

Uncertainty aware sample mass determination of coarse-grained soils for particle size analyses

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Abstract

Determining particle size distributions (PSD) of soils is a basic first step in many geotechnical analyses and guidance is given in different national standards. For ambiguous reasons, the recommended minimum sample mass (m_{min}) for the PSD-analyses of soils with a main component of gravel or greater is based on equations including the soil's maximum grain diameter (D_{max}). We claim that the recommended m_{min} is overestimated as D_{max} does not represent the relevant large soil fraction but only the PSD's uppermost outlier. Furthermore, the recommended m_{min} is not based on a specific sampling confidence (i.e. how closely does the sample's PSD need to approximate the soil's PSD?) and thus it is not clear why the m_{min} should even be necessary. We conducted Monte-Carlo simulation-based sieve analyses of coarse-grained soils and developed a new, practically applicable framework to determine m_{min} based on D_{90} that also includes explicit consideration of sampling confidence. A survey was conducted that shows that there is no significant difference in how well operators are able to assess parameters like D_{90} or D_{max} . Real sieve tests performed on three different sands and gravels corroborate the theoretical results and show that substantially lower sample masses yield PSDs with only marginal differences to PSDs from samples according to the standards. While the results are promising, they open up for new research questions about which geotechnical application requires which soil sampling confidence.

27 **List of notations**

28	C_u	coefficient of uniformity
29	C_c	coefficient of curvature
30	D_{min}	estimated minimum grain diameter of soil
31	D_{max}	estimated maximum grain diameter of soil
32	D_{xx}	grain diameter at xx percent of a sieve curve
33	KS	Kolmogorov-Smirnov statistic used as error metric between two sieve curves
34	KS_{med}	median of multiple KS values
35	KS_{p95}	95 th percentile of multiple KS values
36	$m_{available}$	available soil sample mass
37	m_{min}	required minimum soil sample mass
38	S_0	sorting coefficient
39	U	Uniform distribution
40	ε	error exponent to control desired soil sampling confidence
41	ρ	grain density

42 **Definitions and conventions**

- 43 ▪ Soil: A volume of granular material in the ground that is too large to analyze as a whole. This
44 definition only applies in the herein given context of soil sampling for grain size distribution
45 determination. For other definitions of soil see e.g. EN ISO 14688-1.
- 46 ▪ Sample: a portion of a larger soil volume, taken to represent its characteristics (based on e.g.
47 O'Toole (2015)). The term “specimen” is not used herein due to ambiguous definitions where a
48 specimen may either be a subset of a sample or the other way round.
- 49 ▪ Grading and sorting are two equivalent terminologies to describe the shape of a sieve curve. In
50 this work, we consistently use “grading” where “well graded” \approx “poorly sorted” and “poorly
51 graded” \approx “well sorted”.
- 52 ▪ Uncertainty communicating language is given in accordance with Erharter et al. (2024).

53 **Keywords**

54 Soil classification; Soil characterization; Grain Size Distribution; Uncertainty, Survey, Confidence

55 1. Introduction

56 A reliable particle size distribution (PSD) analysis is key in geotechnical front-end engineering
57 design and imperative for engineering geological soil characterization and classification. For
58 instance, preliminary design of offshore structures relies on PSDs as the percentages of fines
59 content, or D_{10} are key to estimate soil behavior to loading, e.g. drainage conditions, cyclic
60 response, consolidation, etc. (see Andersen (2015); Andersen and Schjetne (2013)). In tailings
61 dams reliable PSDs are crucial for material characterization and modelling (Liu et al., 2024) and
62 to determine if the dam's composition complies with regulations in all depths. Extraterrestrial
63 geotechnics is a more exotic field where PSDs are required for preliminary ground investigations
64 for potential human settlements (Quinteros et al., 2024).

65 The first step to determine a PSD is to take a test sample from the soil. Several significant error
66 sources such as the sampling technique or the choice of the sample mass are entailed in this
67 process (Rawle, 2015). Readers are referred to works like Gerlach et al. (2002); Gerlach et al.
68 (2003) or Dubé et al. (2021) for information about sampling techniques such as riffle splitting or
69 fractional shoveling. With respect to the sample mass, the primary goal is to take a sample that is
70 sufficiently large to be representative for whichever characteristic of the soil that one is interested
71 in (Al-Rumaithi and Al-Sherrawi, 2020; Dubé et al., 2021; Pitard, 2019). It must be noted, however,
72 that it makes a difference for the practical sampling if, for example, an investigation's goal is a
73 soil's chemical composition that permits crushing of large grains, or an investigation's goal is the
74 actual soil PSD that does not allow that. The former case is relevant in the context of mining,
75 metallurgy and environmental studies (Gy, 2012). The latter case is relevant in engineering
76 geological investigations in the context of geotechnical engineering projects.

77 The present paper is exclusively concerned with the sample mass determination to assess a soil's
78 PSD for engineering geological soil characterization. In that context, achieving the best possible

79 representation of a soil is also the goal, but practical problems that come with too large samples
80 such as transport difficulties, storage capacity limitations or uneconomic testing efforts must
81 also be considered. In contrast to the above-mentioned applications, the literature on the sample
82 mass determination for engineering geological soil characterization is remarkably sparse and
83 Zhang et al. (2017) and the recent publication of Jia et al. (2024) are few exceptions.

84 Methods of engineering geological investigation such as soil sampling for PSD determination are
85 regulated and codified through different national and international standards. These methods are
86 related to sieving, sampling techniques, sampling of aggregates, reducing sample sizes,
87 alternative grain size determination through images, sample size estimates and sampling
88 probability: ISO 17892-4 (2017), ASTM D6913/D6913M (2017), ASTM C136/C136M (2020), ASTM
89 C702 (2018), ASTM E1382 (2023), ASTM D75 (2019), ASTM D3665 (2024), ASTM E105 (2021), ASTM
90 E122 (2022), ASTM E141 (2023). Besides ISO and ASTM standards, other relevant ones are
91 AASHTO T2, Australian Standard AS 1141.11, DJS 112-4:2015. Standards from Ontario, Canada
92 recommend similar minimal masses, but lower than the European counterpart.

93 These standards recommend to determine the required minimum sample mass (m_{min}) as a
94 function of the soil's estimated maximum grain diameter (D_{max}). As also pointed out by Zhang et
95 al. (2017), the origin and scientific justification for this procedure is unknown, despite widespread
96 adoption. This is of particular relevance in coarse-grained soils (i.e. \geq sand acc. to ISO 14688
97 (2019)) where the suggested sample masses easily exceed tens of kilograms if one follows the
98 recommendations. Equally unknown is the desired sampling confidence that the different
99 guidelines seek to achieve. Gale and Hoare (1992) also addressed the topic of soil sample mass
100 determination and give a recommendation based on D_{max} . But as others, i) they do not justify why
101 a D_{max} based approach is adopted and ii) they aim for "reliable" grain size analyses but do not
102 specify what reliable means in terms of how close the soil is approximated.

103 From a statistical point of view, using D_{max} as the decisive criterium to determine m_{min} implies
104 that m_{min} depends on the extreme large grain sizes of the PSD, resp. on the rightmost point of the
105 distribution. We hypothesize that today's standards overestimate the required sample mass in
106 many cases and that D_{max} is a conservative criterium to determine m_{min} . This often forces
107 practitioners who deal with coarse-grained soils to act outside the standard framework without
108 being aware of what the consequences of smaller sample masses are. Furthermore, it is
109 problematic that the recommendations for m_{min} are made without the indication of a desired
110 sampling confidence.

111 This paper investigates the issue of sample mass determination for coarse-grained soils and
112 proposes a new criterium to determine m_{min} that is easily applicable in practice as it is just an
113 equation with estimated input values. We show through a dedicated survey that the inputs that
114 are required for our criterium can be as well estimated as those recommended by today's
115 standards. The new criterium is developed through Monte-Carlo simulation of virtual sieve tests
116 and allows one to explicitly set a desired level of confidence. The Monte-Carlo simulation
117 simulates real laboratory tests as closely as possible with only minor assumptions such as
118 spherical grain shapes. To provide a baseline, the sampling confidence of today's standards is
119 back calculated within the simulations. The approach i) allows one to take samples according to
120 a desired level of confidence that is to be achieved; ii) provides the possibility to assess the
121 uncertainty that needs to be expected if one has a sample mass that is $< m_{min}$; iii) reduces the
122 required m_{min} for many soils and especially for those where D_{max} comes from single large grains.

123 2. Background

124 In this section, extended information about the sample mass recommendations from ISO 17892-
125 4 and ASTM ASTM D6913/D6913M is given as they explicitly give recommendations for soil
126 characterization. The rest of this paper also directly refers to these two standards. Other

127 standards that were mentioned in the introduction are thematically connected to this work, but
128 are not directly relevant as they address other issues such as aggregates for concrete.

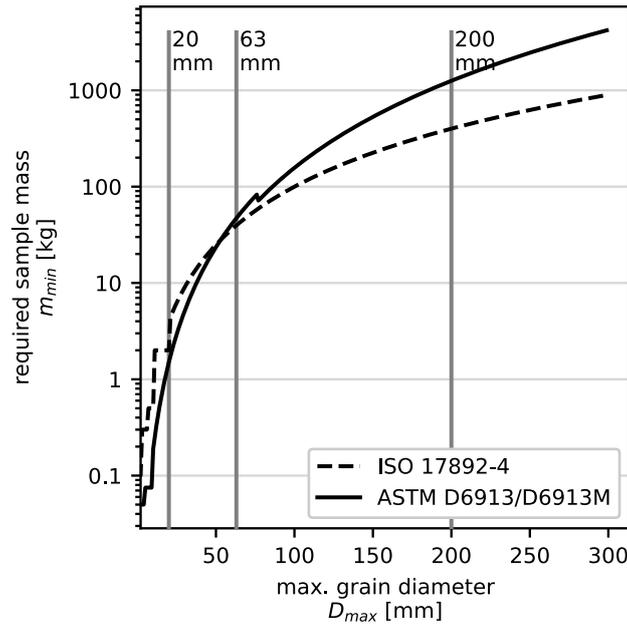
129 ISO 17892-4 (2017) defines that m_{min} [kg] depends solely on D_{max} [mm], for soils with a $D_{max} >$
130 20 mm. m_{min} according to this standard is to be derived from eq. 1.

$$m_{min} = \left(\frac{D_{max}}{10} \right)^2 \quad \text{eq. 1}$$

131 The ASTM D6913/D6913M (2017) standard also defines m_{min} in dependence of D_{max} , for a D_{max}
132 > 9.5 mm. m_{min} is "based on the mass of an individual spherical shaped grains, at the given sieve,
133 multiplied by 100 then 1.2 (factor to account uncertainty) and finally rounded to a convenient
134 number." For soils with a $D_{max} > 76.2$ mm, the same applies "except 1.2 factor is omitted". ASTM
135 D6913/D6913M only gives this instruction and no equation, so eq. 2 was reconstructed based on
136 that explanation. ρ in eq. 2 denotes the grain density which is also not directly specified in the
137 standard but based on the therein given values for m_{min} , it can be back calculated that a ρ of
138 3.016 g/cm^3 must have been applied.

$$m_{min} = \frac{4}{3} * \pi * \left(\frac{D_{max}}{2} \right)^3 * \rho * 100 * 1.2 \quad \text{eq. 2}$$

139 Based on these equations, both standards require minimum sample masses in the range of
140 hundreds of kilograms for soils with a D_{max} larger than 5-10 centimeters which is unpracticable
141 and often impossible to achieve in terms of practical sampling, availability and sievability in the
142 laboratory. Figure 1 shows the required m_{min} for the mentioned standards for up to a maximum
143 grain size of 300 mm diameter where ISO 17892-4 would require a sample with a mass of 900 kg
144 and ASTM D6913/D6913M more than 1200 kg.



145

146 *Figure 1: Minimum required sample masses as defined in ISO 17892-4 and ASTM D6913/D6913M. Steps in the plot*
147 *result from fixed sample masses and conditions in the standards.*

148 3. Development of new minimum sample mass criterium

149 In this study, we propose an alternative way of determining m_{min} . We first investigate the sample
150 mass determination problem theoretically with Monte-Carlo simulations using virtual sieve tests
151 and then underpin it with experimental results from real sieve tests. The Python source code, the
152 simulation- and experimental results are available in the Github repository in the supplementary
153 information of the paper.

154 3.1. Monte-Carlo Simulations

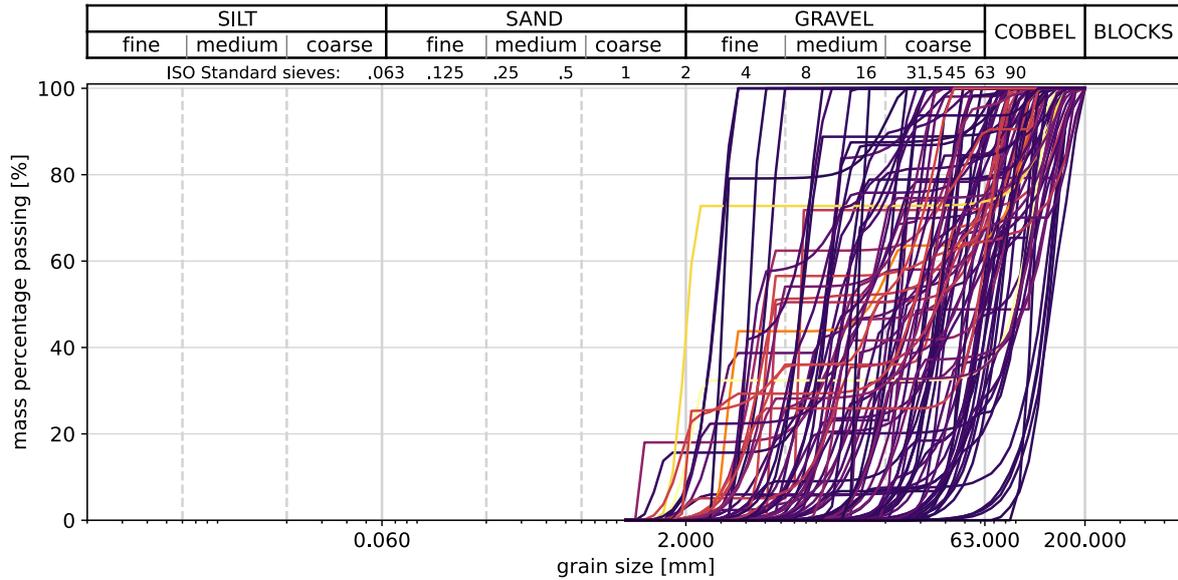
155 To theoretically investigate this problem, virtual sieve tests were conducted on generated coarse-
156 grained soils. The basic idea is that first a "ground-truth" coarse-grained soil is generated and then
157 samples with different masses are taken from this soil to investigate how large the error between
158 the samples' PSDs and the soil's PSD is. The Monte-Carlo simulation was set up with the goal to
159 generate a wide variety of PSDs including poorly graded-, well graded- and gap graded coarse-

160 grained soils to reflect many possible geological scenarios. All grains are modelled as spherical
161 which slightly reduces its realism (Kaviani-Hamedani et al., 2024), (see also section 6).

162 The soils are generated by the following process:

- 163 ▪ Step 1: The simulation should include well- to poorly graded sediments. While poorly
164 graded sediments can be modelled with a single statistical distribution (e.g. normal as
165 done by Jia et al. (2024), lognormal or exponential) , well graded ones are compositions of
166 multiple distributions due to different depositional environments. To account for this in
167 the simulation, the first step is to randomly generate between 1 and 5 percentages of soil
168 distributions (e.g. a soil may consist 100% of one distribution, or, for example, 30% of
169 distribution A, 20% of distribution B and 50% of distribution C).
- 170 ▪ Step 2: For each distribution, randomly set the minimum- and maximum grain diameters
171 between 1 and 200 mm. The minimum diameter must be smaller than the maximum.
172 These diameters are sampled from a uniform distribution U with $\ln(1)$ and $\ln(200)$ being
173 the lower and upper limits of the distribution. The logarithm is taken to avoid oversampling
174 of large diameters. The logarithmic values are then scaled back between 1 and 200 mm
175 by calculating their exponential. This gives: lower-/upper limit = $\exp\left(U(\ln(1), \ln(200))\right)$.
- 176 ▪ Step 3: For each distribution, individual grain diameters are generated by sampling from a
177 beta distribution that gives numbers between 0 and 1 and then scaling the output to the
178 minimum and maximum grain diameters that were chosen in the previous step. The beta
179 distribution's parameters alpha and beta parameters are uniformly, randomly set between
180 1 and 4 for each sample.

181 This sample generation process is an attempt to mimic real soils that may consist of one or several
182 soil distributions dependent on the geological history. In Figure 2, 100 exemplary sieve curves are
183 shown to visualize the diversity of PSDs that were generated. The sieve curves are colored
184 according to the sorting coefficient (S_0 , see eq. 5 in Table 1).



185

186 *Figure 2: 100 exemplary sieve curves of samples that were generated for the Monte-Carlo simulation. Sieve curves are*
 187 *colored according to the sorting coefficient (S_0): dark purple = 1, yellow = 7.*

188 To quantify the difference/error between the PSD of the soil and a sample's PSD, the Kolmogorov-

189 Smirnov statistic (KS) was chosen. KS denotes the maximum vertical distance between two

190 cumulative density functions which in this case means the maximum mass percentage difference

191 between two sieve curves. Thus, KS – herein – has the unit of mass percent and the minimum and

192 maximum of 0 or 100 would be reached if a sample's sieve curve either has a perfect fit or

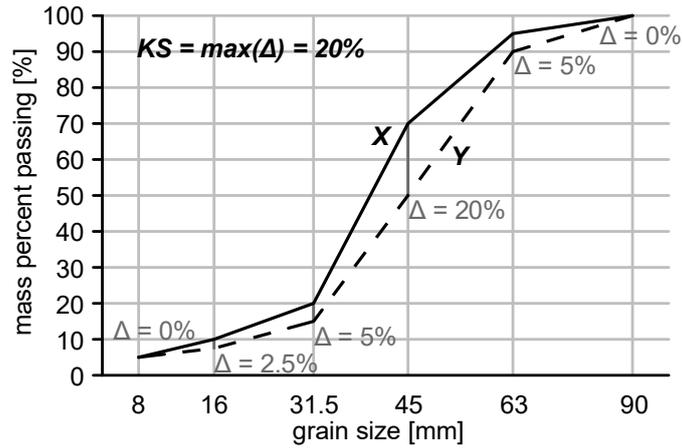
193 complete misfit with respect to the soil. For example, let $X = \{100, 95, 70, 20, 10, 5\}$ and $Y =$

194 $\{100, 90, 50, 15, 7.5, 5\}$ be the mass percent passing sieves of mesh sizes 90-, 63-, 45-, 31.5-, 16-

195 and 8 mm. KS is then computed as $KS = \max(|X - Y|)$ and would be 20% in this example (Figure

196 3). KS is seen as a well-suited error metric for this task as the goal for the soil sampling is to find

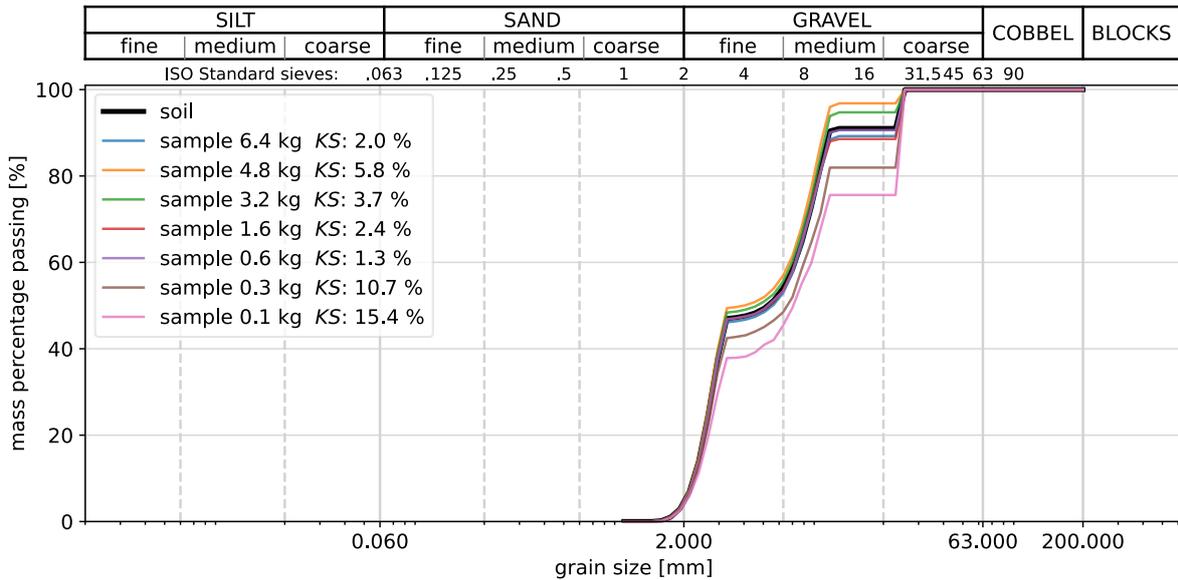
197 a sample mass whose sieve curve fits as well as possible to the sieve curve of the soil.



198

199 Figure 3: Example of how the Kolmogorov-Smirnov statistic (KS) quantifies the difference between two sieve curves X
 200 (solid) and Y (dashed).

201 Figure 4 shows an example where a soil was generated and multiple samples with decreasing
 202 masses were taken. The highest sample mass was determined according to eq. 1 (ISO 17892-4)
 203 and the subsequent samples are 75%, 50%, 25%, 10%, 5% and 1% fractions of the recommended
 204 sample mass. The lowest sample mass results in the highest KS with respect to the soil (i.e.
 205 highest error). Note, however, that KS is not consistently increasing with decreasing sample size
 206 which will be explained in the next section.



207

208 Figure 4: One example of a generated soil, where multiple samples with decreasing sample masses were taken and the
 209 Kolmogorov-Smirnov statistic computed for each of them.

210 For each simulation, the parameters given in Table 1 were recorded. A multitude of parameters
 211 was recorded to facilitate comprehensive Monte-Carlo simulation analyses afterwards.

212 Table 1: Parameters that are recorded for each simulated sample.

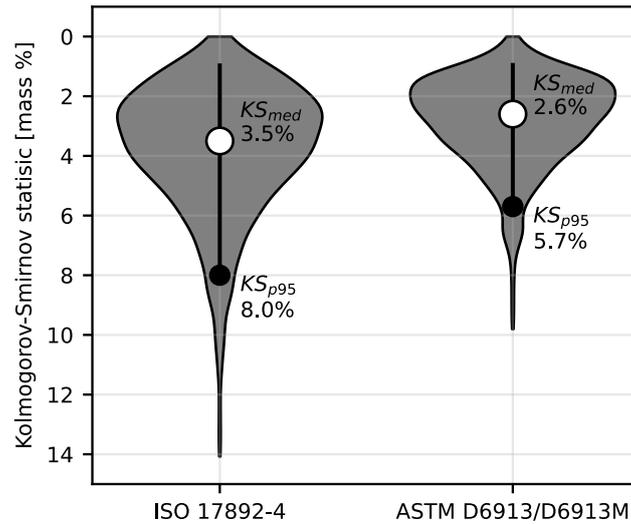
Parameter	Description
ID	A unique id of the simulation for later identification.
C_u [-]	Coefficient of uniformity $C_u = \frac{D_{60}}{D_{10}}$ eq. 3
C_c [-]	Coefficient of curvature $C_c = \frac{D_{30}^2}{D_{60} \cdot D_{10}}$ eq. 4
S_0 [-]	Sorting coefficient $S_0 = \sqrt{\frac{D_{75}}{D_{25}}}$ eq. 5
USCS soil classes	Soil classification according to the unified soil classification system (ASTM D 2487 – 06, 2006).
D_{min} [mm]	Minimum grain diameter of soil.
D_{max} [mm]	Maximum grain diameter of soil.
total masses [kg]	Total mass of generated underlying soil.
req. mass ks_p95 <= 10 [kg]	Required mass to achieve a KS_{p95} of $\leq 10\%$ in a “bottom up” approach (see section 3.2).
X.X mm sieve [m%]	Mass percent soil passing a sieve of mesh size X.X mm. Mesh sizes increase logarithmically from 1 to 200 mm in 50 steps. This large number of virtual mesh sizes was chosen to get higher resolution sieve curves than would be possible with standard mesh sizes.
D_{xx} [mm]	Grain diameters at 10, 12, 20, 25, 30, 40, 50, 60, 70, 75, 80 and 90 mass % of the soil from a cumulative density function.
ISO req. mass [kg]	Required sample mass acc. to ISO 17892-4 (2017).
ASTM req. mass [kg]	Required sample mass acc. to ASTM D6913/D6913M (2017).
const req. mass [kg]	Constant sampling mass of 10kg as a reference.
new X.X req. mass [kg]	Required sample mass acc. to eq. 6 with an $\varepsilon = X.X$. X.X ranges from 1.0 to 2.5 in steps of 0.1
ISO ks [%]	KS between a sample’s sieve curve that was taken acc. to ISO 17892-4 and the underlying soil's sieve curve.
ASTM ks [%]	KS between a sample’s sieve curve that was taken acc. to ASTM D6913/D6913M and the underlying soil's sieve curve.
const ks [%]	KS between the sieve curve of a sample with constant mass = 10 kg and the underlying soil's sieve curve.
new X.X ks [%]	KS between a sample’s sieve curve that was taken acc. to eq. 6 and the sieve curve of the underlying soil with an $\varepsilon = X.X$. X.X ranges from 1.0 to 2.5 in steps of 0.1.

213 3.2. Bottom-up determination of required sample mass

214 One of the goals of the simulation was to experimentally determine the required sample mass by
215 generating a soil and then taking samples with progressively increasing masses until a defined KS
216 threshold is reached. As individual samples with the same or only slightly differing masses may
217 show a significant variability of KS (see Figure 4) each sampling was repeated 20 times as a trade-
218 off between computational efficiency and representative results. The large fluctuation in repeated
219 sampling with same masses originates from the chance whether or not individual large grains that
220 significantly influence the resulting PSD are being sampled. The KS threshold was set so that the
221 sample mass is seen as sufficient if the p95 percentile (i.e. 95% of values are lower than this) of
222 the KS s of the 20 repeated samples is ≤ 10 mass %. In other words, if 19 of the 20 samples achieve
223 a $KS \leq 10$ mass %, the sample mass is sufficient. Note that this threshold has no general
224 geotechnical meaning and was only set to have a threshold to experimentally determine a
225 required sample mass to qualitatively investigate the relationship between sample mass,
226 sampling confidence and further parameters such as D_{max} or D_{90} .

227 3.3. Insights from the Monte-Carlo Simulations

228 The Monte-Carlo simulations were used to i) investigate the sampling confidence / error that
229 results from determining m_{min} according to ISO and ASTM and ii) to develop a new approach for
230 m_{min} determination that reduces the required sample mass and explicitly considers the sampling
231 confidence. To this end, 1200 simulations were made and it was observed that the ISO
232 recommendation (eq. 1) achieves a median KS (KS_{med}) of 3.5% and a p95 percentile of KS (KS_{p95})
233 of 8.0%. This means that 95% of samples taken according to ISO have a $KS < 8.0\%$ to the soil. Due
234 to the higher required sample masses, the ASTM recommendation (eq. 2) achieves lower KS error
235 of a KS_{med} of 2.6% and a KS_{p95} of 5.7%. A violin plot of the ISO- and ASTM- recommended sample
236 masses and the achieved KS errors for all 1200 simulations is given in Figure 5.



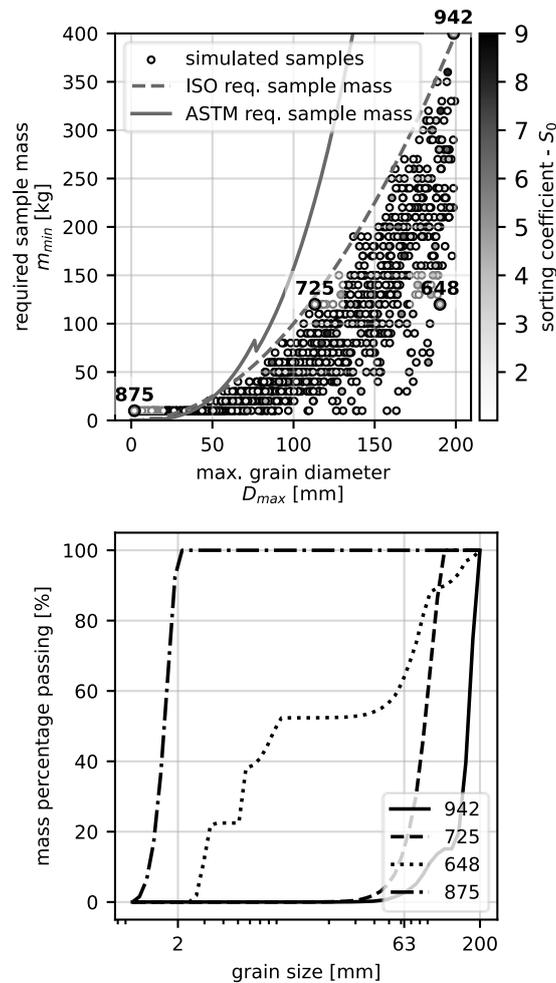
237

238 *Figure 5: Violin plots of the Kolmogorov Smirnov error for samples taken according to ISO and ASTM standards.*

239 The “bottom up” determination of required sample mass (see section 3.2) allows to investigate
240 the relationship between the experimentally determined required sample mass to achieve a
241 certain error and other parameters that describe the samples. This study’s original hypothesis
242 was that the required sample mass to achieve a certain error must be dependent on the grading
243 of the soil rather than solely on D_{max} . Figure 6 was made to verify if grading can be used to
244 complement the selection of m_{min} . The following insights are gathered from this:

- 245 ▪ There is a relationship between grading and required sample mass as samples with a high
246 S_0 (i.e. well graded) also require larger sample masses. However, the figure also shows
247 that there are samples with a low S_0 that require a large sample mass and thus this
248 hypothesis was rejected (high confidence).
- 249 ▪ The recommendations from the standards (esp. ISO) do not always overestimate the
250 required sample mass but rather describe the upper limit of the required sample mass.
251 Thus, it can be qualitatively confirmed that there is a relationship between a soil's large
252 grain sizes and the required sample mass to reach a certain sampling confidence (high
253 confidence).

254 ▪ It is observed that there are samples that have a comparably large D_{max} but require
255 sample masses several times smaller than suggested by the standards. It is thus shown
256 that the standards overestimate the required sample mass in several- but not in all cases
257 (high confidence).



258

259 Figure 6: Top: Relationship between a soil's maximum grain diameter (x-axis) and the required sample mass (y-axis).
260 The datapoint color indicates the soil's sorting coefficient (S_0). Theoretically, required sample masses acc. to ISO and
261 ASTM are also shown for reference. Bottom: Exemplary sieve curves from the top figure, marked with sample "ID" (see
262 data in the supplementary information).

263 Based on these insights, we investigated the correlation between different parameters that
264 describe a sieve curve's geometry and the required sample mass. We used Pearson's correlation
265 coefficient where values of 1 and -1 indicate very strong positive and very strong negative
266 correlations respectively and 0 indicates very weak correlation. The results are shown in Table 2.

267

268 *Table 2: Correlation analyses between parameters that describe a sieve curve's geometry and the required sample*
 269 *mass that was determined in the Monte Carlo simulation.*

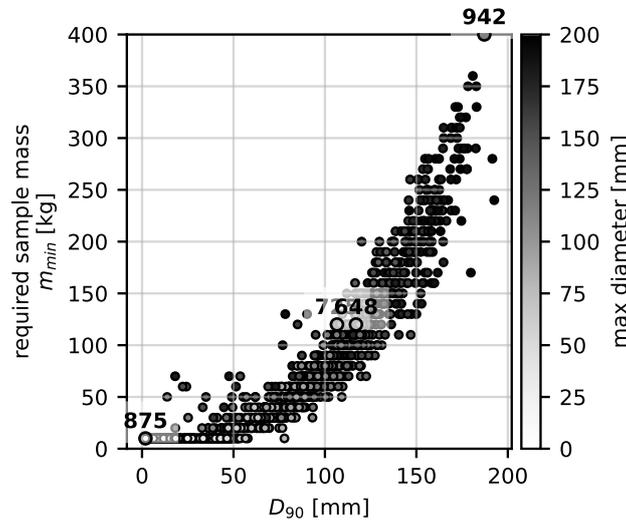
Parameter	Correlation with required sample mass
C_u [-]	0.25
C_c [-]	0.09
S_0 [-]	0.25
D_{min} [mm]	0.12
D_{10} [mm]	0.36
D_{20} [mm]	0.42
D_{30} [mm]	0.48
D_{40} [mm]	0.56
D_{50} [mm]	0.62
D_{60} [mm]	0.72
D_{70} [mm]	0.80
D_{80} [mm]	0.87
D_{90} [mm]	0.91
D_{max} [mm]	0.84

270

271 This analysis showed that the currently used parameter to determine the required sample mass -
 272 D_{max} – only achieves a correlation of 0.84 with it. A slightly stronger correlation of 0.87 is achieved
 273 by d_{80} and the strongest correlation of 0.91 by D_{90} (i.e. the grain size where 90% of a sample's
 274 mass has a smaller diameter).

275 Visualizing the simulations as D_{90} vs. required sample mass and coloring the data points
 276 according to the maximum grain diameter (Figure 7) shows that soils with a large D_{90} also require
 277 large sample masses for representative sampling. The same exemplary PSDs as in Figure 6 are
 278 marked in Figure 7. Note for example that samples 648 and 725 have very different D_{max} but
 279 similar D_{90} . In general, can it be seen that there are several soils with a low D_{90} that still have a
 280 large maximum grain diameter, but they do not require large sample masses for representative
 281 sampling. We thus conclude with high confidence that the relationship between grain size and
 282 required sample mass as implied by the standards is qualitatively correct, but D_{max} is an ill-suited
 283 criterium as it represents the rightmost point of a soil's PSD which is often an outlier in coarse-
 284 grained soils. Consequently, D_{max} does not represent a soil's significant large grain sizes and is

285 affected by outliers. D_{90} – which is not a PSD’s extreme value – on the other hand, is not sensitive
 286 to outliers and shows a more robust relationship with the required sample mass.



287

288 *Figure 7: Relationship between a soil's D_{90} (x-axis), the required sample mass (y-axis) and the maximum grain*
 289 *diameter (datapoint color). The same PSDs as shown in Figure 6 (bottom) are marked.*

290 3.4. Proposed criterium for minimum required mass

291 Based on the insights from the Monte-Carlo simulations, a new criterium to determine m_{min} for
 292 coarse-grained soils was developed. The theoretical framework is presented in this chapter and
 293 an exemplary application is given in Appendix 1. Based on eq. 1, D_{max} was replaced with D_{90} and
 294 a dedicated error-exponent ε that gives control over the maximum error that one wants to achieve
 295 with the taken sample mass was introduced (eq. 6).

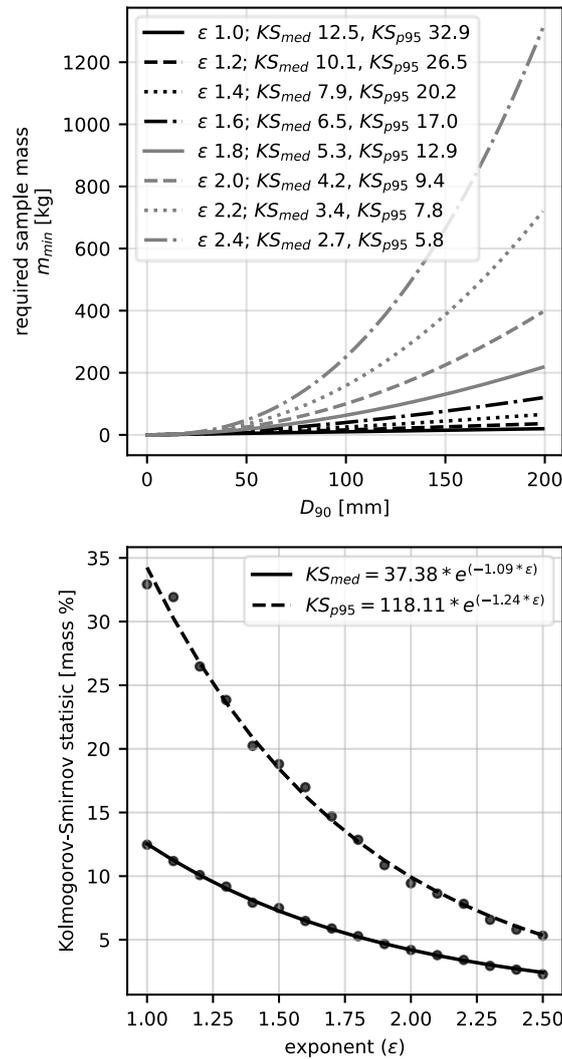
$$m_{min} = \left(\frac{D_{90}}{10}\right)^\varepsilon \quad \text{eq. 6}$$

296 This new criterium was included in the Monte-Carlo simulation to determine the KS errors that
 297 are achievable with different ε by repeated sampling from one soil with different masses (see
 298 parameters "new X.X req. mass [kg]" and "new X.X ks [%]" in Table 1). As KS_{med} and KS_{p95} of the
 299 current standards were determined in Figure 5 (section 3.3), we determined these errors for
 300 different ε on a range from 1 to incl. 2.5 (Figure 8, top). 2.5 was set as the upper limit as this yields

301 sample masses larger than the ASTM standard. Based on this, the relationships between the
 302 achievable KS_{p95} error and ε , respectively KS_{med} error and ε was assessed and is shown in Figure
 303 8, bottom. These relationships can be described with the exponential functions of eq. 7 and eq.
 304 8.

$$KS_{p95} = 118.11 * e^{-1.24*\varepsilon} \quad \text{eq. 7}$$

$$KS_{med} = 37.38 * e^{-1.09*\varepsilon} \quad \text{eq. 8}$$



305
 306 *Figure 8: Top: The new criterium to determine the minimum sample mass (m_{min}) with different error exponents (ε).*
 307 *Bottom: The assessed KS_{p95} and KS_{med} vs. different error exponents ε .*

308 Solving eq. 7 for ε and substituting for ε in eq. 6, finally gives the new recommended equation to
 309 determine m_{min} in a sampling confidence-aware manner in eq. 9.

$$m_{\min} = \left(\frac{D_{90}}{10} \right)^{\frac{\ln(KS_{p95}) - \ln(118.11)}{-1.24}}$$

eq. 9

310 This equation allows one to determine the minimum required sample mass, given an estimated
311 D_{90} of the soil and a desired sampling confidence in mass percent (KS_{p95}). The m_{\min} will in 95%
312 of cases be a sample mass that is sufficient to satisfy the desired error threshold.

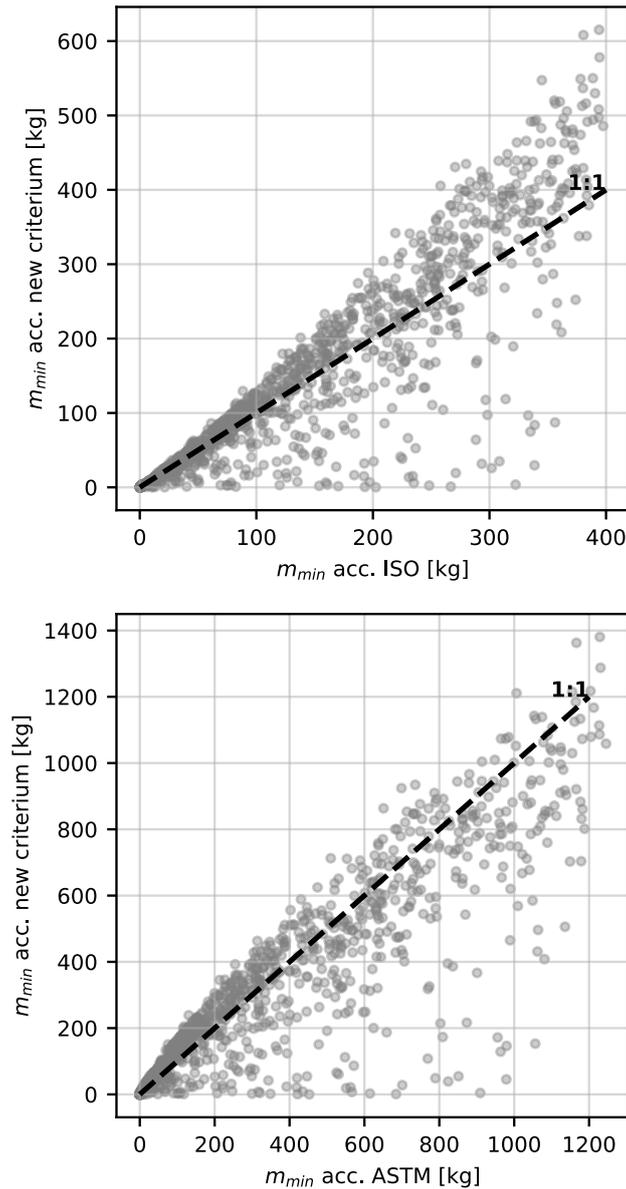
313 A decisive question that comes up in this context is how reliably an operator can come up with a
314 field estimate of a sample's D_{90} vs. a field determination of a sample's D_{max} as it is required in
315 today's standards. First, one must acknowledge that both parameters can only be estimated as
316 the full soil body under investigation is never observable. Secondly, a dedicated survey that
317 investigates whether operators achieve a higher performance in estimating one parameter over
318 the other showed that there is no significant reason to believe that. The capability to estimate
319 parameters is equally well / poor for all D -values. Gap graded soils may be the only exception here,
320 where it can be seen that the D -value closest to the gap has a significant variation but the
321 characterization of gap-graded soils constitutes a research problem on its own and cannot be
322 addressed herein. The full survey results can be found in Appendix 2. We recommend estimating
323 D_{90} in the field as *the maximum relevant grain size of the soil excluding obvious large outliers*.

324 Defining desirable PSD errors for different geotechnical applications is not in the scope of this
325 study and should be investigated with dedicated research (see discussion). As fine-grained soils
326 were not considered in the simulation and sands and fine-gravels only represent the lower
327 boundary of the Monte-Carlo simulation, the same criteria as specified in the ISO standard should
328 be applied for soils with a $D_{max} \leq 20$ mm. Furthermore, in cases where the estimated $D_{max} > 20$
329 mm but the estimated $D_{90} < 10$ mm, 1 kg of sample mass should be used. Otherwise, eq. 9 is to
330 be used.

331 3.5. Comparison to standards and further usage

332 Figure 5 shows that ISO and ASTM achieve KS_{p95} of 8.0% and 5.7 % respectively. Using these
333 values in eq. 9 allows to directly compare the required sample masses from the new criterium to
334 the previous standards (Figure 9). On average, across all simulated samples, the new criterium
335 requires ca. 4 times lower sample masses than the ISO standard and ca. 9 times lower sample
336 masses than the ASTM to achieve similar sampling confidences. In extreme cases, however, the
337 required sample masses according to the new criterium are several thousand times lower than
338 the ISO or ASTM standards while reaching the same sampling confidence.

339 In Figure 9 top, it can be seen that for the majority of samples the new criterium to determine m_{\min}
340 yields a larger sample masses than the ISO standard. While this is only a theoretical result, it
341 indicates that the ISO standard is unconservative and inconsistent when it comes to
342 recommending required sample masses for very coarse-grained soils that contain a significant
343 amount of large grains (low confidence). Nevertheless, in both cases of ISO and ASTM, it can be
344 seen that there are samples that are far below the 1:1 line in Figure 9 thus suggesting with high
345 confidence that the newly proposed criterium is more precise for sample mass determination and
346 not sensitive to outliers.



347

348 *Figure 9: Comparison between sample masses acc. to ISO (top) and ASTM (bottom) to the new criterium at equal*
349 *confidence levels. Dashed lines indicate lines of 1:1 equal mass in the plots. Datapoints are 50% transparent.*

350 Lastly it must be acknowledged that there are cases where the available sample mass is smaller
351 than the desired / required sample mass and acquiring more sample is unviable. Today, operators
352 either avoid sampling all together in these cases or must do sampling outside the standards'
353 framework. Thus they are not aware of the error that they may or may not introduce through this
354 undersampling. We recommend also taking samples to determine a PSD in these cases, but the
355 operator should be aware of the expectable error that the sampling is subjected to. In this case

356 m_{min} in eq. 6 can be substituted with the available sample mass ($m_{available}$) and then the
357 equation solved for ε , thus giving eq. 10.

$$\varepsilon = \frac{\ln(m_{available})}{\ln(D_{90}) - \ln(10)} \quad \text{eq. 10}$$

358 By using the determined ε in eq. 7 and eq. 8 or Figure 8 bottom, one can find which KS_{med} and
359 KS_{p95} is to be expected given the available sample mass. The consequence of knowing the error
360 that must be expected given the available sample mass is that the subsequent geotechnical
361 analysis can consider this uncertainty by setting a higher focus on probabilistic analyses,
362 adjusting how conservative approaches are or considering different plausible scenarios.

363 4. Experimental underpinning

364 4.1. Experimental program and tested soils

365 Several sieve analyses were performed in the laboratory to practically test the hypotheses
366 presented in the previous chapter. The goal of the sieve analyses was to investigate if it is also
367 practically the case that significantly lower sample masses than recommended by the standards
368 yield sufficient PSDs. Three different soils were used, namely a (A) medium to fine sand, (B) a
369 medium to fine gravel and (C) a sandy, medium to coarse gravel. Different test programs were
370 conducted for each soil:

- 371 ▪ Soil A: A medium to fine sand from the Isle of Rum in Scotland (United Kingdom) was used
372 to investigate how far one can go with reducing the ISO recommended sample mass even
373 below the considered size of the Monte-Carlo analyses. With an estimated D_{max} of 4 mm,
374 an ISO 17892-4 recommended (dry) sample mass of 200 g was taken from one large
375 sample. Further samples with 100 g, 75 g, 50 g, and 5 g were also taken and PSDs
376 determined for all of them.

- 377 ▪ Soil B: A medium to fine fluvial gravel was collected from the river Akerselva in Nydalen,
 378 Oslo (Norway). The D_{max} is estimated to be 30 mm, thus the ISO required sample mass is
 379 9 kg of soil (eq. 1) which was used for one sieve test. The estimated D_{90} , however, is around
 380 8 mm and thus < 10 mm. Therefore, the new recommendation of 1 kg sample mass was
 381 tested (see end of section 3.4). To also include an extreme case, one more sieve analysis
 382 with 300 g of sample was done.
- 383 ▪ Soil C: An artificial, pre-sieved, sandy, medium to coarse gravel from Austria with a known
 384 D_{max} of 70 mm was used for soil C. One sieve test with a sample mass of 50 kg according
 385 to ISO was done and one with a 2.5 times lower sample mass of 20 kg.

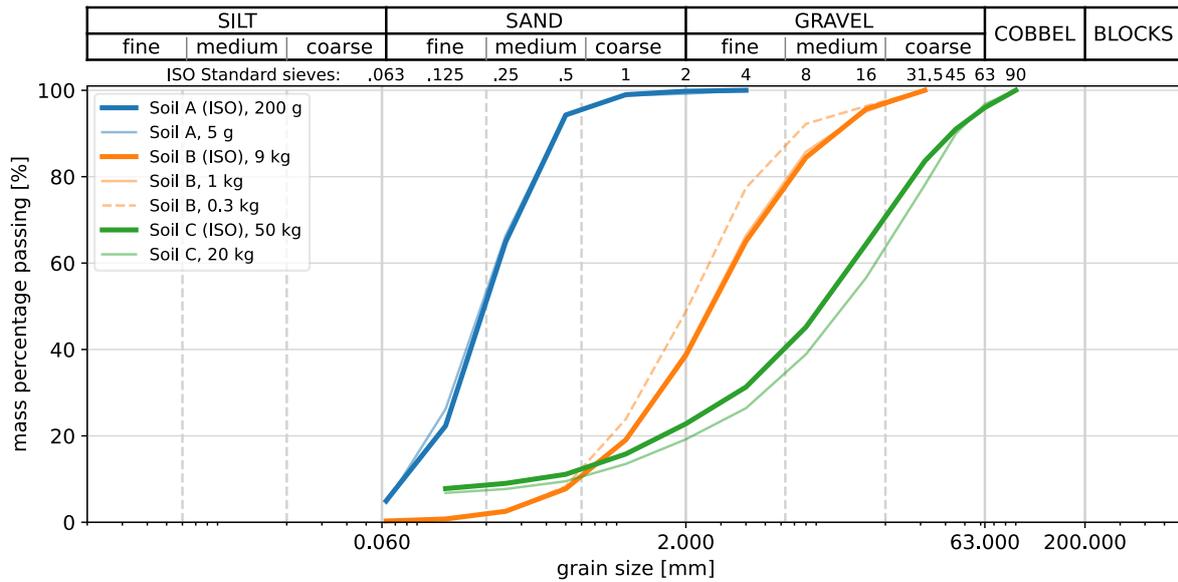
386 4.2. Experimental results

387 Table 3 gives an overview of the experimental results and Figure 10 shows the sieve curves for the
 388 different soils.

389 Table 3: Overview of the experimental results.

Test	Sample mass [g]	D_{10} [mm]	D_{30} [mm]	D_{60} [mm]	C_c	C_u	KS to ISO [mass %]
Soil A (ISO)	200	0.081	0.148	0.236	2.90	1.14	-
Soil A1	100	0.085	0.145	0.227	2.66	1.08	3.32
Soil A2	75	0.090	0.158	0.242	2.69	1.14	3.97
Soil A3	50	0.082	0.140	0.227	2.74	1.05	3.18
Soil A4	5	0.079	0.137	0.230	2.91	1.03	3.88
Soil B (ISO)	9000	0.599	1.557	3.615	1.12	6.04	-
Soil B1	1000	0.608	1.536	3.527	1.10	5.80	1.34
Soil B2	300	0.553	1.245	2.782	1.08	5.03	12.34
Soil C (ISO)	50000	0.369	3.694	14.167	2.610	38.387	-
Soil C1	20000	0.563	5.152	18.451	2.557	32.802	7.8

390

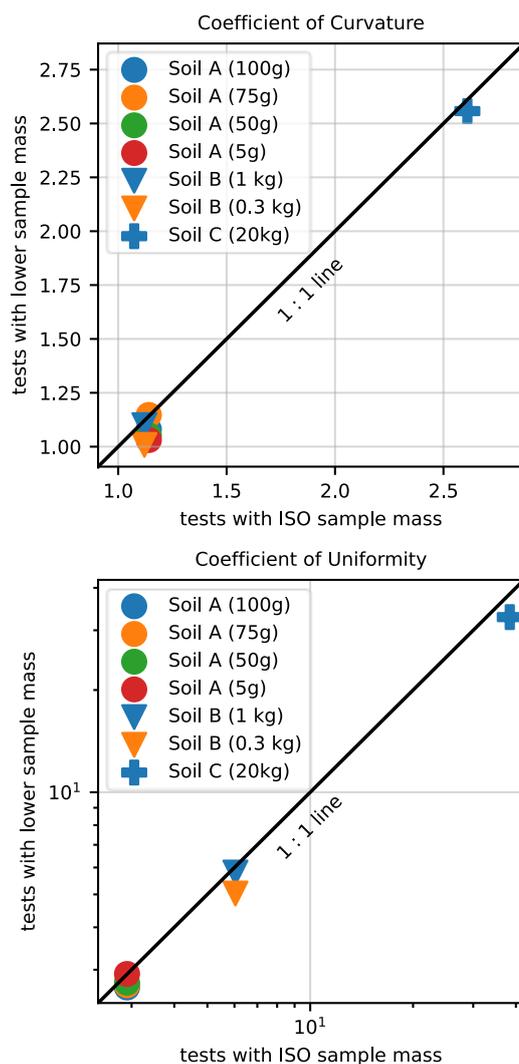


391

392 *Figure 10: Sieve curves of the conducted lab tests to investigate how different sample masses influence practical*
 393 *results. For each soil, the sieve curve with a sample mass acc. to ISO 17892-4 and the sieve curve based on the smallest*
 394 *sample mass is shown.*

395 For all soils, no remarkable discrepancy can be observed between the PSDs obtained using
 396 different amounts of sample mass. While this study aims at coarse-grained soils with the main
 397 grain size being gravel or larger, soil A demonstrates that lower sample masses can also give
 398 sufficient results for sands. In soil A, even a 40 times lower sample mass than what would be
 399 required by ISO 17892-4 only yields a *KS* of 3.88%. For Soil B, a mass 9 times lower than the
 400 suggested by ISO (i.e. the mass as recommended herein) shows a *KS* of 1.34% only. A test with a
 401 30 times lower sample mass (300 g) was also conducted on Soil B and results in a *KS* of 12.34%
 402 with respect to the ISO recommended of 9000 g. This more substantial deviation results from a
 403 low sample mass which is also not recommended, and the test was done for demonstration
 404 purposes only to show what happens in substantially lower sample masses in coarse-grained
 405 soils. In case of Soil C, the error between the PSD resulting from the ISO recommended sample
 406 mass of 50 kg and a test with a 2.5 times lower sample mass yielded a *KS* of 7.8%. While the effort
 407 of doing a sieve test with 20 kg instead of 50 kg of sample mass is significantly lower, the resulting
 408 difference in the PSD is small and still leads to the same characterization of the soil as a sandy,
 409 medium to coarse gravel.

410 Table 3 shows that also the differences between the parameters that describe the sieve curves'
411 geometry are small and Figure 11 visualizes the difference in C_c and C_u between tests with a
412 sample mass according to ISO and tests with a lower sample mass. In all cases, the values
413 become slightly lower with decreasing sample masses. Nevertheless, the total differences are
414 small and would not change a soil's classification based on C_c and C_u .



415

416 *Figure 11: C_c and C_u differences for tests with a sample mass acc. to ISO and tests with a lower sample mass.*

417

418 5. Discussion

419 The proposed new method for m_{min} determination leads to more precise recommendations for
420 the required sample masses for coarse-grained soils including a significant reduction of the
421 required sample mass for few cases. It is easily applicable in practice and also permits to take
422 samples under explicit consideration of the sampling confidence. The practicality, outlier
423 awareness, explicit accounting for sampling confidence and consideration of a wide range of soil
424 types are improvements over previously proposed methods for sample mass determination (Gale
425 and Hoare, 1992; Jia et al., 2024; Zhang et al., 2017).

426 The proposed new methodology is based on simulations of laboratory sieve tests, but practical
427 laboratory sieve tests on real soils corroborate the theoretical results thus new recommendations
428 and conclusions are made with very high confidence. Nevertheless, the simulation includes some
429 simplifying assumptions such as perfectly spherical grains which might influence the result,
430 especially for very coarse grain sizes that seldomly are perfectly spherical. Studies such as
431 Kaviani-Hamedani et al. (2024) address this issue, but in large scale simulation of sieve tests,
432 explicitly including non-spherical grains heavily impacts the computational performance and
433 thus renders large scale Monte-Carlo simulations infeasible, today.

434 The simulation of individual and discrete grains and the subsequent explicit sampling from these
435 grains is on the one hand seen as a benefit of this study as it is the most realistic way of simulating
436 sieve tests, on the other hand it is computationally very demanding as especially memory limits
437 are reached fast the smaller the grain sizes become. Besides the main goal to investigate coarse
438 grain sizes, the lower grain size boundary of 1 mm in this study is related to computational
439 limitations of this approach. To conduct simulated PSD analyses starting from clay sizes, would
440 require a different simulation concept, that is rather based on statistical distributions than on
441 individual grains.

442 6. Conclusions and Outlook

443 A new method to determine the minimum required sample mass for PSD assessments was
444 proposed. The new method explicitly considers sampling confidence, which is an improvement
445 on the one hand but on the other opens up for a plethora of new research questions related to
446 "How much is enough for application X?". As given in the introduction, PSDs are not only
447 fundamental for general purpose soil characterization but also feed directly into different
448 geotechnical engineering applications. These may, however, tolerate different sampling errors
449 depending on the downstream usage of a PSD and derived parameters such as D_{10} , D_{60} , C_u , C_c ,
450 etc. Speculating about required confidences of soil sampling for different geotechnical
451 applications is out of the scope of this study and future research related to this topic is highly
452 encouraged to provide a sound decision base for sampling confidences.

453 The conducted survey to investigate how reliable parameters like D_{max} and D_{90} can be estimated
454 by operators in the field showed that there is no significant difference for visual assessments
455 (medium confidence). More surveys like this and similar ones (Elmo and Stead, 2021; Skretting et
456 al., 2023) are required to get a quantitative understanding of the cognitive biases and human
457 uncertainty that is involved in engineering geological and geotechnical observations. Further
458 surveys like this are encouraged where the survey scope could be extended by the use of real soil
459 samples instead of generic visualizations. However, in the case of PSD determination of coarse-
460 grained soils the use of image processing technology for PSD-pre-assessment (Ferrer et al., 2021)
461 could be considered. Nevertheless, due to the required level of technological proficiency and
462 eventually also soft- and hardware cost, it is not expected that image processing techniques will
463 replace estimations of PSDs in practice in the near future and approaches like the one proposed
464 herein will remain relevant.

465 Supplementary information

466 The code for the Monte-Carlo Simulations and the results of the real laboratory tests can be found
467 in the following Github repository: [https://github.com/norwegian-geotechnical-](https://github.com/norwegian-geotechnical-institute/sieve_analyses/releases/tag/v2.0.0)
468 [institute/sieve_analyses/releases/tag/v2.0.0](https://github.com/norwegian-geotechnical-institute/sieve_analyses/releases/tag/v2.0.0)

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542

543 Appendix

544 Appendix 1 – Application example

545 For example, one wants to determine the PSD of a coarse-grained fluvial soil with an estimated
546 D_{max} of 150 mm (there are some cobbles) and an estimated D_{90} of 80 mm. According to eq. 1
547 from ISO 17892-4 the required m_{min} is 225 kg of soil (eq. 11) and it is not clear why so much soil
548 would be required. In contrast to that, the new eq. 9 allows setting a desired maximum error /
549 sampling confidence (KS_{p95}) of e.g. 10 %. Based on the estimated D_{90} one can then estimate the
550 required sample mass to be ~63 kg with explicit consideration of that desired sampling
551 confidence (eq. 12). If the total available soil sample mass would, however, only be 20 kg, then
552 eq. 10 can be used to determine the error exponent ε (eq. 13) which is 1.44. Substituting this into
553 eq. 7 reveals that in this particular soil, one needs to expect that the determined PSD has an error
554 of up to ~20% with respect to the real soil's PSD if only 20 kg of soil sample are available (eq. 14).

$$m_{min}[kg] = 225 = \left(\frac{150}{10}\right)^2 \quad \text{eq. 11}$$

$$m_{min}[kg] = 63 = \left(\frac{80}{10}\right)^{\frac{\ln(10) - \ln(118.11)}{-1.24}} \quad \text{eq. 12}$$

$$\varepsilon = 1.44 = \frac{\ln(20)}{\ln(80) - \ln(10)} \quad \text{eq. 13}$$

$$KS_{p95}[m\%] = 19.8 = 118.11 * e^{-1.24*1.44} \quad \text{eq. 14}$$

555

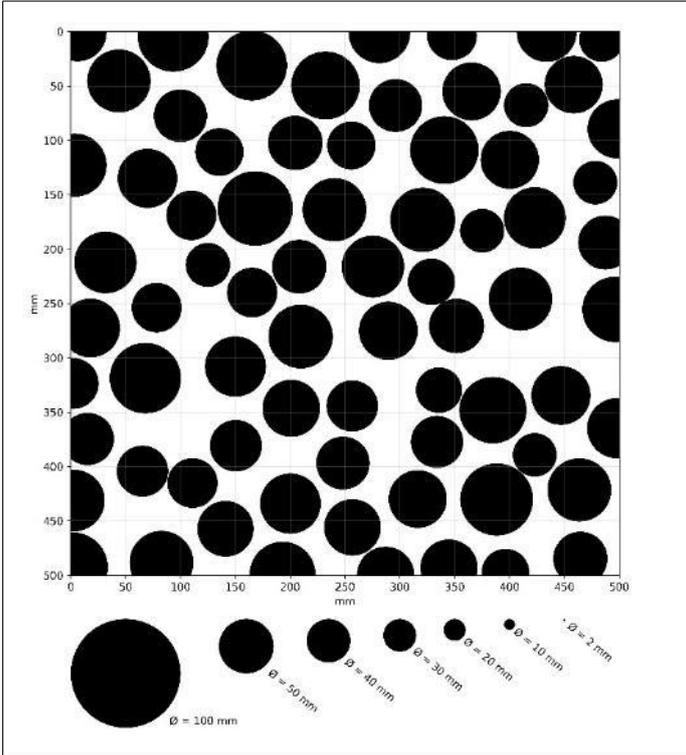
556 Appendix 2 - Grain size distribution characterization survey

557 A survey was conducted to investigate how well operators can visually estimate different
558 parameters that describe the geometry of a sieve curve. The survey was done using Microsoft
559 Forms and responses that were submitted between the start of the survey on 25th of November
560 2024 until its end on the 9th of December 2024 were included in this analysis.

561 The following metadata was collected from each participant:

- 562 - Name
- 563 - Email Address
- 564 - Main area of expertise, where participants could choose one of the following answers:
565 Geotechnical engineering, Engineering Geology, Sedimentology, Hydrogeology,
566 Quaternary geology, other (to be specified).
- 567 - Current main field of work, where participants could choose one of the following answers:
568 Academia, Industry (consulting, contractors, technology development,...), Other
- 569 - Years of experience post master, where participants could choose one of the following
570 answers: 0-5, 5-10, 10-20, 20-30, >30, None (still student or not from this field).

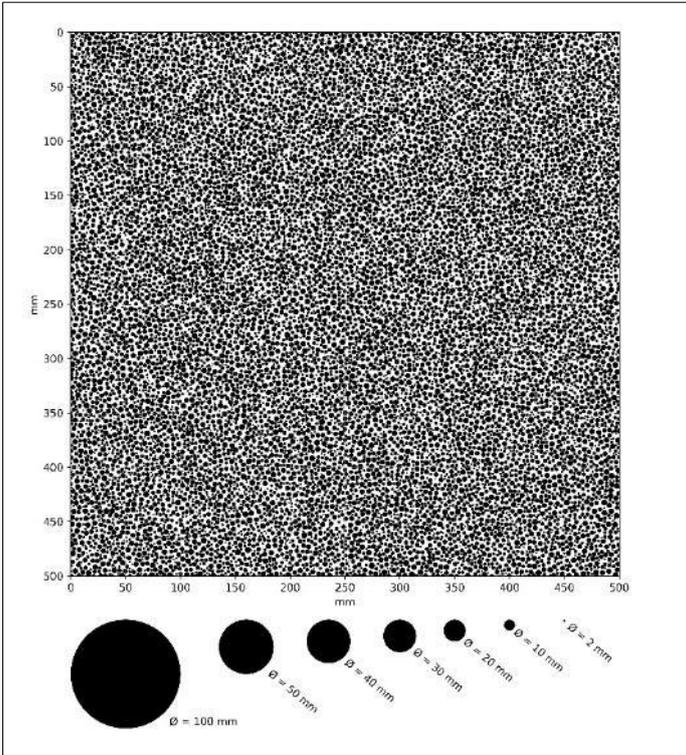
571 After collecting this information, the participants were presented with a series of four synthetic
572 sediment samples that were generated with the code framework of this project that is provided in
573 the Supplementary information of the paper. Each sample shows spherical black grains in a 500
574 by 500 mm large field on white ground. A measuring scale is given on the border of the field with
575 50 mm spaced ticks and some reference grains are given below the sample with sizes between
576 $\varnothing=100$ to $\varnothing=2$ mm. The samples are shown in Figure A 1 to Figure A 4.



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578

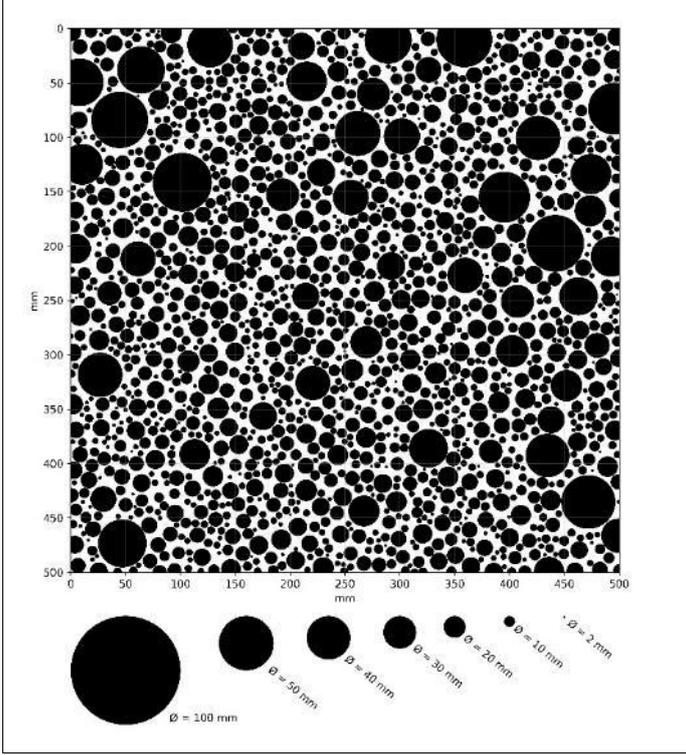
Figure A 1: Sample 1.



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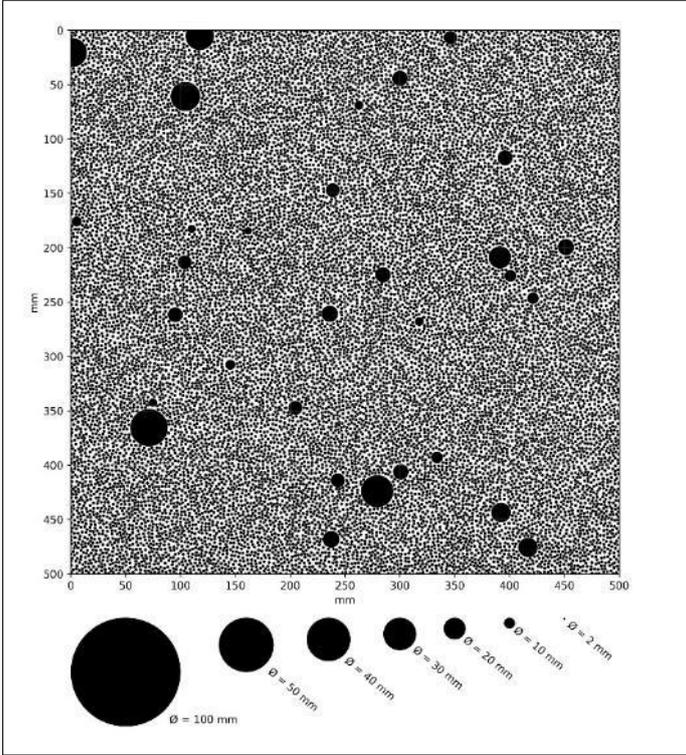
Figure A 2: Sample 2.



581

582

Figure A 3: Sample 3.

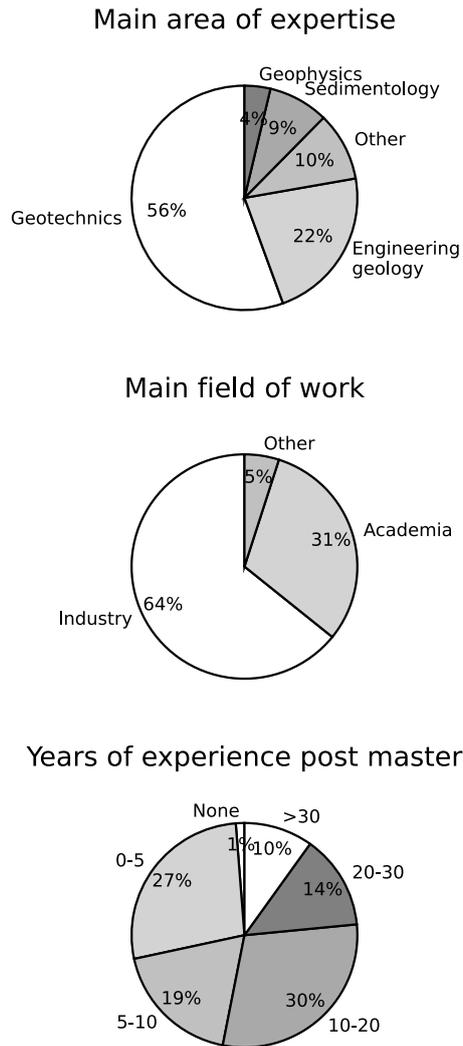


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584

Figure A 4: Sample 4.

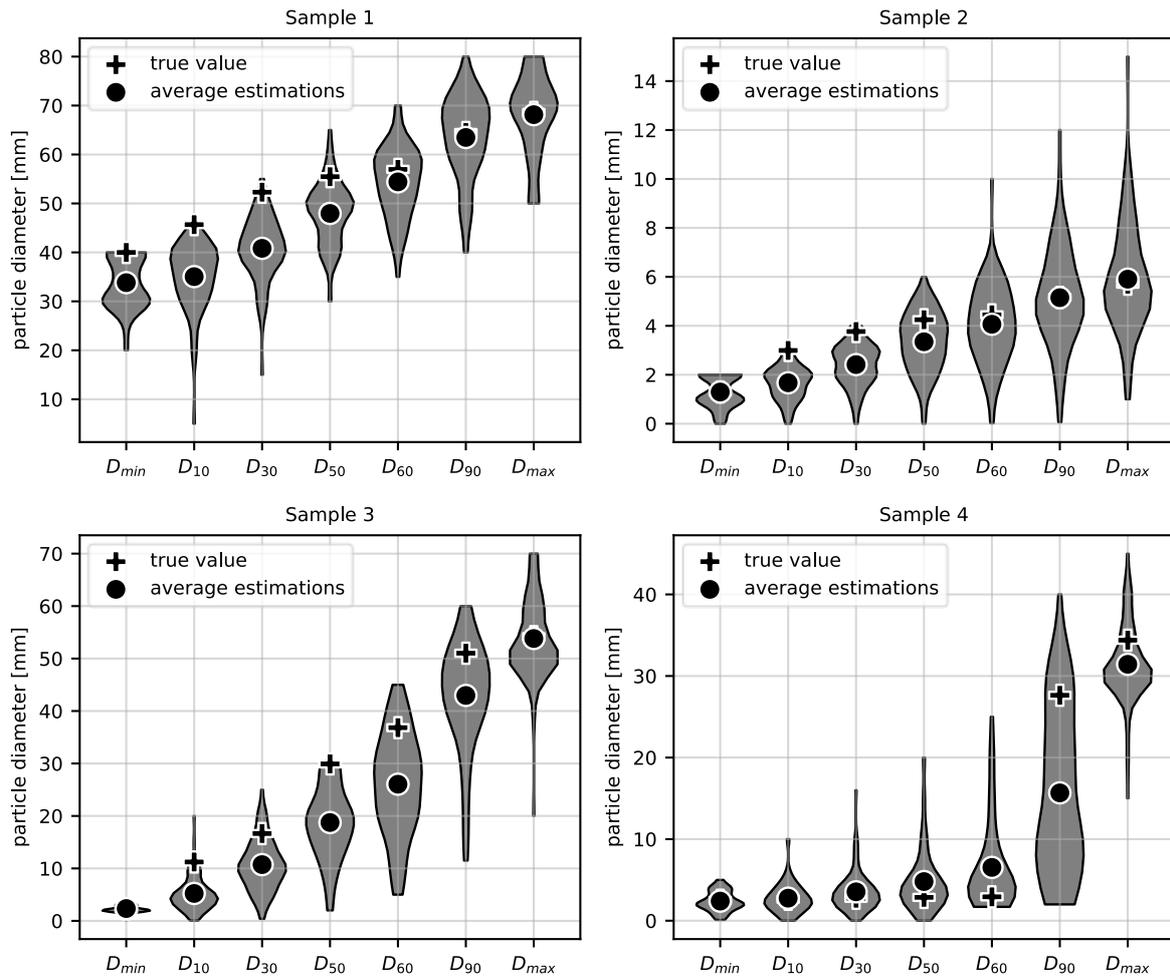
585 For each sample, the participants were asked to estimate the D_{min} , D_{10} , D_{30} , D_{50} , D_{60} , D_{90} and
586 D_{max} . The participants were told not to be too precise and to take not more than 3 minutes per
587 sample. A total number of 95 responses were collected. From these 95 responses, 14 had to be
588 completely removed because the participants gave consistently not credible responses that
589 indicated a misunderstanding of the survey (e.g. always the same number, decreasing grain sizes
590 from D_{min} to D_{max} , etc.). Furthermore, single results for samples had to be removed for similar
591 reasons but it can be observed that there are more erroneous submissions for sample 1 than for
592 the others, thus indicating that some participants needed the first sample to get used to the task.
593 After response cleaning, a total of 71, 81, 80 and 80 responses were left for the samples 1-4
594 respectively. A visualization of the collected participant meta-information is shown in Figure A 5.



595

596 *Figure A 5: Statistics of the metainformation that was collected from the participants in the survey.*

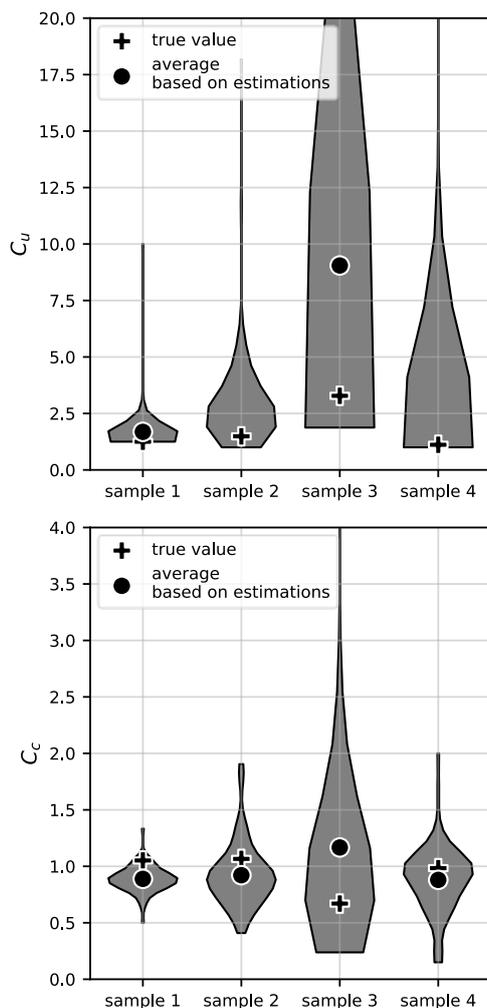
597 A visualization of the participants' responses in relation to the true values (assessed based on the
598 simulated grain distribution) for every sample is given in figure Figure A 6. While the average
599 estimated parameters are close to the true values, it can be seen that all parameters show
600 substantial variability. There are no generally observable trends, and it is not observable that the
601 D_{max} is, for example, significantly easier to assess than other D -values. The only exception is
602 sample 4 which has a pronounced gap graded distribution, and it is visible that participants
603 alternate between assigning the D_{90} to the small or the large grain sizes. Analyzing these results
604 also must consider the logarithmic scale of the problem where e.g. overestimating the size of a 4
605 mm grain by 100% is less severe than overestimating the size of a 40 mm grain by 50%.



606

607 *Figure A 6: Results of the survey. The distribution and bandwidth of participants' responses is shown with grey violin*
608 *plots.*

609 Lastly, the participant assessed values were used to compute C_u and C_c for the samples and their
610 respective distribution based on the participants feedback variability (Figure A 7). It can be seen
611 that the variability for these computed values is substantial but it also must be considered that
612 these are calculated values and not directly estimated values. The ground truth values for the
613 parameters under investigation of the survey are given in Table A 1.



614

615

Figure A 7: Variability of C_u and C_c computed from the participants responses.

616

617

Table A 1: Ground truth values for the parameters of the survey.

Sample	D_{min} [mm]	D_{10} [mm]	D_{30} [mm]	D_{50} [mm]	D_{60} [mm]	D_{90} [mm]	D_{max} [mm]	C_u	C_c
1	40.0	45.7	52.3	55.5	57.0	64.5	68.6	1.2	1.1
2	1.3	3.0	3.8	4.2	4.4	5.2	5.7	1.5	1.1
3	2.3	11.2	16.6	29.9	36.8	51.0	54.2	3.3	0.7
4	2.5	2.6	2.8	2.9	2.9	27.6	34.4	1.1	1.0

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