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12 **Probability of Detection and Multi-Sensor Persistence of** 13 **Methane Emissions from Coincident Airborne and Satellite** 14 **Observations**

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21

22 **Abstract**

23 Satellites are becoming a widely used measurement tool for methane detection and
24 quantification. The landscape of satellite instruments with some methane point-source
25 quantification capabilities is growing. Combining information across available sensor platforms
26 could be pivotal for understanding trends and uncertainties in source-level emissions. However,
27 to effectively combine information across sensors of varying performance levels, the probability
28 of detection (POD) for all instruments must be well characterized, which is time-consuming and
29 costly, especially for satellites. In August of 2023, we timed methane-sensing aerial surveys from
30 the Global Airborne Observatory (GAO) to overlap with observations from the NASA Earth
31 Surface Mineral Dust Source Investigation (EMIT). We show how these co-incident observations
32 can be used to determine and verify the detection limits of EMIT and to develop and test a multi-
33 sensor persistence framework. Under favorable conditions the 90% probability of detection at 3
34 m/s for EMIT is 1060 kg/hr. We further derive a Bayesian model to infer probabilistically
35 whether non-detected emissions were truly off, and we use this model to assess the intermittency
36 of emissions across GAO and EMIT. Time-averaged emission rates from persistent sources can
37 be underestimated if POD is not characterized and if differences in POD across multi-sensor
38 frameworks are not properly accounted for.

39 **Keywords**

40 Methane, EMIT, Remote Sensing, Point Source Emissions, Persistence, Probability of Detection

41 **Synopsis**

42 In this study we coordinated methane-sensing aerial surveys to overlap with observations from a
43 similar satellite instrument in an area with large and frequent methane emissions. We use these
44 data to show how these coordinated observations can be used to determine the detection limits of
45 the satellite instrument and to develop and test a multi-sensor methane plume persistence
46 framework.

47

48 **Introduction**

49

50 Reducing methane emissions has received increased attention for addressing global climate
51 change, due to methane's short lifetime and powerful radiative forcing (Etiman et al., 2016;

52 Ocko et al., 2021). In 2021, 150 nations signed the Global Methane Pledge with the goal to
53 reduce emissions 30% by 2030 (Global Methane Pledge). Reducing emissions by this magnitude
54 is both ambitious and critical for achieving global climate targets and requires finding near-term
55 mitigation solutions. In response, and in parallel, to the Global Methane Pledge, efforts to
56 increase monitoring of methane emission sources have been proposed and prototyped, including
57 the UN International Methane Emissions Observatory (IMEO) Methane Alert and Response
58 System (MARS; UNEP 2022), the United States Environmental Protection Agency's updated oil
59 & gas rule (Environmental Protection Agency 2024), including provisions reporting for super-
60 emitting sources (localized emissions above $100 \text{ kg CH}_4 \text{ h}^{-1}$), the European Union's proposed
61 new methane rule (European Commission 2020), the State of California's new oil&gas rules
62 (Greenhouse Gas Emission Standards for Crude Oil and Natural Gas Facilities 2017), among
63 other regulations and initiatives. Satellites have demonstrated the capability of detecting and
64 quantify methane emissions at the scales relevant to these initiatives (Jacob et al., 2022).
65 Understanding and assessing the performance of satellite technologies is therefore critical for
66 evaluating their ability to address near-term climate goals.

67
68 Some passive remote sensing technologies use the shortwave infrared portion of the
69 electromagnetic spectrum for column methane concentration quantification, which can then be
70 used for methane detection for certain classes of high-emitting sources. In particular, one class of
71 passive remote sensing technology, known as imaging spectrometers, measures reflected and
72 backscattered radiance across visible to infrared wavelengths (typically 400-2500 nm) at medium
73 spectral resolution (typically 5-15 nm). There are many imaging spectrometers currently on orbit
74 (PRISMA, EnMAP, EMIT, GaoFen5) that have demonstrated methane sensing and localized
75 super-emitter detection capabilities (Guanter et al. 2021, Roger et al. 2024, Thorpe et al. 2023,
76 He et al. 2023). This paper will specifically focus on the NASA Earth Surface Mineral Dust
77 Source Investigation (EMIT) instrument, onboard the International Space Station (ISS) that has
78 been active since late 2022. EMIT builds on decades of imaging spectrometer development at
79 NASA Jet Propulsion Laboratory, including the Next Generation Airborne Visible/Infrared
80 Imaging Spectrometer (AVIRIS-NG) and the Global Airborne Observatory (GAO), both of
81 which have been leveraged for large scale surveys of super-emitters across oil&gas, solid waste,
82 and livestock sectors (Duren et al., 2019; Cusworth et al., 2022). EMIT, as well as any imaging
83 spectrometer technology, or any other passive remote sensing technology capable of methane
84 detection (e.g., GHGSat, Sentinel-2, LandSat-8, WorldView-3), is limited to detecting a subset of
85 all emission sources. This detection limit is characterized by an instrument's signal-to-noise
86 (SNR) ratio, its spectral resolution, its spatial resolution, and the environmental conditions at the
87 time of observation. For this expanding suite of methane sensing technologies to be used
88 together to understand and reduce methane emissions, the performance, most importantly the
89 detection limit, of these instruments must be well characterized.

90
91 Detection limits for remote sensing of methane are typically reported as the Minimum Detection
92 Limit (MDL) or the Probability of Detection (POD). The MDL can be estimated theoretically for
93 an instrument of estimated column measurement precision, spatial resolution, or ground
94 sampling distance (GSD), for certain environmental conditions (Jacob et al. 2016). POD assigns
95 probabilities of detection for an observing system at specific emission rate levels (Conrad et al.
96 2023). POD is best calculated from real observations, preferably controlled release experiments,
97 where detection for an observing system is evaluated against a wide range of known release

98 rates. Derived POD models from empirical studies are more representative of the true
99 performance of an observing system, including algorithms or manual processes deployed for
100 CH₄ plume detection. However, they require, at minimum, dozens of observations at known
101 release rates, preferably across a set of real-world observing conditions. Controlled release
102 experiments are time consuming and costly to execute, especially for satellites, where
103 observations are typically limited to a single overpass per day, and repeat overpasses are set by
104 an observing system's sample revisit interval.
105

106 In addition to different instruments with different detection limits, multiple instruments are now
107 being used in combined multi-scale efforts to assess the total methane impact and persistence of
108 individual facilities (Cusworth et al., 2021; Guanter et al., 2024). Persistence is a metric of how
109 frequently a source emits methane and is crucial for calculating the lifetime methane contribution
110 of a source. By combing data from multiple instruments, we can increase the number of
111 observations of a source and therefore improve persistence characterization. However, when one
112 source is measured at different times by many different instruments with different probabilities
113 of detection it can be difficult to tell if a source has stopped emitting or if the emission is simply
114 being missed by the instrument.
115

116 Here we show how to generate a POD model for a satellite instrument (EMIT) efficiently using
117 coincident airborne (GAO) under flights with an airborne instrument whose detection and
118 quantification performance are well characterized. While these coincident observations are still
119 difficult to coordinate, they result in more efficient acquisition of observation samples required
120 to estimate a POD model. We demonstrate an EMIT POD model based on GAO under flights to
121 be consistent with theoretical estimates. This POD model is used to create a new multi-sensor
122 persistence framework from EMIT and GAO observations in the Permian Basin in August of
123 2023. This framework allows for better probabilistic evaluation of EMIT non-detections for
124 sources where airborne observations showed previous emission activity and shows the
125 importance of POD when analyzing source trends using multiple sensors.
126

127 **Methods And Data**

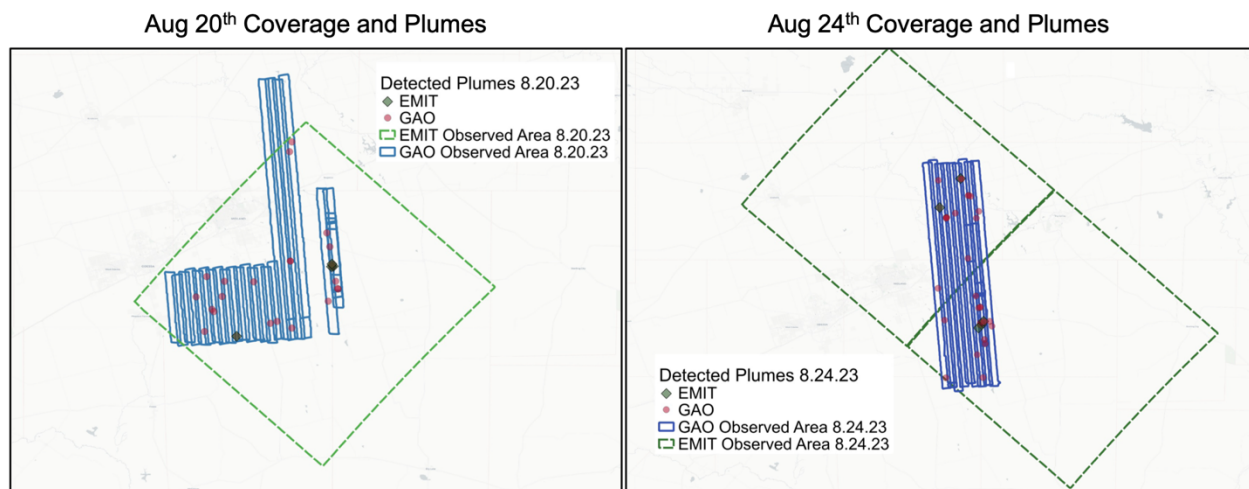
129 *Data*

130 This study is comprised of data from two imaging spectrometers, EMIT and GAO. Both imaging
131 spectrometers measure radiance between 400 and 2500 nm at roughly 5 nm spectral spacing for
132 GAO and roughly 7 nm for EMIT. GAO has a swath width and pixel size that vary with the
133 altitude of the aircraft; however, for this study the swath width was ~3 km and the pixel size was
134 5 m. EMIT orbits at about 400 km above Earth's surface. EMIT images are generally 80 km by
135 80 km and it can collect continuous images along track. The pixel resolution of EMIT can vary
136 depending on the height of the ISS, but is generally 60 m.
137

138 On August 20th and 24th 2023, EMIT observed large areas of the Permian Basin and we
139 coordinated GAO observations to coincide with the EMIT overpasses. The Permian Basin is a
140 target rich environment that has reliably been observed with a high density of large, super-
141 emitting methane plumes. It is also a relatively arid region with a homogenous background, little
142 urban development, and few heavily vegetated areas. These conditions make it a good area to test

143 and compare the GAO and EMIT instruments for methane detection. In addition, these
144 conditions are similar to the conditions where GAO was repeatedly evaluated against blinded
145 controlled releases (Casa Grande, Arizona; El Abbadi et al., 2024).

146
147 The field deployment of GAO was designed to ensure that GAO and EMIT observed at least one
148 plume at the same time. Many plumes in the Permian Basin are intermittent (Cusworth et al.,
149 2021); however, there are a few exceptions, including persistent activity at some gas processing
150 plants. To better ensure coincident observation of at least one plume, we targeted a large
151 persistently emitting gas processing plant (31.845285°, -101.77253°) as our primary target. For
152 the hour surrounding the predicted EMIT observation, we repeatedly surveyed this gas
153 processing plant. For the remainder of the flight day, GAO surveyed additional high priority
154 regions within the predicted EMIT observation area. Beyond these co-incident observations,
155 GAO surveyed the same general areas on Aug. 16, 17, 19 and 21. The additional data helped us
156 to identify persistent sources for the EMIT POD assessment described later. Figure 1 shows the
157 EMIT and GAO coverage for the 20th and 24th. In addition, we have detected and quantified
158 plumes observed by EMIT across its observing record.
159
160



161
162 **Figure 1.** Map of EMIT and GAO coverage on August 20th 2023 (left panel) and August 24th
163 2023 (right panel) as well as detected plumes.
164

165 *Methane Emission Detection and Quantification Methods*

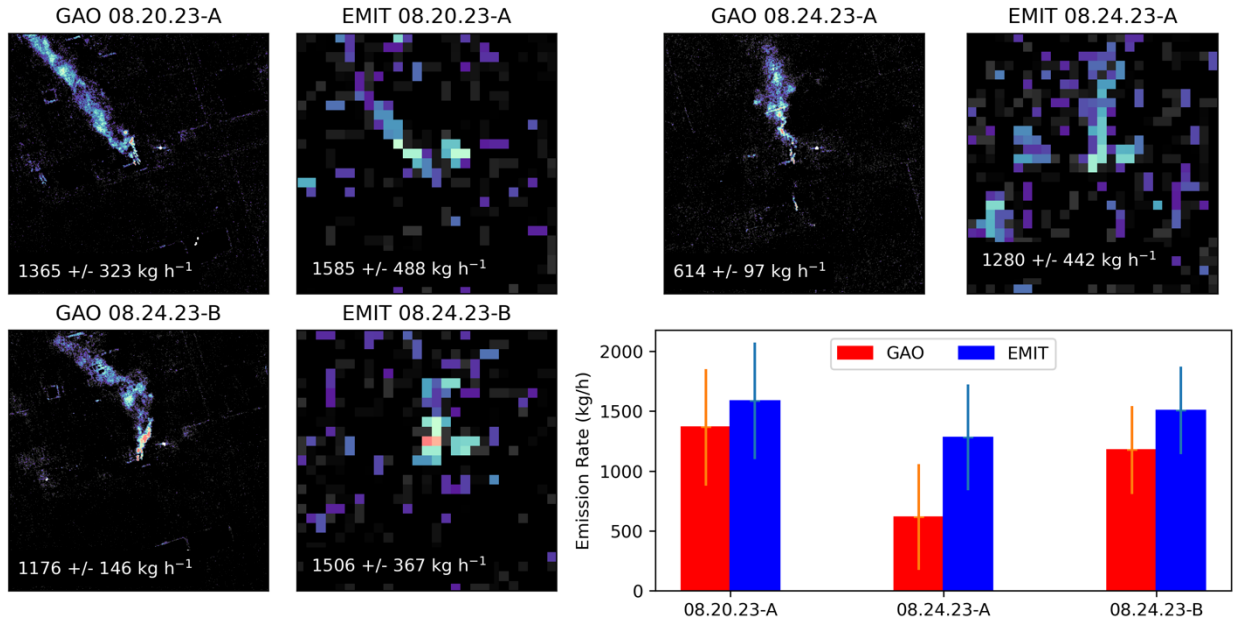
166
167 Both the GAO and EMIT data were processed from radiance data to the methane concentration
168 fields using a columnwise matched filter (Thompson et al. 2015, Foote et al. 2021). Plumes were
169 manually identified by analysts (Carbon Mapper). For GAO, emission rates for each plume were
170 calculated using a concentric circle implementation of the Integrated Mass Enhancement (IME)
171 approach (Duren et al., 2019). In this implementation the IME is calculated iteratively with an
172 expanding radial fetch distance and then averaged across a set of radii starting near the plume's
173 origin until the plume's radial terminal point, or until a maximum fetch of 285 m is reached.
174 Variability in wind estimates and in length normalized IME across radial iterations is propagated
175 to emission rate uncertainty. This GAO quantification approach has been shown to provide

176 results that are correlated and in aggregate unbiased with metered emission rates in controlled
177 release experiments (El Abbadi et al., 2024).

178
179 For EMIT we build on the approach introduced in Thorpe et al (2023). Specifically, we calculate
180 the IME of all plume pixels starting from the plume origin and extending to the plume's terminal
181 radial point or maximum fetch of 2500 m. Source emission rate is quantified by dividing this
182 IME by the fetch and multiplying the by 10-m wind speed. Uncertainties in wind, IME, and
183 plume length are all propagated to the total emission rate. IME uncertainty is the sum of retrieval
184 and delineation uncertainties, which are derived from the variability in retrieved local
185 background concentrations and the IME variability across plume delineations at fixed L. Length
186 uncertainty is a function of pixel size. The wind uncertainty is the variability in space, which is
187 calculated using the standard deviation from a 9 km window around the source location, and
188 time, which is the standard deviation from a 3 hour window surrounding the plume. For both
189 instruments the wind products used for this analysis came from High Resolution Rapid Refresh
190 (HRRR) 10 m wind product (Dowell et al. 2022).

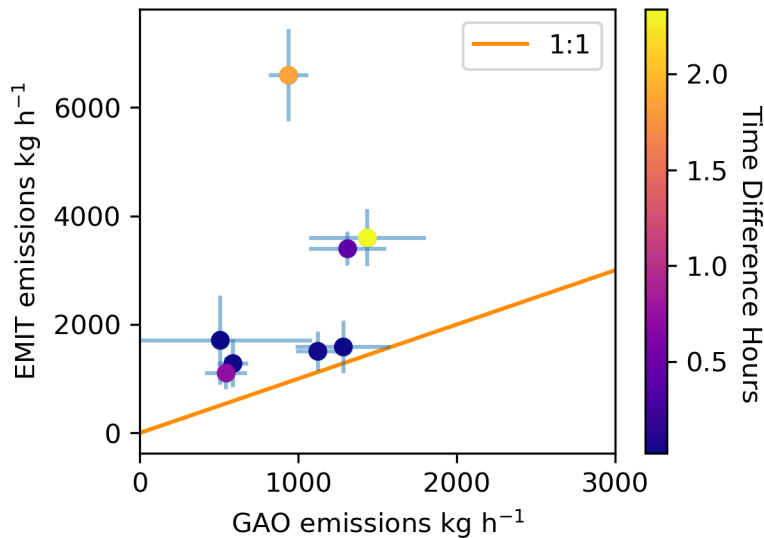
191
192 At the time of this study, no quantification algorithm applied to EMIT has been rigorously tested
193 with controlled releases, however, Figure 2 shows the results of three simultaneous EMIT and
194 GAO detections spaced less than three minutes apart. The GAO and EMIT plume observed 1.4
195 min apart on Aug. 20th (08.20.23-A) show good agreement on both the shape of the plume and
196 the derived emission rates. On Aug. 24th both GAO and EMIT independent detections were
197 observed 2.8 min apart. Source 08.24.23-B also shows close agreement between GAO and
198 EMIT, while source 08.24.23-A shows some discrepancy between GAO and EMIT. The
199 discrepancy could be due to variable wind speeds, even under near simultaneous observation, the
200 shapes of the plumes for source 08.24.23-A suggestion changing wind directions between GAO
201 and EMIT overpasses.

202



203
 204 **Figure 2.** The images are methane concentration images (matched filter outputs) from EMIT and
 205 GAO for the three plumes measured with in 3 minutes of one another. The emission rate for each
 206 plume is included on the image as well as displayed on the bar chart on the bottom right.

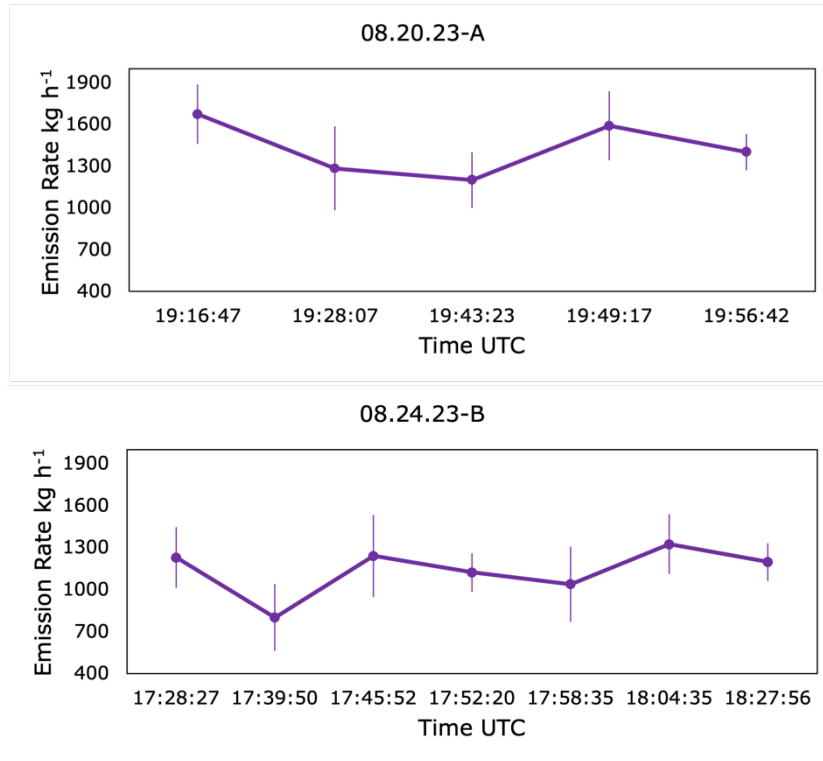
207
 208
 209 An additional six plumes were detected and quantified between GAO and EMIT on Aug 20th and
 210 24th, though with more temporal spacing. This resulted in large difference in quantified emission
 211 rates between GAO and EMIT overpasses (Figure 3).



212
 213 **Figure 3.** Parity plot between GAO and EMIT for sources measured on the same day by each
 214 instrument. The points are colored by the time difference between the GAO and EMIT
 215 observation.
 216

217 This discrepancy may be due to variability of individual sources. For example, Figure 4 shows
 218 results of GAO emission quantification at the targeted gas processing plant that was observed on

219 Aug 20th by GAO (5 times within a 40-minute period) and EMIT and again by just GAO on
 220 August 25th (8 times within a 60-minute period). On the 20th, quantified emission rates by GAO
 221 varied as much as 28% within 12 minutes. On the 24th, quantified emission rates varied as much
 222 as 43% in 11 minutes. Emissions over time, even short periods of time, can vary therefore only
 223 observations that are at nearly the exact same time are useful for direct comparison.
 224



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Figure 4. Emission rate time series from multiple GAO observations at the targeted gas processing plant on Aug. 20th and Aug. 24th 2023.

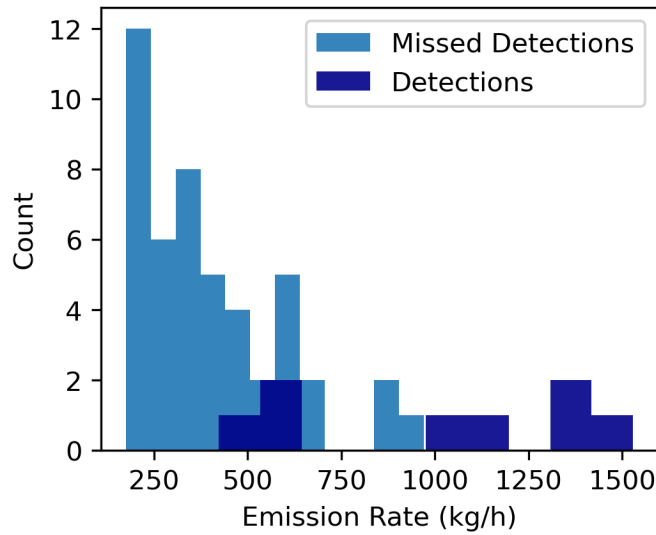
233 **Results and Discussion**

234

235 *Probability of Detection*

236 POD is generally empirically estimated using a sampling of plumes that are above, at, and below
 237 the detection limit of the instrument using controlled emission releases (Conrad et al., 2023).
 238 Though not a controlled test environment, on Aug 20th and 24th GAO and EMIT were able to
 239 sample a distribution of plumes that were above and below EMIT’s detection limits (Figure 5).
 240 However, while we had very close to simultaneous acquisitions over our main target, for the rest
 241 of the area surveyed by GAO there could be as much as a 3-hour time difference between when a
 242 source was observed by GAO and EMIT. This time difference can make a direct comparison of
 243 emission rates challenging, but for POD we can tolerate higher emission rate variability if the
 244 emissions are significantly above or below the detection limit. For observations near the
 245 detection limit we may be incurring some error due to time variability and this error will have to

246 be corrected for as more data become available. Sources can also be highly intermittent even
 247 within a few hours, therefore we selected sources where we had high confidence of continuous
 248 emission for the duration of the campaign. High confidence in source persistence is critical for
 249 classifying EMITs non-detections resulting from the detection limit and not due to potential
 250 short-duration emission events. To build this confidence in persistence, we used GAO data
 251 collected on August 16th, 17th, 19th and 21st that covered roughly 1900 km² or 15-30 % of the
 252 EMIT area. If the source was emitting on all overpasses and has at least three overpasses then we
 253 considered the source to be persistent and we assumed the source was emitting at the time of the
 254 EMIT acquisition. If the source was only present in one image, then we considered that source to
 255 be intermittent and excluded it from the probability of detection analysis. Some sources had
 256 multiple overpasses by GAO on the 20th and 24th, for these sources we use the emission estimate
 257 that is closest in time to the EMIT acquisition. This left us with a total of 55 detected plumes at
 258 sources identified by GAO, 9 of which were detected by EMIT and 46 missed by EMIT (Figure
 259 5).



260
 261
 262 **Figure 5.** Detection and missed detection by EMIT from the coincided GAO/EMIT acquisition.
 263 The detects/missed detects are binned by emission rate.
 264
 265

266 POD is the probability that an instrument, retrieval, and detection algorithm detects a methane
 267 plume given the emission rate, the wind speed, the solar and albedo properties of the location,
 268 and the instrument properties. This can be summed up in theoretical model developed by Conrad
 269 et. al., 2023 (here after referred to as Conrad et.al.) that takes the following form:
 270

$$271 \quad x = \Phi_7 * \frac{(Q - \Phi_1)^{\Phi_3}}{(h)^{\Phi_5} * (U - \Phi_2)^{\Phi_6}} \quad (1)$$

$$272 \quad P = 1 - (1 + (x^2))^{-1.5} \quad (2)$$

273 where Q is the emission rate, h is the pixel resolution, and U is the wind speed. Φ is used to
 274 denotate coefficients that will be optimized from the EMIT and GAO data. Signal-to-Noise Ratio
 275
 276

277 (SNR), which is determined by a combination of instrument properties, solar zenith angle, and
 278 the surface albedo, can be added to the denominator as N^{ϕ^4} . However, given that SNR did not
 279 vary in our study this parameter is not used in the calculations. Equation 2 is the inverse link
 280 function, which is specified here as the Burr cumulative distribution function (CDF) but more
 281 generally could be the CDF of any distribution with non-negative support (Conrad et al. 2023).

282

283 We optimized the coefficients by minimizing l in the following equation:

284

$$285 \quad l(\phi, \theta) = \sum_i -(D_i \ln F_i + (1 - D_i) \ln(1 - F_i)) \quad (3)$$

286

287 where ϕ and θ are a pair of predictor and inverse link functions respectively. In this case ϕ is
 288 equation 1 and θ is equation 2. D_i represents a successful detect (1) or a missed detect (0) by
 289 EMIT for every GAO observation (i). F_i is the output of the predictor and inverse link function
 290 for a given GAO observation (i). The final form of the POD model for EMIT resulted in the
 291 following equation with the inverse link function (equation 2):

292

$$293 \quad x = .0138 * \frac{(Q + .00379)^{1.97}}{(h)^{1.97} * (U + .00064)^{0.88}} \quad (4)$$

294

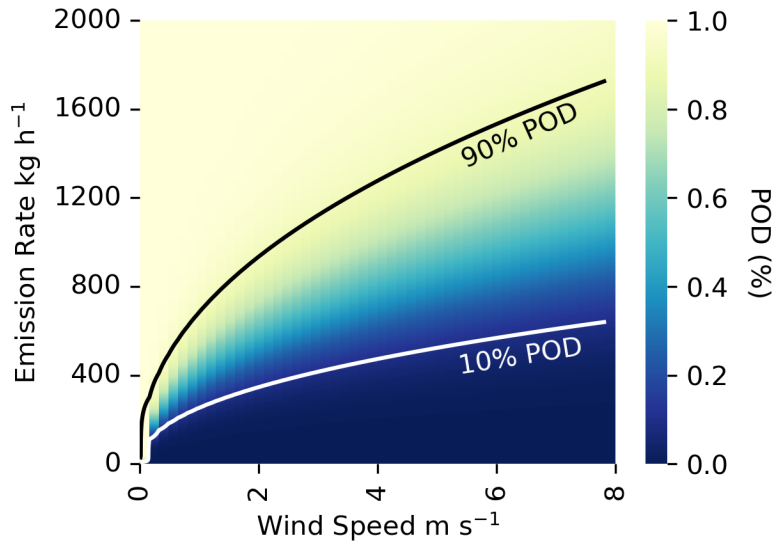
295 We also looked at alternative models from Conrad et. al. and found little substantive difference in
 296 the predicted probabilities.

297

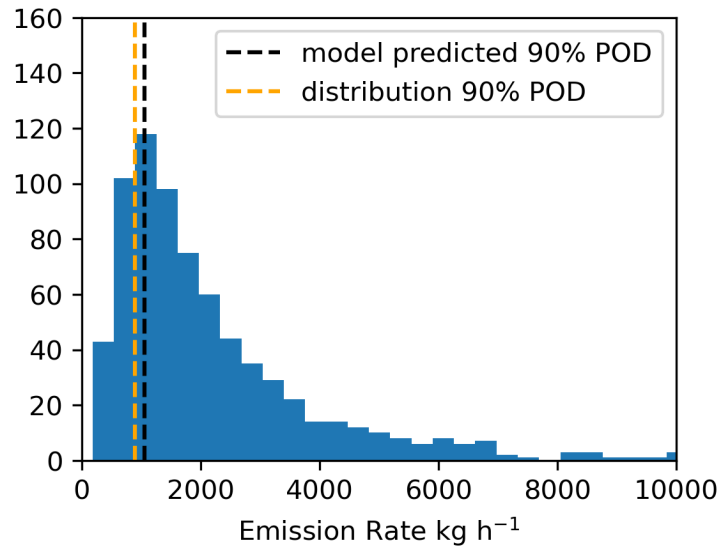
298

299 We find that at a 3 m/s wind speed the 90% POD is 1060 kg/hr (Figure 6). This is consistent with
 300 what we have observed by analyzing a global distribution of emission rates quantified with
 301 EMIT. The most frequent emission rate range for windspeeds below 4 m/s in all plumes collected
 302 and processed by Carbon Mapper from EMIT data, is 900-1200 kg/hr (figure 7). If we assume
 303 that emission rates follow a power law (Sherwin et al., 2024), then we can assume that the point
 304 just past the peak of the histogram is the 90% POD and all emissions below the peak are not
 305 representative of the true distribution of emissions but rather the partial detection limit of the
 306 instrument. The good agreement between the modeled 90% POD and the observed emission
 307 peak indicates that the model is likely representative of the performance of the instrument. The
 308 theoretical minimum detection assumptions from Jacob et. al. 2016 predicts the MDL to be 244
 309 kg/hr for a 3 m/s wind speed. We find that this emission rate results in a 2% POD, which is to be
 310 expected as the MDL represents the theoretical bottom limit. While this POD model aligns with
 311 independent methods, we do caution that the concentration and detection methods and the
 312 limited sample size may affect its global applicability. Methane concentration retrievals methods
 313 and plume detection methods can also affect the POD. The POD presented here is only
 314 applicable within the methods presented in this paper; a different set of detection methods
 315 applied to the EMIT instrument could result in a different POD estimate. In addition, the small
 316 amount of data and the limited geography of these data may bias the results and a larger and
 317 more diverse data set is crucial to creating a better constrained model. However, this analysis
 318 demonstrates how these types of data can be used to characterize the performance of satellite
 319 instruments when controlled release data is not available.

320



321
 322 **Figure 6.** POD heat map for EMIT, windspeed is on the x-axis, emission rate on the y-axis, and
 323 the colors represent the POD. The 90% POD and 10% POD line are displayed for reference on
 324 the figure.



325
 326
 327 **Figure 7.** Distribution of all quantified methane emission from EMIT under 4 m/s windspeeds at
 328 time of analysis ($n = 735$, bins = 50). The Model predicated 90% POD is the 90% POD at 3 m/s
 329 that comes from the model in equation 4. The distribution 90% POD is where we estimate the
 330 EMIT distribution starts to diverge from a theoretical true distribution.

331
 332
 333 *Assessing persistence using multiple sensors*

334 Persistence, or plume detection frequency at the source level, is a key metric for understanding
 335 and quantifying methane emissions. Persistence provides information on how frequently a given
 336 source or area likely needs observation to reliably detect a plume and it helps us to quantify the
 337 total methane contribution of a source. A large plume from a highly intermittent source may

338 contribute less methane than a small but persistent source over the sources' lifetimes. Calculating
 339 persistence becomes acutely difficult for multi-sensor applications with varying POD
 340 characteristics. For example, a persistently emitting facility at a low emission rate, may be
 341 detected by a low detection limit instrument, but not a high detection limit instrument. Not
 342 accounting for instrument differences would bias persistence estimates for that theoretical
 343 facility.

344
 345 We propose a prototype multi-sensor persistence algorithm, based on empirical POD information
 346 using Bayesian inference. Calculating multi-sensor persistence requires decomposing the number
 347 of instrument overpasses (N) into two components: overpasses that can be used to conclusively
 348 calculate persistence (N_c) overpasses that cannot be used to conclusively calculate persistence
 349 (N_N), where $N = N_c + N_N$. N_N includes overpasses where observations may have been obscured
 350 (e.g., cloudy scenes), but may also include overpasses where one lacks confidence that a non-
 351 detection truly captured reality (i.e. the non-detect was due to detection limits rather than a source
 352 that stopped emitting). This lack of confidence can be estimated probabilistically: here the goal is
 353 to estimate the probability that a source is emitting CH₄ (*on*) given that an observation was made
 354 without a detection (-), here written as $p(\text{on} | -)$. Using Bayes's Theorem, this is explicitly
 355 estimated using the following form:

$$357 \quad p(\text{on} | -) = \frac{p(- | \text{on}) p(\text{on})}{p(- | \text{on}) p(\text{on}) + p(- | \text{off}) p(\text{off})} \quad (5)$$

358
 359 where $p(- | \text{on})$ represents the probability of not detecting a source that is emitting. This value
 360 is estimated using an empirical POD curve derived for an instrument using Equations 1 and 2:

$$362 \quad p(- | \text{on}) = 1 - POD^I(q^*, u) \quad (6)$$

364 where POD^I represents a unique POD function for instrument I , and q^* is a representative
 365 emission rate for the emitting source. This value would ideally be the emission rate at the time of
 366 observation. However, in practice it is impossible to estimate this value given that the
 367 observation resulted in no detection. Instead, one can assume this value, possibly using a
 368 distribution of previously estimated emission rates at that source. The value $p(- | \text{off})$
 369 represents the probability of not detecting a source that is off. This value can be estimated by the
 370 true negative rate (TNR), which is a function of true negative (TN) and false positive (FP)
 371 detections, derived from controlled release or other validation experiments:

$$373 \quad TNR = \frac{TN}{TN + FP} \quad (7)$$

374
 375 The values $p(\text{on})$ and $p(\text{off})$ represent prior probabilities that an emission source is emitting or
 376 not, respectively.

377
 378 Assumptions on prior probability distributions influence estimation of $p(\text{on} | -)$. We show two
 379 applications of this framework under differing assumptions for $p(\text{on})$. First, we assume $p(\text{on})$ to
 380 be emission persistence (f^*) of that source derived from previous overflights, assuming at least 3
 381 previous overpasses with GAO: $f^* = M/N$, where M = number of detections and N = number of

382 overpasses from previous airborne overpasses. The value $p(off)$ is then estimated as $1-f^*$.
 383 Using these assumptions, $p(on|-)$ reduces to the following form:

$$384 \quad p(on|-) = \frac{(1 - POD^I(\bar{q}, u))(f^*)}{(1 - POD^I(\bar{q}, u))(f^*) + TNR(1 - f^*)} \quad (8)$$

386 Multi-sensor persistence is then estimated using Equation 8 and the following algorithm:

388 Algorithm 1

389 If airborne observations at a source satisfy $N_c > 3$;

390 For observation $i=N+1$ of instrument I at a source:

391 Set $f_{i-1}^* = \frac{M}{N_c}$

392 Set $q^* = \bar{q}$

393 Compute $p(on|-) = \frac{(1-POD^I(q^*,u))(f_{i-1}^*)}{(1-POD^I(q^*,u))(f_{i-1}^*)+TNR(1-f_{i-1}^*)}$

394 If $p(on|-) < 0.5$:

395 $N_c = N_c + 1$

396 Else

397 $N_N = N_N + 1$

398 $f_i^* = \frac{M}{N_c}$

399 Else:

400 No persistence estimate can reliably be computed.

401

402

403
 404 Second, we assume $p(on)$ as the probability defined by an autocorrelative model. Here, this
 405 underlying assumption is that the most recent previous observation at that source is most
 406 predictive of the sources current on/off state. We assume an autocorrelative model of the
 407 following form:

$$408 \quad X_t = a + bX_{t-1} + c[\overline{(X_{t-2}, \dots, X_N)}] \quad (9)$$

409 where X represents the binary outcome of whether a plume was detected at some time of
 410 observation $t \in [1, \dots, N]$. Values a, b, c represent regression coefficients, and $[\bullet]$ represents a
 411 rounding operation. We fit the coefficients of this model using source-level observations from
 412 previous airborne campaigns in the Permian Basin (Cusworth et al., 2022). When trained on the
 413 entire dataset, we find fair predictive ability of this model to estimate the “on” state of a source,
 414 with precision of 0.73, recall of 0.79, and f-1 score of 0.76. We assume $p(on)$ to be the predicted
 415 probabilities from the logistic regression model. There are only 4 permutation of model states
 416 that exist in Equation 10 given the state of the previous overpass (t_{-1}) and overpasses prior to
 417 that (t_{-2+}). Let $\varphi(t_{-1}, t_{-2+})$ be the function that maps previous overpass states to probabilities,
 418 then $\varphi(t_{-1}, t_{-2+})$ takes the following form:

421

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423

$$\varphi(t_{-1}, t_{-2+}) = \begin{cases} 0.72 & \text{if } t_{-1} = 1 \text{ and } t_{-2+} = 1 \\ 0.65 & \text{if } t_{-1} = 1 \text{ and } t_{-2+} = 0 \\ 0.26 & \text{if } t_{-1} = 0 \text{ and } t_{-2+} = 1 \\ 0.19 & \text{if } t_{-1} = 0 \text{ and } t_{-2+} = 0 \end{cases} \quad (10)$$

Therefore, the most recent previous overpass is the largest driver in the proximal state of emission for the source. Using these explicit probabilities, the multi-sensor persistence algorithm takes the following form:

Algorithm 2

If airborne observations at a source satisfy $N_c > 2$;

For observation $i=N+1$ of instrument I at a source:

Set $q^* = \bar{q}$

Compute $p(\text{on} | -) = \frac{(1-POD^I(q^*, u))(\varphi(t_{-1}, t_{-2+}))}{(1-POD^I(q^*, u))(\varphi(t_{-1}, t_{-2+})) + TN R(1-\varphi(t_{-1}, t_{-2+}))}$

If $p(\text{on} | -) < 0.5$:

$N_c = N_c + 1$

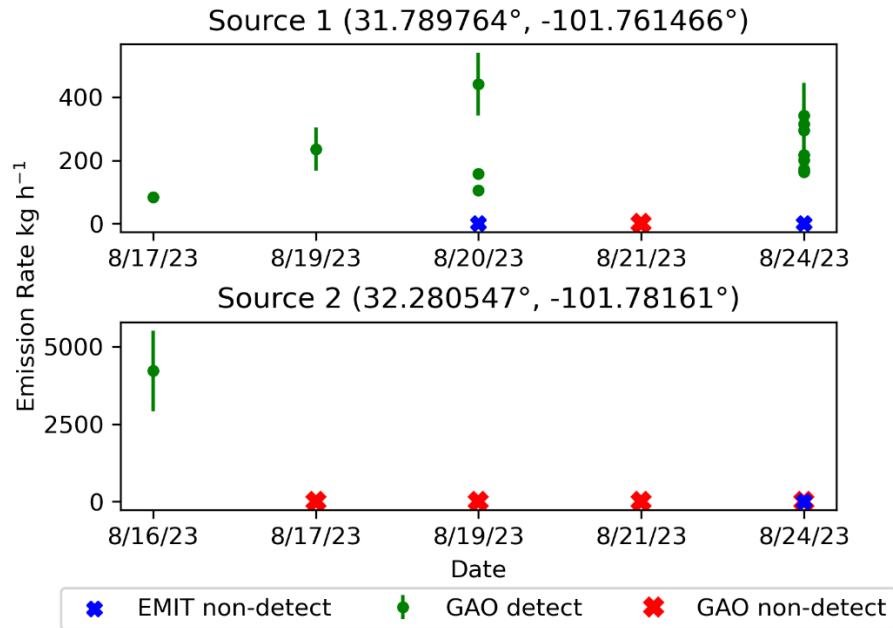
Else

$N_N = N_N + 1$

Else:

No persistence estimate can reliably be computed.

Persistence can impact emissions at a facility or source scale and at a basin scale. In figure 8 we show an example of 2 sources that were observed by EMIT on the Aug 24th but where no plume was detected. One source is truly ‘off’ (Figure 8, source 2) and the other is ‘on’ but below the EMIT detection limit (Figure 8, source 1). Source 1 was observed 4 times by GAO between Aug 17 and Aug 21, and plumes were observed 3 of the 4 times, yielding a persistence of 75%. On Aug. 24th, if we assume EMIT was the only observation, a simple persistence would lead us to recalculate the persistence to be 60% however if we consider the emission rate ($q^* = 227 \text{ kg h}^{-1}$) from the previous airborne observations and the wind speed at the time of the EMIT observation ($u = 5 \text{ ms}^{-1}$), Equation 4 tells us the POD for EMIT at this source is 1%. Given the POD and the prior persistence ($f^* = .75$) this yields a probability $p(\text{on} | -) > 0.5$, meaning that N_N and not N_c was incremented. Therefore, this non-detect was not conclusive enough to make the determination that the source was truly not emitting. This results in the source persistence remaining at 75%. We can confirm this result with the GAO observations from Aug 24th that show the source was indeed emitting but below the EMIT detection limit. Source 2 shows an example of an airborne detection that had a higher emission estimate ($q^* = 4217 \text{ kg h}^{-1}$), if the source had been emitting, Equation 4 tells us that the POD for EMIT would be 99%. In this case, given the prior persistence ($f^* = .25$), $p(\text{on} | -) < 0.5$, providing more confidence that this non-detection truly represented the state of this source, so N_c was incremented the persistence is adjusted to 20%. Again, we can confirm this result with the GAO observations that shows the source was not emitting on this day. For the two examples described above, because they are extreme examples, the autocorrelation prior approach results in the same persistence as the standard simple prior Bayesian persistence.



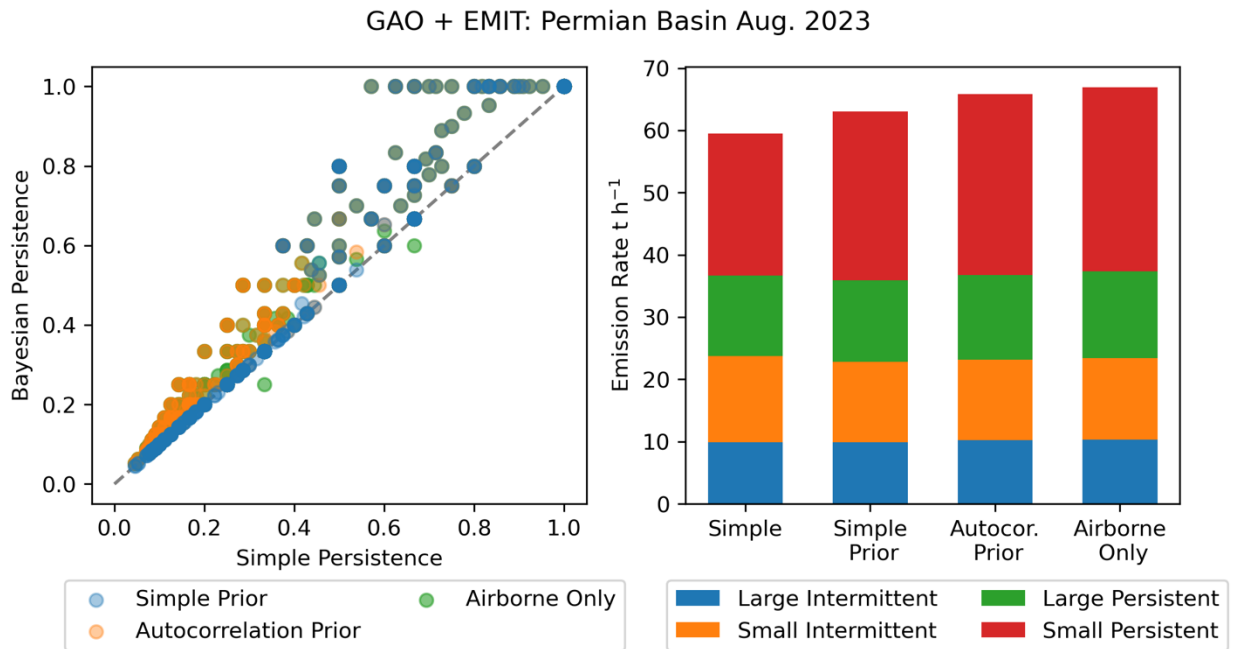
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Figure 8. Time series of two example sources from the GAO/EMIT dataset. Both include EMIT non-detects however for Source 1 the EMIT non-detects are due to EMIT’s detection limit and for Source 2 the EMIT non-detect is due to the source no longer emitting. This distinction is critical for understanding source/facility level methane emission dynamics.

474 The multi-sensor Bayesian approach (regardless of prior choice) for updating persistence will
475 always result in higher persistence estimation than using a straight detection frequency as some
476 non-detects will be considered inconclusive. This is shown clearly in the right panel of Figure 9.
477 However, the choice of prior can also impact the persistence estimation across a large population
478 of sources. The autocorrelation prior (Bayesian multi-sensor persistence with an autocorrelation
479 weighted prior) approach results in higher persistence across the whole population compared to
480 the simple persistence approach (Figure 9). In general, the Autocorrelation approach is less likely
481 to assume confidence in the EMIT non-detects and therefore the autocorrelation prior approach is
482 more like the airborne only persistence (i.e. what would happen if we excluded EMIT entirely).
483 However, where the Autocorrelation approach has confidence in the EMIT non-detects, the
484 sample size increases and provides more confidence in the persistence estimate than the aircraft
485 data alone. The standard Bayesian simple prior (Bayesian multi-sensor persistence with a simple
486 persistence prior) approach is more likely to assume confidence in the EMIT non-detects
487 especially for prior intermittent sources ($f^* < 0.5$) and therefore has the largest effect on
488 persistent sources.

489
490 For the data within our study, we show that not accounting for POD when calculating persistence
491 leads to an underestimate in the total emission estimate, particularly from small persistent
492 sources. In the left panel of Figure 9, we show the total persistence adjusted emission rate for all
493 sources in this study using the simple persistence approach, the multi-sensor persistence
494 approaches, and airborne alone (excluding EMIT data). The simple persistence has a 11%
495 underestimate compared the Autocorrelation approach and a 6% underestimate compared to the

496 standard Bayesian approach. Most of this underestimate comes from the small persistent sources.
 497 The aircraft data alone shows the highest total emission rates but also has the fewest number of
 498 samples per-source and therefore we have lower confidence in the persistence estimates. This
 499 study only represents a short time period of time (< 1 month) but if you extrapolate out quarterly
 500 or annually, and include more EMIT data, the underestimate of the methane emission
 501 contribution from persistent sources would become significantly larger. Therefore, when
 502 assessing facility or basin scale emissions using data from multiple sensors it is crucial that the
 503 POD for each sensor be well characterized, and the proposed multi-sensor persistence framework
 504 be adopted to characterize persistence.
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 509 **Figure 9.** The left panel shows the simple persistence on the x-axis for all sources. On the y-axis
 510 are the two Bayesian models (simple prior and autocorrelation prior) and the Airborne Only (no
 511 EMIT data) persistence. The right panel shows the total persistence adjusted emission rate for all
 512 sources within the study using the 4 different persistence estimation methods from left panel. For
 513 each bar the total emission is broken out by large intermittent ($q > 700$ kg/hr, $f < 0.5$), Small
 514 intermittent ($q < 700$ kg/hr, $f < 0.5$), Large persistent ($q > 700$ kg/hr, $f > 0.5$) and Small persistent
 515 ($q < 700$ kg/hr, $f > 0.5$).
 516
 517

518 **Conclusion**

519
 520 We use two days of coincident EMIT and GAO observations to identify the POD for EMIT,
 521 verify the EMIT emission rates, and demonstrate a multi-scale persistence framework. We show
 522 that under good conditions the 90% POD of EMIT at 3 m/s wind speed is 1060 kg/hr. While we
 523 find generally good agreement between the coincident GAO and EMIT observations, the

524 variability in emissions over time complicates direct comparisons with a small number of
525 measurements. We stress the need for robust controlled release experiments to fully validate the
526 EMIT emissions estimates.

527
528 We also introduce a Bayesian approach for determining source persistence when using multiple
529 sensors with different detection limits. Our coincident data provided a unique dataset with which
530 to test and verify the accuracy of this framework. We show that by adopting the multi-sensor
531 Bayesian approach we avoid underestimating emissions, particularly smaller persistent
532 emissions. Going forward these methods could enable quantification of both basin and facility
533 level emissions and persistence with multiple instruments, provided that each instrument has a
534 well-characterized POD. This framework is increasingly necessary as the number of methane
535 sensing instruments grows. In the coming year more remote sensing technologies are scheduled
536 to come online including Carbon Mapper and MethaneSat (Zandbergen et al. 2022, Hamburg et
537 al. 2022). In addition to satellites there are, and will continue to be, airborne instruments
538 mapping methane plumes. For this expanding suite of methane sensing technologies to be used
539 together to understand and reduce methane emissions, the probability of detection of these
540 instruments must be well characterized and methods to accurately integrate the data, like the
541 proposed multi-sensor persistence estimation method, must be adopted.

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