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On the influence of pressure, phase transitions, and water on large-scale seismic anisotropy underneath a subduction zone

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- ¹³ P−dependent olivine textures can explain the evolution of upper mantle anisotropy.
- $\bullet\;$ A relatively wet upper transition zone could likely explain faster V_{SV} than V_{SH}
- ¹⁵ speeds.

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Abstract

 Seismic anisotropy mainly originates from the crystallographic preferred orientation (CPO) of minerals deformed in the convective mantle flow. While fabric transitions have been previously observed in experiments, their influence on large-scale anisotropy is not well- documented. Here, we implement 2D geodynamic models of intra-oceanic subduction $_{21}$ coupled with mantle fabric modelling to investigate the combined effect of pressure (P)- and water-dependent microscopic flow properties of upper mantle and upper transition zone (UTZ) minerals, respectively, on large-scale anisotropy. Our results for the upper mantle correlate well with observations, implying that the P-dependence of olivine fab- rics is sufficient to explain the variability of anisotropy. Meanwhile, a dry UTZ tends to be near-isotropic whereas a relatively wet UTZ could produce up to 1% azimuthal and $27 \sim 2\%$ radial anisotropy. Because water facilitates CPO development, it is therefore likely a requirement to explain the presence of anisotropy in the transition zone close to sub-ducting slabs.

Plain Language Summary

 Subduction causes the surrounding mantle to deform according to the movement ³² and pressure exerted by the plates. This influences the alignment of minerals making up the mantle, which in turn, affects the speed and direction of seismic waves known as seis-³⁴ mic anisotropy. In this study, we investigate the role of pressure in the upper mantle and water in the transition zone on large-scale seismic anisotropy across a subduction zone. ³⁶ In the upper mantle, we show that the patterns of anisotropy at places where deforma- tion is presumed to be large are affected by changes in pressure. In the transition zone, anisotropy tends to favour a wetter environment.

1 Introduction

 Understanding subduction dynamics is crucial as it regulates, to first order, the cou-⁴¹ pling between deep mantle convection and surface deformation. Changes in mineralogy and viscosity structure at designated mantle transition zone boundaries control the style of subduction, and to some extent, the overall dynamics of plate tectonics (Agrusta et al., 2017; Goes et al., 2017). A plethora of geophysical observables can be used to con-strain mantle flow; one of them is seismic anisotropy.

 Seismic anisotropy mainly results from the crystallographic preferred orientation (CPO) in intrinsically anisotropic minerals upon progressive deformation along convective flows (Long & Becker, 2010). The parameters $ξ$ for S –wave radial anisotropy (i.e., 49 the ratio of the squares of V_{SH} and V_{SV} for horizontally-propagating S–waves) and a_z for azimuthal anisotropy (i.e., directional-dependence of V_{SV}) are simple yet intuitive ways of quantifying seismic anisotropy, and hence, are often constrained in tomographic imaging (e.g. Smith & Dahlen, 1973; Montagner, 1998; Panning & Romanowicz, 2006). In a subduction zone, the mantle wedge is characterized by a layer of positive radial anisotropy $\zeta > 1$ (e.g. French & Romanowicz, 2014; Chang et al., 2015; Simmons et al., 2021) and 2−3% peak-to-peak azimuthal anisotropy (e.g. Yuan & Beghein, 2013; Debayle et al., 2016). Underneath the oceanic lithosphere away from the slab, the patterns of anisotropy appear less complex exhibiting an age-independent distribution of $\xi > 1$ and $a_{V_{SV}}$ 2% with maximum amplitudes appearing at ∼ 150 km (e.g. Yuan & Beghein, 2013; Debayle et al., 2016; Chang et al., 2015). Reduction of seismic anisotropy is observed past ∼ 250 km depth (e.g. Nettles & Dziewo´nski, 2008; Burgos et al., 2014). Across the upper transi-61 tion zone (UTZ, 410 – 520 km) around slabs, ξ < 1 and $a_{V_{SV}} \sim 1-2\%$ is generally observed (e.g. Montagner et al., 2021).

 The prevalent seismic anisotropy observed around subduction zones may be attributed either in terms of large strains that the entrained mantle adjacent to the slab experiences (Mainprice, 2010), structural layering of plate remnants (Karato, 1998), or possibly an

–3–

2 Methods

 We carry out 2D 6000 km $\times1000$ km thermo-chemical modelling of intra-oceanic subduction with phase transformations using the open software ASPECT (Kronbichler

–4–

2.1 Mantle fabric modelling

 Starting at the initial step along a pathline followed by a tracer, we estimate the local velocity gradient \mathbf{L}' , local total pressure (hydrostatic + dynamic) P' , and local tem- $_{104}$ perature T' by introducing a new velocity, total pressure, and temperature fields at the ¹⁰⁵ current time step t from ASPECT. Local density ρ' along the pathline is estimated with the help of the density map (Figure S2a). At the final time step t_{final} , tracers are reg- ularly distributed inside the white dashed rectangle of Figure S2c where anisotropy has $_{108}$ been calculated. We use the full L' for strain accumulation.

 To model mantle fabrics, we implement the modified viscoplastic self-consistent (VPSC) method of Lebensohn and Tom´e (1993) that incorporates P−induced slip transitions and P−induced phase transformations (Magali et al., 2024). While kinematic models are less computationally demanding and can replicate large-scale anisotropy features (e.g. Kamin- ski et al., 2004), VPSC offers the capability to work with an arbitrary number of inde- pendent slip systems. Furthermore, it explicitly accounts for variations in intragranu- lar stress and strain, resulting in more precise predictions of the mechanical behavior of deforming polycrystals (Castelnau et al., 2008). Each tracer with density ρ' is composed of 3000 initial randomly oriented grains with the following modal abundancies: Upper mantle $(\rho' < 3720 \text{ kg} \cdot \text{m}^{-3})$: 60% P-dependent olivine (Magali et al., 2024) and 40%

–5–

other phases (assumed isotropic), UTZ (3720 $\leq \rho' < 3850 \text{ kg} \cdot \text{m}^{-3}$): 60% wadsleyite

 μ_{120} (Ledoux et al., 2023a) and 40% garnet, and lower transition zone (LTZ, 3850 $\leq \rho' <$

 $_{121}$ 4170 kg · m⁻³): 60% ringwoodite and 40% garnet. Both garnet and ringwoodite are deemed ¹²² isotropic (e.g. Mainprice, 2007). The single crystal elastic constants of the phases at am- 123 bient conditions, including their PT derivatives are listed in Magali et al. (2024). Wad-¹²⁴ sleyite properties are more complex to incorporate and will henceforth be discussed be-¹²⁵ low.

¹²⁶ 2.2 An ersatz to compute water-dependent anisotropy in the transition ¹²⁷ zone

¹²⁸ In this study, we assume that the ambient UTZ is dry and the slab, together with ¹²⁹ the entrained mantle, is relatively wet. To do this, tracers are specified with either hy- 130 drous (i.e., C_{wd} -type) or dry wadsleyite (i.e., B_{wd} -type) depending on their positioning relative to the slab (Ledoux et al., 2023a). Tracers with $T' < 1750$ K envelope the cold $_{132}$ and slightly hydrated slab, and hence C_{wd} -type CPO is calculated. Consequently, those with $T' \ge 1750$ K are prescribed with a B_{wd}-type fabric. The latter corresponds to trac-¹³⁴ ers scattered around the dry and ambient UTZ. We also test the effect of a fully dry UTZ 135 by computing the CPO of B_{wd}-type wadsleyite aggregates across the entire UTZ.

 P and T-dependent wadsley the polycrystal elastic tensors are also computed us-¹³⁷ ing Voigt-Reuss-Hill averaging around their single crystal counterparts. Hydrous and dry ¹³⁸ elastic constants are inferred from Zhou et al. (2022) and N´u˜nez-Valdez et al. (2013), respectively. Their PT derivatives are also listed in Magali et al. (2024). CPO of a tracer ¹⁴⁰ crossing a phase transition boundary determined by the density crossovers is erased and ¹⁴¹ instead replaced with random textures according to experimental results of microstructures induced by the olivine \rightarrow wadsleyite transition (Smyth et al., 2012; Ledoux et al., ¹⁴³ 2023b). Anisotropy calculations are ceased past $\rho' = 4150 \text{ kg} \cdot \text{m}^{-3}$ (i.e., 660 km). Min-¹⁴⁴ eral assignments are summarized in Figure 1.

–6–

2.3 Elastic homogenization

3 Results

3.1 Predictions of large-scale upper mantle anisotropy induced by sub-duction

 The influence of P−induced slip transitions on anisotropy can be observed in the subslab mantle (Figures 2a and 3a). Here, anisotropy strength decreases with depth; drop-¹⁵⁹ ping to $\xi \sim 1.01$ and $a_z \sim 1\%$ at $z = 400$ km. The presumed switch in primary ac- tivities from the $[100](010)$ to the $[001](010)$ slip systems may have caused this (Raterron et al., 2014; Magali et al., 2024), as also evidenced by the slight re-alignment of the [100] axes towards the (010) direction (Figure S3e-g). The mantle wedge mainly exhibits pos-163 itive radial anisotropy $ξ > 1$ and nonzero azimuthal anisotropy $a_z \sim 5\%$. However, the entrained mantle immediately beneath the back-arc basin ($z \sim 90 - 150$ km) ex- periences rapid trench retreat motion due to a decreased upper plate forcing of a thin overriding lithosphere (Agrusta et al., 2017). This creates a localized region of complex 167 anisotropy patterns with ξ < 1 and a_z < 5%. Negative radial anisotropy ($\xi \sim 0.97$) and near-zero azimuthal anisotropy are generated just above the upper transition zone (UTZ) close to the slab ($\sim 290-400$ km). At these depths, the lateral extent x of sub-170 horizontal FSE orientations cover \sim 2000 km \leq x \leq 3200 km (Figure 1b). Li et al.

 (2014) revealed aggregates submitted to subduction zone stresses exhibit olivine [100] axes that are approximately aligned with the FSE long axis. The existence of a negative radial anisotropy $\xi < 1$ at these depths, where the fast directions are now sub-normal to the FSE, is also indicative of P−induced slip transitions in olivine.

3.2 Effect of water around the slab on mantle transition zone anisotropy

 A wet UTZ near the slab is generally characterized by an accumulation of nega-177 tive radial anisotropy with $\xi \sim 0.97$ above the slab and $\xi \sim 0.98$ in the subslab area 178 (Figure 2a). A localized area of weak positive radial anisotropy ($\xi \sim 1.01$) forms close to the slab tip which can be attributed to the preferential alignment of the [100] axes of the C_{wd}−type phase with the horizontal (Figure S3h) in response to rapid changes in the deformation patterns of the entrained mantle close to the slab tip. Small amounts ¹⁸² of azimuthal anisotropy $a_Z \sim 1.1\%$ far from the slab tip and up to $a_Z \sim 1\%$ in the remaining regions close to the slab can be found (Figure 3a).

 Figures 2b and 3b show the results of the same calculations assuming a fully dry ¹⁸⁵ transition zone (i.e., B_{wd} -type texture and elastic constants retrieved from Núñez-Valdez et al. (2013)). Such an assumption leads to an almost isotropic UTZ around the slab. $a_Z \sim 1.1\%$ away from the slab tip can also be detected which means that dry fabrics can produce enough azimuthal anisotropy but may fail to generate observable radial anisotropy.

 3.3 Comparison with tomographic observations: a case for the Honshu **arc**

 We select cross-sections of radial anisotropy and azimuthal anisotropy from SGLOBE- Rani (Chang et al., 2015) and 3DLGL-TPESv.v2022-11 (Debayle et al., 2016), respec- tively, for the Honshu subduction zone which, to some extent, displays a similar geom- etry and subduction style to our model. For comparison, we solely homogenize the CPO model with a wet UTZ since we find that no substantial anisotropy is developed assum-ing a fully dry UTZ, contrary to tomographic observations where anisotropy is present

–8–

¹⁹⁷ around slabs (e.g. Chang et al., 2015; Debayle et al., 2016; Montagner et al., 2021). Sup-¹⁹⁸ plementary Figures S4 and S5 show the effective anisotropy models at different homog-199 enization wavelengths λ_0 .

2200 3.3.1 Effective radial anisotropy $(\lambda_0=65\;\mathrm{km})$ comparison with SGLOBE- $_{201}$ Rani

 Γ ²⁰² ²⁰² comparable to SGLOBE-Rani, we choose 203 a homogenization wavelength of $\lambda_0 = 65$ km (Figure 2c). Localized areas of the observed $_{204}$ negative radial anisotropy $\xi_{\rm obs}$ < 1 underneath the back-arc basin and just above the ²⁰⁵ stagnant slab is evident (Figure 2d). Whether these peculiar features are robust or not, ²⁰⁶ however, warrants regional tomography for better resolution. Nonetheless, their pres-²⁰⁷ ence can be reproduced with a geodynamic model that accounts for transient flows and ²⁰⁸ P-dependent fabrics in olivine (Figures 2c; 2e red and green dashed lines). Across the subslab mantle, the decrease in ξ^* with depth correlates well with observations. In the ²¹⁰ UTZ, modelling with wet wadsleyite fabrics captures the persistence of ξ_{obs} < 1 near 211 the slab. P−induced phase transformations from olivine to wadsleyite at \sim 410 km, and ²¹² to ringwoodite at ∼520 km introduce sharp velocity contrasts that when homogenized, produce a thin layer of weak $\xi^* > 1$ which is not observed in SGlobe-Rani. Finally, ξ^* 213 cannot explain the prevalence of ξ_{obs} in the LTZ. Small-scale heterogeneities unaccounted ²¹⁵ for in our model such as petrological layering of transformed subducted material could ²¹⁶ explain such observations (Karato, 1998). Smearing effects from the tomographic inver-²¹⁷ sion could also lead to the presence of radial anisotropy in the LTZ.

218 3.3.2 Effective azimuthal anisotropy $(\lambda_0 = 164 \text{ km})$ comparison with 3DLGL- 219 $TPESv. v2022-11$

220 Choosing a longer homogenization wavelength $(\lambda_0 \sim 165 \text{ km})$ intensifies the spa- $_{221}$ tial averaging of small-scale heterogeneities in azimuthal anisotropy (Figure 3c). This ²²² leads to a decrease in azimuthal anisotropy of about 1%. Comparison with the 3DLGL-

²³⁵ 4 Discussion

²³⁶ 4.1 Pressure-dependence of single-phase fabrics and its implications for ²³⁷ the upper mantle

²³⁸ Laboratory studies have already reported the existence of pressure-dependence of ²³⁹ olivine microstructures (Mainprice et al., 2005; Raterron et al., 2007; Jung et al., 2009; ²⁴⁰ Ohuchi et al., 2011), and most recently of bridgmanite (Gay et al., 2024). To this day, ²⁴¹ however, it is still not clear how textures evolve with hydrostatic pressure (Karato et al., ²⁴² 2008) since high-P experiments are also characterized by high differential stresses $\sigma \sim$ ²⁴³ 100−500 MPa which could contribute to fabric transitions (e.g. Katayama et al., 2004). ²⁴⁴ Deformed peridotites extracted from xenoliths gathered mostly from the Western US, however, recorded lower differential stresses of about ~ 30 MPa (Bernard et al., 2019). 246 Under low σ , Raterron et al. (2012) numerically demonstrated using the first-principles ²⁴⁷ approach of Durinck et al. (2007) the slip transition from $[100](010)$ to $[001](010)$ olivine ²⁴⁸ slip system in the deep upper mantle; consistent with Raterron et al. (2007); Jung et al. $_{249}$ (2009); Ohuchi et al. (2011).

4.1.1 Can P−induced slip transitions be used as a proxy to describe the alphabet fabrics (i.e, A-, B-, C-, and E-type olivine)?

 The response of strain-induced anisotropy on pressure becomes more evident in re- gions associated with large deformation (Magali et al., 2024); in our model, across the mantle wedge and the subslab mantle where the entrained mantle experiences first-hand the influence of slab pull. At low pressures, our implementation of P−induced olivine $_{256}$ fabric transitions emulates an A-type fabric because of increased activities at the $[100](010)$ slip system. At high pressures, it somehow follows a B-type fabric due to the switch in $_{258}$ primary activities to the [001](010) slip system (Raterron et al., 2012, 2014). While P-induced apparent B-type fabrics could explain the distribution of anisotropy around the slab at high pressures, we could also not dismiss the effect of water on the generation of such fabric at low confining pressures (Ohuchi et al., 2012). Proxies of a water-rich environ- ment in the convective flow are required to differentiate the possible origin (i.e. P−induced or water-induced) of B-type fabrics; although there is still no apparent relationship be-tween olivine fabric types and water fugacity (Bernard et al., 2019).

 Different conditions must be met to derive a suite of fabrics other than A- and B- type. Under low stresses and at increasing temperatures and a relatively dry mantle, an A -type transitions to an E-type¹ fabric, and increasing water content, to a C-type² fab- ric (Karato et al., 2008). Results from geodynamic simulations of upper mantle flow suggest $\xi > 1$ for A, B, and E-type fabrics, with E-type exhibiting minimal strength, whereas ζ < 1 for C-type, in the case of horizontal simple shear. As for a_z , all except B-type exhibit fast propagation directions parallel to the direction of shear (Long & Becker, 2010).

easiest slip system at $[100](001)$

easiest slip system at $[001](100)$

4.1.2 On the reduction of free-parameters to constrain patterns of large-scale anisotropy

 In recent years, models of upper mantle anisotropy are derived from carefully cho- sen methodologies such as: (a) implementation of a two-phase aggregate composed of 60% olivine and 40 % enstatite reminiscent of a pyrolitic mantle (Ringwood, 1991), (b) strain partitioning where a fraction accommodated by dislocation creep is used for CPO development consistent with Karato and Wu (1993), and (c) the extension of homoge- nization methods for CPO modelling by incorporating dynamic recrystallization. Sev- eral studies have applied such methodologies in a subduction setting where the variabil- ity of radial anisotropy has been correctly predicted in certain places (Faccenda & Cap- itanio, 2012; Faccenda, 2014; Sturgeon et al., 2019; Ferreira et al., 2019). Implementa- tion of such methodologies, however, becomes increasingly difficult due to the sheer amount of free parameters that control the variability of anisotropy. This is not to say that these methods should not be implemented given that such values can be obtained from liter- ature. However, a more grounded approach should not be ruled out either. We argue that a simple depth-dependent anisotropy of single-phase aggregates, without the need for strain partitioning and additional mechanisms for CPO development, is enough to ex plain the variability of large-scale anisotropy in the upper mantle. This is especially true ³⁰⁰ given the uncertainty surrounding where dislocation creep should subjugate (Hirth & Kohlstedf, 2003; Becker & Lebedev, 2021) and the inability of seismic waves to distin-³⁰² guish deformation from recrystallization textures (Wenk & Tomé, 1999).

4.2 Importance of water on the variability of transition zone anisotropy

 In light of our conducted numerical experiments, a relatively wet UTZ subjected to subduction stresses produces substantial radial anisotropy and about 1% azimuthal anisotropy. Contrastingly, a fully dry UTZ appears mostly isotropic. The anisotropy dis- tribution in the hydrous model is thus consistent with source-side splitting observations surrounding deep earthquakes, particularly in the western Pacific (Nowacki et al., 2015; 309 Mohiuddin et al., 2015). Our predictions, however, are not perfect, particularly a_z where $_{310}$ its amplitude appears underestimated. Around slabs, Moulik and Ekström (2014) mea-311 sured radial anisotropy of about $\xi \sim 1.04$ underneath the circum-Pacific region; whereas 312 azimuthal anisotropy could reach up to $a_z \sim 3\%$ according to Huang et al. (2019). There are several propositions for the increased anisotropy around subduction zones aside from wadsleyite CPO. Local enrichment of akimotoite may be the leading cause for source- $_{315}$ side shear wave splitting observations underneath stagnant slabs (Foley & Long, 2011). Dense hydrous magnesium silicates (DHMS) have also been shown to be very anisotropic at UTZ conditions (Nowacki et al., 2015) but their abundance and stability remain in- conclusive (Hao et al., 2020). Although Nowacki et al. (2015) suggested shape preferred 319 orientation may contribute to the development of anisotropy, this may be unlikely since $_{320}$ elliptical inclusions must be periodically aligned vertically to match $\xi < 1$ around sub- duction zones where horizontal laminations are more rampant instead (Faccenda et al., 2019; Magali et al., 2021). Furthermore, neither metastable olivine nor topotactical re- lationships between olivine and wadsleyite could be possible candidates due to their un- likely existence in hydrous environments (Smyth et al., 2012). It is thus plausible that the amount of effective strains in our models did not achieve that of actual subduction

 systems, and that our 2D setting relegates the complexity of deformation patterns which would explain the discrepancy in anisotropy strength (McKenzie, 1979). Even so, we as-sert that the patterns of UTZ anisotropy we predict remain robust.

 The incorporation of water in wadsleyite promotes CPO development and there- fore captures the variability of anisotropy. This challenges the study of Chang and Fer- reira (2019) where it is inferred that a dry UTZ is likely the cause of substantial radial anisotropy ($\xi \sim 1.02-1.03$) across slabs underneath the western Pacific. While a dry single crystal wadsleyite indeed contains larger intrinsic anisotropy, Zhou et al. (2022) reported anisotropy increases with water content in the case of deformed wadsleyite ag- gregates, primarily due to increased crystallographic defects that weaken its rheology. With enough deformation accumulated in the UTZ, we model, for the first time, the de-337 pendence of the distribution of large-scale anisotropy on water. The relatively misun- derstood effect of strong accumulation, however, precludes the prediction of anisotropy strength with the degree of hydration in the UTZ. Further analyses are imperative to reconcile seismic observations (e.g. Chang & Ferreira, 2019) and mineralogical exper- iments (e.g. Ohuchi et al., 2014; Zhou et al., 2022) with the help of additional constraints such as electrical conductivity measurements (Kelbert et al., 2009; Karato, 2011).

5 Conclusion

 \mathcal{S}_{344} We have integrated pressure(P)-induced olivine fabric transitions and P-induced phase transformations in CPO calculations to predict the distribution of large-scale anisotropy around a subduction zone. Coupled with an elastic homogenization algorithm that acts as a tomographic filter, depth-dependent anisotropy of a single-phase fabric is enough to capture the variability of the observed anisotropy in the upper mantle. Strain par- titioning, modelling of multi-phase aggregates, and implementations of other potential mechanisms for CPO development may not be warranted; reducing the number of free parameters that need to be constrained. In the upper transition zone (UTZ), the CPO

–14–

 of deformed hydrous wadsleyite is likely the leading cause for the observed anisotropy near the subducting slab. This opens a fresh perspective on how water is integral to its deformation history. Discrepancies in the strength of anisotropy, however, remain an open question. Further challenges therefore await such as identifying an empirical relation-ship between the amount of water and the strength of anisotropy in deformed aggregates.

Open Research Section

 Subduction flow modelling was done using the open software ASPECT (https:// aspect.geodynamics.org/), and fabric calculations were performed using VPSC (https:// github.com/lanl/VPSC code) The Fast Fourier Homogenization (FFH) code can be made available upon reasonable request to Y. Capdeville. Its foundation is based upon the fol- lowing in-text citation references: (Capdeville et al., 2015) and (Capdeville & Métivier, 2018). This study is entirely numerical. The input files for Aspect and VPSC, useful rou- tines for calculating single crystal elastic constants and CRSS as a function of P and T, and output elastic tensor files can be found in https://doi.org/10.5281/zenodo.12774418.

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Figure 1. (a) Distribution of mineralogical fabrics across the subduction zone at the present day: Ol - olivine, Wd - wadsleyite, Gt - garnet, Rw - ringwoodite. In the upper transition zone, the distribution of hydrous and dry Wd is solely determined by the evolution of the 1750 K isotherm (solid red line) that encapsulates the slab (in blue). Solid black lines are the predicted topographies of the phase transition boundaries. For a fully dry UTZ, dark green shades associated with Cwd−type wadsleyite cover the entire UTZ. (b) Second invariant of the strain rate tensor ε II. Arrowless vectors correspond to the orientation of the finite strain ellipse.

Figure 2. (a) Radial anisotropy $\xi = (V_{SH}/V_{SV})^2$ for a mantle model with a wet UTZ. (b) Same as (a) but for a dry UTZ. (c) Effective radial anisotropy ξ^* at $\lambda_0 = 65$ km for the wet UTZ model. The effective radial anisotropy in the case of a dry UTZ model is not shown since no significant anisotropy is produced. (d) Radial anisotropic tomography image across the Honshu arc retrieved from SGlobe-Rani Chang et al. (2015). (e) 1D radial anisotropy profiles from our model (in green and in red for dry and wet UTZ, respectively), across Honshu (in blue), and global average (in black). Individual depth profiles are taken at the back-arc basin. The choice of λ_0 is a conservative estimate for the wavelength of the SS phase sampling the upper mantle and the UTZ.

Figure 3. (a) Peak-to-peak azimuthal anisotropy a_z for a mantle model with a wet UTZ. (b) Same as (a) but for a dry UTZ. (c) Effective azimuthal anisotropy after homogenization a_z^* at λ_0 = 165 km for the wet UTZ model. Similarly, the effective azimuthal anisotropy in the case of a dry UTZ model is excluded as it produces near-zero amplitudes close to the slab. (d) Azimuthal anisotropic tomography image across the Honshu arc retrieved from 3DLGL-TPESv.v2022-11 Debayle et al. (2016). (e) 1D azimuthal anisotropy profiles from our model (in green and in red for dry and wet UTZ, respectively), across Honshu (in blue), and global average (in black). The chosen value of λ_0 roughly corresponds to the wavelength of first overtones with maximum sensitivity kernels at that same depth range.

Supplementary information for

On the influence of pressure, phase transitions, and water on large-scale seismic anisotropy underneath a subduction zone

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Contents of this file

Text S1 to S4

Figures S1 to S4

Text S1. Geodynamic modelling of intraoceanic subduction

To implement a 2-D geodynamic model of intra-oceanic subduction, we use the open software ASPECT [\(Kronbichler et al.,](#page-35-0) [2012\)](#page-35-0) that solves the conservation mass, momentum, and energy equations for an incompressible fluid and assume an infinite Prandtl number:

$$
\nabla \cdot \mathbf{u} = 0,\tag{1}
$$

$$
-\nabla \cdot 2\eta_{\text{eff}}\dot{\varepsilon}(\mathbf{u}) + \nabla P = \rho \mathbf{g},\tag{2}
$$

$$
\rho C_p \frac{DT}{Dt} - \mathbf{\nabla} \cdot k \mathbf{\nabla} T = H,\tag{3}
$$

where $\frac{DT}{Dt}$ $\frac{D}{Dt}$ is the material derivative, and **u**, η_{eff} , $\dot{\varepsilon}$, *P*, ρ , **g**, C_p , *T*, and *k* are the velocity, effective viscosity, strain rate tensor, total pressure, density, gravitational acceleration, heat capacity, temperature, and thermal diffusivity, respectively. *H* refers to heat generation or consumption that takes into account adiabatic (through the extended Boussinesq approximation), latent, radiogenic, and shear heating effects.

We include four compositional fields reminiscent of [Glerum et al.](#page-34-0) [\(2018\)](#page-34-0): (a) overriding plate (OP) , (b) subducting crust (SC) , (c) subducting plate (SP) , and (d) background mantle (M) whose time evolution follow an advection type equation. The computational domain is 6000 km \times 1000 km and with adaptive mesh refinements incorporated, spatial resolutions vary from 5 km \times 5 km across regions with sharp viscosity contrasts and across the slab up to 325 km \times 325 km in regions of quiescence far from the slab.

The initial temperature field conforms to a half-space cooling model [\(Schubert et al.,](#page-35-1) [2001\)](#page-35-1) with a surface adiabatic temperature of 1573 K. The OP age evolves from 0 My at $x = 0$ km to 20 My at the trench $(x = 3000 \text{ km})$. Meanwhile, the SP, initially dipping at 30° , age evolves from 0 My at $x = 6000$ km to 150 My at the trench. A linear mantle geotherm is then established from the lithosphere-asthenosphere boundary (LAB) to a depth of 1000 km. Fixed temperature boundary conditions are imposed at the top (293 K) and at the bottom (2100 K). Zero heat flux is imposed at the sidewalls. The initial compositional structure also follows an age-based plate model for OP and SP. A 7.5-km subducting crust is augmented to serve as a weak decoupling Newtonian layer. Free-slip boundary conditions are imposed across all boundaries. The initial setup is shown in Figure [S1.](#page-36-0)

Text S1.1. Formulation of the viscoplastic rheology

We implement viscoplastic rheology where the viscoplastic effective viscosity η_{vp} is a harmonic average of viscous creeping and plastic yielding capped by a minimum and a maximum value, $\eta_{\text{min}} = 1.0 \times 10^{20}$ Pa-s and $\eta_{\text{max}} = 1.0 \times 10^{25}$ Pa-s, respectively:

$$
\eta_{\rm vp} = \eta_{\rm min} + \left(\frac{1}{\eta_{\rm max}} + \frac{1}{\eta_{\rm df/dI/pl}}\right)^{-1},\tag{4}
$$

with:

$$
\eta_{\text{df/dl/pl}} = \left(\frac{1}{\eta_{\text{df}}} + \frac{1}{\eta_{\text{dl}}} + \frac{1}{\eta_{\text{pl}}}\right)^{-1}.
$$
\n(5)

The first two terms in Eq. [\(5\)](#page-29-0) correspond to the effective viscosities due to diffusion and dislocation creeps [\(Karato and Wu,](#page-34-1) [1993\)](#page-34-1):

$$
\eta_{\text{df/dl}} = \frac{1}{2} A^{-\frac{1}{n}} \dot{\varepsilon}_{II}^{\frac{1}{n}-1} \exp\left(\frac{E+PV}{nRT}\right),\tag{6}
$$

where $\dot{\varepsilon}_{II}$ is the second invariant of the strain rate tensor, *A* is a prefactor, *d* is grain size, *E* and *V* are the activation energy and volume, *P* is hydrostatic pressure, *R* is gas constant, and *T* is temperature. The last term in Eq. [\(5\)](#page-29-0) is the effective viscosity due to plastic yielding:

$$
\eta_{\rm pl} = \frac{\sigma_y}{2\varepsilon_{II}},\tag{7}
$$

where the yield strength σ_y follows a Drucker Prager criterion [\(Davis and Selvadurai,](#page-34-2) [2005\)](#page-34-2):

$$
\sigma_y = C\cos\theta + P\sin\theta,\tag{8}
$$

in which *C* is the cohesion, and θ is the internal friction angle. We set $\theta = 0$ for the weak decoupling layer which ensues a constant yield stress (von Mises criterion). Table [1](#page-31-0) summarizes the viscoplastic rheology parameter values chosen in this study.

Text S1.2. Formulation of the effective mantle viscosity

To further promote slab stagnation, we implement a depth-dependent compositing model for the ambient mantle [\(Mitrovica and Forte,](#page-35-2) [1997\)](#page-35-2) whose effective viscosity η_0 depends on depth z according to:

$$
\eta_0(z) = \begin{cases} \eta_{\min} + (1.0 \times 10^{21} [\text{Pa-s}] - \eta_{\min}) \frac{z}{660 [\text{km}]} & \text{if } z < 660 \text{ km} \\ 5.0 \times 10^{21} [\text{Pa-s}] & \text{if } x \geq 660 \text{ km} \end{cases}
$$

Finally, the effective mantle viscosity η_{eff} is simply [\(Kronbichler et al.,](#page-35-0) [2012\)](#page-35-0):

$$
\eta_{\text{eff}}(z, P, T, \ldots) = \eta_0(z) \frac{\eta_{\text{vp}}(P, T, \ldots)}{\eta_{\text{min}}}
$$
\n(9)

Note that a viscosity jump by a factor of ~ 5 is implicitly defined at 660 km (Cížková et al., [2012;](#page-34-3) [Agrusta et al.,](#page-33-0) [2017\)](#page-33-0). We do not consider the effect of crystallographic preferred orientation (CPO) strength on viscosity. Figure [S1b](#page-36-0) illustrates the effective mantle viscosity at the final time step of the simulation.

Text S1.3. Modelling pressure-induced phase transformations

Following the method of [Christensen and Yuen](#page-34-4) [\(1985\)](#page-34-4), ASPECT employs an analytical phase function *X* to approximate the time evolution of a fraction of a material that underwent phase transformation and calculate the entropy change ∆*S* to calculate latent heat production. Both *X* and ΔS depend on the Clapeyron slope β_{410} (positive for an endothermic process and negative for an exothermic process), phase transition temperature T_{410} , phase transition width *w*, phase transition density contrasts $\Delta \rho_{410}$, and phase transition depths z_{410} . The aforementioned parameters are initialized in the material model plugin (see Table [2\)](#page-31-1).

Text S2. Textures at selected locations across the subduction zone

We select several locations along independent pathlines to examine the orientations of the crystallographic axes in the evolved CPO of olivine (i.e. Figure [S3a](#page-38-0)−g) and wadsleyite (Figure [S3h](#page-38-0)−j) aggregates.

Text S3. Tomographic filtering through elastic homogenization

The foundation behind elastic homogenization can be found in the studies of [Capdeville et al.](#page-33-1) $(2010, 2015)$ $(2010, 2015)$ $(2010, 2015)$ and Capdeville and Métivier (2018) , and its application to anisotropic media are detailed in [Magali et al.](#page-35-3) [\(2021\)](#page-35-3) and [Magali et al.](#page-35-4) [\(2024\)](#page-35-4) for *P*−independent and *P*−dependent fabrics, respectively. Elastic homogenization is based upon the minimum wavelength theory in seismology where small-scale heterogeneities in a 3-D medium with no scale separation such as

Parameter	Symbol	SC	SP	OP	М	Unit
Density	ρ	3150	3350	3350	3350	$\text{kg} \cdot \text{m}^{-3}$
Thermal diffusivity	\boldsymbol{k}	1.0×10^{-6}	1.0×10^{-6}	1.0×10^{-6}	1.0×10^{-6}	$m^2 \cdot s$
Heat capacity	C_p	1250	1250	1250	1250	$J \cdot K^{-1} \cdot kg^{-1}$
Dislocation creep						
Activation energy	E	Ω	5.4×10^{5}	4.3×10^{5}	4.3×10^{5}	$J \cdot mol^{-1}$
Activation volume	V	0	2.0×10^{-5}	1.85×10^{-5}	1.5×10^{-5}	$mol3 \cdot mol-1$
Prefactor	V	1.0×10^{-19}	2.4×10^{-16}	2.42×10^{-16}	3.91×10^{-15}	$Pa^{-n} \cdot s^{-1}$
Stress exponent	\boldsymbol{n}	1.0	3.5	3.0	3.0	
Diffusion creep						
Activation energy	E	Ω	3.0×10^{5}	2.4×10^5	2.4×10^{5}	$J \cdot mol^{-1}$
Activation volume	V		5.0×10^{-6}	5.0×10^{-6}	2.5×10^{-6}	$mol3 \cdot mol-1$
Prefactor	V	1.0×10^{-19}	6.08×10^{-14}	6.08×10^{-14}	3.74×10^{-14}	$Pa^{-n} \cdot s^{-1}$
Plastic yielding						
Cohesion	\mathcal{C}	1.0×10^{15}	1.0×10^{6}	1.0×10^{15}	1.0×10^{6}	MPa
Internal friction angle $\overline{\cdots}$ $\frac{1}{1}$ $\frac{1}{1}$	θ	θ \cdots	20	Ω \overline{c} $\overline{1}$	20 $\sqrt{2}$	\circ \cdot \cdot

Table 1: Viscoplastic rheology parameters for each compositional field.

"SC" stands for the subducting crust, "SP" for the mantle part of the subducting plate, "OP" for the overriding plate, and "M" the background mantle.

Values are loosely based on [Hirth and Kohlstedf](#page-34-6) [\(2003\)](#page-34-6).

Other input parameters in the viscoplastic material model of ASPECT are set to their default values unless otherwise specified.

Density contrast corresponds to the expected density of a pyrolitic composition.

the true Earth are replaced with effective properties when:

$$
k_{\text{max}} = \frac{1}{\epsilon_0 \lambda_0},\tag{10}
$$

where k_{max} is the maximum wavenumber of the heterogeneities, λ_0 is the minimum wavelength of the observed wavefield, and ϵ_0 is the scale separation constant which we set to $\epsilon_0 = 0.5$. Capdeville and Métivier [\(2018\)](#page-33-2) numerically verified that seismic tomography can be represented by an operator \mathcal{H} that when applied to an elastic medium **S**, the resulting effective medium S^{*} is the best possible model one could obtain from seismic tomography assuming perfect data coverage:

$$
\mathbf{S}^* = \mathcal{H}^{\lambda_0}(\mathbf{S}).\tag{11}
$$

Of course in the limit $\lambda_0 \to 0$, that is a wavefield with an infinite frequency band, one obtains the true structure **S** assuming a homogeneous distribution of source-receiver pairs.

One method to test the reliability of our anisotropy model is by comparing it with anisotropic tomography images of a subduction zone. To date, SGlobe-Rani [Chang et al.](#page-34-7) [\(2015\)](#page-34-7) and 3DLGL-TPESv.v2022-11 [Debayle et al.](#page-34-8) [\(2016\)](#page-34-8) are two of the most comprehensive global anisotropy models with the former having over 100,000 free-surface reflected S waves as data that help to constrain transition zone structures, and the latter having over 2,000,000 Rayleigh wave observations up to the fifth overtone to constrain azimuthal anisotropy at upper and mid-mantle depths. In our work, we compare our results with tomographic images of the Honshu subduction zone whose subduction style and implied geometry resemble our geodynamic model of intraoceanic subduction.

Text S4. Expressions for large-scale seismic anisotropy

Once the effective medium is obtained, we use two parameters that are often recovered from anisotropic tomography as means to describe our anisotropy models namely, *S*−wave radial anisotropy ξ , and peak-to-peak azimuthal anisotropy a_z .

In a weakly anisotropic medium, [Montagner and Nataf](#page-35-5) [\(1986\)](#page-35-5) showed that *ξ* is simply the radial anisotropy associated with an azimuthally-average vertically transverse isotropic (VTI)

medium whose elastic constants *N* and *L* relate to *ξ* through:

$$
\xi = \frac{N}{L},\tag{12}
$$

where:

$$
N = \frac{1}{8}(S_{11} + S_{22}) - \frac{1}{4}S_{12} + \frac{1}{2}S_{66})
$$
\n(13)

$$
L = \frac{1}{2}(S_{55} + S_{66}).
$$
\n(14)

Likewise, *a^z* describes horizontally-propagating *SV* waves in a horizontally-transverse isotropic (HTI) medium. It depends on elastic constants G_c and G_s through:

$$
a_z = 2\frac{G_c^2 + G_s^2}{L},\tag{15}
$$

where:

$$
G_c = \frac{1}{2}(S_{55} - S_{44})
$$
\n(16)

$$
G_s = S_{54}.\tag{17}
$$

Effective radial and azimuthal anisotropies across the subduction zone are shown in Figures [S4](#page-39-0) and [S5,](#page-40-0) respectively, at several homogenization wavelengths: $\lambda_0 = [10 \text{ km}, 50 \text{ km}, 100 \text{ km}, 200 \text{ km}]$.

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Figure S1: a.) Initial and boundary conditions, and simulation domain of our 2-D geodynamic model. Four compositional fields with distinct rheological properties are included namely, subducting plate (SP), subducting crust (SC), overriding plate (OP), and the background mantle (M) whose evolution follow an advection equation. The initial temperature field follows an agebased plate cooling model that increases from the leftmost part of the modelling domain to 20 My for the OP, and from the rightmost part to 150 My for the SP. Fixed temperature boundary conditions are imposed at the top (293 K) and at the bottom (2100 K) . Free slip is imposed on all sides. Red box corresponds to the domain at which we calculate seismic anisotropy. b.) Effective mantle viscosity at the present day in log[Pa-s] units.

Figure S2: (a) Density map predicted from Perple X for a pyrolitic mantle composition. Black contour lines correspond to arbitrary density crossovers associated with the following phase transitions: Olivine → wadsleyite $(\sim 3720 \text{ kg} \cdot \text{m}^3)$, wadsleyite → ringwoodite $(\sim 3850 \text{ kg} \cdot \text{m}^3)$, and ringwoodite → bridgmanite (∼4170 kg · m³). (b) Predicted 1D density, *V^P* and *V^S* structure of pyrolite (solid lines) versus the preliminary reference Earth model, PREM [\(Dziewonski and](#page-34-9) [Anderson,](#page-34-9) [1981\)](#page-34-9) (dashed lines). (c) Density structure of our subduction model at the present time using (a). White dashed rectangle corresponds to the region at which seismic anisotropy is calculated. Solid black lines delineate the subducting slab.

Figure S3: Top panel: Predicted large-scale radial anisotropy $(\xi = V_{SH}^2/V_{SV}^2)$ across a stagnating oceanic lithospheric slab (solid black line). Solid gray lines delineate the presumed topography of the 410 and 520-km seismic discontinuities assuming a pyrolitic mantle. Arrows represent mantle flow velocity at the final time step. Bottom panel: Computed *P*−dependent olivine and hydrous wadsleyite aggregate textures at selected locations along the model, *a*-*g* for olivine and *h*-*j* for wadsleyite, respectively. M.u.d. refers to the multiples of uniform distribution which measures texture strength.

Figure S4: Effective radial anisotropy at varying homogenization wavelengths.

Figure S5: Effective azimuthal anisotropy at varying homogenization wavelengths.