

# Mesoscale fractures control the scale dependences of seismic velocity and fluid flow in subduction zones

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## Abstract

Natural geological systems contain porosity structures of various scales that play different roles in geophysical properties, fluid flow, and geodynamics. To understand seismic activity associated with high pore-fluid pressure and fluid migration in subduction zones, it is necessary to explore the scale dependence of geophysical properties such as seismic velocity and permeability. Here, we compare laboratory-measured ultrasonic velocity (1 MHz) measured on core samples from the Susaki area in the Shimanto accretionary complex, SW Japan, with sonic velocity (15 kHz) measured by borehole logging experiments. Results show that P-wave velocity decreases from the laboratory (~6 km/s) to the borehole scales (~5 km/s). This scale-variant effect can be explained by a differential effective medium model whereby mesoscale porosity that is undetectable at the ultrasonic wavelength is introduced into the matrix phase with microscale porosity. Assuming typical apertures for micro- and mesoscale fractures, we estimate that the effective permeability can increase to  $10^{-12}$ – $10^{-11}$  m<sup>2</sup> with increasing in the mesoscale porosity and decreasing P-wave velocity down to 4–5 km/s. These results indicate that seismic velocity anomalies and related seismic activity are associated with the presence of mesoscale fractures in subduction zones.

## Highlights

- Measured P-wave velocity decreases from laboratory to borehole scales
- Presence of mesoscale fractures is indicated by upscaled effective medium modeling
- Mesoscale fractures can facilitate rapid fluid drainage in subduction zones

## Keywords

seismic velocity; upscaling; permeability; Nankai Trough

# 1 Introduction

Seismic activity in subduction zones has been related to high-pore fluid pressure and the properties of the fluid drainage system on the basis that fluids play a dominant role in controlling the frictional and rheological properties of rock (Saffer and Tobin, 2011). As pore fluid can also influence the elastic properties of rock (Mavko et al., 2020), seismic velocity structures have been obtained by seismological surveys and borehole logging in various subduction zones to understand the causes of seismic activity (e.g., Audet and Schwartz, 2013; Eberhart-Phillips et al., 2017; Kamei et al., 2013; Saffer, 2003; Shiraishi et al., 2019). These velocity structures have revealed low-velocity anomalies and episodic changes in velocity along the plate boundaries, which are likely associated with the presence of high pore-fluid pressure and transient fluid migration (Tonegawa et al., 2022; Tsuji et al., 2014).

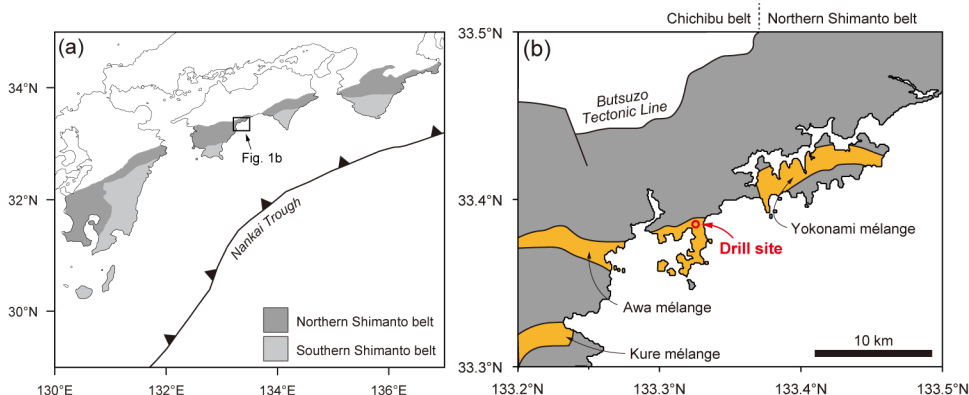
To link seismic velocity and the pore fluid state, laboratory measurements of elastic wave velocity using rock samples from the Nankai subduction zone, including drillcore from the seafloor and an ancient accretionary complex on land, have been conducted (Hamahashi et al., 2013; Hoffman and Tobin, 2004; Kitamura et al., 2021; Raimbourg et al., 2011). These studies have revealed the role of microscopic pores and cracks in controlling elastic wave velocity, which has been applied to interpretations of observed seismic velocity structures (Kitajima and Saffer, 2012; Tsuji et al., 2014). However, there is a large gap in the scales of observations among laboratory measurements, borehole logging, and seismic surveys, primarily because of the different probing frequencies and hence different wavelengths for measurements at each scale. Laboratory measurements are typically carried out at ultrasonic frequency ( $\sim$ MHz) with hand-sized samples, and the measured elastic wave velocity reflects millimeter-scale structures, such as microcracks and pores. In contrast, borehole sonic logging and seismological surveys are performed typically at frequencies of  $\sim$ kHz and  $\sim$ Hz, respectively, which correspond to wavelengths of meters to kilometers. Given that natural geological systems are heterogeneous and contain defects of different scales at each scale of observation, the observed sonic and seismic velocities at relatively low frequencies should be affected not only by microscopic pore structures but also by larger-scale defects, such as fractures and faults (Bailly et al., 2019; Matonti et al., 2015). As the permeability of rocks depends strongly on the dimensions of conduits, such large-scale defects can lead to more effective fluid drainage compared with microscopic pores and cracks, and may be related to the episodic occurrence of slow slip and tremor associated with rapid fluid migration along subduction plate interfaces (Ide, 2010; Muñoz-Montecinos and Behr, 2023). It is therefore crucial to explore the scale dependence of elastic wave velocity to quantitatively relate the seismic velocity structures to seismic activity in subduction zones via pore fluid behavior.

This study aims to obtain porosity structures at two scales (micro- and mesoscales) in a rock mass sourced from a deep subduction zone and estimate the contribution of pore fluid to seismic velocity at each scale. We use core samples from the Cretaceous Shimanto belt in the Susaki area, Kochi, SW Japan, which is originated from the depths of seismogenic zone in a subduction zone similar to the present-day Nankai Trough (Itaba et al., 2014). We first measured the P-wave velocity of the core samples at the MHz frequency and dense intervals to obtain spatial variations in microscopic porosity at a macroscopic scale. We then compared our data with sonic logging velocities measured at the kHz frequency in the borehole. Results show a decrease in the P-wave velocity at larger scales,

82 suggesting the presence of mesoscale fractures. Finally, we estimated the effective perme-  
 83 ability of the rock at each scale, and discuss the potential role of mesoscale fractures on  
 84 seismic velocity and fluid flow in subduction zones.

## 85 2 Geologic setting and borehole logging data

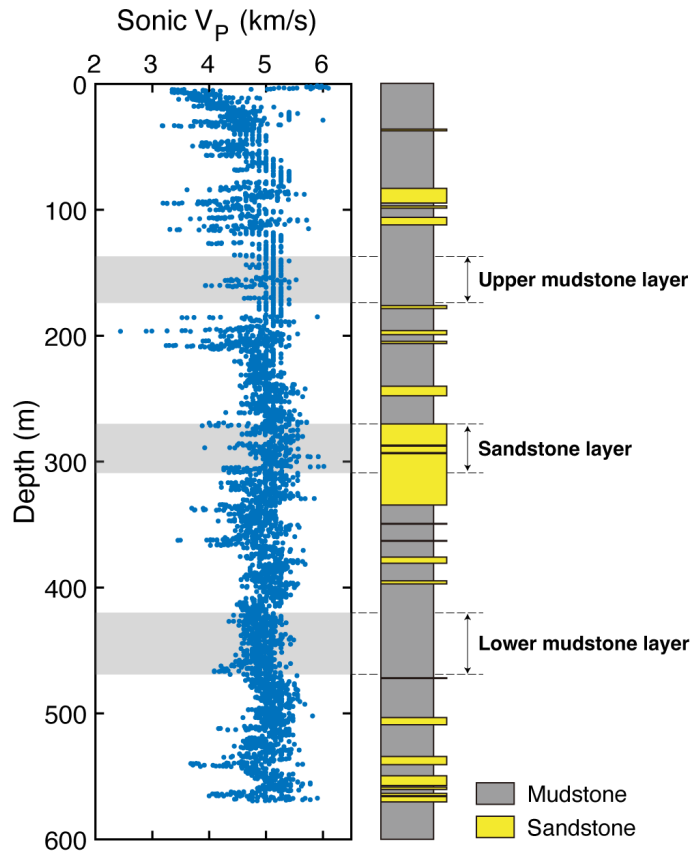
86 The Susaki area is located in the Cretaceous Shimanto belt in SW Japan, which consists  
 87 of an accretionary complex associated with a plate subduction similar to the modern  
 88 Nankai Trough (Fig. 1). Drilling was conducted in this area by the Geological Survey  
 89 of Japan (GSJ) in 2009, and continuous cores of ~600 m in total length were recovered  
 90 (Itaba et al., 2014). The drillcores consist mainly of sandstones and mudstones with inter-  
 91 calations of tuff layers, as well as quartz and calcite veins. Visual descriptions of the core  
 92 samples revealed few major faults in the core, with mélangé-like deformation being ob-  
 93 served throughout the entire core (Itaba et al., 2014). As the drilling site is located in the  
 94 area which can be geologically extended from the Yokonami mélangé and Awa mélangé  
 95 (Taira, 1988), the core is presumed to have undergone a similar subduction–exhumation  
 96 history to the two mélanges. According to the previous studies that utilized fluid inclu-  
 97 sion analysis and vitrinite reflectance geothermometry, the mélanges reached a depth  
 98 equivalent to ~200 °C (i.e., the seismogenic zone depths) during the late Cretaceous and  
 99 were then exhumed (Hashimoto et al., 2012; Sakaguchi, 1999). This history indicates that  
 100 the entire core section from the Susaki area underwent the same subduction–exhumation  
 101 history as these mélanges.



**Fig. 1** (a) Geological map of SW Japan; (b) map of the area around the site of the Susaki drillhole (modified after Hashimoto et al., 2012). Colored areas are mélangé zones.

102 Geophysical logging measurements in the studied boreholes were conducted by GSJ, and  
 103 downhole physical properties were obtained, including sonic velocity, electrical resistivity,  
 104 and natural gamma rays (Itaba et al., 2014). Here, we focus on the sonic velocity data for  
 105 comparison with ultrasonic velocity. Sonic logging was conducted at a probe frequency  
 106 of ~15 kHz, which corresponds to a wavelength of ~0.3 m. This means that the downhole  
 107 profile in sonic velocity reflects variations in submeter-scale structures. P-wave velocity  
 108 from sonic logging was determined by picking the onset of the waveforms at each 10 cm  
 109 increment in depth. During sonic logging, the hole was saturated with groundwater, so

110 the measured velocities should be considered as values under water-saturated conditions.  
 111 Although the sonic P-wave velocity shows an overall monotonic depth trend ranging from  
 112 4 to 5.5 km/s (median of 5.0 km/s), sandstone layers tend to have slightly higher velocities  
 113 than mudstone layers (Fig. 2).



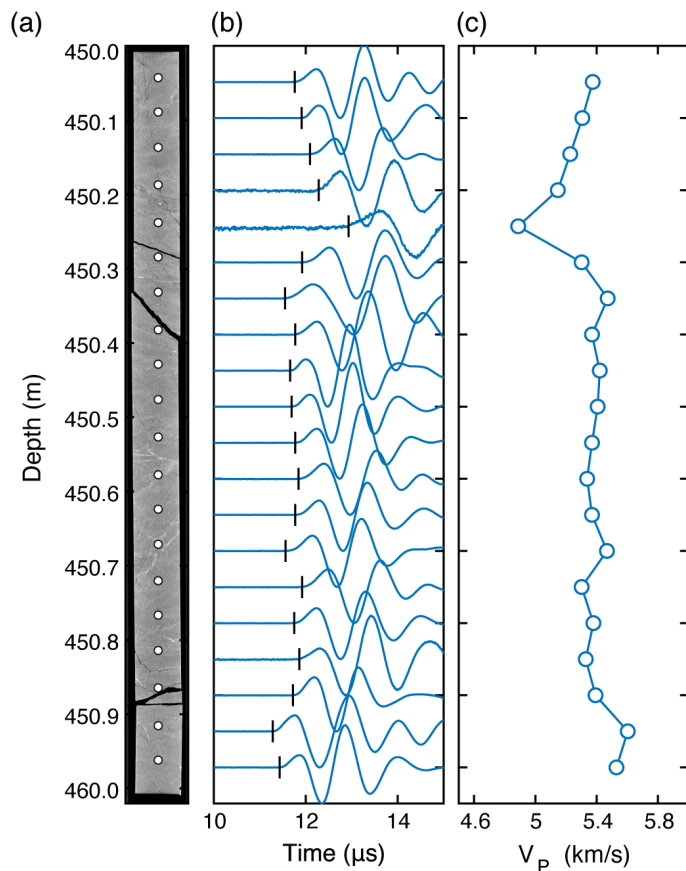
**Fig. 2** Downhole profile of P-wave velocity obtained by sonic logging in the Susaki boreholes and stratigraphic column of the core samples (modified after Itaba et al., 2014). Gray shading indicates the core intervals subjected to ultrasonic velocity measurements in this study.

### 114 3 Method

#### 115 3.1 Measurement of ultrasonic velocity

116 To evaluate the spatial distribution of microscopic porosity in the Susaki core samples,  
 117 we performed dense measurements of ultrasonic P-wave velocity under dry conditions at  
 118 room temperature and pressure. Measurements were performed on whole core sections  
 119 from the following intervals (Fig. 2): 137–175 m (upper mudstone layer), 270–310 m  
 120 (sandstone layer), and 420–470 m (lower mudstone layer). The core sections from these  
 121 depths were reasonably intact and retained a cylindrical shape. P-wave velocity at the

122 ultrasonic frequency was determined using a pulse transmission method, in which travel  
 123 times of ultrasonic waves passing through the core were measured. The core sections were  
 124 sandwiched by a pair of ultrasonic transducers with a resonant frequency of 1 MHz in  
 125 the direction orthogonal to the core axis. An input pulse with an amplitude of 10 V was  
 126 sent to the transducer by a pulse generator and was transmitted through the core, with  
 127 the output signal being received by another transducer mounted on the opposite side and  
 128 digitalized by an oscilloscope. The time of the first arrival of the ultrasonic wave was  
 129 determined using the Akaike Information Criterion (Akamatsu et al., 2023; Sarout et al.,  
 130 2009), and the P-wave velocity was then calculated by dividing the core diameter (56.5  
 131 mm for upper mudstone layer and 63.2 mm for sandstone and lower mudstone layers) by  
 132 the travel time (Fig. 3). This procedure was performed at each 5 cm interval for each core  
 133 section over a total length of 128 m.



**Fig. 3** Example of results of ultrasonic velocity measurements. (a) Cross-section of a core sample (depths range 445–446 m) imaged using X-ray computed tomography. (b) Waveforms recorded at points indicated by white dots in (a). Vertical black lines denote the arrival times determined by the AIC. (c) Calculated P-wave velocities.

### 134 3.2 Effective medium modeling

135 Although the ultrasonic velocity measurements were performed under dry conditions,  
 136 the borehole logging measurements from the Susaki boreholes were carried out under  
 137 groundwater-saturated conditions. It is therefore necessary to correct the ultrasonic ve-  
 138 locity for water-saturated (wet) conditions for accurate comparison with the sonic logging  
 139 velocity. Effective medium theory allows us to predict the velocity under wet conditions  
 140 from that under dry conditions if porosity and pore geometry are known. Here, we em-  
 141 ployed the differential effective medium (DEM) model (Berryman et al., 2002; Mavko  
 142 et al., 2020). For an isotropic medium containing randomly oriented spheroidal (penny-  
 143 shaped) pores, the effective bulk modulus  $K^*$  and shear modulus  $G^*$  can be calculated as  
 144 follows:

$$(1 - \phi) \frac{d}{d\phi} [K^*(\phi)] = (K_i - K^*(\phi)) P^*(\phi), \quad (1)$$

$$(1 - \phi) \frac{d}{d\phi} [G^*(\phi)] = (G_i - G^*(\phi)) Q^*(\phi), \quad (2)$$

145 with initial conditions  $K^*(0) = K_0$  and  $G^*(0) = G_0$ , where  $K_0$  and  $G_0$  are the bulk and  
 146 shear moduli of the porosity-free material, respectively;  $K_i$  and  $G_i$  are the bulk and shear  
 147 moduli of the pore-filling phase, respectively; and  $\phi$  is the porosity.  $P^*$  and  $Q^*$  are the  
 148 volumetric and deviatoric strain concentration factors for a penny-shaped pores (cracks),  
 149 respectively, described as follows:

$$P^* = \frac{K^* + \frac{4}{3}G_i}{K_i + \frac{4}{3}G_i + \pi\alpha\beta^*}, \quad (3)$$

$$Q^* = \frac{1}{5} \left[ 1 + \frac{8G^*}{4G_i + \pi\alpha(G^* + 2\beta^*)} + \frac{2K_i + \frac{4}{3}(G_i + G^*)}{K_i + \frac{4}{3}G_i + \pi\alpha\beta^*} \right], \quad (4)$$

$$\beta^* = G^* \frac{3K^* + G^*}{3K^* + 4G^*}, \quad (5)$$

150 where  $\alpha$  is the mean aspect ratio of cracks (defined as  $\alpha = w/c$ ), with  $c$  and  $w$  being the  
 151 mean pore radius and aperture, respectively. These equations indicate that the effective  
 152 elastic wave velocity under wet conditions can be predicted from its dry velocity if the  
 153 relationships among elastic wave velocity, porosity, and aspect ratio for the Susaki cores  
 154 are known.

155 Here, we use the relationships among elastic wave velocity, porosity, and aspect ratio for  
 156 the Susaki cores that were obtained by Okuda et al. (2024), who measured the P- and  
 157 S-wave velocities and porosity of discrete cylindrical samples taken from the core. Those  
 158 authors found that the porosity of the core ranged from 1% to 4% and that the relation-  
 159 ship between velocity and porosity generally fell between the trends for  $\alpha = 0.01$  and  
 160  $\alpha = 0.03$ . We therefore assumed an average aspect ratio of 0.02 for modeling the wet ve-  
 161 locities and porosity from the dry velocities that we measured. The porosity-free elastic

162 moduli were taken to be  $K_0 = 64$  GPa and  $G_0 = 37$  GPa, which were estimated from the  
163 velocity–porosity relationship established for the Susaki cores (Okuda et al., 2024). The  
164 bulk modulus for the inclusion phase was set as 0 GPa for dry air and 2.2 GPa for water,  
165 whereas the shear modulus was 0 GPa for both conditions.

166 Effective medium models postulate non-isobaric conditions for pore fluid within any unit  
167 volume (i.e., representative elementary volume: REV) and are applicable to the high-  
168 frequency regime without equilibration of pore pressure (i.e., pore pressure differs from  
169 crack to crack) during loading. Here, the logging measurements were performed at a fre-  
170 quency of  $\sim 15$  kHz, which can lie within the validity range of effective medium models  
171 (Fortin and Guéguen, 2021).

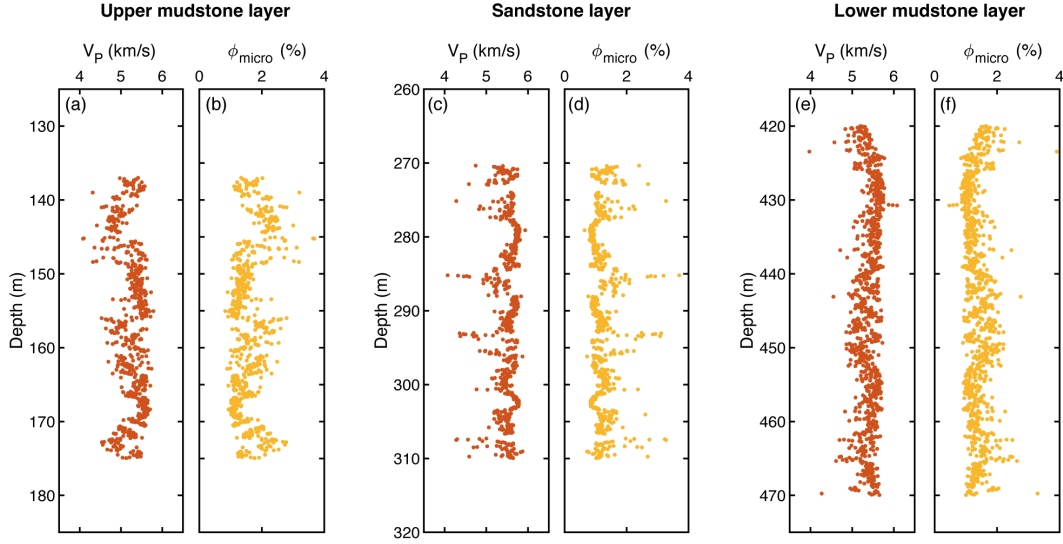
## 172 4 Results and discussion

### 173 4.1 Ultrasonic velocity profiles

174 Ultrasonic P-wave velocity profiles for each analyzed depth interval of the studies core are  
175 shown in Fig. 4a, c, and e. The velocity ranges broadly from 4 to 6 km/s, with a median  
176 of 5.44 km/s for all three layers. The sandstone layer has slightly higher velocity (median  
177 of 5.55 km/s) than the mudstone layers (median of 5.38 km/s). These results are consis-  
178 tent with laboratory results using discrete cylindrical samples taken from the Susaki cores  
179 (Okuda et al., 2024), are similar to high-velocity zones observed at the Nankai Trough  
180 (Kamei et al., 2013; Shiraishi et al., 2019), and are higher than those measured on other  
181 core samples from the Nankai subduction zone and the Shimanto accretionary complex  
182 (Hamahashi et al., 2013; Tsuji et al., 2006).

183 Fig. 4b, d, and f shows microscale porosity profiles estimated via the DEM model, assum-  
184 ing a mean crack aspect ratio of 0.02. The porosity ranges from 0.5% to 4%, with a me-  
185 dian of 1.3%. The sandstone layer has slightly lower porosity (median of 1.1%) than the  
186 mudstone layers (median of 1.4%). Given the ultrasonic wavelength used here of 4–6 mm,  
187 these porosity variations indicate a heterogeneous distribution of millimeter to submil-  
188 limeter scale defects. Microstructural observations of these core samples indicated that  
189 pressure solution processes, possibly driven by fluid migration, can have lowered the mi-  
190 crocrack density and that variations in microscopic porosity are due mainly to variation  
191 in pore space along clay minerals, such as illite and chlorite (Okuda et al., 2024). Miner-  
192 alogical analyses have also indicated that the mudstone samples have high clay mineral  
193 contents compared with the sandstones (Okuda et al., 2024), which is consistent with the  
194 relatively high porosity of the mudstone layers measured in this study. These observations  
195 suggest that the spatial variations in microscopic porosity can be attributed partly to clay  
196 mineral contents. Nevertheless, there are localized high-porosity zones, particularly in the  
197 sandstone layer (Fig. 4d), which may be attributable to localized areas of intense brittle  
198 damage.

199 To compare the ultrasonic velocity profiles measured under dry conditions with sonic log-  
200 ging velocity measured under water-saturated conditions, we modeled ultrasonic velocity  
201 under wet conditions from the dry velocity and porosity via DEM. The modeled velocities  
202 are higher than the dry velocities, ranging from 5.0 to 6.1 km/s (Fig. 5). Compared with  
203 the sonic logging velocities, these velocities are also higher by 0.1–2.1 km/s. This means  
204 that the observed sonic velocities cannot be explained by water-saturated microscopic



**Fig. 4** Depth variations in ultrasonic P-wave velocity (a, c, and e) and microscale porosity estimated from the DEM model (b, d, and f) for each analyzed depth interval of the studies core.

205 porosity alone. Given that natural geological systems contain defects of different scales,  
 206 the decrease in P-wave velocity of the Susaki core from ultrasonic to sonic scales implies  
 207 the additional contribution of relatively large-scale porosities that are invisible via ultra-  
 208 sonic velocities.

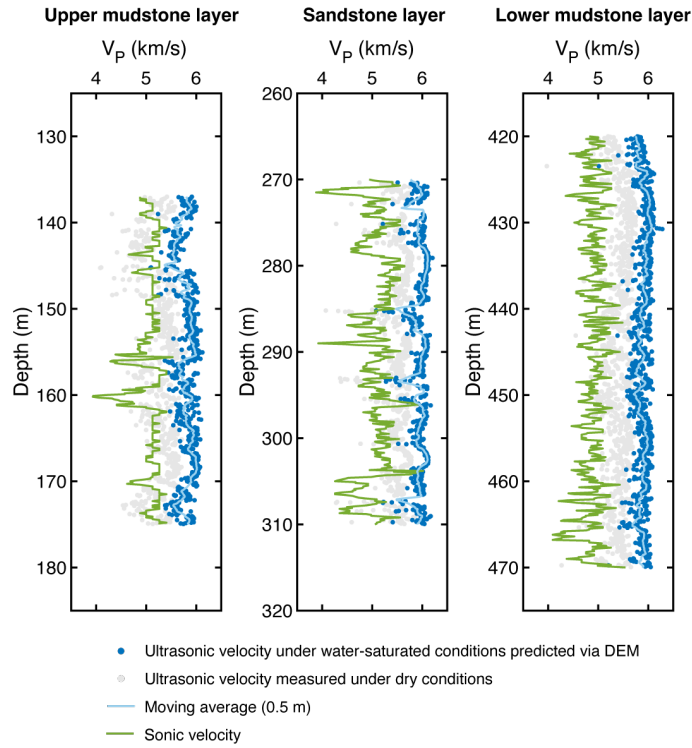
## 209 4.2 Estimation of mesoscale porosity

210 To account for the discrepancies between the sonic and ultrasonic velocities, we in-  
 211 troduced an effective medium model that includes mesoscale porosity in addition to  
 212 microscale porosity, on the basis of DEM theory (Fig. 6). As described in the previous  
 213 section, the effective elastic properties estimated via ultrasonic velocity can be expressed  
 214 as a matrix phase containing (randomly oriented) penny-shaped cracks of a given mean  
 215 aspect ratio (Eqs. 1, 2, 3, 4, 5). At the sonic wavelength scale (mesoscale), such an  
 216 effective medium including microscopic porosity should be regarded as a matrix phase,  
 217 and the effective elastic properties can be expressed by introducing a second family of  
 218 mesoscale inclusions that are larger than the ultrasonic wavelength but smaller than  
 219 the sonic wavelength (Fig. 6) (Bailly et al., 2019). Consequently, the effective elastic  
 220 properties estimated via sonic velocity ( $K^{**}$  and  $G^{**}$ ) can be expressed as follows:

$$(1 - \phi_{\text{meso}}) \frac{d}{d\phi_{\text{meso}}} [K^{**}(\phi_{\text{meso}})] = (K_i - K^{**}(\phi_{\text{meso}})) P^{**}(\phi_{\text{meso}}), \quad (6)$$

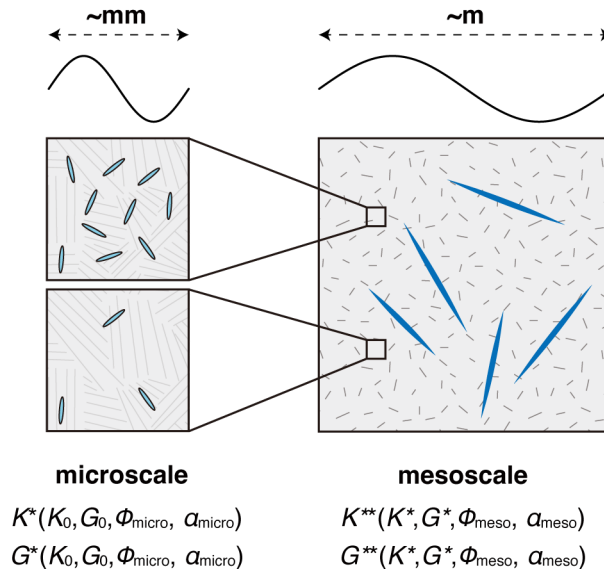
$$(1 - \phi_{\text{meso}}) \frac{d}{d\phi_{\text{meso}}} [G^{**}(\phi_{\text{meso}})] = (G_i - G^{**}(\phi_{\text{meso}})) Q^{**}(\phi_{\text{meso}}), \quad (7)$$





**Fig. 5** Comparison of modeled P-wave velocity under water-saturated conditions (blue dots) with that predicted from dry velocity (gray dots) via DEM, with sonic logging velocities (green lines) for each analyzed depth interval of the studied core.

221 with the initial conditions  $K^{**}(0) = K^*(\phi_{\text{micro}})$  and  $G^{**}(0) = G^*(\phi_{\text{micro}})$ , where  $\phi_{\text{micro}}$   
 222 and  $\phi_{\text{meso}}$  are the microscale and mesoscale porosities, respectively, and the total porosity  
 223 is  $\phi_{\text{total}} = \phi_{\text{micro}} + \phi_{\text{meso}}$ . Here, we used  $P^{**}$  and  $Q^{**}$  for penny-shaped cracks assuming  
 224 the mean aspect ratio of the mesoscale cracks to be 0.002. This value is based on a typical  
 225 value for vein minerals that are traces of mesoscale fractures (van Everdingen, 1995).  
 226 Using this model and the microscale porosity determined in the previous section, we per-  
 227 formed an inversion of the observed sonic velocity and estimated mesoscale porosity. The  
 228 microscale porosity used at each depth was a moving average of 0.5 m based on the sonic  
 229 wavelength (Fig. 5).



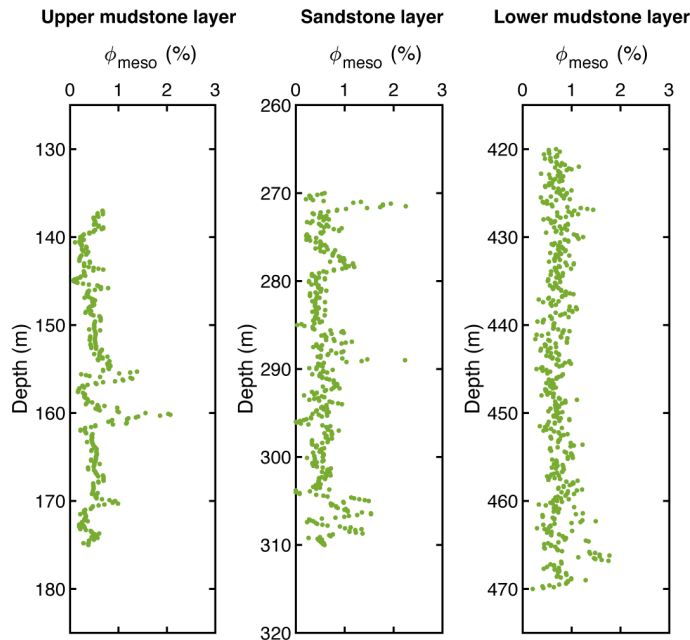
**Fig. 6** Schematic illustrations showing modeling of effective elastic properties at the micro- and mesoscales by adding water-saturated microcracks and mesoscale fractures observed by different wavelengths (frequencies).

230 Fig. 7 shows the mesoscale porosity determined by the inversion of the sonic logging  
 231 velocities, assuming a mean aspect ratio of mesoscale cracks of 0.002. The addition of  
 232 mesoscale porosity of 0.1%–1.0% well explains the observed discrepancies between the  
 233 ultrasonic and sonic velocities (Fig. S1). In contrast to the microscale porosity, the  
 234 mesoscale porosity shows no clear difference between the sandstone layer (median of 0.5%)  
 235 and the mudstone layers (median of 0.6%), implying that mesoscale fractures can develop  
 236 regardless of lithology. According to the DEM model, mesoscale porosity with a low  
 237 mean aspect ratio can readily decrease the elastic wave velocity compared with microscale  
 238 porosity with a relatively high mean aspect ratio (Fig. 9a).

239 As described in the previous section, the DEM model is considered valid primarily for  
 240 a relatively high-frequency regime ( $\leq\text{kHz}$ ) where non-isobaric pore pressure conditions  
 241 within the homogeneous unit volume (REV) can be assumed (e.g., Mavko et al., 2020).  
 242 Thus, care should be taken when modeling the effect of porosity at seismic frequencies  
 243 ( $\ll\text{kHz}$ ). However, our dense data indicate that the spatial distributions of ultrasonic-  
 244 scale (4–6 mm) and sonic-scale (0.3–0.4 m) porosities are not homogeneous at scales larger

245 than their wavelengths, implying that a larger REV of porosity at each scale can be valid  
 246 for the seismic frequencies in the order of a Hz ( $\sim$ km). This could prolong the time for the  
 247 pore pressure equilibration within a given REV and extend the applicability of the effective  
 248 medium model to even lower frequencies (Akamatsu et al., 2024).

249 Our model also assumes an isotropic orientation of fractures. Nevertheless, actual  
 250 mesoscale fractures may exhibit anisotropy if they were formed under a deviatoric stress  
 251 field. Although it is difficult to constrain the influence of anisotropy on the sonic velocity  
 252 from our dataset alone, the presence of mesoscale fractures remains necessary even if the  
 253 effect of anisotropy is ignored.



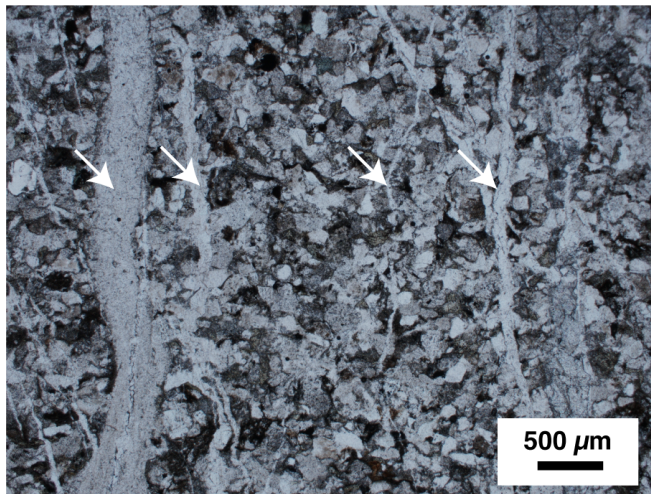
**Fig. 7** Mesoscale porosity estimated for each analyzed depth interval of the studied core.

### 254 4.3 Role of mesoscale fractures in subduction zones

255 Numerous seismological surveys have been conducted in subduction zones to explore the  
 256 relationship between seismic activity and geophysical structure. In the Nankai Trough,  
 257 seismic velocity structure has been acquired by seismic reflection surveys and waveform  
 258 inversion techniques, and low- and high-velocity anomalies have been identified in the  
 259 hanging wall side of the plate boundary fault (Kamei et al., 2013; Shiraishi et al., 2019).  
 260 Given the in situ lithostatic pressure, the identified low-velocity anomalies have been in-  
 261 terpreted as an indicator of extremely high pore-fluid pressure close to the lithostatic  
 262 pressure (i.e., low effective pressure) that can maintain open pore spaces (Kitajima and  
 263 Saffer, 2012; Tsuji et al., 2014). This interpretation of velocity anomalies has been at-  
 264 tributed to microscale pore space only because it is based on the velocity–porosity rela-  
 265 tionship for subduction-zone rocks established at ultrasonic frequency, i.e., microscale  
 266 pore space (Hoffman and Tobin, 2004; Tsuji et al., 2006). However, our results demon-

267 strate that the P-wave velocity of subduction-zone rocks can readily decrease down to 5  
 268 km/s or even lower when a part of the total porosity is accommodated by the mesoscale  
 269 fractures (Fig. 9a). As the Susaki core without mesoscale fractures (i.e., measurements  
 270 at the ultrasonic frequency) shows high velocities similar to those of high-velocity zones  
 271 along the Nankai Trough, the variations in the seismic velocity observed in the Nankai  
 272 Trough may reflect the distribution of mesoscale fractures with high pore pressure.

273 It is to be noted that our estimates of mesoscale porosities for the Susaki cores could be  
 274 formed during their exhumation processes. Thus, the mesoscale fractures estimated from  
 275 the sonic logging at the Susaki boreholes are not the ones which are in deep subduction  
 276 zones. In fact, fluid-saturated fractures that were present at subduction plate interfaces  
 277 can now be observed as veins (Muñoz-Montecinos and Behr, 2023; Otsubo et al., 2020;  
 278 Ujiie et al., 2018). The Susaki cores commonly contain quartz veins with apertures of sev-  
 279 eral tens to hundreds of microns (Fig. 8). Such veins are possibly remnants of mesoscale  
 280 fractures under high pore fluid pressure in the deep subduction zone before exhumation  
 281 and likely affected seismic velocities in the subduction zones.



**Fig. 8** Representative photomicrographs (plane-polarized light) of sandstone from the Susaki core showing quartz veins (white arrows) with apertures of several tens to hundreds of microns.

282 Fluid migration through pore spaces may trigger characteristic seismic activity in subduc-  
 283 tion zones (e.g., Tonegawa et al., 2022). The mesoscale fractures can act as effective fluid  
 284 pathways and facilitate rapid fluid drainage in the deep subduction zone, since permeabil-  
 285 ity of rock is also scale-dependent (Heap and Kennedy, 2016). The effective permeability  
 286 of rock containing randomly oriented penny-shaped cracks  $k$  is given as follows:

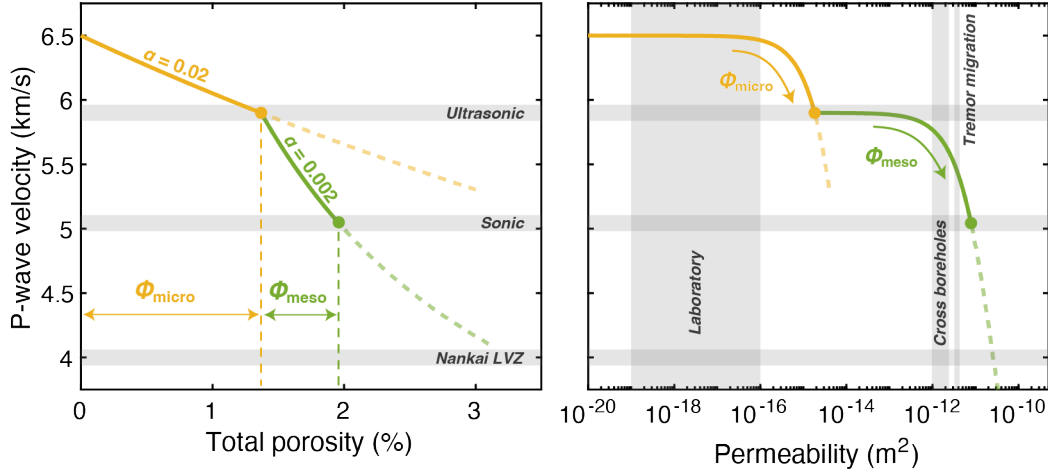
$$k = \frac{2}{15} f \phi w^2, \quad (8)$$

287 where  $f$  is the connectivity of pore space ( $0 \leq f \leq 1$ ),  $\phi$  is the porosity, and  $w$  is the mean  
 288 aperture of cracks (Guéguen and Palciauskas, 1994). This equation predicts the perme-

289 ability to be strongly dependent on crack aperture. For a rock mass containing micro- and  
 290 mesoscale porosities, the effective permeability can be expressed as follows:

$$k = k_{\text{micro}} + k_{\text{meso}} = \frac{2}{15}(f_{\text{micro}}\phi_{\text{micro}}w_{\text{micro}}^2 + f_{\text{meso}}\phi_{\text{meso}}w_{\text{meso}}^2), \quad (9)$$

291 where the subscripts denote each scale. Here, we incorporated this model into our up-  
 292 scaled DEM model and estimated the relationship between  $V_P$  and  $k$  for subduction zones,  
 293 which accounts for the scaling effect. First, we calculated  $V_P$  and  $k$  for microscale porosity  
 294 until  $V_P$  reaches the median of ultrasonic velocity of the Susaki core with a mean aspect  
 295 ratio of 0.02.  $w_{\text{micro}}$  was set as 1  $\mu\text{m}$ , based on microstructural observations (Okuda et al.,  
 296 2024). We then added mesoscale porosity into the matrix phase with the microscale  $V_P$   
 297 and  $k$  until  $V_P$  reaches the median of sonic velocity of the Susaki area with a mean aspect  
 298 ratio of 0.002.  $w_{\text{meso}}$  was set as 100  $\mu\text{m}$ , based on the sonic wavelength and the assumed  
 299 aspect ratio. Since the connectivity of pore space is not measurable from our data, we as-  
 300 summed  $f = 1$  for each scale, and the estimated permeability should therefore be considered  
 301 as the maximum value.



**Fig. 9** (a) P-wave velocity as a function of total porosity modeled for the median values of ultrasonic and sonic velocities obtained in this study (gray lines). Data from a low-velocity zone (LVZ) in the Nankai Trough (Shiraishi et al., 2019) is also presented. (b) Relationship between P-wave velocity and permeability modeled by incorporating micro- and mesoscale porosities. The vertical gray shadings represent values obtained from laboratory measurements using drill core samples from the Nankai Trough (Song and Underwood, 2017; Takahashi et al., 2013; Valdez et al., 2015), a cross-hole experiment in the Nankai Trough (Kinoshita and Saffer, 2018), and constraints based on tremor migration patterns observed in the Nankai Trough (Hendriyana and Tsuji, 2021).

302 Fig. 9b shows the relationship between  $V_P$  and  $k$  modeled using the upscaled DEM model.  
 303 The permeability initially increases by several orders of magnitude with decreasing velocity.  
 304 As  $\phi_{\text{micro}}$  increases,  $k$  increases up to  $10^{-15}$  to  $10^{-14}$   $\text{m}^2$  with a slight decrease in  $V_P$ ,  
 305 but the the rate of increase in permeability becomes more gradual once  $\phi_{\text{micro}}$  no longer

306 changes by orders of magnitude. Although these permeability values are 1–2 orders of  
307 magnitude higher than those typically measured for hand-sized sedimentary rocks in the  
308 laboratory (Song and Underwood, 2017; Takahashi et al., 2013; Valdez et al., 2015), this  
309 is likely resulted from a fixed crack aperture and assumption of perfectly connected pore  
310 spaces. When the effects of mesoscale porosity are included,  $k$  further increases by several  
311 orders of magnitude as  $V_P$  continues to decrease. Eventually,  $k$  increases to the order of  
312  $10^{-12}$  to  $10^{-11}$  m<sup>2</sup> as  $V_P$  decreases to those of the sonic velocity in the Susaki area and a  
313 low-velocity zone in the Nankai Trough (Shiraishi et al., 2019). These permeability values  
314 cover the range of permeability determined at a scale of  $\sim 100$  m by a cross-hole experi-  
315 ment in the Nankai Trough (Kinoshita and Saffer, 2018). Such high permeability values  
316 are also required to explain tremor migration patterns observed in the Nankai subduc-  
317 tion zone, which may represent fracture permeability that was enhanced during slow slip  
318 events (Hendriyana and Tsuji, 2021). Our results suggest that mesoscale fractures consti-  
319 tute highly permeable and low-velocity regions where characteristic seismic activity occurs  
320 in subduction zones. In fact, temporal changes in seismic velocity structure observed in  
321 the Nankai subduction zone have been shown to be associated with fluid migration before  
322 slow earthquakes (Tonegawa et al., 2022).

## 323 5 Conclusions

324 To explore the scale dependence of seismic velocity in subduction zones, we compared ul-  
325 trasonic and sonic velocities of core samples from the Susaki area in the Cretaceous Shi-  
326 manto accretionary complex. The comparison revealed a decrease in P-wave velocity from  
327  $\sim 6$  to 5 km/s with increasing scale, which we explain by accounting for mesoscale porosity.  
328 This finding indicates that low-velocity anomalies observed along the Nankai Trough may  
329 be associated with the presence of mesoscale fractures with high pore pressure. Mesoscale  
330 fractures can also lead to high permeability in subduction zones of up to  $10^{-12}$  to  $10^{-11}$   
331 m<sup>2</sup> and hence effective fluid drainage. Seismic activity related to transient fluid migra-  
332 tion around low-velocity zones could therefore be associated with the occurrence of the  
333 mesoscale fractures.

## 334 Declaration of competing interest

335 The authors declare no conflicts of interest.

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## 346 Data availability

347 All the laboratory data and borehole logging data used in this study are provided in the  
348 Supplementary Materials.

## 349 References

- 350 Akamatsu, Y., Kuwatani, T., Katayama, I., 2024. Spatial heterogeneity of pore structure  
351 in the crustal section of the samail ophiolite: Implications for high VP/Vs anomalies  
352 in subducting oceanic crust. *Geophysical research letters* 51, e2023GL106943. <https://doi.org/10.1029/2023GL106943>
- 353
- 354 Akamatsu, Y., Nagase, K., Abe, N., Okazaki, K., Hatakeyama, K., Katayama, I., 2023.  
355 Cross-property relationship between electrical resistivity and elastic wave velocity of  
356 crustal rocks from the Oman drilling project hole GT3A: Implications for in situ geo-  
357 physical properties of oceanic crust. *Journal of Geophysical Research, [Solid Earth]*  
358 128. <https://doi.org/10.1029/2022jb026130>
- 359 Audet, P., Schwartz, S.Y., 2013. Hydrologic control of forearc strength and seismicity in  
360 the Costa Rican subduction zone. *Nature geoscience* 6, 852–855. [https://doi.org/10.](https://doi.org/10.1038/ngeo1927)  
361 [1038/ngeo1927](https://doi.org/10.1038/ngeo1927)
- 362 Bailly, C., Fortin, J., Adelinet, M., Hamon, Y., 2019. Upscaling of elastic properties in  
363 carbonates: A modeling approach based on a multiscale geophysical data set. *Journal*  
364 *of Geophysical Research, [Solid Earth]* 124, 13021–13038. [https://doi.org/10.1029/](https://doi.org/10.1029/2019jb018391)  
365 [2019jb018391](https://doi.org/10.1029/2019jb018391)
- 366 Berryman, J.G., Pride, S.R., Wang, H.F., 2002. A differential scheme for elastic properties  
367 of rocks with dry or saturated cracks. *Geophysical Journal International* 151, 597–611.  
368 <https://doi.org/10.1046/j.1365-246X.2002.01801.x>
- 369 Eberhart-Phillips, D., Bannister, S., Reyners, M., 2017. Deciphering the 3-D distribution  
370 of fluid along the shallow Hikurangi subduction zone using P- and S-wave attenuation.  
371 *Geophysical Journal International* 211, 1032–1045. <https://doi.org/10.1093/gji/ggx348>
- 372 Fortin, J., Guéguen, Y., 2021. Porous and cracked rocks elasticity: Macroscopic poro-  
373 elasticity and effective media theory. *Mathematics and mechanics of solids: MMS* 26,  
374 1158–1172. <https://doi.org/10.1177/10812865211022034>
- 375 Guéguen, Y., Palciauskas, V., 1994. Introduction to the physics of rocks. Princeton Uni-  
376 versity Press.
- 377 Hamahashi, M., Saito, S., Kimura, G., Yamaguchi, A., Fukuchi, R., Kameda, J., Hamada,  
378 Y., Kitamura, Y., Fujimoto, K., Hashimoto, Y., Hina, S., Eida, M., 2013. Contrasts in  
379 physical properties between the hanging wall and footwall of an exhumed seismogenic  
380 megasplay fault in a subduction zone—an example from the Nobeoka thrust drilling  
381 project. *Geochemistry, Geophysics, Geosystems* 14, 5354–5370. [https://doi.org/10.](https://doi.org/10.1002/2013gc004818)  
382 [1002/2013gc004818](https://doi.org/10.1002/2013gc004818)
- 383 Hashimoto, Y., Eida, M., Kirikawa, T., Iida, R., Takagi, M., Furuya, N., Nikaizo,  
384 A., Kikuchi, T., Yoshimitsu, T., 2012. Large amount of fluid migration around  
385 shallow seismogenic depth preserved in tectonic mélange: Yokonami mélange,  
386 the Cretaceous Shimanto belt, Kochi, southwest Japan. *Island Arc* 21, 53–64.  
387 <https://doi.org/10.1111/j.1440-1738.2011.00806.x>
- 388 Heap, M.J., Kennedy, B.M., 2016. Exploring the scale-dependent permeability of frac-  
389 tured andesite. *Earth and Planetary Science Letters* 447, 139–150. [https://doi.org/10.](https://doi.org/10.1016/j.epsl.2016.05.004)  
390 [1016/j.epsl.2016.05.004](https://doi.org/10.1016/j.epsl.2016.05.004)

- 391 Hendriyana, A., Tsuji, T., 2021. Influence of structure and pore pressure of plate interface  
392 on tectonic tremor in the nankai subduction zone, japan. *Earth and planetary science*  
393 *letters* 558, 116742. <https://doi.org/10.1016/j.epsl.2021.116742>
- 394 Hoffman, N.W., Tobin, H.J., 2004. An empirical relationship between velocity and poros-  
395 ity for underthrust sediments in the nankai trough accretionary prism. *Proc. Ocean*  
396 *Drill. Program Sci. Results*, 190 196, 1–23.
- 397 Ide, S., 2010. Striations, duration, migration and tidal response in deep tremor. *Nature*  
398 466, 356–359. <https://doi.org/10.1038/nature09251>
- 399 Itaba, S., Umeda, Y., Koizumi, N., Watanabe, H., Nakayama, N., Sakai, S., 2014. Geo-  
400 logical data of the GSJ boring core at the susaki-otani observation station (No. 595).  
401 *Geol. Surv. Japan, AIST*.
- 402 Kamei, R., Pratt, R.G., Tsuji, T., 2013. On acoustic waveform tomography of wide-angle  
403 OBS data—strategies for pre-conditioning and inversion. *Geophysical Journal Interna-*  
404 *tional* 194, 1250–1280. <https://doi.org/10.1093/gji/ggt165>
- 405 Kinoshita, C., Saffer, D.M., 2018. In situ permeability and scale dependence of an active  
406 accretionary prism determined from cross-borehole experiments. *Geophysical research*  
407 *letters* 45, 6935–6943. <https://doi.org/10.1029/2018gl078304>
- 408 Kitajima, H., Saffer, D.M., 2012. Elevated pore pressure and anomalously low stress in  
409 regions of low frequency earthquakes along the nankai trough subduction megathrust.  
410 *Geophysical research letters*. <https://doi.org/10.1029/2012GL053793>
- 411 Kitamura, M., Hirose, T., Lei, X., 2021. Mechanical weakness of the nankai accretionary  
412 prism: Insights from V p measurements of drill cuttings. *Geochemistry, Geophysics,*  
413 *Geosystems* 22. <https://doi.org/10.1029/2020gc009536>
- 414 Matonti, C., Guglielmi, Y., Viseur, S., Bruna, P.O., Borgomano, J., Dahl, C., Marié, L.,  
415 2015. Heterogeneities and diagenetic control on the spatial distribution of carbonate  
416 rocks acoustic properties at the outcrop scale. *Tectonophysics* 638, 94–111. <https://doi.org/10.1016/j.tecto.2014.10.020>
- 417
- 418 Mavko, G., Mukerji, T., Dvorkin, J., 2020. *The rock physics handbook*. Cambridge Uni-  
419 *versity Press*.
- 420 Muñoz-Montecinos, J., Behr, W.M., 2023. Transient permeability of a deep-seated sub-  
421 duction interface shear zone. *Geophysical research letters* 50. <https://doi.org/10.1029/2023gl104244>
- 422
- 423 Okuda, H., Akamatsu, Y., Kitamura, M., Sawai, M., 2024. Elastic properties of hanging  
424 wall rock at the seismogenic zone and critical nucleation length for megathrust earth-  
425 quakes. *ESS Open Archive*. <https://doi.org/10.22541/essoar.171838469.98902412/v1>
- 426 Otsubo, M., Hardebeck, J.L., Miyakawa, A., Yamaguchi, A., Kimura, G., 2020. Localized  
427 fluid discharge by tensile cracking during the post-seismic period in subduction zones.  
428 *Scientific reports* 10, 12281. <https://doi.org/10.1038/s41598-020-68418-z>
- 429 Raimbourg, H., Hamano, Y., Saito, S., others, 2011. Acoustic and mechanical properties  
430 of nankai accretionary prism core samples. *Geochemistry: Exploration, Environment,*  
431 *Analysis*. <https://doi.org/10.1029/2010GC003169>
- 432 Saffer, D., 2003. Pore pressure development and progressive dewatering in underthrust  
433 sediments at the costa rican subduction margin: Comparison with northern barba-  
434 dos and nankai. *Journal of geophysical research* 108, 2261. <https://doi.org/10.1029/2002JB001787>
- 435
- 436 Saffer, D.M., Tobin, H.J., 2011. Hydrogeology and mechanics of subduction zone forearcs:  
437 Fluid flow and pore pressure. *Annual review of earth and planetary sciences* 39, 157–  
438 186. <https://doi.org/10.1146/annurev-earth-040610-133408>



- 439 Sakaguchi, A., 1999. Thermal maturity in the shimanto accretionary prism, southwest  
440 japan, with the thermal change of the subducting slab: Fluid inclusion and vitrinite  
441 reflectance study. *Earth and planetary science letters* 173, 61–74. [https://doi.org/10.](https://doi.org/10.1016/S0012-821X(99)00219-8)  
442 1016/S0012-821X(99)00219-8
- 443 Sarout, J., Ferjani, M., Guéguen, Y., 2009. A semi-automatic processing technique for  
444 elastic-wave laboratory data. *Ultrasonics* 49, 452–458. [https://doi.org/10.1016/j.ultras.](https://doi.org/10.1016/j.ultras.2008.12.001)  
445 2008.12.001
- 446 Shiraishi, K., Moore, G.F., Yamada, Y., Kinoshita, M., Sanada, Y., Kimura, G., 2019.  
447 Seismogenic zone structures revealed by improved 3-D seismic images in the nankai  
448 trough off kumano. *Geochemistry, Geophysics, Geosystems*. [https://doi.org/10.1029/](https://doi.org/10.1029/2018gc008173)  
449 2018gc008173
- 450 Song, C., Underwood, M.B., 2017. Data report: Permeability and microfabric of core sam-  
451 ples from IODP expedition 348, hole C0002P, nankai trough accretionary prism, in:  
452 Proceedings of the IODP, Proceedings of the Integrated Ocean Drilling Program . In-  
453 tegrated Ocean Drilling Program. Integrated Ocean Drilling Program. [https://doi.org/](https://doi.org/10.2204/iodp.proc.348.201.2017)  
454 10.2204/iodp.proc.348.201.2017
- 455 Taira, A., 1988. The shimanto belt in shikoku, japan-evolution of cretaceous to miocene  
456 accretionary prism. *Shimanto Belt, Modern Geology* 12, 5–46.
- 457 Takahashi, M., Azuma, S., Uehara, S.-I., Kanagawa, K., Inoue, A., 2013. Contrasting hy-  
458 drological and mechanical properties of clayey and silty muds cored from the shallow  
459 nankai trough accretionary prism. *Tectonophysics, Proceedings of the integrated ocean*  
460 *drilling program 314/315/316Mechanical behavior of crustal RocksProceedings of the*  
461 *integrated ocean drilling program 314/315/316Fault mechanics and transport proper-*  
462 *ties of RocksProceedings of the integrated ocean drilling program 314/315/316The seis-*  
463 *mogenic zone of subduction thrust FaultsAmerican geophysical union 2008 fall meet-*  
464 *ing, T31A-1980Proceedings of the integrated ocean drilling program 314/315/316Phys-*  
465 *ical properties of rocks: Fundamentals and principles of PetrophysicsProceedings of*  
466 *the integrated ocean drilling program 314/315/316The seismogenic zone of subduction*  
467 *thrust faults 600, 63–74. https://doi.org/10.1016/j.tecto.2013.01.008*
- 468 Tonegawa, T., Takemura, S., Yabe, S., Yomogida, K., 2022. Fluid migration before and  
469 during slow earthquakes in the shallow nankai subduction zone. *Journal of Geophys-*  
470 *ical Research, [Solid Earth]* 127. <https://doi.org/10.1029/2021jb023583>
- 471 Tsuji, T., Kamei, R., Pratt, R.G., 2014. Pore pressure distribution of a mega-splay fault  
472 system in the nankai trough subduction zone: Insight into up-dip extent of the seismo-  
473 genic zone. *Earth and planetary science letters* 396, 165–178. [https://doi.org/10.1016/](https://doi.org/10.1016/j.epsl.2014.04.011)  
474 j.epsl.2014.04.011
- 475 Tsuji, T., Kimura, G., Okamoto, S., Kono, F., Mochinaga, H., Saeki, T., Tokuyama, H.,  
476 2006. Modern and ancient seismogenic out-of-sequence thrusts in the nankai ac-  
477 cretionary prism: Comparison of laboratory-derived physical properties and seismic re-  
478 flection data. *Geophysical research letters* 33. <https://doi.org/10.1029/2006GL027025>
- 479 Ujiie, K., Saishu, H., Fagereng, Å., Nishiyama, N., Otsubo, M., Masuyama, H., Kagi, H.,  
480 2018. An explanation of episodic tremor and slow slip constrained by crack-seal veins  
481 and viscous shear in subduction mélange. *Geophysical research letters* 45, 5371–5379.  
482 <https://doi.org/10.1029/2018gl078374>
- 483 Valdez, R.D., II, Lauer, R.M., Ikari, M.J., Kitajima, H., Saffer, D.M., 2015. Data report:  
484 Permeability and consolidation behavior of sediments from the northern japan trench  
485 subduction zone, IODP site C0019, in: Proceedings of the IODP, Proceedings of the  
486 Integrated Ocean Drilling Program . Integrated Ocean Drilling Program. Integrated

487 Ocean Drilling Program. <https://doi.org/10.2204/iodp.proc.343343t.201.2015>  
488 van Everdingen, 1995. Fracture characteristics of the sheeted dike complex, troodos ophi-  
489 olite, cyprus: Implications for permeability of oceanic crust. *Journal of geophysical*  
490 *research* 100, 19957–19972. <https://doi.org/10.1029/95JB01575>