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Sensitivity of modelled mass balance and runoff to representations of debris and accumulation on the Kaskawulsh Glacier, Yukon, Canada

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Sensitivity of modelled mass balance and runoff to representations of debris and accumulation on the Kaskawulsh Glacier, Yukon, Canada

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ABSTRACT. Runoff from glaciers accounts for half the total freshwater discharge to the Gulf of Alaska, with glacier contributions to streamflow changing as mass loss accelerates. We reconstruct the 1980–2022 mass balance, runoff and water budget of the 70% glacierized Kaskawulsh River Headwaters in Yukon, Canada, using an enhanced temperature-index model driven by down-scaled and bias-corrected reanalysis data. Debris is treated using melt-scaling factors based on site-specific measurements of the critical debris thickness. To estimate accumulation, we apply an elevation-dependent correction based on in-situ measurements. The model tuning approach incorporates observations of the geodetic mass balance and snowlines. We assess model sensitivity to the representation of supraglacial debris and the accumulation bias correction, including treatments of these processes that can be applied in the absence of in-situ data. The representation of debris produces variations <1% in the catchment-wide runoff and water budget. In contrast, accumulation inputs that omit in-situ data produce variations of 33–40% in modelled runoff relative to a catchment-specific correction. This work highlights the value of catchment-specific data and the impact that representations of debris and accumulation can have on modelled runoff.

26 1 INTRODUCTION

27 The downstream hydrological effects of glacier mass loss impact important river systems around the world
28 (e.g. Chesnokova and others, 2020; Huss and Hock, 2018; Bliss and others, 2014; Huss, 2011). In glacierized
29 basins, ice melt exerts an influence on the timing and magnitude of downstream discharge (e.g. Valentin and
30 others, 2018; Addor and others, 2014; Farinotti and others, 2012; Neal and others, 2010) and the physical
31 and chemical characteristics of proglacial streams (e.g. Hood and Berner, 2009), impacting freshwater and
32 near-shore marine ecosystems (e.g. Pitman and others, 2021). Concern for water resources is also mounting
33 in many regions of the world as thinning rates of glaciers outside of the Antarctic and Greenland ice sheets
34 have doubled in recent decades (Hugonnet and others, 2021), and current mass-loss rates suggest that many
35 small glaciers, especially those at mid-latitudes, may disappear entirely by the end of the century (Rounce
36 and others, 2023; Zemp and others, 2019). Quantifying the contributions of glacier melt to catchment-wide
37 water budgets and assessing long-term trends in glacier melt is therefore important, especially as discharge
38 regimes change in response to sustained mass loss (Huss and Hock, 2018). Reconstructing long-term
39 glacier runoff records is challenging in part due to the fact that many catchments in remote, mountainous
40 environments are ungauged. In the absence of in-situ discharge measurements, observations of glacier mass
41 change derived from remote sensing products such as Digital Elevation Models (DEMs) (e.g. Moore and
42 others, 2020; Young and others, 2021a; Foy and others, 2011; Berthier and others, 2010) can be used to
43 estimate the meltwater produced by glacier wastage (La Frenierre and Mark, 2014). Others have employed
44 distributed glacier mass-balance and hydrological models (e.g. Li and others, 2020; Bliss and others, 2014;
45 Immerzeel and others, 2012; Farinotti and others, 2012) to partition sources of runoff and estimate the
46 glacier contribution to catchment-wide discharge. Model challenges persist, however, and generally include
47 high uncertainties in input data as well as observations insufficient to constrain model parameters (van
48 Tiel and others, 2020).

49 Here, we use a distributed mass-balance model to reconstruct the runoff and water budget of a highly-
50 glacierized, ungauged catchment in southwest Yukon. We examine how the use of in-situ observations to
51 parameterize and tune the mass-balance model influences the estimated runoff and water budget compared
52 to alternative parameterizations that omit glacier-specific information and could be applied in data-scarce
53 catchments. In particular, we assess model sensitivity to (1) the representation of supraglacial debris
54 and (2) the accumulation bias correction. Debris on a glacier surface can either enhance or inhibit melt,

55 depending on the critical debris thickness (Østrem, 1959). The representation of debris in mass-balance
56 models has been shown to influence estimated sub-debris ablation rates and mass-balance gradients (e.g.
57 Compagno and others, 2022; Rounce and others, 2021; Juen and others, 2014). Accumulation inputs also
58 generally represent large sources of uncertainty in glacier mass-balance models (e.g. Tarasova and others,
59 2016; Machguth and others, 2009), with model performance depending strongly on the availability of
60 observational data (e.g. Immerzeel and others, 2014). We further assess the sensitivity of the estimated
61 water budget to sources of tuning data including the glacier-wide geodetic mass balance and distributed
62 snowlines delineated from satellite images.

63 2 STUDY AREA

64 The Kaskawulsh Glacier catchment, which we refer to as the Kaskawulsh River Headwaters (Fig. 1), is a
65 highly-glacierized region located within the Traditional Territories of the Kluane, Champagne & Aishihik,
66 and White River First Nations, in the St. Elias Mountains of Yukon, Canada. The catchment is 1704 km²
67 and ~70% glacierized over an elevation range of approximately 750–3500 m a.s.l. The Kaskawulsh Glacier
68 itself is a 70 km-long valley glacier representing ~9% of the glacier-ice volume in the Yukon (Farinotti and
69 others, 2019). The debris-covered terminus marks a drainage divide between the Yukon and Alsek River
70 watersheds, and is the site of a recent drainage reorganization in which meltwater that previously drained
71 to the Bering Sea was abruptly rerouted to the Gulf of Alaska (Shugar and others, 2017). Recent estimates
72 suggest the Kaskawulsh Glacier lost mass at an average rate of -0.46 ± 0.17 m w.e. a⁻¹ between 2007–
73 2018 (Young and others, 2021a), nearly matching the regional mass loss rate estimated for the St. Elias
74 Mountains as a whole (Berthier and others, 2010). Mass loss in the catchment is expected to accelerate
75 in the future as temperatures rise in southwest Yukon, which has already experienced more warming than
76 nearly all other regions in Canada (Bush and Lemmen, 2019). Even under a stable climate, however,
77 estimated ice fluxes on the Kaskawulsh Glacier suggest that the glacier is still in the early stages of
78 dynamic adjustment to sustained mass loss over the last several decades, with a minimum committed
79 terminus retreat of 23 km estimated under the 2007–2018 climate (Young and others, 2021a).

80 3 MASS-BALANCE MODEL

81 The distributed mass-balance model used in this study is adapted from Young and others (2021a), and
82 described only briefly here. Changes to the model introduced in this study include an annually adjusted

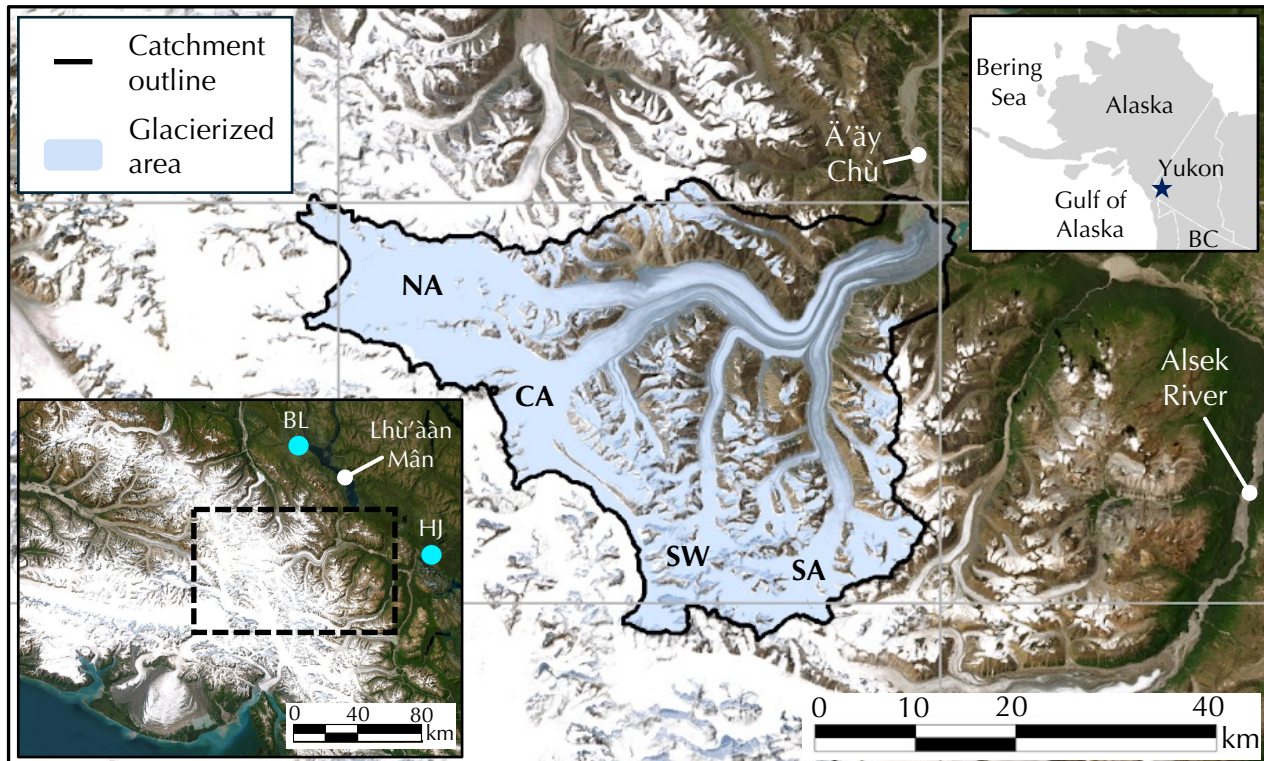


Fig. 1. Study area (blue star, inset upper right) located within the Traditional Territories of the Kluane, Champagne & Aishihik, and White River First Nations. Blue shading indicates the glacierized area, with major tributaries of the Kaskawulsh Glacier labelled: North Arm (NA), Central Arm (CA), Stairway Glacier (SW), South Arm (SA). Regional inset at bottom left shows the locations of two Environment and Climate Change Canada (ECCC) weather stations (cyan circles) located in Burwash Landing (BL) and Haines Junction (HJ). Basemap sources: Esri, Maxar, Earthstar Geographics, and the GIS User Community.

83 surface-elevation scheme and use of distributed snowline observations in the model tuning procedure (see
 84 Robinson, 2024). We also introduce revised parameterizations of debris-covered ice ablation and snow
 85 accumulation, described in §4 and §5, respectively.

86 3.1 Model description

The mass-balance model calculates the distributed climatic mass balance $\dot{b}_{\text{sfc}}(x, y)$ as

$$\dot{b}_{\text{sfc}}(x, y) = \dot{c}_{\text{sfc}}(x, y) - \dot{a}_{\text{sfc}}(x, y), \quad (1)$$

where $\dot{c}_{\text{sfc}}(x, y)$ is the distributed surface accumulation and $\dot{a}_{\text{sfc}}(x, y)$ is the distributed surface ablation. Ablation is approximated as the surface melt (M ; m w.e.), calculated using the enhanced temperature-index model of Hock (1999),

$$M = \begin{cases} (MF + a_{\text{snow/ice}}I)T & \text{if } T > 0^\circ\text{C} \\ 0 & \text{if } T \leq 0^\circ\text{C}, \end{cases} \quad (2)$$

87 where T ($^\circ\text{C}$) is air temperature and I is the potential direct clear-sky solar radiation (W m^{-2}). MF
 88 (m w.e. $3\text{hr}^{-1}\text{ }^\circ\text{C}^{-1}$), a_{snow} and a_{ice} (m w.e. $3\text{hr}^{-1}\text{ }^\circ\text{C}^{-1}\text{ m}^2\text{ W}^{-1}$) are, respectively, the melt factor and radi-
 89 ation factors for snow and ice that are empirically determined during the tuning process.

The refreezing process is accounted for using a thermodynamic parameterization to estimate the total amount of liquid water (from snowmelt or rainfall) that can be retained by percolation and refreezing in the snowpack, referred to as the total potential retention mass P_τ (m w.e.) (Janssens and Huybrechts, 2000). P_τ is approximated as a proportion (P_r) of the total annual precipitation in a given hydrological year (P_{annual} ; m w.e.):

$$P_r = \frac{c}{L} |\min(T_{\text{mean}}, 0)| \frac{d}{P_{\text{mean}}}, \quad (3)$$

where c ($2097\text{ J kg}^{-1}\text{ K}^{-1}$) is the specific heat capacity of ice, L (333.5 kJ kg^{-1}) is the latent heat of fusion Cuffey and Paterson (2010), T_{mean} is the local mean annual air temperature for a given hydrological year, P_{mean} (m w.e.) is the mean annual precipitation over the whole study period (1980–2022), and d is a prescribed thickness of the thermal active layer, set to 2 m (Janssens and Huybrechts, 2000; Young and others, 2021a). The maximum allowable value of the retention fraction P_r is 1, therefore the maximum

Robinson and others:

possible potential retention mass P_τ is equal to the annual precipitation (P_{annual}), since

$$P_\tau = P_r P_{\text{annual}}. \quad (4)$$

While $P_\tau > 0$, any melt that occurs is assumed to refreeze, therefore the maximum amount of refreezing that can occur is capped at P_τ . Once the upper limit of P_τ has been reached, any additional snowmelt or rainfall is assumed to run off (Huybrechts and De Wolde, 1999; Janssens and Huybrechts, 2000) until P_τ is renewed at the beginning of the next hydrological year. Therefore the amount of water that is refrozen (R ; m.w.e.) is related to the available meltwater (M_{snow}) and the potential retention mass (P_τ) at each timestep by

$$R = \begin{cases} M_{\text{snow}} & \text{if } P_\tau \geq M_{\text{snow}} \\ P_\tau & \text{if } 0 \leq P_\tau < M_{\text{snow}}. \end{cases} \quad (5)$$

We follow Bliss and others (2014) in defining glacier runoff, Q_g , as the sum of all sources of runoff over the glacierized area:

$$Q_g = M_{\text{ice}} + M_{\text{snow}} + P_l - R, \quad (6)$$

90 including ice melt (M_{ice}), snowmelt (M_{snow}), and rainfall (P_l) minus the snowmelt and rainfall that is
 91 refrozen (R). Ice melt is further partitioned into melt from glacier ice and melt from superimposed ice
 92 formed during a previous refreezing event. The total catchment runoff is the sum of glacier runoff and
 93 runoff from the non-glacierized area. Snowmelt, rainfall, and refreezing are treated the same over the
 94 non-glacierized area as the glacierized area. Losses from groundwater infiltration and evapotranspiration
 95 are neglected.

96 3.2 Catchment geometry

97 Delineation of the glacierized area within the catchment is based on outlines from the Global Land Ice
 98 Measurements from Space inventory (GLIMS) Randolph Glacier Inventory (RGI 6.0) (RGI Consortium,
 99 2017) (Kaskawulsh Glacier RGI ID: 60-01.16201). The model neglects changes in glacier area over time,
 100 however the surface elevation of the glacierized area is updated annually based on a distributed estimate
 101 of the average annual elevation-change rate between 1977–2018. To generate this estimate, we use DEMs
 102 of the study area from 1977, 2007, and 2018 (Berthier and others, 2010; Young and others, 2021a). We
 103 calculate the time-weighted average annual elevation change on the Kaskawulsh Glacier between the periods

104 1977–2007 and 2007–2018. We generate a smoothed annual elevation-change map for 1977–2018 by fitting
105 a curve to the time-weighted mean elevation change between the two periods in 200 m elevation bins (Fig.
106 S1). The resulting distributed estimate of annual elevation-change is applied to all glaciers in the catchment
107 to get the distributed surface elevation for each year in the study period prior to 2018. In the absence of
108 DEMs after 2018 we assume that the surface is fixed for the remainder of the study period (2018–2022).

109 3.3 Input data

110 The temperature and precipitation data used to drive the mass-balance model are obtained by downscaling
111 and bias correcting the North American Regional Reanalysis (NARR) dataset (Mesinger and others, 2006).
112 NARR data are available beginning in 1979 and include gridded outputs for a suite of meteorological
113 variables at 3-hourly timesteps on a 32 km×32 km grid, downscaled to a 200 m grid over the catchment.
114 Potential direct clear-sky solar radiation (I in Equation 2) is calculated using the Hock (1999) Distributed
115 Enhanced Temperature-Index Model (DETIM), which accounts for the effects of topographic shading,
116 slope, and aspect.

117 3.3.1 Temperature

118 We downscale and bias correct NARR temperature data following the approach of Young and others
119 (2021a). Temperature downscaling involves an interpolation scheme from Jarosch and others (2012) in
120 which a linear regression is used to correlate NARR air temperature and geopotential height within the
121 lower layer of the atmosphere. The slope and intercepts of the linear regression are taken as the local
122 lapse rate and sea-level air temperature, respectively, for each NARR grid point. These lapse rates and
123 air temperatures are then bilinearly interpolated across the model domain at the 200 m grid spacing and
124 used to calculate 2 m air temperature at the gridcell elevation. We adopt monthly temperature bias
125 correction factors from Young and others (2021a) based on air temperatures measured on or proximal to
126 the Kaskawulsh Glacier.

127 3.3.2 Precipitation

Following Young and others (2021a), NARR precipitation is downscaled using a regression-based approach
from Guan and others (2009) that relates NARR surface precipitation to the Easting, Northing and el-
elevation of the coarse NARR gridcells (Fig. S2). Downscaled precipitation is partitioned into rain and

snow using a prescribed temperature threshold of 1°C. Snow accumulation is bias corrected by multiplying downscaled accumulation ($c_{ds}(x, y, t)$) by an elevation-dependent correction factor $C(z)$:

$$c_{bc}(x, y, t) = c_{ds}(x, y, t) C(z). \quad (7)$$

128 The accumulation bias-correction $C(z)$ is determined from the ratio between measured and downscaled
129 accumulation as a function of elevation (see §5).

130 4 SITE-SPECIFIC TREATMENT OF SUPRAGLACIAL DEBRIS

131 4.1 Debris thicknesses on the Kaskawulsh Glacier

132 We use a distributed estimate of debris thickness for the Kaskawulsh Glacier from a global dataset (Rounce
133 and others, 2021) (Fig. S3) but discard the associated critical debris thickness of 13 cm. Studies that have
134 measured the critical debris thickness (e.g. Juen and others, 2014; Mattson, 1993; Khan, 1989; Østrem,
135 1959) have found values <5 cm, including a 1966 study on the Kaskawulsh Glacier where measurements
136 indicated a critical debris thickness of approximately 4 cm (Loomis, 1970). Thus, the estimated critical
137 thickness of 13 cm in the global dataset is likely too high and would suggest enhanced melt along the medial
138 moraines (Fig. 2d), which are instead observed to be raised above the adjacent clean-ice surface. We use
139 in-situ measurements of melt on clean and debris-covered ice to determine a site-specific critical debris
140 thickness with which to correct the sub-debris melt-enhancement factors from the global dataset (Rounce
141 and others, 2021).

142 4.2 Field experiment

143 Seven ablation stakes were installed on or proximal to the medial moraine at the North Arm–Central Arm
144 confluence (Fig. 1): one in clean ice, one in dirty ice (DI00), and five in debris-covered ice (DB01–DB04)
145 (Fig. 2a). Circular frames were installed around the ablation stakes and filled with fine-grained sediment
146 (Fig. S5) to control the debris thickness (between 1–4 cm-thick debris), with the exception of one stake
147 which was installed on the nearby medial moraine in debris approximately 7 cm thick. Debris thicknesses
148 and stake heights were measured on 19 July 2022 when the stakes were installed and again on 31 August
149 2022. Stake DB01 had formed a depression in the surface approximately 5 ± 3 cm deep, while stakes DB02,
150 DB03, and DB04 had developed ice-cored debris cones ranging in height from 40 ± 10 cm to 110 ± 30 cm

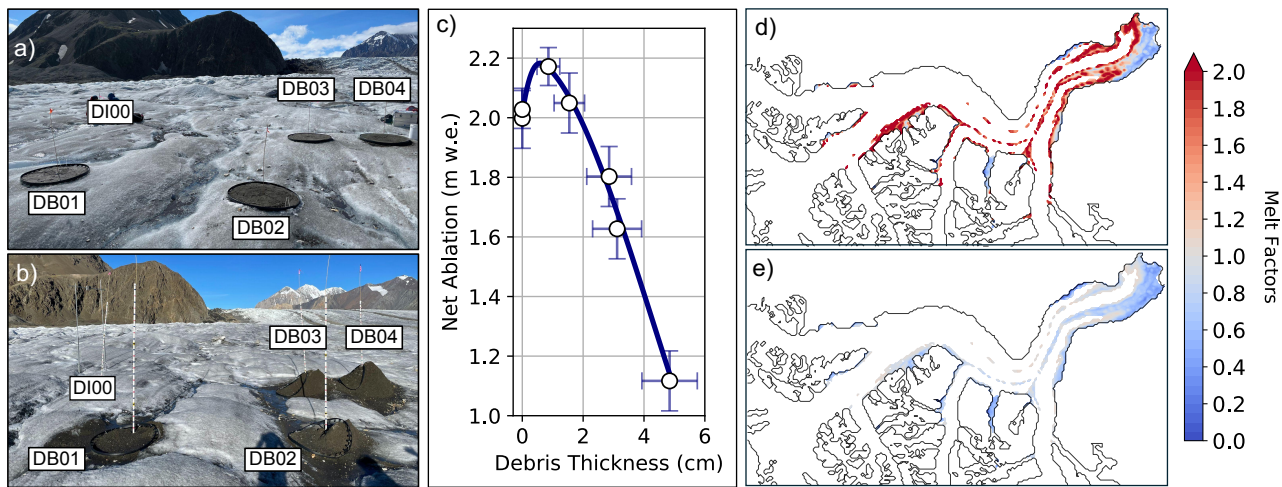


Fig. 2. Overview of field experiment to measure the critical debris thickness and resulting melt factors. Ablation stakes were installed in dirty ice (DI00) and debris-covered ice (DB01–DB04) on 19 July 2022 (a) and measured on 31 Aug 2022 (b). Measured debris thicknesses and net ablation are listed in Table S1. c) Relationship between debris thickness and ablation on the Kaskawulsh Glacier. d) Original sub-debris melt-scaling factors for the Kaskawulsh Glacier from Rounce and others (2021) with a critical thickness of 13 cm. e) New site-specific sub-debris melt-scaling factors generated using a critical thickness of 1.9 cm, determined from the curve in panel (c).

151 (Fig. 2b).

152 Over the course of the ~six-week experiment, debris cover within the framed areas thinned due to
 153 washout from surface streams and downslope redistribution as the cones developed. Average debris thick-
 154 nesses from July 19 to August 31 2022 were estimated using a positive degree-day weighted average of the
 155 initial and final debris thickness measurements (Table S1). Data from the field experiment were interpo-
 156 lated using a cubic spline to construct a site-specific “Østrem curve”, which we then apply to the whole
 157 Kaskawulsh Glacier to generate new sub-debris melt-scaling factors (Fig. 2c). From this curve, the critical
 158 debris thickness was determined to be 1.9 ± 0.7 cm, with maximum melt occurring at a debris thickness
 159 of 0.6 ± 0.3 cm. For debris thicknesses outside our measurement range (>5 cm), we adopt the same debris
 160 thickness–ablation relationship as Rounce and others (2021) (Fig. S6).

161 4.3 Impact of site-specific sub-debris melt factors

162 Our estimate of the critical debris thickness represents a substantial reduction from the estimate of 13 cm in
 163 the global debris dataset (Rounce and others, 2021). The new site-specific melt factors predict differential
 164 ablation that is more consistent with the observed morphology of the medial moraines. Sub-debris melt

165 is inhibited over roughly 82% of the debris-covered area, compared to 37% melt-inhibited area estimated
166 by Rounce and others (2021). For debris thicker than 35 cm ($\sim 10\%$ of the debris-covered area), the site-
167 specific melt factors and the melt factors from the global debris dataset (Rounce and others, 2021) are
168 nearly identical.

169 5 SITE-SPECIFIC ACCUMULATION BIAS CORRECTION

170 5.1 In-situ accumulation measurements

171 In April/May from 2007–2022, 27 sets of measurements of snow depth and density were made at 18 different
172 locations within the Kaskawulsh River Headwaters between 1220–2670 m a.s.l. (Fig. 3a, Table S2). At each
173 site, snow water equivalent was calculated by integrating discrete density measurements, made with a wedge
174 sampler, over the snowpack depth (see e.g., Pulwinski and others, 2018). Additional estimates of seasonal
175 snow accumulation are available from NASA’s Operation IceBridge (NASA-OIB) airborne radar campaign,
176 which surveyed large portions of the North Arm, Central Arm, and South Arm of the Kaskawulsh Glacier
177 on May 10 2021 (Li and others, 2023). We convert these measured snow depths to snow water equivalent
178 using a density of 338 kg m^{-3} , the mean measured depth-integrated snow density within the catchment
179 between 2007–2022.

180 5.2 Selection of elevation-dependent bias-correction function

181 The elevation-dependent accumulation bias correction $C(z)$ (Equation 7) is determined from the ratio of
182 observed seasonal snow accumulation to downscaled NARR accumulation (Fig. 3a). We generate a suite
183 of potential functional forms for the bias correction by linearly interpolating between values of observed to
184 downscaled accumulation averaged over a range of elevation bins (Fig. S7). Co-located measurements of
185 accumulation from the NASA-OIB survey of Kaskawulsh Glacier in May 2021 are compared with down-
186 scaled and bias-corrected NARR accumulation on the same date to select the precise functional form of the
187 bias correction (Fig. S8): averaging over 450 m elevation bins produced the minimum root mean square
188 error between NASA-OIB-measured accumulation and the downscaled and bias-corrected NARR accumu-
189 lation (Fig. 3c). The resulting elevation-dependent bias-correction function $C(z)$ ranges from 1.27–2.43,
190 indicating an underestimation of measured accumulation at all elevations by the downscaled NARR data.
191 For elevations outside the range covered by the in-situ data, the value of $C(z)$ is kept uniform and equal
192 to the nearest interpolated value.

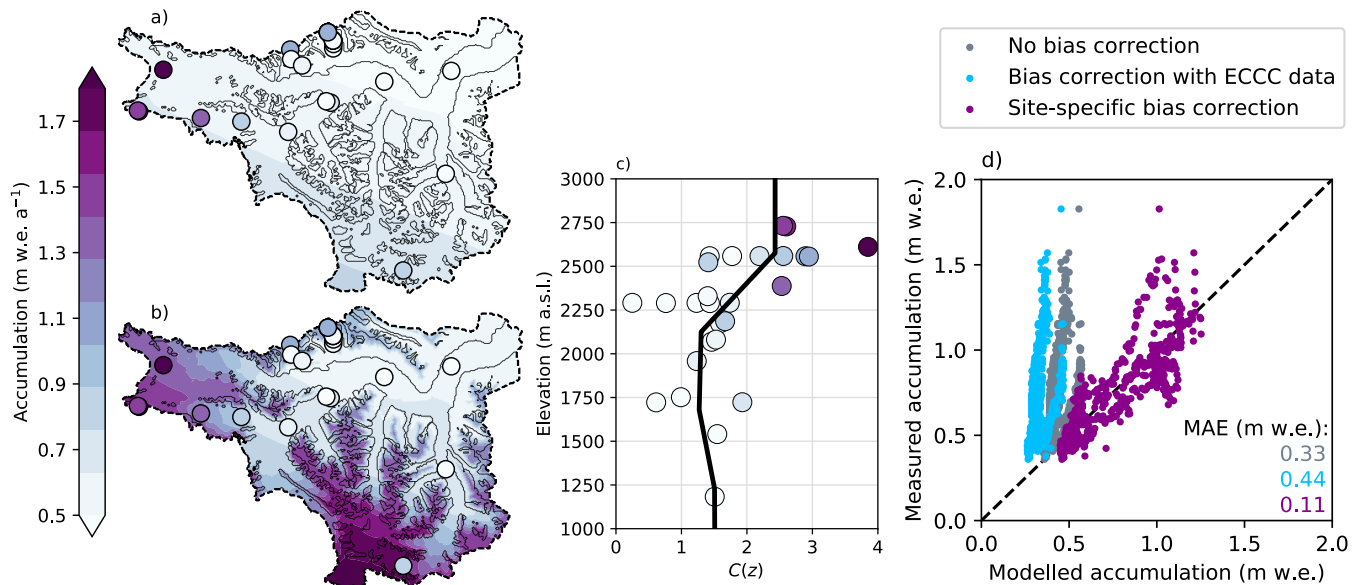


Fig. 3. Overview of the accumulation bias correction. (a) Downscaled, uncorrected NARR annual accumulation for 1980–2022, with in-situ measurements from snowpits shown by circles. (b) NARR annual accumulation bias corrected with the site-specific elevation-dependent correction based on the ratio between measured and downscaled accumulation (Equation 7) shown in (c). (d) Comparison of co-located accumulation measurements from NASA’s Operation IceBridge and downscaled NARR accumulation with no bias correction (grey), the new site-specific bias correction in (b) (purple), and a bias correction based on ECCC precipitation-gauge data (blue). Mean Absolute Error (MAE) between measured and modelled accumulation is reported for each.

193 **5.3 Bias correction with precipitation-gauge data**

194 We also evaluate the changes in modelled mass balance and runoff under the assumption that no in-
195 situ accumulation data exists for the Kaskawulsh River Headwaters. In this scenario, we could drive the
196 model with uncorrected downscaled NARR data (Fig. 3a) or develop an alternative bias correction based
197 on publicly available precipitation gauge data from Environment and Climate Change Canada (ECCC)
198 stations. The two closest ECCC stations to the Kaskawulsh River Headwaters are “Burwash A”, located
199 at 820 m a.s.l. approximately 65 km northwest of the Kaskawulsh Glacier terminus, and “Haines Junction
200 YTG”, located at 596 m a.s.l. approximately 59 km east of the terminus (Fig. 1). NARR precipitation is
201 downscaled at each of the station locations following the approach described in §3.3.2 and compared to
202 measured monthly precipitation at both stations (Fig S10). Monthly correction factors for each gridcell in
203 the model are calculated as the distance-weighted average of the correction factors from the two stations.
204 Downscaled NARR precipitation generally overestimates precipitation measured at the two stations (Fig
205 S11), in contrast to the biases within the catchment where NARR generally underestimates the observed
206 accumulation.

207 **5.4 Impact of accumulation bias correction**

208 The site-specific accumulation bias correction based on snow depth and density measurements from within
209 the catchment increases the catchment-wide mean annual accumulation from 1980–2022 by 80% compared
210 to downscaled, uncorrected NARR accumulation (Fig. 3a,b). Conversely, the alternative bias correction
211 based on regional precipitation gauge data reduces mean annual accumulation by 25% relative to the un-
212 corrected data. The performance of each representation of accumulation (uncorrected, corrected based on
213 catchment-specific accumulation measurements, corrected based on regional precipitation gauge data) is
214 evaluated for the 2021 accumulation season by comparing against the co-located airborne radar-derived
215 measurements. Relative to uncorrected data, the site-specific bias correction improves the spatial distri-
216 bution of accumulation in the catchment, reducing the mean absolute error (MAE) between measured
217 and modelled accumulation by 67% (Fig. 3d). The precipitation-gauge bias correction exacerbates the
218 mismatch between measured and modelled accumulation, resulting in a 33% increase in the MAE relative
219 to uncorrected data.

220 6 MODEL TUNING PROCEDURE

221 6.1 Mass balance and snowline targets

222 The melt model (Equation 2) is tuned to two empirical targets: (1) the 2007–2018 glacier-wide geodetic
223 mass balance (Young and others, 2021a) and (2) the observed snow cover determined by snowline positions
224 delineated from satellite imagery. The geodetic mass balance was determined by Young and others (2021a)
225 using DEMs of the glacier surface in 2007 and 2018 derived from SPOT5/6/7 satellite observations.

226 Snowline positions were delineated from over 50 Landsat-8 and Sentinel-2 satellite images from May
227 to September from 2013–2019. Snowlines were categorized as either upper bounds, marking the boundary
228 above which the surface is continuously snow covered, or lower bounds, marking the boundary below which
229 the surface is completely snow-free (Fig. 4a). We delineated separate upper and lower bounds on each of
230 the major tributaries to the Kaskawulsh Glacier for a total of 223 individual snowlines. A rasterized version
231 of the observed snow cover in each satellite image was generated by categorizing each model gridcell as a
232 snow-covered surface, snow-free surface, or an intermediate transition zone, depending on the elevation of
233 the gridcell relative to the mean elevation of the upper and lower bounds on each tributary (Fig. 4b). A
234 “snowline score” is calculated for each simulation that indicates how well observed snow coverage in space
235 and time is replicated in the model. The snowline score is a temporally weighted average of individual scores
236 for each satellite image. Individual image scores are calculated as $N_{\text{matching}}/N_{\text{gridcells}}$, where N_{matching} is
237 the number of gridcells where the modelled surface type (snow or ice) matches the rasterized observed
238 surface type, and $N_{\text{gridcells}}$ is the total number of gridcells. The final snowline scores are normalized by
239 the score representing a perfect match between modelled and observed snow cover in every satellite image,
240 such that the maximum score is 1.

241 6.2 Parameter selection procedure

242 We initially perform 10,000 simulations using randomly selected combinations of the melt-model parameters
243 MF , a_{snow} , and a_{ice} sampled from independent normal distributions (Young and others, 2021a) (Fig. 5a–c).
244 Simulations where $a_{\text{ice}} < a_{\text{snow}}$ are discarded (e.g. Hock, 1999, 2003; Young and others, 2018), since snow
245 generally has a higher albedo than bare ice (e.g. Warren, 2019). Of the remaining simulations, only those
246 with a modelled mass balance that falls within three standard deviations of the 2007–2018 geodetic mass
247 balance, $-0.46 \pm (3 \times 0.17) \text{ m w.e. a}^{-1}$, are retained and are binned according to their modelled 2007–2018

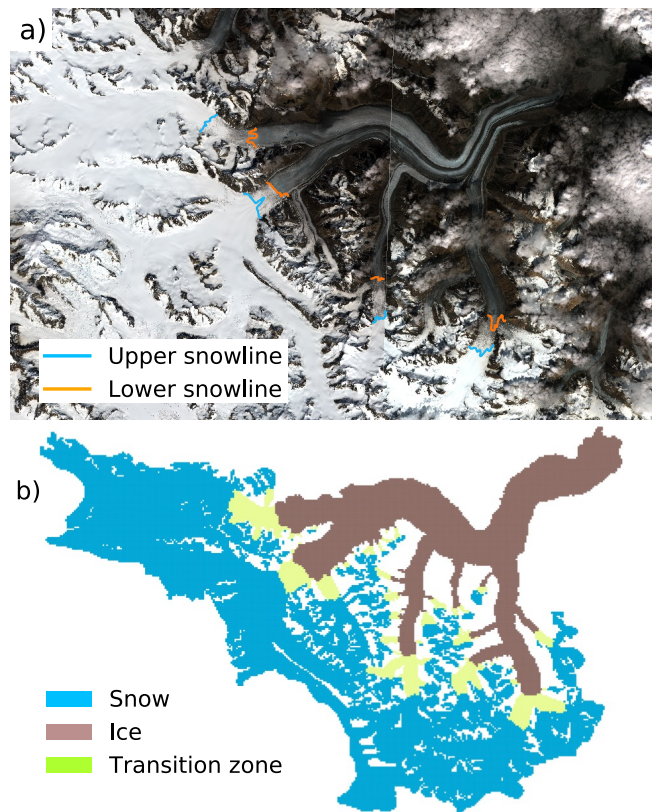


Fig. 4. Snowline delineation and rasterization. a) Sentinel-2 satellite image of the Kaskawulsh Glacier on 2016-07-17, one of the 51 such satellite images used in snowline delineation. Lower bounds (orange) and upper bounds (blue) of the snow are delineated for each major tributary. b) Rasterized version of the snow cover in (a), showing bare ice (brown, below the lower bound), snow (blue, above the upper bound), and transition zone (green, between the upper and lower bounds).

248 mass balance (Fig. 5d). A normal distribution defined by the mean and standard deviation of the geodetic
249 mass balance is imposed on the binned results and scaled such that it encompasses exactly 100 simulations,
250 which are then selected from each bin as those with the highest snowline scores (Fig. 5e). This procedure
251 ensures that simulations with the top snowline scores comprise the final ensemble of model simulations,
252 and that the ensemble yields a mean modelled 2007–2018 average glacier-wide mass balance identical to
253 the observed.

254 We refer to the tuned mass-balance model with site-specific representations of debris and accumulation
255 (described in the previous sections) as the reference model. The mass-balance model is then re-tuned
256 following the same procedure to explore alternative treatments of debris or accumulation. These are (1) a
257 debris-free case, (2) using sub-debris melt factors from a global debris dataset (Rounce and others, 2021),
258 (3) using downscaled, uncorrected NARR accumulation, and (4) using a bias correction based on ECCC
259 precipitation-gauge data from outside the catchment (Table S4). In each of the re-tuned models, only one
260 parameterization (debris or accumulation) is changed at a time.

261 6.3 Value added analysis

262 Finally, we test the model sensitivity to the tuning procedure by excluding each of the tuning targets in
263 turn. In each of these tests, we run the mass-balance model with the site-specific representation of debris
264 and accumulation and select the 100 simulation ensemble as described below:

- 265 1. Test 1 removes the constraint $a_{\text{ice}} \geq a_{\text{snow}}$, but otherwise follows §6.2.
- 266 2. Test 2 excludes the observed 2007–2018 glacier-wide mass balance as a constraint and selects the 100
267 simulations with the highest snowline scores from those where $a_{\text{ice}} \geq a_{\text{snow}}$.
- 268 3. Test 3 excludes snowline observations as a constraint. From the simulations where $a_{\text{ice}} \geq a_{\text{snow}}$, we ran-
269 domly sample from the normal distribution on the binned mass balance rather than sampling according
270 to the highest snowline scores.

271 7 MODEL RESULTS

272 7.1 Reference mass balance and water budget

273 From the reference model we estimate that the average 1980–2022 mass balance for the glacierized area
274 was -0.38 ± 0.15 m w.e. a⁻¹ with a mean equilibrium line altitude (ELA) of about 2100 m a.s.l. Modelled

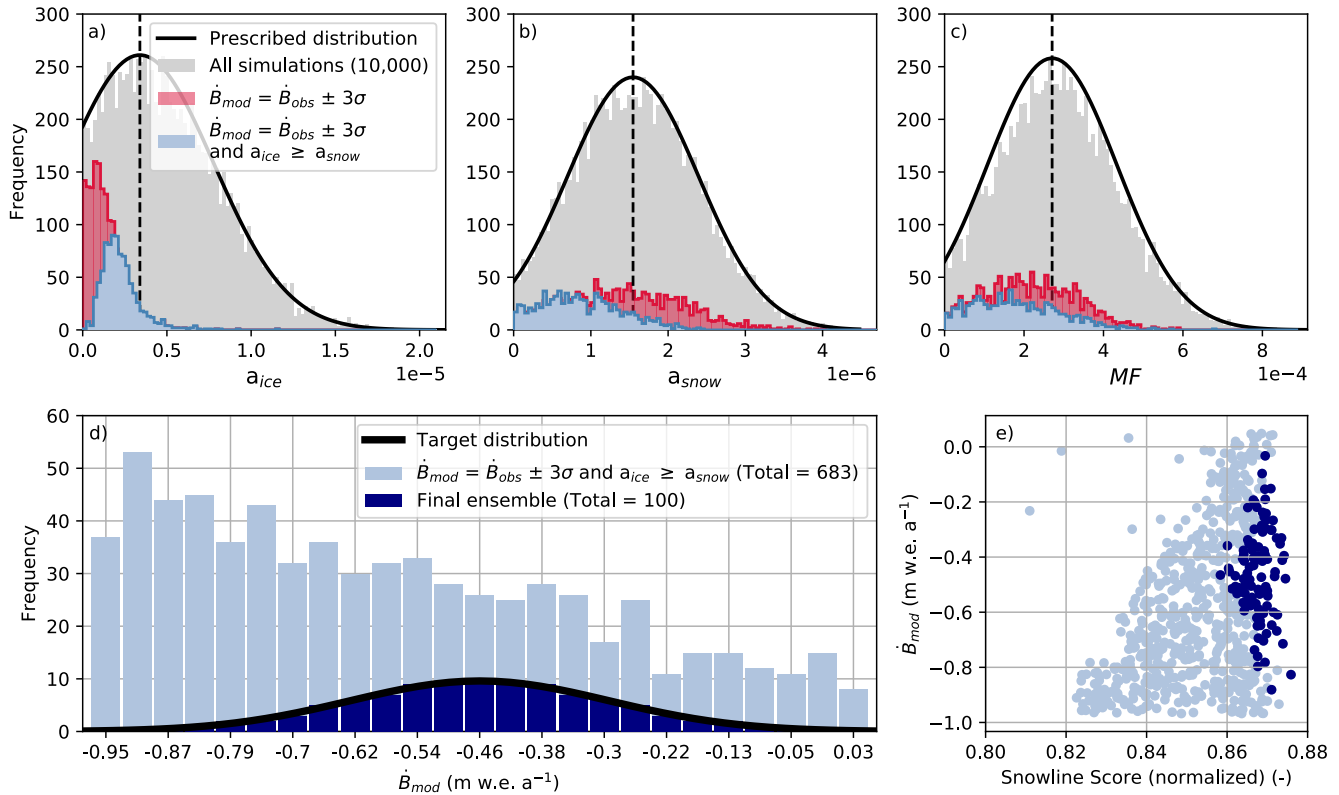


Fig. 5. Overview of model tuning procedure. (a–c) 10,000 combinations of a_{ice} , a_{snow} (m w.e. $3\text{hr}^{-1}\text{°C}^{-1}\text{m}^2\text{W}^{-1}$), and MF (m w.e. $3\text{hr}^{-1}\text{°C}^{-1}$) (grey bars) are randomly selected from truncated normal distributions (black curves). Parameter combinations that yield a modelled 2007–2018 mass balance (\dot{B}_{mod}) within 3 standard deviations of the 2007–2018 geodetic mass balance (\dot{B}_{obs}) (red and light blue bars) and have $a_{ice} \geq a_{snow}$ (light blue bars only) are retained. (d) Simulations that meet the criteria described above are binned according to \dot{B}_{mod} (number of bins is square root of sample size, bin size = $0.041\text{ m w.e. a}^{-1}$). A normal distribution (black curve) defined by the mean and standard deviation of \dot{B}_{obs} is scaled such that it encompasses exactly 100 simulations, which are selected from each bin on the basis of their snowline scores (navy bars), resulting in the distribution shown in panel (e).

275 thinning rates exceed $9.5 \text{ m w.e. a}^{-1}$ on the northern edge of the Kaskawulsh Glacier terminus where thin
276 debris produces a slight melt enhancement. The distributed mean mass balance (Fig. 6a) shows the melt-
277 inhibiting effect of debris over a large portion of the terminus region where lighter shades of orange (debris-
278 covered ice) can be seen adjacent to darker shades of red (debris-free ice). Sinuous patterns corresponding to
279 medial moraines originate at the confluence of Stairway Glacier with the main trunk, and at the confluence
280 of South Arm with the trunk, extending to the debris-covered region of the terminus. The medial moraines
281 are approximately 200–400 m across and exhibit less melt than the surrounding clean ice due to the shielding
282 effect of debris thicker than the estimated critical thickness.

283 We estimate that the average annual runoff from the Kaskawulsh River Headwaters over 1980–2022
284 was $1.89 \pm 0.70 \text{ Gt a}^{-1}$, with peak daily discharge rates of approximately $300 \text{ m}^3 \text{ s}^{-1}$ in early to mid July.
285 61% of catchment-wide runoff originates from glacier ice melt, while snowmelt contributes 31% (Table 1).
286 Refreezing (Fig. 6b) plays an important role in reducing runoff early in the melt season, with approximately
287 20% of the annual snowmelt refrozen. A fraction of the superimposed ice that forms as a result ($\sim 28\%$)
288 is later remelted, contributing $\sim 2\%$ of the annual runoff. At high elevations ($> 2900 \text{ m a.s.l.}$) all surface
289 melt is refrozen and thus no runoff occurs from this zone (Fig. 6c), while at lower elevations the refreezing
290 potential (Equation 4) is generally reached by early August, after which all subsequent snowmelt contributes
291 directly to runoff. Rainfall contributes 6% of the annual runoff, and occurs primarily at low elevations in
292 late July and early August.

293 7.2 Model sensitivity to debris

294 The modelled glacier-wide mass balance over 1980–2022 is independent of debris treatment, a product of
295 retuning the model to match the geodetic mass balance from 2007–2018. Above the ELA, differences in
296 modelled ablation are negligible, but below the ELA local ablation rates differ considerably for both debris-
297 covered and debris-free ice (Fig. 7). The sub-debris ice ablation rate averaged over the debris-covered area
298 is $3.90 \text{ m w.e. a}^{-1}$ using the reference model, increasing to $4.72 \text{ m w.e. a}^{-1}$ for the debris-free model, and
299 $5.49 \text{ m w.e. a}^{-1}$ for the model with melt factors from Rounce and others (2021). These differences produce
300 variations in the modelled glacier topography, including inverted moraines that exhibit higher melt rates
301 than the surrounding ice when using melt factors from Rounce and others (2021). Using the site-specific
302 melt factors yields ablation rates up to $3.7 \text{ m w.e. a}^{-1}$ higher over clean ice compared to the medial moraines
303 at similar elevations.

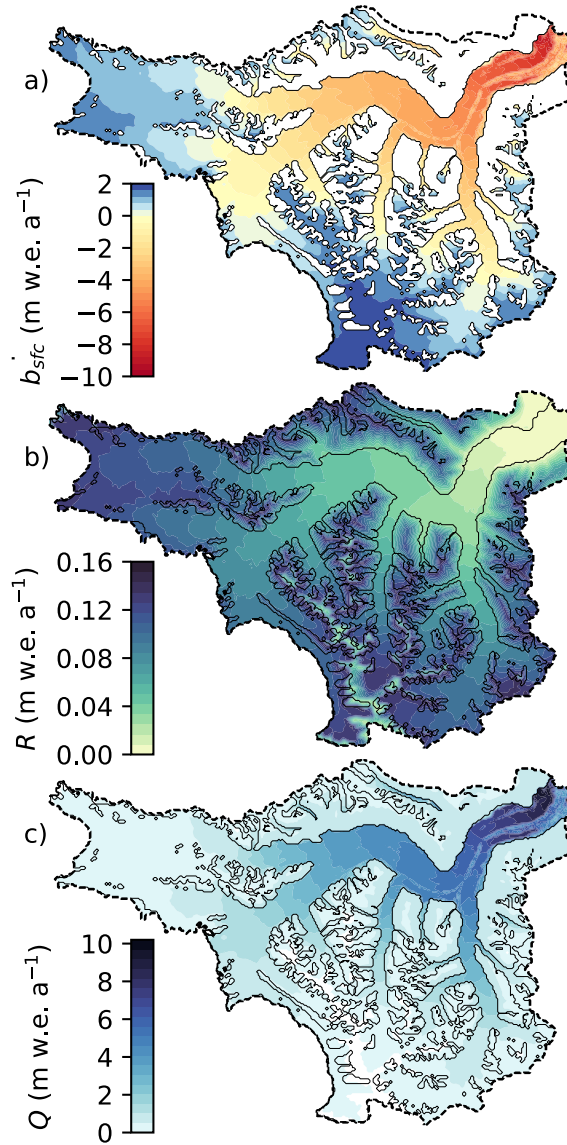


Fig. 6. The reference model (a) mass balance (Equation 1) (b), refreezing (Equation 5), and (c) runoff (Equation 6) from 1980–2022.

	Reference model	Debris-free	Melt factors from global dataset (Rounce et al. 2021)	Uncorrected accumulation	Bias corrected with precipitation- gauge data
Mass balance (m w.e. a ⁻¹)	-0.38 ± 0.15	-0.38 ± 0.16	-0.38 ± 0.16	-0.40 ± 0.15	-0.38 ± 0.15
Total discharge (Gt a ⁻¹)	1.89 ± 0.70	1.89 ± 0.72	1.90 ± 0.62	1.31 ± 0.66	1.06 ± 0.62
Glacier ice melt (Gt a ⁻¹)	1.15 ± 0.36	1.14 ± 0.38	1.14 ± 0.31	0.77 ± 0.35	0.69 ± 0.32
Snowmelt (Gt a ⁻¹)	0.58 ± 0.21	0.59 ± 0.22	0.60 ± 0.20	0.39 ± 0.20	0.25 ± 0.16
Rain (Gt a ⁻¹)	0.11 ± 0.004	0.11 ± 0.004	0.11 ± 0.004	0.11 ± 0.007	0.08 ± 0.007
Refrozen ice melt (Gt a ⁻¹)	0.04 ± 0.11	0.04 ± 0.11	0.04 ± 0.10	0.04 ± 0.12	0.04 ± 0.13

Table 1. Glacierized area-wide mass balance and catchment-wide discharge for 1980–2022 from the reference model and alternative debris-treatment and accumulation bias-correction models (two each). Uncertainties reported are the standard deviations of the 100 simulations comprising each model ensemble.

304 Widespread debris-cover over the south lobe of the terminus (Main and others, 2023) leads to reduced
 305 ablation compared to the surrounding clean ice for both the reference model and the model with melt
 306 factors from Rounce and others (2021), as both treatments of sub-debris melt are similar over the 20–
 307 50 cm-thick debris (Rounce and others, 2021) in this zone. Compared to the reference model, neglecting
 308 debris produces increased ablation over the debris-covered part of the south lobe by up to 6.5 m w.e. a⁻¹.
 309 Despite the local variations in ablation rates between debris treatments, adjustments to the melt-model
 310 parameters from re-tuning compensate for differences in ablation across the catchment. As a result, the
 311 catchment-wide runoff and water budget vary by <1% (Table 1).

312 7.3 Model sensitivity to accumulation bias correction

313 The reference model has an 1980–2022 average winter balance of 0.74 m w.e a⁻¹ at the end of the accumu-
 314 lation season, while the model with uncorrected accumulation and the model bias corrected with ECCC
 315 precipitation-gauge data have, respectively, winter balances of 0.38 m w.e a⁻¹ and 0.29 m w.e a⁻¹ (Fig. 8a–
 316 c). As a result, net ablation and runoff differ significantly across the three models to compensate for
 317 differences in accumulation and achieve the same mass balance as enforced through the tuning procedure.
 318 Relative to driving the model with downscaled uncorrected NARR precipitation, bias correcting with site-
 319 specific data increases the annual catchment-wide runoff by 44%, while bias correcting with precipitation
 320 gauge data reduces runoff by 19%. Peak annual discharge is also sensitive to the accumulation bias correc-
 321 tion, varying from ~200 m³ s⁻¹ in the model with uncorrected accumulation to ~300 m³ s⁻¹ in the reference

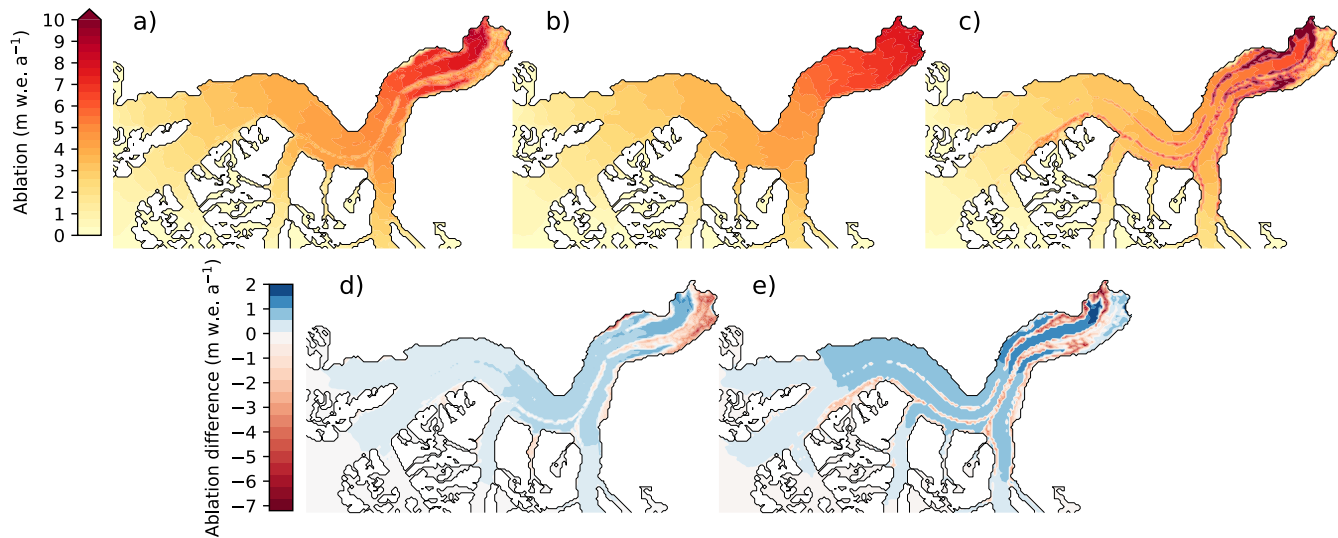


Fig. 7. Annual ablation (1980–2022) on the main trunk of the Kaskawulsh Glacier estimated using the reference model (a), debris-free model (b), and Rounce and others (2021) debris model (c). Differences in modelled ablation are shown for the reference model minus the debris-free model (a)–(b) in (d) and the reference model minus the Rounce and others (2021) debris model (a)–(c) in (e).

322 model and $\sim 170 \text{ m}^3 \text{ s}^{-1}$ in the model bias corrected with ECCC precipitation-gauge data (black lines in
 323 Fig. 8d–e).

324 The estimated water budget across all representations of accumulation varies by $< 10\%$ for each compo-
 325 nent, despite significant changes in runoff magnitude. The tuning procedure ensures the best match between
 326 modelled and observed snow cover, leading to little variation in the duration of accumulation/ablation sea-
 327 sons between models and thus little variation in the modelled water budget. Similarly, the ELA and
 328 accumulation area ratio (AAR) vary by $< 2\%$ across accumulation models.

329 7.4 Value added analysis

330 7.4.1 Test 1: Excluding $a_{\text{ice}} \geq a_{\text{snow}}$ constraint

331 Retaining simulations where $a_{\text{ice}} < a_{\text{snow}}$ increases the number that fall within the geodetic mass-balance
 332 target by 130% (+893) out of the initial 10,000 parameters combinations (Fig. 5). However, following
 333 the tuning procedure, none of the simulations with $a_{\text{ice}} < a_{\text{snow}}$ are selected for the model ensemble since
 334 they yield consistently lower snowline scores than simulations where $a_{\text{ice}} \geq a_{\text{snow}}$ (Fig. 9a). This constraint
 335 therefore adds no value beyond what the delineated snowlines offer, as the final ensemble for Test 1 is

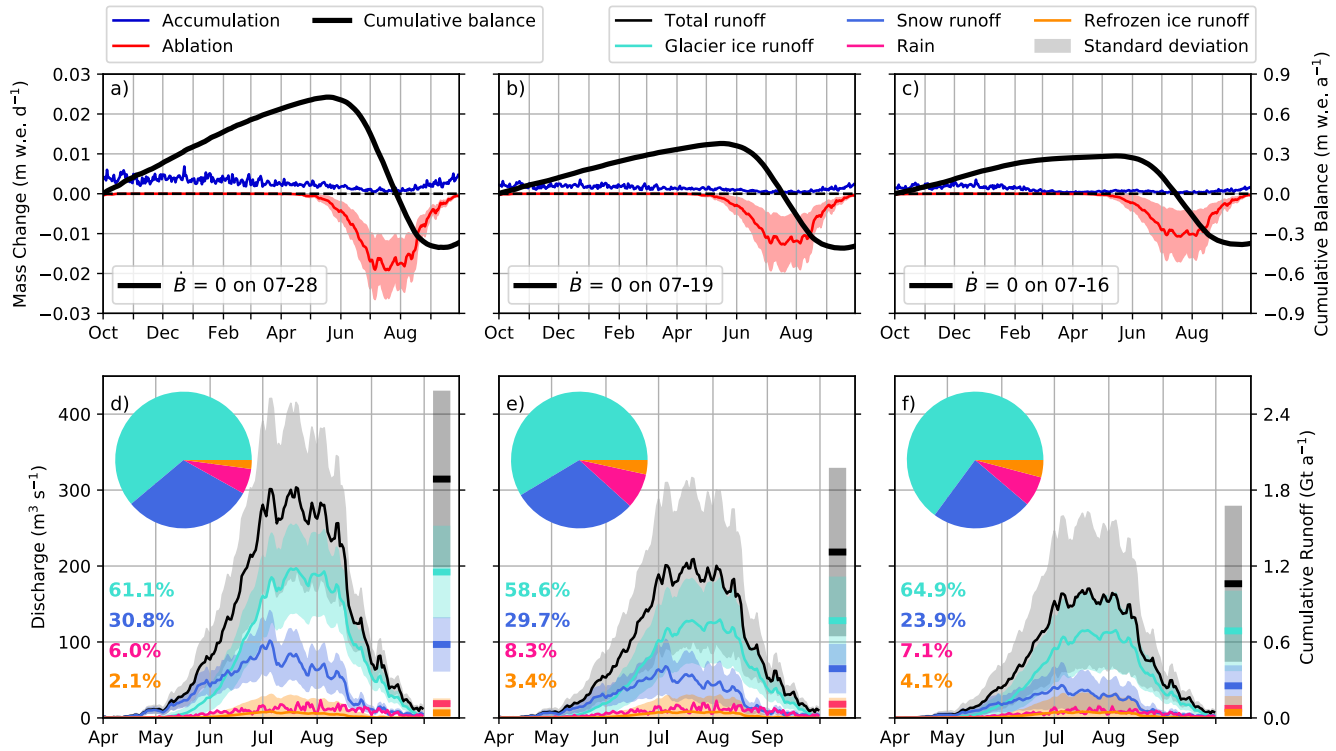


Fig. 8. Comparison of modelled mass balance and runoff from the reference model (a,d), the model with uncorrected accumulation (b,e) and the model bias corrected with ECCC precipitation-gauge data (c,f). (a–c) Glacier-wide annual accumulation (blue), ablation (red), and cumulative mass balance (black) averaged over 1980–2022. The date where $\dot{B} = 0$ (printed) is the average onset of net ablation. (d–f) Catchment-wide melt-season daily discharge (m³ s⁻¹) averaged over 1980–2022. Pie chart and percentages represent the fractional contributions to total runoff from each source in legend. Bars on the right y-axis show the cumulative runoff (Gt a⁻¹) from each source (listed in Table 1). Shading on the timeseries and cumulative totals show $\pm 1\sigma$ of variability in the 100 simulations that comprise each model ensemble.

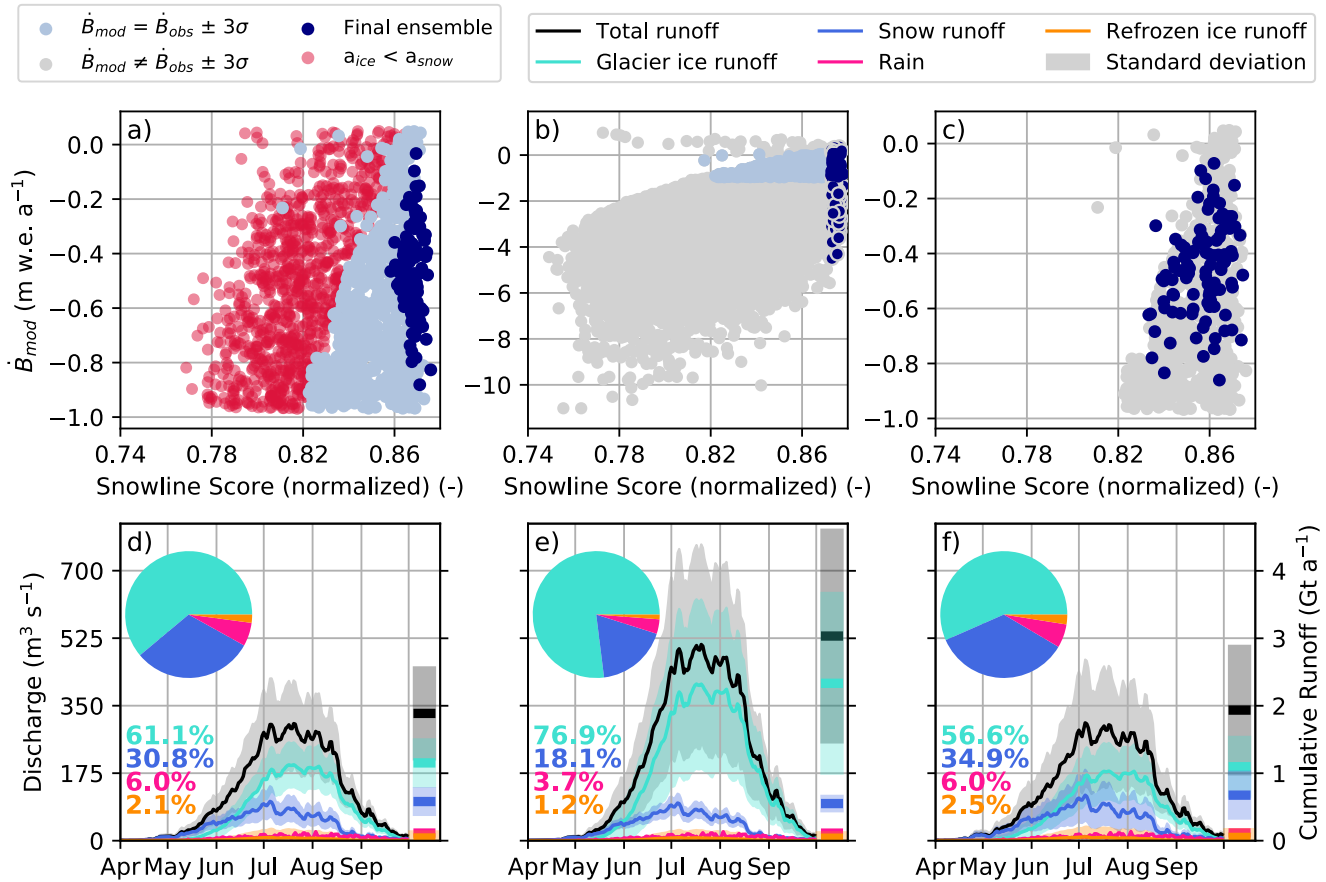


Fig. 9. Summary of results from value added analysis Test 1 (a,d), Test 2 (b,e), and Test 3 (c,f). (a–c) Final simulation ensembles (blue dots) selected for each test based on the tuning criteria described in §6.3. (d–f) Catchment-wide melt-season daily discharge (m³ s⁻¹) averaged over 1980–2022. Pie chart and percentages represent the fractional contributions from each source to total discharge. Bars on the right y-axis show the cumulative runoff (Gt a⁻¹) from each source in legend (listed in Table 2).

336 identical to the reference ensemble. Excluding simulations where $a_{\text{ice}} < a_{\text{snow}}$ (and thus excluding generally
337 lower snowline scores) is a simple means of model improvement in the absence of snowline data.

338 7.4.2 Test 2: Excluding the geodetic mass balance

339 Without the 2007–2018 mass-balance constraint, the mean snowline score in the final ensemble for Test
340 2 is the same as the mean snowline score in the reference ensemble, but the modelled mass balances
341 are considerably different, ranging from -4.50 to $+0.36$ m w.e. a^{-1} (Fig. 9b). Modelled snow cover is well
342 constrained by choosing the best snowline scores, such that the mass balance and runoff differences between
343 the reference model and Test 2 are negligible above the ELA, with catchment-wide snowmelt just 5% less
344 than the reference model (Table 2). Parameters a_{snow} and MF , which together control snow melt and
345 thus the distributed snow cover, occupy a much narrower range compared to the reference ensemble (Fig.
346 10). Without tuning the model to the observed glacier-wide mass balance, a_{ice} and thus ice ablation is
347 completely unconstrained, leading to a 103% increase in ice ablation and a mean 1980–2022 mass balance
348 of -1.38 ± 1.15 m w.e. a^{-1} (Table 2). Mass balance data are thus a critical part of the tuning procedure.

349 7.4.3 Test 3: Excluding snowline observations

350 Randomly selecting simulations to populate the normal distribution on the observed mass balance, rather
351 than selecting them based on snowline scores, leads predictably to a greater spread in scores (Fig. 9c) and
352 in the range of melt-model parameter values, especially for a_{snow} and MF (Fig. 10). While differences in
353 the long-term glacier-wide mass balance and runoff are minimal between Test 3 and the reference model,
354 neglecting snowline scores produces a 17% increase in discharge from snowmelt and a 4% decrease in
355 discharge from glacier ice melt compared to the reference model. Compared to Test 2, which we assume
356 leads to the best representation of observed snow cover, excluding snowline data from tuning yields a higher
357 mean ELA (+110 m), and a smaller AAR (0.58 vs 0.63) (Table 2). The primary value of including snowline
358 observations in tuning is thus to constrain snowmelt and other parameters related to snow cover, which in
359 turn influence the mass balance.

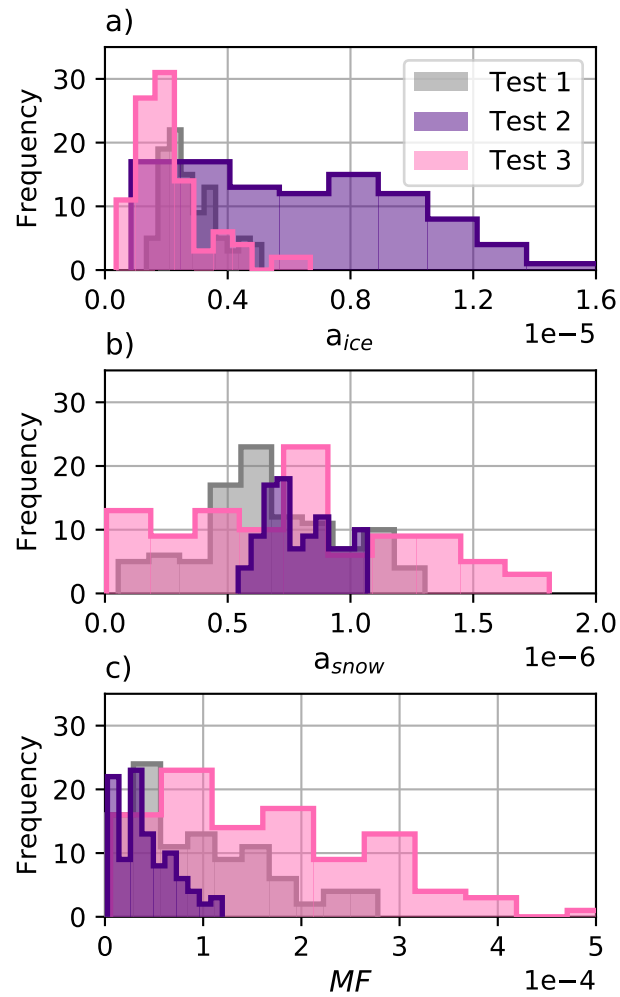


Fig. 10. Histograms of the melt-model parameters (a) a_{ice} , (b) a_{snow} (m w.e. $3\text{hr}^{-1}\text{ }^{\circ}\text{C}^{-1}\text{ m}^2\text{ W}^{-1}$), and (c) MF (m w.e. $3\text{hr}^{-1}\text{ }^{\circ}\text{C}^{-1}$) that comprise the final ensembles for each value added test. Note that Test 1 is identical to the reference ensemble.

	Reference model	Test 2	Test 3
Mass balance (m w.e. a ⁻¹)	-0.38 ± 0.15	-1.38 ± 1.15	-0.39 ± 0.16
Total discharge (Gt a ⁻¹)	1.89 ± 0.70	3.03 ± 1.59	1.94 ± 0.97
Glacier ice melt (Gt a ⁻¹)	1.15 ± 0.36	2.33 ± 1.36	1.10 ± 0.46
Snowmelt (Gt a ⁻¹)	0.58 ± 0.21	0.55 ± 0.13	0.68 ± 0.36
Rain (Gt a ⁻¹)	0.11 ± 0.004	0.11 ± 0.002	0.12 ± 0.007
Refrozen ice melt (Gt a ⁻¹)	0.04 ± 0.11	0.04 ± 0.10	0.05 ± 0.14
AAR	0.62	0.63	0.58
ELA (m a.s.l.)	2106	2069	2179

Table 2. Glacier-wide mass balance and catchment-wide discharge for 1980–2022 from the reference model and Test 2 and 3 of the value added analysis. The results of Test 1 (not shown) are identical to the reference model. The accumulation area ratio (AAR) and equilibrium line altitude (ELA) are also reported.

8 DISCUSSION

8.1 Low catchment-scale sensitivity to debris

The site-specific treatment of debris includes a substantial reduction in the critical debris thickness, resulting in widespread reductions in the sub-debris melt-enhancement factors compared to those of Rounce and others (2021). At local scales, the choice of debris parameterization produces considerable variations in modelled ablation and surface topography, particularly in the terminus region (e.g. Compagno and others, 2022). At glacier termini, thick insulating debris can result in inverted ablation gradients (e.g. more ablation upglacier compared to at the terminus) (Rounce and others, 2021) and can inhibit retreat compared to the debris-free scenario (e.g. Compagno and others, 2022). Thick debris in the terminus region of the Kaskawulsh Glacier may be contributing to observed stagnation (e.g. Main and others, 2023) and minimal retreat (e.g. Foy and others, 2011). The complicating effects of debris argue in favour of realistic and glacier-specific representations of debris in models, particularly for future projections of glacier evolution (e.g. Rounce and others, 2021; Compagno and others, 2022).

Despite local variations in ablation on the Kaskawulsh Glacier as a function of debris treatment, the net effect of changing the debris treatment is minimal. The low sensitivity of the modelled water budget to changes in the debris treatment is due in part to the relatively small fraction of debris cover on the

376 Kaskawulsh Glacier. Debris-covered ice represents 7% of the glacierized area, which is within the typical
377 range for glaciers in the Yukon–Alaska region (5–15%) (Scherler and others, 2018). Tuning the models to
378 the geodetic mass balance also forces net ablation across each debris model to be identical and reduces
379 model sensitivity.

380 Other studies that have employed mass-balance data in model tuning have also shown that tuning
381 specifically for debris-present versus debris-free scenarios reduces model sensitivity. Compagno and others
382 (2022) showed that for all glaciers across High Mountain Asia (12–13% debris covered), re-tuning a glacier-
383 evolution model with and without debris changed the projected mass loss in 2100 by just 1–3%. However,
384 the difference in projected mass loss becomes much more significant for individual glaciers with > 50%
385 debris cover. Conversely, Rounce and others (2021) tune a global glacier evolution model with regional
386 mass-balance data for the debris-present scenario, then conducted simulations without retuning the model
387 for the debris-free scenario, resulting in a 37% reduction in sub-debris ablation globally. While re-tuning
388 a model when the model structure or physics changes (as is done in this study) reduces model sensitivity,
389 applying a model without retuning (as was done by Rounce and others (2021)) facilitates a better process-
390 based understanding of the impact of debris on glacier runoff and mass balance.

391 **8.2 Importance of catchment-specific accumulation data**

392 Gridded reanalysis precipitation products often perform poorly in topographically complex, high-elevation
393 terrain (e.g. Hunter and others, 2020; Bannister and others, 2019; Immerzeel and others, 2015). For the
394 Kaskawulsh Glacier, we find that NARR data generally underestimate accumulation, especially at high
395 elevations. Machguth and others (2009) showed that driving a glacier mass-balance model of the Swiss
396 Alps with downscaled, uncorrected regional climate-model precipitation led to underestimating the mass
397 balance of four Swiss glaciers by 0.25–0.75 m w.e due to systematic biases in the underlying accumulation
398 data. While our tuning approach reduces model sensitivity to the accumulation bias correction with respect
399 to the net mass balance, there are still significant differences in modelled mass-balance gradients, winter
400 balances, and ablation. These sensitivities necessitate careful treatment of accumulation, especially for
401 studies of glacier dynamics and evolution.

402 Correctly estimating the total volume of precipitation is one of the most important controls on mod-
403 elled runoff (e.g. Tarasova and others, 2016), especially for glacierized catchments like the Kaskawulsh
404 River Headwaters where most precipitation falls as winter accumulation. More spatially and temporally

405 extensive in-situ accumulation observations would thus help improve the accuracy of modelled runoff in
406 this catchment. Here, we assumed a constant relationship between downscaled and measured accumu-
407 lation over time, however repeat surveys of accumulation using airborne radar would help quantify the
408 interannual variability in seasonal accumulation and examine the time-dependence of the biases in NARR
409 data. Additional observations are also needed to characterize the relationship between accumulation and
410 elevation where observations are sparse (e.g., in the southern tributaries). More broadly, improving esti-
411 mates of snow water equivalent derived from spaceborne remote-sensing products (e.g. Eppler and Rabus,
412 2021) is an important avenue for future work, as ground measurements of snow density are still needed in
413 combination with remotely-sensed snow depth to estimate snow water equivalent.

414 8.3 Value of observational targets in model tuning

415 Tuning the model to the geodetic mass balance integrates both accumulation and ablation processes (Konz
416 and Seibert, 2010), while the snow lines serve to constrain the timing of runoff from snow and ice melt.
417 Our results highlight, unsurprisingly, the high value that the geodetic mass balance adds to model tuning.
418 Indeed, excluding the geodetic balance from tuning produces ice ablation rates that are largely inconsistent
419 with observations. By contrast, when snowlines are excluded, total ice ablation differed by <5%. However,
420 tuning to the geodetic balance can also lead to compensating errors in modelled ablation if the estimated
421 accumulation is incorrect (e.g. van Tiel and others, 2020; Konz and Seibert, 2010). Including other observa-
422 tional datasets in model tuning, such as point measurements of ablation (e.g. Young and others, 2021a) and
423 accumulation (e.g. Young and others, 2021b), streamflow data (e.g. Tarasova and others, 2016; Konz and
424 Seibert, 2010), and glacial melt extents (e.g. Scher and others, 2021) in addition to the geodetic balance,
425 may help reduce compensating errors in the net ablation (e.g. Finger and others, 2015).

426 An advantage to our tuning approach is that it only uses remote-sensing-derived data, making it more
427 applicable to in-situ data-scarce catchments. If data from detailed local studies are not available, however,
428 regional mass-balance datasets (e.g. Hugonnet and others, 2021) can fill this gap (e.g. Compagno and
429 others, 2022; Rounce and others, 2021).

430 9 CONCLUSION

431 This study quantifies the multi-decadal mass balance and runoff from a hydrologically important, highly-
432 glacierized ungauged catchment in southwest Yukon, with particular attention to assessing model sensitivity

433 to (1) the treatment of sub-debris melt and (2) the accumulation bias correction. We include in our
434 investigation treatments of these processes that can be applied in the absence of in-situ or catchment-
435 specific data.

436 Treating debris using site-specific sub-debris melt factors produces variations $<1\%$ in the catchment-
437 wide discharge and water budget, compared to neglecting debris or using melt factors from a global dataset.
438 Differences in local ablation rates with various debris treatments are significant, however, over the exten-
439 sively debris-covered terminus region of the Kaskawulsh Glacier where ablation rates are highest. Though
440 debris-cover represents a small fraction of the glacierized area in the Kaskawulsh River Headwaters, ac-
441 counting for it using site-specific observations may improve estimates of glacier surface evolution and
442 retreat, especially as the terminus nears stagnation.

443 In contrast to the treatment of debris, catchment-wide discharge varies considerably as a function of the
444 accumulation bias correction. Accumulation inputs that omit site-specific observations reduce catchment-
445 wide discharge by 33–40% compared to the site-specific accumulation bias correction. Despite tuning the
446 model to the observed mass balance, major challenges still include high uncertainties in the input
447 precipitation data which can produce compensating errors in modelled ablation. Improving the spatial
448 coverage of accumulation measurements should thus be a high priority for future in-situ data collection
449 efforts in this area and similarly glacierized catchments. Measurements spanning large elevation ranges
450 and multiple accumulation seasons will be of particular help in characterizing the spatial and temporal
451 stability of any bias correction.

452 Glacier runoff estimates can be critical for understanding downstream changes in water availability,
453 impacts to aquatic ecosystems, and landscape evolution. In the case of the Kaskawulsh River Headwaters,
454 local and regional glacio-hydrological changes are already producing shifts in the timing and magnitude
455 of freshwater that is delivered to the Gulf of Alaska. There is thus a need for coupled mass-balance and
456 ice-dynamics model projections of the Kaskawulsh Glacier in response to its recent climatic imbalance
457 (Young and others, 2021a). The treatment of debris and accumulation impact important mass-balance
458 parameters that will influence these projections, and our work highlights the value of catchment-specific
459 data in this pursuit.

460 **10 SUPPLEMENTARY MATERIAL**

461 The supplementary material for this article can be found at [doi].

462 11 DATA AVAILABILITY

463 The Kaskawulsh Glacier outline was obtained from <https://www.glims.org/maps/glims>. The NARR
464 data used as input to the mass balance model were obtained from [https://downloads.psl.noaa.gov/
465 Datasets/NARR](https://downloads.psl.noaa.gov/Datasets/NARR). SFU Glaciology Group snow depth and density measurements can be found in Table S2
466 of the Supplementary Material. NASA Operation IceBridge radar data products are available at [https://
467 data.cresis.ku.edu/data/snow/2021_Alaska_S0/](https://data.cresis.ku.edu/data/snow/2021_Alaska_S0/), and the seasonal snow thickness data were obtained
468 from https://data.cresis.ku.edu/data/misc/Alaska_seasonal_snow/ (CReSIS, 2021). Precipitation
469 gauge data were obtained from the Environment and Climate Change Canada Historical Climate Data
470 website (https://climate.weather.gc.ca/historical_data/search_historic_data_e.html, last ac-
471 cessed 2023-11-26). Downscaling and melt-model code will be made public on github upon manuscript
472 publication. Model inputs and outputs will be made available on Zenodo upon manuscript publication.

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482 13 AUTHOR CONTRIBUTIONS

483 GF conceived of the original study and KR/GF/DR co-developed the details. KR developed the model
484 code, tuned and ran the mass-balance model, and performed the analysis of model output. KR also su-
485 pervised M. Aulakh's work on snowlines. GF and KR carried out the field work. KR led the manuscript
486 preparation, with contributions from GF and DR. All authors contributed to various aspects of the inter-
487 pretation and edited the manuscript.

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