619

620 The importance of this quantitative analysis stems from the intermittence and heterogeneity
 621 of turbulent mixing in the ocean (Waterhouse et al., 2014). From the perspective of downscale
 622 energy cascade, the crossover wavenumber between the internal wave and turbulence subrange
 623 is linked to the level of internal wave energy, thereby influencing the intensity of turbulence
 624 (section 2.1). This characteristic results in varying crossover wavenumbers, or, in other words,
 625 varying lengths of turbulence subranges across a seismic transect, which means a uniform
 626 smoothing across the entire seismic section might lead to excessive removal of turbulence
 627 subranges in more calmer locations where turbulence subranges start at higher wavenumbers.
 628 With the proposed F-K filter, we can iteratively adjust the filter design for different segments
 629 along a seismic transect, ensuring the fidelity of turbulence subrange and achieving a better
 630 S/N ratio.

631 In summary, the fan-shape F-K filter offers three advantages: (1) preserves the correct
 632 energy level of reflection slope spectra, (2) further improves S/N ratio of the seismic data, (3)
 633 provides quantitative control over the different S/N ratios and varying lengths of turbulence
 634 subranges along a seismic transect.

635 6. Discussion

636 a. Comparison with microstructure measurements

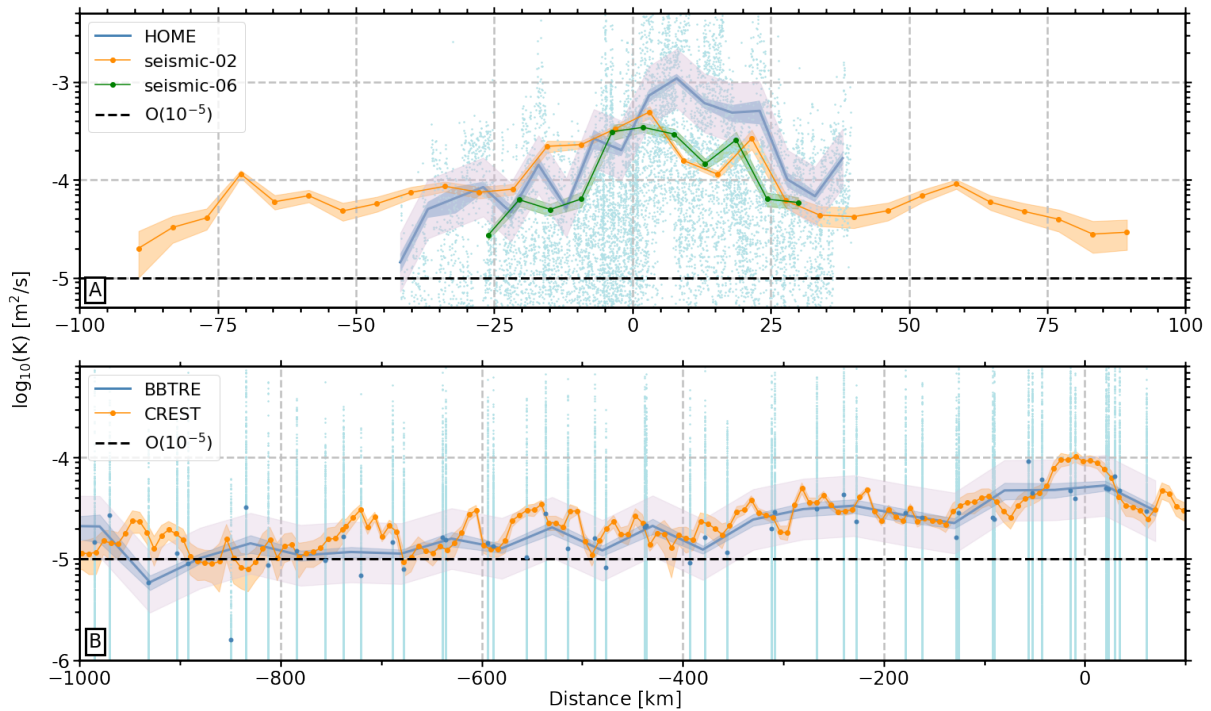
637 Since the discovery and development of seismic slope spectra method, seismic-derived
 638 mixing rates have not been carefully benchmarked against direct measurement of turbulence,
 639 which has stunted the prosperity of seismic oceanography. This gap is attributed not only to
 640 the absence of a standardized data processing approach, but also to the scarcity of existing

641 microstructure measurements. Here, two of our sets of seismic data, the CREST and Hawaii
642 experiments, are positioned in geological settings resembling those of two landmark
643 oceanographic observations that unveiled the critical sinks of energy dissipation in the ocean:
644 the BBTRE and HOME (Polzin et al., 1997; Rudnick et al., 2003). The environments where
645 BBTRE and HOME took place encompass a broad range of turbulence levels, ranging from
646 the energetic ridges to the quiescent ocean interior. Seismic data are processed using the
647 technique described above and reach an average S/N ratio higher than 9 using the criterion by
648 Holbrook et al. (2013). We compare the two kinds of measurements by taking depth averages
649 within bins along spatial directions perpendicular to the mean axes of the bathymetric objects.
650 Although the comparison is not coincident, our work provides valuable information in three
651 aspects: (1) examine the fidelity of seismic-derived diffusivities under different environments,
652 (2) extend observational records temporally and geographically, (3) provide insights into
653 quantitative parametrization of turbulent mixing for numerical models.

654 1) HAWAIIAN RIDGE (HOME)

655 HOME was designed to examine the energy budget of an important open-ocean site of
656 internal tide generation using several observational components ((Rudnick et al., 2003; Klymak
657 et al., 2006). One of the components was conducted by the towed instrument Marlin in the
658 Kauai Channel on a cross-ridge track at depths of 700 and 900 m. Two seismic lines from the
659 Hawaii Experiment are in close vicinity to this Marlin track (Fig. 5). Line06 is nearly aligned
660 with the Marlin track but has a slight northward rotation, while Line02 is positioned southeast
661 of the Marlin track and has a rotation towards the south. The total length of Line02 is ~533 km;
662 however, we only utilize the central 200 km that crosses the ridge because studies discovered
663 large isopycnal displacements within about 100 km of the ridge in the Kauai Channel (Rudnick
664 et al., 2003). Additionally, Hurricane Olivia occurred 10 days before the seismic data
665 acquisition (Cangialosi and Jelsema, 2019). Focusing on areas adjacent to the ridge can help
666 minimize the influence of factors other than topography, such as the dissipation of near-inertial
667 energy, which could contribute to enhanced mixing (Fer, 2014). For both measurements, we
668 follow Klymak et al. (2006) to take averages of diffusivities in 5-km-wide data bins between
669 depths of 700 to 900 m, and the spatial coordinates of the bins are defined relative to the mean
670 ridge direction, with positive distance in the northeast direction (Fig. 14). Average diffusivities
671 from seismic data are calculated using diffusivities derived from each individual reflections
672 within bins. Reflections longer than 0.8 km are used for spectra analysis (Krahmann et al.,

673 2009). This comparison is more compelling than previous seismic-hydrographic comparisons
 674 for two reasons: (1) they are both horizontally continuous measurements, (2) they both
 675 represent “snapshots” of ocean states, no systematic bias due to different temporal scales are
 676 introduced during averaging (Whalen, 2021).



677

678 Fig. 14. Comparison between seismic and microstructure measurements as a function of
 679 distance. (A) Diffusivities in cross-ridge direction for the Kauai Channel. (B) Diffusivities
 680 away from the Mid-Atlantic Ridge. Blue, orange, green shades represent 95% confidence
 681 intervals. Pink shades bounds the ± 0.3 logarithmic units of microstructure measured
 682 diffusivities. Blue dots = average diffusivities of each BBTRE vertical profile. Light blue dots
 683 = microstructure samples. Dashed black lines = background diffusivity of $10^{-4} \text{ m}^2 \text{ s}^{-1}$.

684

685 Similar to the microstructure measurements, the diffusivities derived from seismic data
 686 exhibit highest values over the ridge crest and extend across the width of the ridge saddles (Fig.
 687 14A). The highest mean diffusivities for Line06 and Line02 are $3.4 \times 10^{-4} \text{ m}^2/\text{s}$, and 4.9×10^{-4}
 688 m^2/s , respectively, an order of magnitude higher than the background level of $10^{-5} \text{ m}^2/\text{s}$.
 689 Notably, the diffusivities measured by Line06 and Marlin exhibit similarity: (1) rapid decay to
 690 the background level within 40-60 km from the ridge, (2) comparable widths of enhanced
 691 diffusivities over the ridge top spanning approximately 20-30 kilometers, and (3) significant
 692 drop-off from $\sim 2 \times 10^{-4} \text{ m}^2/\text{s}$ to $\sim 6 \times 10^{-5} \text{ m}^2/\text{s}$ occurring around -7.5 km (Fig. 14A). However,
 693 for Line02, the decay is much slower, taking $\sim 100 \text{ km}$ for diffusivities to decrease to $10^{-5} \text{ m}^2/\text{s}$.
 694 The coherence between Line06 and Marlin and their differences from Line02 suggest a pattern

695 change of energy dissipation. The corrugated bathymetry beneath Line02 on both sides of the
696 ridge favors the generation of high-mode internal tides so that more energy is dissipated locally
697 (Vic et al., 2019), contributing to the longer decay distance. In contrast, along Line06 and
698 Marlin track where steep topographic relief is present, more energy propagates away as low-
699 mode internal tides (Rudnick et al., 2003; Klymak et al., 2006). The observed two patterns
700 support the importance of topography in distributing internal wave energy in the ocean, as
701 previous studies have shown the different forms of tidal energy transfer affected by the ratios
702 between the tidal beam and topographic slopes (Klymak et al., 2011). Bottom scattering of
703 low-mode internal waves into high-modes that facilitate mixing might also contribute to the
704 observed differences (Müller and Xu, 1992; Bühler and Holmes-Cerfon, 2011).

705 It is noteworthy that neither Line06 nor Line02 capture the extremely high diffusivities
706 measured by microstructure data (e.g., 10^{-3} m²/s), due to the limitation of the reflection slope
707 spectra method, which depends on tracking continuous reflections. Krahnemann et al. (2009)
708 suggest that reflections with wavelengths between 0.8 and 2.8 km can be approximated as
709 isopycnals so that the assumption of the slope spectra holds true. We conducted tests by using
710 reflection lengths of 0.8 km and 1.6 km and found that in areas away from the ridge where
711 background values are found, both cases yield similar levels of diffusivities. However, close to
712 the ridge where turbulence is high, using longer reflections severely underestimates
713 diffusivities because only stronger reflections are tracked and spectrally analyzed. These results
714 are expected as high amplitude, continuous reflections denote relatively stable stratification
715 and weaker turbulence. In contrast, reflections become choppier as turbulence intensifies,
716 reducing the efficacy of the tracking algorithm (Holbrook et al., 2013; Fortin et al., 2016). Our
717 experiment suggests that it is preferable to use shorter reflections for spectra analysis in
718 energetic regions to capture the enhanced turbulence. The choice of reflection length clearly
719 influences how well turbulence is represented by slope spectra, an issue that remains
720 unresolved and as such more quantitative analysis is needed in the future. Ideally, with
721 technical advancement, spectra could be computed directly from seismic-inverted sections of
722 temperature and salinity, avoiding the need to track reflections (Dickinson and Gunn, 2022).

723 For the Hawaiian experiment, the average uncertainty of spectra fitting for both lines is up
724 to 0.25 in logarithmic units. In the selected depth range of 700-900 m, the average uncertainty
725 of N is less than 4% (Fig. 6), it will introduce an uncertainty of 0.018 in logarithmic units.
726 Combined with the uncertainties from other parameters summarized in section 2.1 and

727 assuming independence in error propagation, the total uncertainty for $\log_{10}(K_\rho)$ is ~ 0.33 .
728 Compare with microstructure measurements, seismically derived diffusivities are generally
729 within ± 0.3 logarithmic units off the ridge crest (Fig. 14A).

730 2) MID-ATLANTIC RIDGE (BBTRE)

731 BBTRE is one of the pioneering physical oceanographic observations that examine the
732 intensity, spatial distribution, and mechanisms of mixing across the entire water column over
733 a large region (Polzin et al., 1997). Here, we use the High-Resolution Profilers (HRP)
734 microstructure data collected during the second leg of the BBTRE in 1997 between 21° - 23° S.
735 These stations were relatively densely spaced and sampled along the east-west direction,
736 spanning from the top of the Mid-Atlantic Ridge to the smooth topography of ocean interior
737 (Fig. 5).

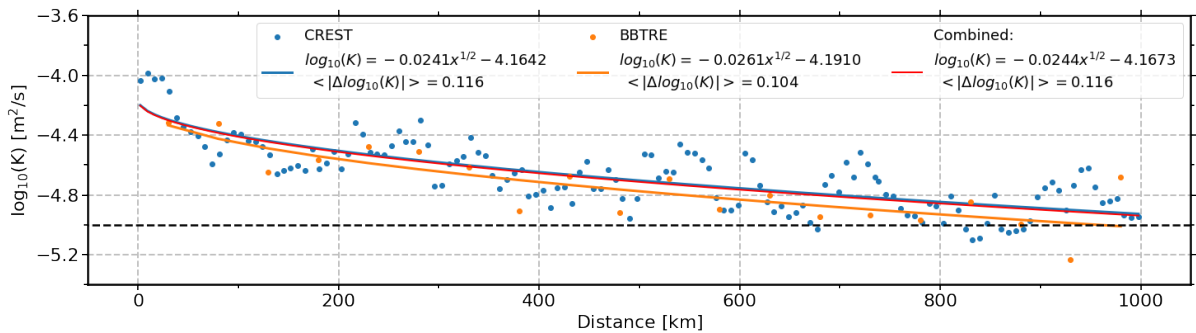
738 The CREST seismic survey is positioned in a similar environment along 30° S, providing
739 an opportunity, for the first time, to compare seismic-derived diffusivities with microstructure
740 measurements over a significant distance. We only selected data between 200-1000 m in the
741 upper ocean as the seismic data are noisier in the deeper regions, resulting in fewer trackable
742 reflections. Including data below 1000 m will bias the comparison due to inconsistent sampling
743 density and data quality (Fig. 4A). Following the strategy in section 5.1.1, we take depth-
744 averages within bins as a function of distance away from the Mid-Atlantic Ridge for both
745 measurements (Fig. 14B). Since the HRPs are not evenly spaced, we average data within 50-
746 km bins to reduce spatial bias, whereas seismic data is averaged in 5-km bins to take advantage
747 of its high spatial resolution. Our tests on different bin sizes suggest lesser impact on results,
748 indicating that spatial bias stemming from the choice of bins is not significant.

749 In comparison to the results around the Hawaiian Ridge in the last section (6.1.1), CREST
750 and BBTRE show better agreement on the level of mixing rates. For both measurements,
751 diffusivities are close to 10^{-4} m²/s over the top of the ridge and decrease gently over a significant
752 distance to the background level more than 800 km away from the ridge (Fig. 14B). Notably,
753 the decay patterns of K_ρ with respect to the distances from the crest of ridges, x , can be
754 approximated by similar 1/2 power-law relationships (Fig. 15). Following Tang (2021, 2022),
755 we have:

$$756 \log_{10} K_\rho^{MC}(x) = -0.0241x^{1/2} - 4.1642 \quad (8)$$

757
$$\log_{10} K_{\rho}^{MB}(x) = -0.0251x^{1/2} - 4.1910 \quad (9)$$

758 where $K_{\rho}^{MC}(x)$ and $K_{\rho}^{MB}(x)$ are the model diffusivity for CREST and BBTRE, respectively. The
 759 mean fitting residual $\langle |\Delta \log_{10} K_{\rho}^M(x)| \rangle = \langle |\log_{10} K_{\rho}(x) - \log_{10} K_{\rho}^M(x)| \rangle$ is 0.116 for CREST and
 760 0.112 for BBTRE in logarithmic units (Fig. 15). The two empirical relationships suggest that
 761 along zonal direction at two different latitudes in the South Atlantic, the nonlinear decay of
 762 turbulence follows a relatively consistent pattern from the Mid-Atlantic Ridge into the ocean
 763 basin.



764
 765 Fig. 15. Power-law fittings of average diffusivities in Fig. 14B for CREST (blue), BBTRE
 766 (orange), and the two combined (red), showing decay of mixing away from Mid-Atlantic
 767 Ridges up to 1000 km. $\langle |\Delta \log_{10} K| \rangle$ is the mean fitting residual. Dashed black lines =
 768 background diffusivity of $10^{-4} \text{ m}^2 \text{ s}^{-1}$.

769
 770 Within 1000 km from mid-ocean ridges, the mechanisms contributing to energy dissipation
 771 are complex. For instance, breaking and dissipation of high-mode internal tides (St. Laurent
 772 and Garrett, 2002; Vic et al., 2019), scattering of low-mode internal tides off irregular
 773 topography (de Lavergne et al., 2019), different types of wave-wave interactions, and lee waves
 774 can all play a role (Whalen et al., 2020). Therefore, the consistency observed in the upper ocean
 775 at two different locations is surprising. It could be related to changes in the roughness of the
 776 seafloor (Polzin et al., 1997; Waterhouse et al., 2014). Or it might simply be due to increasing
 777 water depths away from the ridge, resulting in decreased disturbance in the upper ocean from
 778 breaking of high-mode internal tides. It is also possible that some form of resonance exists
 779 geographically between different mechanisms of energy dissipation which might provide
 780 insights into parametrization. While it is impossible for us to discern between mechanisms, our
 781 results support the notion of a high tidal energy conversion rate by abyssal hills (Vic et al.,
 782 2019). Given that it took almost 1000 km for diffusivity to decay to the background level, and
 783 mode 1 internal tide is unique in its long-range propagation ($>1000 \text{ km}$) (Alford and Zhao,

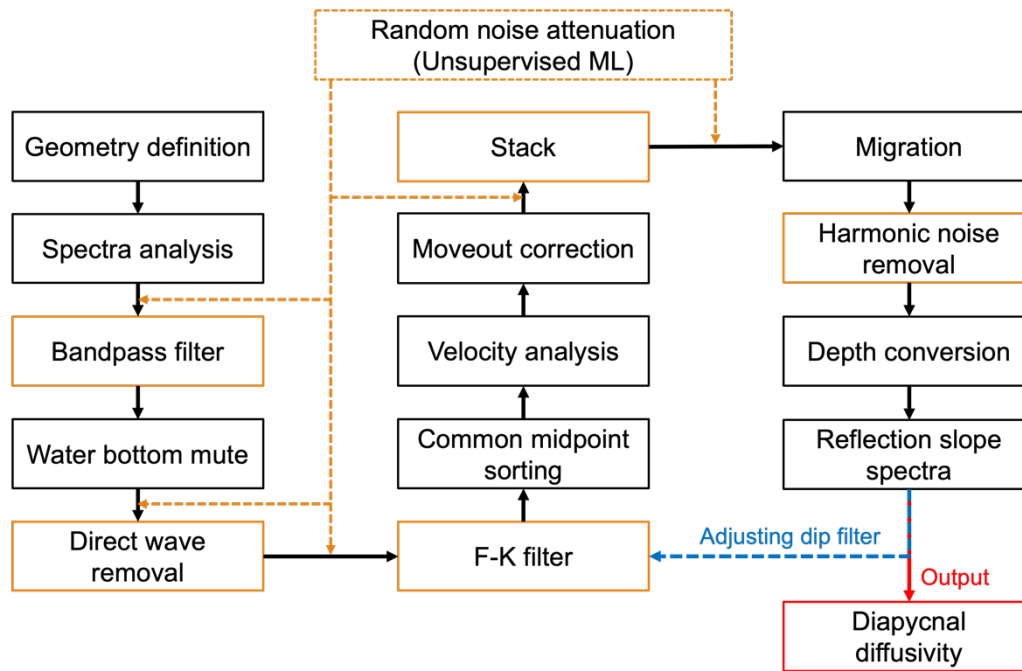
784 2007; Zhao et al., 2016), internal tides with modes > 1 likely dissipated within 1000 km from
785 the Mid-Atlantic Ridge. From the perspective of wave-wave interaction, BBTRE measured
786 turbulence is more likely to be higher than CREST due to a process known as parametric
787 subharmonic instability occurring equatorward of 29° , when high-mode internal waves interact
788 with a low-mode wave with twice their frequency (Hibiya and Nagasawa, 2004; MacKinnon
789 et al., 2013). However, our results show the opposite; CREST measured diffusivities are
790 slightly higher than BBTRE. This discrepancy might be attributed to the residual noise in the
791 seismic data that overestimates the spectra energy (section 4.2). However, it could also be
792 caused by a storm event happened ~ 30 days prior to the seismic survey, which generated near-
793 inertial waves and contributed to elevated turbulence in the upper ocean (Wei et al., 2022).

794 For the CREST experiment, the average uncertainty of spectra fitting for both lines is up to
795 0.16 in logarithmic units. In the selected depth range of 200-1000 m, the average uncertainty
796 of N is less than 5% (Fig. 6); it will introduce an uncertainty of 0.021 in logarithmic units. The
797 combined total uncertainty for $\log_{10}(K_\rho)$ is ~ 0.27 . Compare with microstructure measurements,
798 seismic-derived diffusivities are within ± 0.3 logarithmic units over the analyzed distance of
799 1000 km (Fig. 14B).

800 *b. Toward a standardized workflow*

801 Through the comparison with microstructure data, we have demonstrated that the seismic-
802 derived diffusivities are in good agreement with microstructure measurements in different
803 oceanographic environments, within margins of error. While not concurrent, the seismic-
804 derived diffusivities are generally within ± 0.3 logarithmic units of the microstructure
805 measurements (except for extreme values), indicating the seismic method is capable of
806 measuring ocean turbulence with confidence. The analysis of this study underscores that the
807 accuracy of the seismic method relies on maintaining the correct energy level of the slope
808 spectra. The key in achieving this goal lies in preserving the true reflection amplitude during
809 data processing while minimizing noise as much as possible. While a S/N ratio higher than 9
810 is recommended, an even higher S/N ratio should be considered ideal. Building upon the
811 recommendations of Holbrook et al. (2013), we propose a standardized workflow featuring an
812 iterative F-K filtering process suitable for legacy marine seismic dataset whose original
813 acquisition was not devised for water column research (Fig. 16). The iterative approach allows
814 for balancing considerations between F-K filter design, S/N ratio, and spatial heterogeneity of
815 turbulent mixing. It is advisable to apply differentiated F-K filters to data with varying S/N

816 ratios across a seismic section, using user-defined spatial windows. The fan width of the F-K
 817 filters can also be iteratively adjusted based on the length of the turbulence subrange in the
 818 resulting slope spectra.



819

820 Fig. 16. A standardized workflow for using legacy seismic data to calculate diapycnal
 821 diffusivity. Orange boxes denote steps related to noise attenuation. Dashed orange lines
 822 pointing to the processing phase where machine learning based methods could be useful.

823

824 Nevertheless, this workflow represents an expedient approach that adopts a trade-off
 825 strategy between S/N ratio and high-wavenumber turbulence information. Moreover, the F-K
 826 filter is not efficient on data acquired by small acquisition systems with short streamers (e.g.,
 827 24 channels) as they do not provide enough moveout differences between reflections and
 828 coherent noise. Future endeavors might explore advanced techniques such as machine learning
 829 (ML) based method to keep the slope spectra intact. Attempts have been made using a
 830 supervised denoising convolutional neural network (DnCNN) on post-stack sparker data
 831 (Zhang et al., 2017; Jun et al., 2020). However, DnCNN is not very effective for legacy seismic
 832 data collected by air-gun sources which generate high-amplitude reflections and coherent noise
 833 simultaneously. This is likely due to the lack of ground truth to build high quality training set.
 834 Therefore, future work employing unsupervised ML on either pre-stack or post-stack data
 835 would be valuable to improve the workflow. Because stacking is essential in producing images
 836 of thermohaline fine structures, ML denoising on pre-stack data might be challenging due to

837 weaker reflection amplitudes, which could potentially be misinterpreted as noise by ML
838 algorithms. In any case, with proper tools to ensure the spectra integrity, seismic oceanography
839 can provide a global inventory of oceanic horizontal-wavenumber spectra which could greatly
840 improve our understanding of energy cascade across different length scales and thereby
841 building better parametrizations for climate models (Dickinson and Gunn, 2022).

842 **7. Conclusions**

843 In this study, we discussed the challenges of using legacy marine seismic reflection data to
844 faithfully derive turbulent diapycnal diffusivities. Through full-wavefield synthetic modeling,
845 we have shown that the energy level of reflection slope spectra is sensitive to the S/N ratio of
846 the seismic data, such that increasing noise levels lead to increasing overestimation of
847 diffusivities. In addition, the turbulent subranges of the slope spectra are easily affected by
848 changes in reflection amplitudes which delineate the vertical displacements of isopycnals. Our
849 results emphasize the necessity of a seismic data processing strategy that preserve true
850 reflection amplitudes while minimizing noise simultaneously.

851 To tackle these problems, we developed a workflow that adopts an iterative spectrum
852 filtering approach which allows for quantitative balancing between the considerations of filter
853 design, S/N ratio, and spatial heterogeneity of turbulent mixing. The workflow also leaves
854 spaces for future integration of machine learning techniques to further enhance S/N ratios. Its
855 successful implementation on three seismic datasets collected by different acquisition systems
856 proves its reliability and versatility. The resulted diapycnal diffusivities agree well with the
857 direct measurements of turbulence collected in the Brazil Basin and at the Hawaiian Ridge,
858 with diffusivities within ± 0.3 logarithmic units of the microstructure measurements when
859 diffusivities are weaker than $\sim 10^{-3}$ m²/s. The comparison also highlights the recommendation
860 of using seismic data with S/N ratios higher than 9 in future applications.

861 Combining observations from the microstructure and seismic data underscores the critical
862 role of topography in transferring energy across lengths scales through the internal wave
863 continuum. While discerning individual contributing factors remains challenging, our results
864 across the Kauai Channel and away from the Mid-Atlantic Ridge both support the phenomenon
865 that small scale topography facilitates the cascade of energy from larger to smaller scales and
866 ultimately to turbulence, contributing to extended decay distance of mixing. The surprising
867 consistency between the decay of mixing at different latitudes in the South Atlantic implies

868 internal tides with modes greater than 1 are likely all dissipated within 1000 km of mid-ocean
869 ridges. The constructed empirical models of diffusivity as a function of distance might provide
870 insights on climate model parametrizations. However, more observations and theory
871 development are required to fully understand the evolution of mixing across ocean basins.

872 Building upon the recommendations of Holbrook et al. (2013), our proposed workflow is
873 a key advance towards standardization of seismic derived mixing rates. However, more efforts
874 are needed in the future. For example, we briefly discussed how the choice of tracked reflection
875 lengths affects the derived diffusivities in high turbulence environment, emphasizing the need
876 to examine the validity of the assumption that reflections approximate isopycnals under
877 different turbulence levels. Studies looking into the length scales of shear instabilities relative
878 to the seismic source wavelength are also desirable. Once seismic methods for estimating
879 mixing are standardized, existing seismic datasets will provide a way to investigate possible
880 changes in oceanic mixing during the previous four decades, when few other measurements
881 were available (Dickinson and Gunn, 2022). Furthermore, although our proposed workflow is
882 tailored to standardizing the processing of legacy seismic, it provides valuable insights into
883 future dedicated seismic oceanography surveys, where portable acquisition systems are
884 expected (Ruddick, 2018). More considerations are required in planning shot spacing and
885 recording length to prevent interference from previous shot multiples and to achieve better S/N
886 ratios.

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901 for expocodes A10 33RO20110926. Microstructure data were downloaded and processed
902 using the software by the oceanographic mixing community
903 (<https://github.com/OceanMixingCommunity>). CTDs around Hawaii was obtained via the
904 Hawaii Ocean Time-series HOT-DOGS application; University of Hawai'i at Mānoa; National
905 Science Foundation Award # 1756517. CTD data were analyzed using GSW TEOS-10
906 equation of state for seawater (github.com/TEOS-10/GSW-Python).

907 *Data Availability Statement.*

908 Seismic data is available from the Marine Geoscience Data System's Academic Seismic
909 Portal. MGL1601 DOI: 10.1594/IEDA/323597; MGL1806 DOI: 10.1594/IEDA/324706;
910 JS2203 DOI: 10.26022/IEDA/331509.

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