

Towards Improved Predictions in Ungauged Basins: Exploiting the Power of Machine Learning

Frederik Kratzert¹, Daniel Klotz¹, Mathew Herrnegger², Alden K. Sampson³,
Sepp Hochreiter¹, Grey S. Nearing⁴

¹LIT AI Lab & Institute for Machine Learning, Johannes Kepler University; Linz, Austria

²Institute for Hydrology and Water Management, University of Natural Resources and Life Sciences;
Vienna, Austria

³Upstream Tech, Natel Energy Inc.; Alameda, CA United States

⁴Department of Geological Sciences, University of Alabama; Tuscaloosa, AL United States

Key Points:

- Overall accuracy of LSTMs in ungauged basins is comparable to standard hydrology models in gauged basins
- There is sufficient information in catchment characteristics data to differentiate between catchment-specific rainfall-runoff behaviors

Corresponding author: Grey Nearing, gsnearing@ua.edu

Abstract

Long Short-Term Memory (LSTM) networks offer unprecedented accuracy for prediction in ungauged basins. We trained and tested several LSTMs on 531 basins from the CAMELS data set using k-fold validation, so that predictions were made in basins that supplied no training data. The training and test data set included approximately 30 years of daily rainfall-runoff data from catchments in the US ranging in size from 4 km^2 to 2,000 km^2 with aridity index from 0.22 to 5.20, and including 12 of the 13 IGPB vegetated land cover classifications. This effectively ‘ungauged’ model was benchmarked over a 15-year validation period against the Sacramento Soil Moisture Accounting (SAC-SMA) model and also against the NOAA National Water Model reanalysis. SAC-SMA was calibrated separately for each basin using 15 years of daily data. The out-of-sample LSTM had higher median Nash-Sutcliffe Efficiencies across the 531 basins (0.69) than either the calibrated SAC-SMA (0.64) or the National Water Model (0.58). This indicates that there is (typically) sufficient information in available catchment attributes data about similarities and differences between catchment-level rainfall-runoff behaviors to provide out-of-sample simulations that are generally more accurate than current models under ideal (i.e., calibrated) conditions. We found evidence that adding physical constraints to the LSTM models might improve simulations, which we suggest motivates future research related to physics-guided machine learning.

1 Introduction

Science and society are firmly in the age of Machine Learning (ML) (McAfee & Brynjolfsson, 2017). ML models currently out-perform state-of-the-art techniques at some of the most sophisticated domain problems across the Natural Sciences (e.g., AlQuraishi, 2019; He et al., 2019; Liu et al., 2016; Mayr, Klambauer, Unterthiner, & Hochreiter, 2016). In Hydrology, the first demonstration of ML out-performing a process-based model that we are aware of was by Hsu et al. (1995), who compared a calibrated Sacramento Soil Moisture Accounting Model (SAC-SMA) against a feed-forward artificial neural network across a range of flow regimes. More recently, Nearing et al. (2018) compared neural networks against the half-hourly surface energy balance of hydrometeorological models used operationally by several international weather and climate forecasting agencies, and showed that the former generally out-performed the latter at out-of-sample FluxNet sites. In a companion paper to this one, Kratzert et al. (2019) showed that regionally-trained Long Short-Term Memory Networks (LSTMs) out-perform basin-specific calibrations of several traditional hydrology models, and demonstrated that LSTM-type models were able to extract information from observable catchment characteristics to differentiate between different rainfall-runoff behaviors in hydrologically diverse catchments. The purpose of this paper is to show that we can leverage this capability for prediction in ungauged basins.

There is a long-standing discussion in the field of Hydrology about the relative merits of data-driven vs. process-driven models (e.g., Klemes, 1986). In their summary of a recent workshop on ‘Big Data and the Earth Sciences’ Sellars (2018) noted that “*Many participants who have worked in modeling physical-based systems continue to raise caution about the lack of physical understanding of machine learning methods that rely on data-driven approaches.*” It is often argued that data-driven models might under-perform relative to models that include explicit process representations in conditions that are dissimilar to training data (e.g., Kirchner, 2006; Milly et al., 2008; Vaze, Chiew, Hughes, & Andréassian, 2015). While this may or may not be true (we are unaware of any study that has tested this hypothesis directly), in any case where an ML model *does* out-perform relative to a given process-based model, we can conclude that the process-based model does not take advantage of the full information content of the input/output data (Nearing & Gupta, 2015). At the very least, such cases indicate that there is potential to improve the process-based model(s).

66 One of the situations where the accuracy of out-of-sample predictions matter is for
 67 Prediction in Ungauged Basins (PUB). PUB was the decadal problem of the Interna-
 68 tional Association of Hydrological Sciences (IAHS) from 2003-2012 (Hrachowitz et al.,
 69 2013; Sivapalan et al., 2003). State-of-the-art regionalization, parameter transfer, catch-
 70 ment similarity, and surrogate basin techniques (e.g., Parajka et al., 2013; Razavi & Coulibaly,
 71 2012; Samaniego et al., 2017) result in streamflow predictions that are less accurate than
 72 from models calibrated individually in gauged catchments. Current community best-practices
 73 for PUB center around obtaining detailed local knowledge of a particular basin (Blöschl,
 74 2016), which is expensive for individual catchments and impossible for large-scale (e.g.,
 75 continental) simulations like those from the US National Water Model (NWM) (Salas
 76 et al., 2018) or the streamflow component of the North American Land Data Assimila-
 77 tion System (NLDAS) (Xia et al., 2012). Moreover, Vrugt et al. (2006) argued that re-
 78 liable streamflow predictions from lumped catchment models typically require at least
 79 two to three years of gauge data for calibration (even this is likely an under-estimate of
 80 the amount of data necessary for reliable model calibration). PUB remains an impor-
 81 tant challenge because the majority of streams in the world are either ungauged or poorly
 82 gauged (Goswami, Oconnor, & Bhattarai, 2007; Sivapalan, 2003), and the number of gauged
 83 catchments, even in the US, is shrinking (Fekete et al., 2015).

84 In this technical note, we demonstrate an ML strategy for PUB. Our results show
 85 that out-of-sample LSTMs out-perform, on average, a conceptual model (SAC-SMA) cal-
 86 ibrated independently for each catchment, and also a distributed, process-based model
 87 (NWM). The purpose of this demonstration is twofold. First, to show that there is suf-
 88 ficient information in the available hydrological data record to provide meaningful pre-
 89 dictions in ungauged basins - at least a significant portion of the time. Second, to show
 90 that ML offers a promising path forward for extracting this information, and for PUB
 91 in general. The current authors are unaware of any existing model that performs as well,
 92 on average, as the LSTMs that we demonstrate here. At the end of this technical note
 93 we offer some thoughts - both philosophical and practical - about future work that could
 94 be done to advance the utility of ML in a complex systems science like Hydrology.

95 To re-emphasize our primary findings succinctly, ML in *ungauged basins* out-performs,
 96 on average (i.e., in more catchments than not) a lumped conceptual model calibrated
 97 in *gauged basins*, and also a state-of-the-art distributed process-based model. This rapid
 98 correspondence is intended to highlight initial results that might motivate continued de-
 99 velopment of these and similar techniques - this is not intended to be a comprehensive
 100 analysis of the application of LSTMs or deep learning in general to PUB.

101 2 Data

102 Experimental data for our analysis came from the publicly available Catchment At-
 103 tributes and Meteorology for Large-Sample Studies (CAMELS) data set curated by Na-
 104 tional Center for Atmospheric Research (NCAR) (Addor, Newman, Mizukami, & Clark,
 105 2017a; A. Newman et al., 2015, n.d.). CAMELS consists of 671 catchments in the con-
 106 tinent US ranging in size from 4 km^2 to $25,000 \text{ km}^2$. These catchments were chosen
 107 from the available gauged catchments in the US due to the fact that they are largely nat-
 108 ural and have long gauge records (1980-2010) available from the United States Geolog-
 109 ical Survey National Water Information System. CAMELS includes daily forcing from
 110 Daymet, Maurer, and NLDAS, as well as several static catchment attributes related to
 111 soils, climate, vegetation, topography, and geology (Addor et al., 2018). It is important
 112 to point out that these catchment attributes were derived from maps, remote sensing prod-
 113 ucts, and climate data that are generally available over the continental US and, either
 114 exactly or in close approximation, globally. For this project, we used only 531 of 671 CAMELS
 115 catchments - these were the same basins that were used for model benchmarking by A. J. New-
 116 man et al. (2017), who removed basins from the full CAMELS data set with (i) large dis-

117 crepancies between different methods of calculating catchment area, and (ii) areas larger
118 than 2,000 km^2 .

119 The CAMELS repository also includes daily streamflow values simulated by 10 SAC-
120 SMA models calibrated separately in each catchment using Shuffled Complex Evolution
121 (SCE) (Duan, Gupta, & Sorooshian, 1993) with 10 random seeds. Each SAC-SMA was
122 calibrated on 15 years of data in each catchment (1980-1995). These calibrations were
123 performed in previous work by NCAR (A. Newman et al., 2015). We used this ensemble
124 of SAC-SMA models as a benchmark for our LSTMs. In addition, we benchmarked
125 against the NWM reanalysis, which spans the years 1993-2017 ([https://docs.opendata](https://docs.opendata.aws/nwm-archive)
126 [.aws/nwm-archive](https://docs.opendata.aws/nwm-archive)). All performance statistics that we report (for all models) are from
127 the water years 1996-2010, so that the SAC-SMA models were tested out-of-sample in
128 time but at the same basins where they were calibrated.

129 3 Methods

130 3.1 A Brief Overview of Long Short-Term Memory Networks

131 LSTMs are a type of Recurrent Neural Network (RNN) first proposed by Hochreiter
132 and Schmidhuber (1997). LSTMs have memory cells that are analogous to the states
133 of a traditional dynamical systems model, which make them useful for simulating nat-
134 ural systems like watersheds. Compared with other types of recurrent neural networks,
135 LSTMs avoid exploding and/or vanishing gradients, which allows them to learn long-
136 term dependencies between input and output features. This is desirable for modeling catch-
137 ment processes like snow accumulation and seasonal vegetation patterns that have rel-
138 atively long timescales as compared with input-driven processes like direct surface runoff.
139 Kratzert, Klotz, Brenner, Schulz, and Herrnegger (2018) applied LSTMs to the prob-
140 lem of rainfall-runoff modeling and later demonstrated that the internal memory states
141 of the network were highly correlated with observed snow and soil moisture states with-
142 out the model seeing any type of snow or soil moisture data during training (Kratzert,
143 Herrnegger, Klotz, Hochreiter, & Klambauer, 2018).

144 **Figure 1** provides an illustration of an LSTM, which works as follows. The model
145 takes a time series (more generally, a sequence) of inputs $x = [x[1], \dots, x[T]]$ of data over
146 T time steps, where each element $u[t]$ is a vector containing features (model inputs) at
147 time step t . This is not dissimilar to any standard hydrological simulation model (i.e.,
148 is it not a one-step-ahead forecast model). The LSTM model structure is described by
149 the following equations:

$$i[t] = \sigma(W_i x[t] + U_i h[t-1] + b_i) \quad (1)$$

$$f[t] = \sigma(W_f x[t] + U_f h[t-1] + b_f) \quad (2)$$

$$g[t] = \tanh(W_g x[t] + U_g h[t-1] + b_g) \quad (3)$$

$$o[t] = \sigma(W_o x[t] + U_o h[t-1] + b_o) \quad (4)$$

$$c[t] = f[t] \odot c[t-1] + i[t] \odot g[t] \quad (5)$$

$$h[t] = o[t] \odot \tanh(c[t]), \quad (6)$$

150 where $i[t]$, $f[t]$ and $o[t]$ are the *input gate*, *forget gate*, and *output gate*, respectively,
151 $g[t]$ is the *cell input* and $x[t]$ is the *network input* at time step t ($1 \leq t \leq T$), $h[t-1]$
152 is the *recurrent input* $c[t-1]$ the *cell state* from the previous time step. At the first time
153 step, the hidden and cell states are initialized as a vector of zeros. W , U and b are cal-
154 ibrated parameters. These are specific to each gate, and subscripts indicate which gate
155 the particular weight matrix/vector is associated with. $\sigma(\cdot)$ is the sigmoid activation func-
156 tion, $\tanh(\cdot)$ the hyperbolic tangent function, and \odot is element-wise multiplication. The

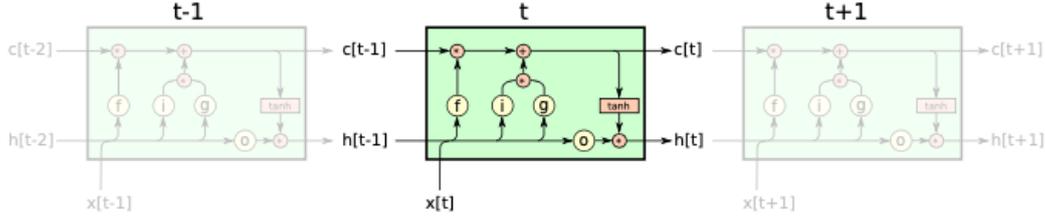


Figure 1. Visualization of (a) the standard LSTM cell as defined by equations (1-6).

157 intuition is that the cell states ($c[t]$) characterize the memory of the system. These are
 158 modified by (i) the forget gate ($f[t]$) which allows attenuation of information in the states
 159 over time and by (ii) a combination of the input gate ($i[t]$) and cell update ($g[t]$), which
 160 can add new information. In the latter case, the cell update contains information to be
 161 added to each cell state, and the input gate (which is a sigmoid function) controls which
 162 cells are 'allowed' to receive new information. Finally, the output gate ($o[t]$) controls the
 163 flow of information from states to model output.

164 3.2 Experimental Design

165 The LSTMs used in this study took as inputs at each timestep the NLDAS mete-
 166 orological forcing data listed in **Table 1**. Additionally, at each timestep, the meteoro-
 167 logical inputs were augmented with the catchment attributes also listed in **Table 1**. These
 168 catchment attributes were described in detail by Addor, Newman, Mizukami, and Clark
 169 (2017b) and remain constant in time throughout the simulation (training and testing).
 170 In total we used 32 LSTM inputs at each daily timestep: 5 meteorological forcings and
 171 27 catchment characteristics. All LSTMs were configured to have 256 cell states with
 172 a dropout rate of 0.4 applied to the LSTM output before a single regression layer.

173 We trained and tested three types of LSTM models:

- 174 1. **Global LSTM without static features:** LSTMs with only meteorological forc-
 175 ing inputs, and without catchment attributes, trained on all catchments simulta-
 176 neously (without k-fold validation).
- 177 2. **Global LSTM with static features:** LSTMs with both meteorological forc-
 178 ings and catchment characteristics as inputs, trained on all catchments simulta-
 179 neously (without k-fold validation).
- 180 3. **PUB LSTM:** LSTMs with both meteorological forcings and catchment charac-
 181 teristics as inputs, trained and tested with k-fold validation ($k = 12$).

182 The third model is the one we want to test - this is the one that simulates in basins
 183 that are different than the ones that the models was trained on. Out-of-sample testing
 184 was done by k-fold validation, which splits the 531 basins randomly into $k = 12$ groups
 185 of approximately equal size, uses all basins from $k-1$ groups to train the model, and then
 186 tests the model on the single group of hold-out basins. This procedure is repeated $k =$
 187 12 times so that out-of-sample predictions are available from every basin. The second
 188 model sets an upper benchmark for our PUB LSTMs. In particular, comparison between
 189 the second and thirds models tells us how much information was lost due to prediction
 190 in out-of-sample basins vs. in-sample basins. Similarly, a comparison between the first
 191 and second models lets us evaluate the value of adding catchment attributes to the model
 192 inputs, since these are what will, at least potentially, allow the model to be transferable
 193 between catchments.

Table 1. Table of LSTM Inputs

Meteorological Forcing Data	
Maximum Air Temp	2-meter daily maximum air temperature [$^{\circ}C$]
Minimum Air Temp	2-meter daily minimum air temperature [$^{\circ}C$]
Precipitation	Average daily precipitation [mm/day]
Radiation	Surface-incident solar radiation [W/m^2]
Vapor Pressure	Near-surface daily average [P_a]
Static Catchment Attributes	
Precipitation Mean	Mean daily precipitation.
PET Mean	Mean daily potential evapotranspiration
Aridity Index	Ratio of Mean PET to Mean Precipitation
Precip Seasonality	Estimated by representing annual precipitation and temperature as sin waves Positive (negative) values indicate precipitation peaks during the summer (winter). Values of approx. 0 indicate uniform precipitation throughout the year.
Snow Fraction	Fraction of precipitation falling on days with temp $< 0^{\circ}C$.
High Precipitation Frequency	Frequency of days with $\leq 5 \times$ mean daily precipitation
High Precip Duration	Average duration of high precipitation events (number of consecutive days with $\leq 5 \times$ mean daily precipitation).
Low Precip Frequency	Frequency of dry days (≤ 1 mm/day).
Low Precip Duration	Average duration of dry periods (number of consecutive days with precipitation ≤ 1 mm/day).
Elevation	Catchment mean elevation.
Slope	Catchment mean slope.
Area	Catchment area.
Forest Fraction	Fraction of catchment covered by forest.
LAI Max	Maximum monthly mean of leaf area index.
LAI Difference	Difference between the max. and min. mean of the leaf area index.
GVF Max	Maximum monthly mean of green vegetation fraction.
GVF Difference	Difference between the maximum and minimum monthly mean of the green vegetation fraction.
Soil Depth (Pelletier)	Depth to bedrock (maximum 50m).
Soil Depth (STATSGO)	Soil depth (maximum 1.5m).
Soil Porosity	Volumetric porosity.
Soil Conductivity	Saturated hydraulic conductivity.
Max Water Content	Maximum water content of the soil.
Sand Fraction	Fraction of sand in the soil.
Silt Fraction	Fraction of silt in the soil.
Clay Fraction	Fraction of clay in the soil.
Carbonate Rocks Fraction	Fraction of the catchment area characterized as “carbonate sedimentary rocks”.
Geological Permeability	Surface permeability (log10).

194 For each model type we trained and tested an ensemble of $N = 10$ LSTM mod-
 195 els to match the 10 SCE restarts used to calibrate the SAC-SMA models. All metrics
 196 reported in Section 4 were calculated from the mean of the 10-member ensembles, ex-
 197 cept for the NWM reanalysis.

198 All LSTM models were trained on the first 15 years of CAMELS data (1981-1995
 199 water years) - this is the same data period that A. Newman et al. (2015) used to cali-
 200 brate SAC-SMA. And all models (LSTMs, SAC-SMA, and NWM) were evaluated on the
 201 last 15 years of CAMELS data (1996-2010 water years). LSTMs were trained and eval-
 202 uated using a k-fold approach ($k = 12$). The training loss function was the average Nash-
 203 Sutcliffe Efficiency (NSE) over all training catchments; this is a squared-error loss func-
 204 tion that, unlike a more traditional MSE loss function, does not overweight catchments
 205 with larger mean streamflow values (i.e., does not overweight large, humid catchments)
 206 (Kratzert et al., 2019).

207 4 Results

208 A comparison between interpolated frequency distributions over the NSE values
 209 from 531 CAMELS catchments from all three LSTM models and both benchmark mod-
 210 els (SAC-SMA, NWM) is shown in **Figure 2**. Mean and median values of several per-
 211 formance statistics are given in **Table 2**. Interpolation was done with kernel density es-
 212 timation using Gaussian kernels and an optimized bandwidth.

213 The primary result is that the out-of-sample PUB LSTM ensemble performed at
 214 least as well as both of the in-sample benchmarks in more than half of the catchments
 215 against all four performance metrics that we tested, except that the basin-calibrated SAC-
 216 SMA has a slightly lower average difference between 95th percentile flows (both SAC-
 217 SMA and the PUB LSTM underestimated peak flows to some extent. The PUB LSTM
 218 had a higher NSE than SAC-SMA in 307 of 531 (58%) catchments, and higher than the
 219 NWM in 347 of 531 (66%) catchments. The PUB LSTM ensemble also had higher mean
 220 and maximum NSE scores than the the benchmark models, however SAC-SMA tended
 221 to out-perform the PUB LSTM in catchments with low NSE values (see the CDF plot
 222 in **Figure 2**).

223 There is some amount of stochasticity associated with training the LSTMs, espe-
 224 cially through the random weight initialization of the LSTMs, but also by the weight op-
 225 timization strategy (we used an ADAM optimizer (Kingma & Ba, 2014)). Because of this,
 226 the LSTM-type models give better predictions when used as an ensemble. It is not nec-
 227 essarily the case that if one particular LSTM model performs poorly in one catchment
 228 that a different LSTM trained on *exactly the same data* will also perform poorly. In our
 229 case, we used an ensemble of $N = 10$ (the same size as the SAC-SMA ensemble devel-
 230 oped by A. Newman et al. (2015) that was used here for benchmarking). **Figure 3** shows
 231 the NSE values for each ensemble member for the PUB LSTM models. In total, there
 232 were 103 basins with at least one PUB LSTM ensemble member with an NSE score of
 233 below zero. Only 9 of these 103 basins have all $N = 10$ ensemble members with NSE
 234 < 0 , while 55 of the 103 have at least one ensemble member with NSE > 0.5 . As an ex-
 235 ample, one of the basins (USGS basin ID: 01142500, which is basin number 232 in **Fig-**
 236 **ure 3**) had 9 of 10 ensemble members with NSE < 0 , but one ensemble member with
 237 NSE > 0.7 . This indicates that a substantial portion of the uncertainty in these LSTM
 238 models is due to randomness, rather than to systematic model structural error.

239 The global LSTM model with static catchment attributes performs better than all
 240 other models against the metrics that we tested. **Figure 4** compares the performance
 241 of the Global LSTM with other benchmark models (SAC-SMA and the Global LSTM
 242 without static catchment attributes). The Global LSTM with catchment attributes per-
 243 forms better in most - but not all - catchments. This indicates two things. First, the com-

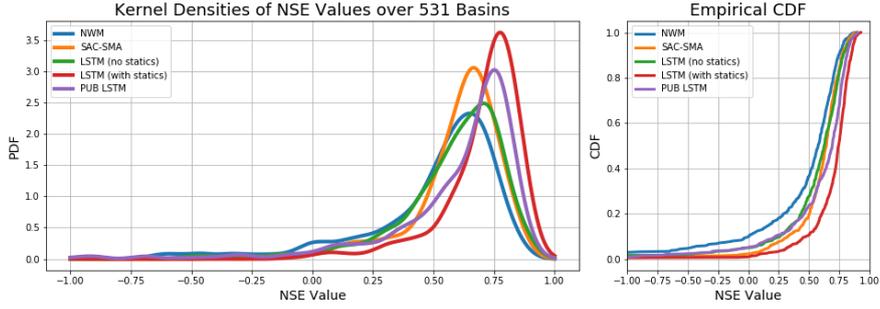


Figure 2. Frequencies of NSE values from 531 catchments given by ‘gauged’ and ‘ ungauged’ LSTMs, calibrated (gauged) SAC-SMA, and the National Water Model reanalysis.

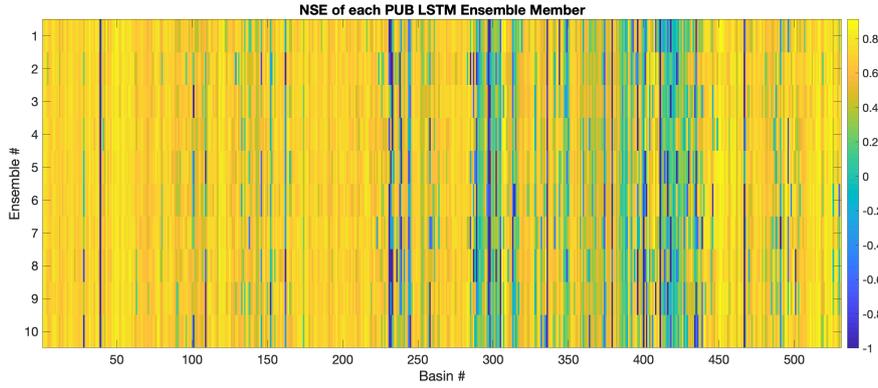


Figure 3. NSE scores for all PUB LSTM ensemble members. In some number of basins, certain ensemble members perform well and certain ensemble members perform poorly. This motivates the use of ensembles of LSTMs.

244 comparison between the Global LSTM with and without static catchment attributes indi-
 245 cates that although there is useful information in the catchment attributes, in some catch-
 246 ments having this data actually hurts us. We explored this relationship briefly, but did
 247 not find any patterns in terms of which catchment attributes might tend to lead to under-
 248 performance. Specifically, **Figure 5** shows that there is generally no correlation between
 249 the values of individual catchment attributes and whether the Global LSTM with vs.
 250 without statics performs better. Our initial conclusion is that the basins where the LSTM
 251 without catchment attributes performs better is likely an indication of error or uncer-
 252 tainty in the catchment attributes data. Nonetheless, these data did generally add sig-
 253 nificant skill to the model (the difference in NSE scores was statistically different at p
 254 $\leq 1e-9$). Future work might use a more sophisticated sensitivity analysis (e.g., sequen-
 255 tial model building or a Sobol’-type analysis) to test which specific catchment attributes
 256 cause this underperformance when added to the model.

257 The second thing that we want to highlight from the comparison between the Global
 258 LSTM and SAC-SMA (**Figure 4**) is that there is substantial room to improve SAC-SMA
 259 overall. This clearly shows that the LSTM finds rainfall-runoff relationships in individ-
 260 ual catchments that SAC-SMA cannot emulate. However, the fact that SAC-SMA per-
 261 forms better in some catchments indicates the potential value of having physical con-
 262 straints in a hydrological model. The LSTMs in these cases are either overfit or are not
 263 able to simulate behaviors of certain similar catchments in the training data set.

Table 2. Summary of Benchmark Statistics for All Models across 531 Catchments

	Median	Mean	Minimum	Maximum
Nash Sutcliffe Efficiency:	$(-\infty, 1]$ – values close to 1 are desirable.			
SAC-SMA:	0.64	0.51	-12.28	0.88
NWM:	0.58	0.31	-20.28	0.89
Global LSTM (no statics):	0.63	0.45	-31.72	0.90
Global LSTM (with statics):	0.74	0.68	-1.78	0.93
PUB LSTM:	0.69	0.54	-13.02	0.90
Fractional Bias:	$(-\infty, 1]$ – values close to 0 are desirable.			
SAC-SMA:	0.04	0.02	-1.76	0.71
NWM:	0.05	-0.01	-4.80	1.00 ^c
Global LSTM (no statics):	0.01	-0.03	-3.01	0.77
Global LSTM (with statics):	-0.01	-0.04	-2.19	0.49
PUB LSTM:	-0.02	-0.09	-4.86	0.72
Standard Deviation Ratio^a:	$[0, \infty)$ – values close to 1 are desirable.			
SAC-SMA:	0.83	0.87	0.10	3.76
NWM:	0.86	0.93	0.00 ^c	4.04
Global LSTM (no statics):	0.74	0.81	0.10	5.83
Global LSTM (with statics):	0.88	0.89	0.17	1.96
PUB LSTM:	0.86	0.91	0.10	3.23
95th Percentile Difference^b:	$(-\infty, 1]$ – values close to 0 are desirable.			
SAC-SMA:	0.02	-0.05	-3.98	0.83
NWM:	0.07	-0.07	-8.59	1.00 ^c
Global LSTM (no statics):	0.12	0.02	-4.97	0.81
Global LSTM (with statics):	0.03	-0.03	-3.30	0.63
PUB LSTM:	0.03	-0.08	-5.26	0.78

^aRatio of the standard deviation of simulated vs. observed flows at each catchment.

^bDifference between the values of the observed vs. simulated 95th percentile flows divided by the observed 95th percentile flows at each catchment.

^cValues of zero and one in the NWM max/min statistics are due to rounding. In particular, for one basin (USGS basin ID: 2108000) the NWM simulates a 95th flow percentile of $\sim 1 \times 10^{-3}$ [mm/day] whereas the 95th percentile of observed flow is ~ 4 [mm/day]

264 5 Discussion

265 The results illustrated in the previous section tell us three things:

- 266 1. The process-driven hydrology models that we used here as benchmarks could be
267 improved. The LSTM often finds a better functional representation of rainfall-runoff
268 behavior in most catchments than either SAC-SMA or the NWM.
- 269 2. The argument that process-driven models may be preferable in out-of-sample con-
270 ditions may not hold water. Modern ML methods are quite powerful at extract-
271 ing information from large, diverse data sets under a variety of hydrological con-
272 ditions.
- 273 3. The comparison between models with and without static catchment attributes as
274 inputs demonstrates that there is sufficient information contained in catchment
275 attribute data to distinguish between different rainfall-runoff relationships in at
276 least most of the US catchments that we tested.

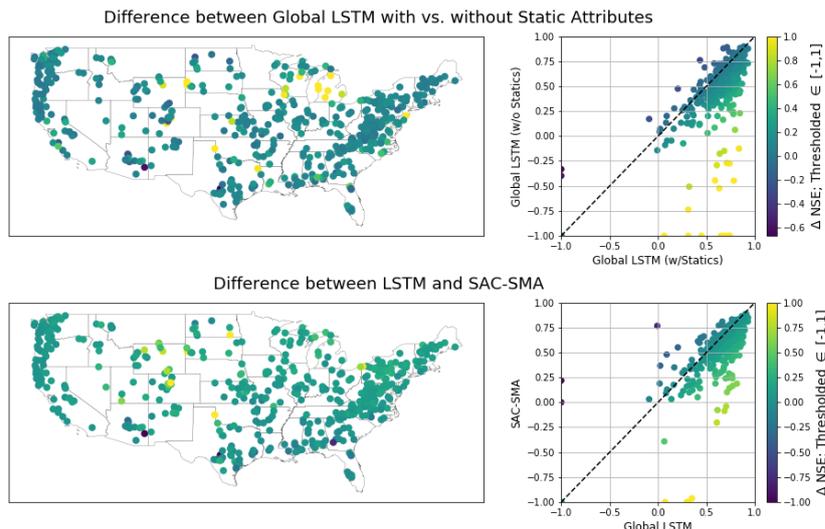


Figure 4. Comparison between the Global LSTM model with static catchment attributes and other benchmark models used in this study: (top) LSTM without static catchment attributes and (bottom) SAC-SMA.

277 Related to the third conclusion, the challenge going forward is about how to ex-
 278 tract the useful information from catchment attributes data for regional modeling. One
 279 of the historical reasons why this has been a hard problem is because the usual strat-
 280 egy is to use observable catchment attributes or characteristics to identify or 'regional-
 281 ize' parameters of conceptual or process-based simulation models (e.g., Prieto, Le Vine,
 282 Kavetski, Garca, & Medina, 2019; Razavi & Coulibaly, 2012). This is hard because of
 283 strong interactions in high-dimensional parameter spaces. There are many methods for
 284 this - notably a family of regionalization methods that Razavi and Coulibaly (2012) called
 285 'model independent', however we are unaware of any approach that is as effective as LSTMs
 286 at extracting this information for streamflow simulation. This is also in line with the re-
 287 cent results by Kratzert et al. (2019), where similar LSTMs were compared against mod-
 288 els calibrated with a parameter regionalization strategy Samaniego, Kumar, and Attinger
 289 (2010). That paper additionally showed that the response of LSTM-type models were
 290 relatively smooth with respect to perturbing catchment attributes, indicating a robust
 291 fit (i.e., that the models were not overfit or simply remembering different catchments).
 292 The results presented here show that the LSTM is able to extrapolate on catchment at-
 293 tributes to new catchments. Taken together, these results indicate that the catchment
 294 attribute data set Addor et al. (2017a) contains a significant amount of useful informa-
 295 tion about the differences between rainfall-runoff behaviors across (eco)hydrological regimes,
 296 and that machine learning is effective at extracting and using these patterns.

297 Related to the first conclusion, this is yet another example where traditional hy-
 298 drological models do not take full advantage of the information available from the Earth-
 299 observation data record. In this case, neither SAC-SMA nor the NWM are able to di-
 300 rectly use the catchment attribute data that we use here, but even if those model could
 301 leverage this information, they still could not compete with the LSTM, since the LSTM
 302 out-performs even when the conceptual model is calibrated in-basin. This means that
 303 not only is there useful information in catchment attributes data, but *also* that there is
 304 more information in meteorological forcing data than is used by the traditional models.
 305 Several recent experiments have shown the same thing for a number of operational ter-
 306 restrial hydrology models (e.g., Nearing, Mocko, Peters-Lidard, Kumar, & Xia, 2016; Near-
 307 ing et al., 2018). Hrachowitz et al. (2013) and others suggest that better process-based

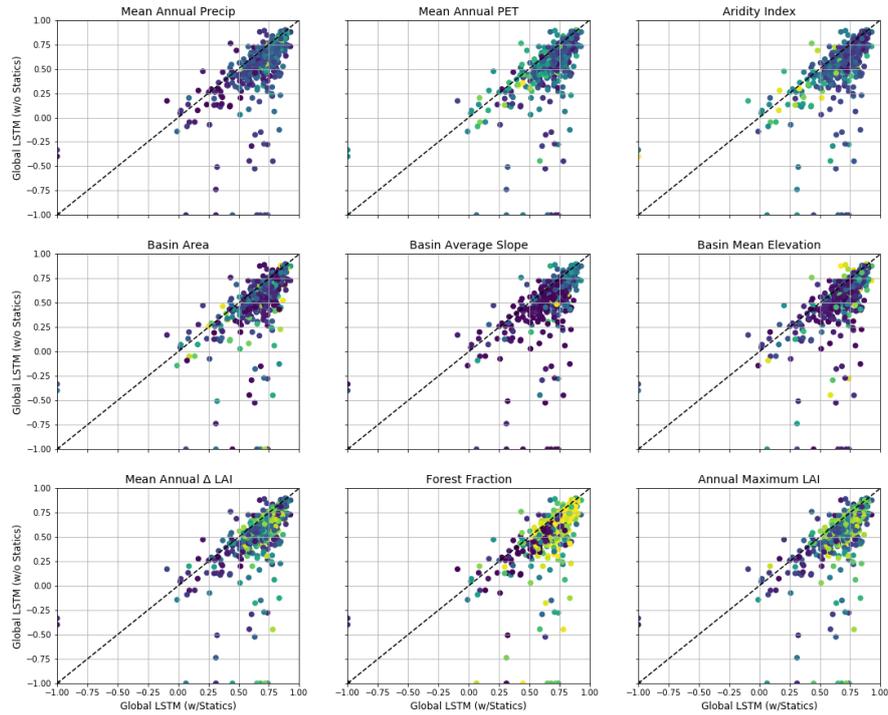


Figure 5. Scatterplots of the LSTM NSE scores in each basin with vs. without static catchment attributes as model inputs. Colors indicate the relative values of a sub-selection of the static catchment attributes from **Table 1** - each subplot has a different colorscale depending on the absolute magnitudes of the specific attributes data. It is the relative values of the attributes that we care about here. There are no apparent direct relationships between the values of different catchment attributes and basins where adding catchment attribute data hurts model performance.

308 understanding of catchment behaviors should result in better out-of sample predictions.
 309 In reality, it is data-driven models that have consistently given increasingly better pre-
 310 dictions. From a more optimistic perspective, ML benchmarking experiments like the
 311 one in this paper show that there are probably organizing theories about watersheds yet
 312 to be discovered, since machine learning models are able to find informative patterns in
 313 multi-basin datasets that our current models don't reproduce.

314 The power of big data and machine learning for problems like this is that such tech-
 315 niques can synthesize information from multiple sites and situations into a single model.
 316 As an example, if we were to want to simulate catchment behavior under nonstationary
 317 conditions (e.g., evolving climate), then a single LSTM trained to recognize and distin-
 318 guish different types of hydrological behavior (as shown here) will have a larger range
 319 of conditions where it can be expected to remain realistic than a model calibrated to a
 320 past conditions in only a single basin.

In our opinion, the most effective strategy moving forward will probably be theory-guided data-science Karpayne et al. (2017). There are now numerous strategies across scientific disciplines that allow for meaningful fusions of domain knowledge with machine learning and other algorithms for learning and predicting directly from data. Adopting approaches like this will be critical moving forward.

6 Code and Data Availability

CAMELS data, including SAC-SMA simulations, are available from NCAR at <https://ral.ucar.edu/solutions/products/camels>. National Water Model reanalysis data are available from the NOAA Big Data Repository at <https://registry.opendata.aws/nwm-archive/>. All code used for this project is available at https://github.com/kratzert/lstm_for_pub.

Acknowledgments

The project relies heavily on open source software. All programming was done in Python version 3.7 (van Rossum, 1995) and associated libraries including: Numpy (Van Der Walt, Colbert, & Varoquaux, 2011), Pandas (McKinney, 2010), PyTorch (Paszke et al., 2017) and Matplotlib (Hunter, 2007). This work was supported by Bosch, ZF, and Google. We thank the NVIDIA Corporation for the GPU donations, LIT with grant LIT-2017-3-YOU-003 and FWF grant P 28660-N31.

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