

1 **How Should Multiple Temperature Time Series be Compared on Graphs?**

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8 **Key Points:**

- 9 • The bias adjustment for intercomparison of multiple temperature time series impacts
10 conclusions about how global warming evolves.
- 11 • Comparison of different methods with 32 climate models shows a proposed trend-based
12 method is superior, especially in the early years.
- 13 • The trend-based method more fully reveals the differences between models whereas other
14 methods partially obscure those differences.

15

16 **Abstract**

17 How temperature biases in both climate models and observations are adjusted in order to make
18 comparisons of climate change signals has been seldom discussed, yet the choice of adjustment
19 method has a large impact on the resulting conclusions. When the primary interest is how global
20 warming evolves through time, how the models' diagnosed equilibrium climate sensitivities
21 (ECS) correlate with yearly temperatures is a logical test of agreement. Unlike other commonly
22 used methods, it is shown that correlations are maximized when all of the time series are
23 adjusted so their trend lines intersect at year zero. The issue is important to the interpretation of
24 how climate models reveal the global warming signal over time, to how well models agree with
25 observations, and to the policy impact and public debates regarding climate change.

26 **Plain Language Summary**

27 When comparing climate models to each other or to observations, the graphical representation of
28 the data can have a large impact on visual interpretation, for instance whether observations
29 support model estimates of global warming. It is shown that removal of model (or observational)
30 biases with different assumed baselines impacts both the graphical presentation as well as the
31 quantitative interpretation of model differences, especially in early years. Using global annual
32 average temperatures as an example, when the intent is to reveal how models' evolving warming
33 through time reflect their future warming, the superior method of baseline removal is to adjust
34 each temperature time series so their trend lines intersect at year zero. This is recommended as
35 the standard method by which future comparisons should be made.

36 **1 Introduction**

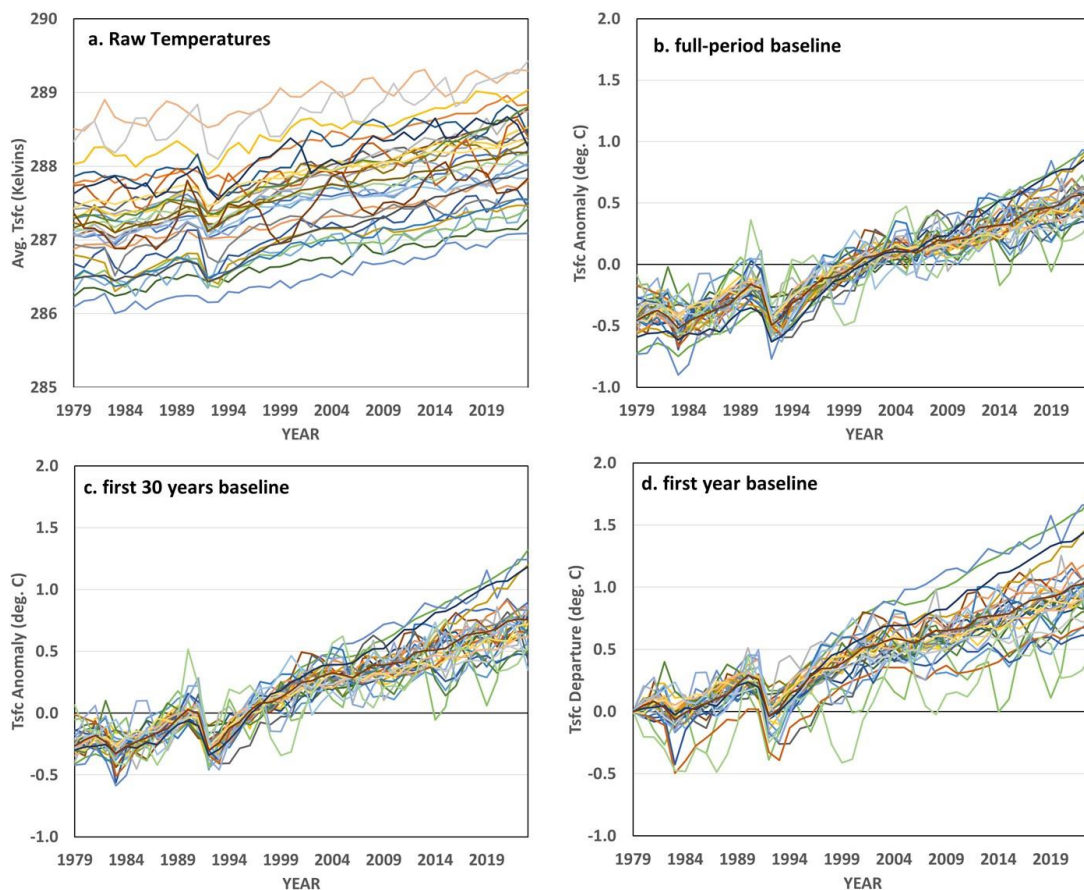
37 For over a decade there has been an ongoing, if informal, disagreement among some climate
38 researchers regarding the proper way of using global temperature time series in the context of
39 comparing climate model projections of warming against observations. While there has been
40 recent progress on this using more complex methods (e.g. Craigmile & Guttorp, 2023), here we
41 address the simple issue of how time series with roughly linear trends are commonly displayed
42 and intercompared. In these graphs one must inevitably deal with differing biases due to
43 limitations and uncertainties: in models, physics and parameterizations differ, and for
44 observations the different mix of weather stations and methods of spatial averaging and data
45 adjustment differ. While understanding those biases is itself a legitimate research topic, here we
46 instead address how bias offsets that are calculated and applied to the data impact meaningful
47 qualitative and quantitative comparison between models and/or observations. The choice of
48 baseline can affect the answer to such questions as: Does observed warming in recent years fall
49 well within the range of climate model projections of warming? Does the strength of a model's

50 response to major volcanic eruption correspond to that model's long-term warming response to
51 increasing greenhouse gas concentrations?

52 Here it is shown that commonly used approaches for baseline adjustment have serious
53 limitations, and quantitative evidence is presented for a better alternative approach.

54 **2 Time Series Comparison Using Various Baseline Removal Methods**

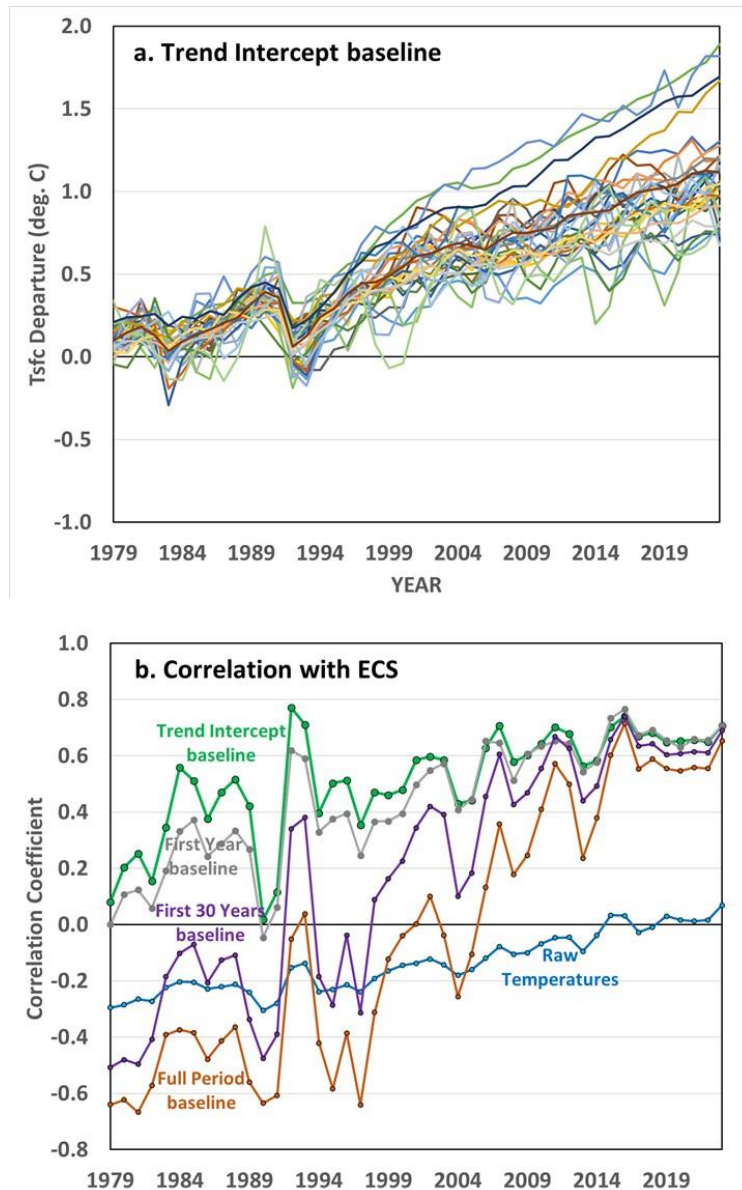
55 For 32 models taking part in the sixth Coupled Model Intercomparison Project (CMIP6, Eyring
56 et al., 2016) the global average surface air temperature (T_{sfc}) between models over the 45-year
57 period 1979-2023 varies by over 2.4 deg. C (Fig. 1a), which is large compared to expected
58 climate change signals. To intercompare the models during this (or any) period, a common
59 method is to remove from each model an average of multiple years, resulting in a temperature
60 'anomaly'. This is shown for a full-period average (Fig. 1b), an average of the first 30 years (Fig.
61 1c), and for only the first year, 1979 (Fig. 1d). We chose 1979 as the start year because the
62 strength of observed global warming has been a maximum since then, as have global
63 anthropogenic greenhouse emissions, and global satellite observations of temperature began in
64 1979.



65

66 **Figure 1.** Annual, global average surface air temperature anomalies for 32 CMIP6 climate
67 models displayed as (a) raw temperaures, (b) relative to the full-period average, (c) relative to the
68 average of the first 30 years, and (d) relative to the first year.

69 While panels b, c and d in Fig. 1 qualitatively seem to show how warming in the different
70 models evolves over time, a quantitative test of this is necessary. The most obvious way is to use
71 the Equilibrium Climate Sensitivities (ECS) of those models in response to a doubling of
72 atmospheric carbon dioxide levels above pre-Industrial levels that have been diagnosed
73 separately (e.g. see Zelinka et al., 2020 for a model summary). If we correlate the model
74 temperature anomalies in each year with the models' ECS values, the results in Fig. 2b reveal
75 that models with the warmest temperature anomalies late in the record tend to have the coolest
76 temperatures early in the record as evidenced by the generally negative correlations before 1998.



77
78 **Figure 2.** (a) As in Fig. 1, but after removal of the regression trend intercept relative to the first
79 year, and (b) yearly correlation coefficients between the 32 models' ECS values and their
80 temperature anomalies seen in the five different baseline removal methods represented in Fig. 1
81 and Fig. 2a.

82 This is not desirable if one wishes to compare models in individual years, or even groups of
83 years, in terms of how warming evolves over time. In fact, any multi-year baseline period from
84 early in the record shows this problem to some extent, that is, a tendency for the models having
85 the most long term warming (highest ECS) to have the coolest temperature anomalies early in
86 the record. Only using the first year (1979) as a baseline avoids this problem entirely.

87 But even the use of the first year as a baseline is not optimum because each climate model
88 develops its own year-to-year internal climate “noise” due to (for example) warm El Nino or
89 cool La Nina years. If one model is experiencing cool La Nina conditions in 1979, all subsequent
90 years will be anomalously warm after bias adjustment using only 1979 as a baseline. Thus, a
91 trade-off arises: Use as few years as possible early in the record to minimize the problem of
92 models with the most warming being the coolest early in the record, but use as many years as
93 possible to remove biases due to internal climate variability.

94 The most straightforward solution to this problem is to use the linear trend lines (slopes) fitted to
95 each model time series through regression, and force all of the model time series to have their
96 trend lines intersect in the first year. The easiest way to do this is to remove the regression
97 intercept value from each model’s time series, relative to year zero (1979). The result (Fig. 2b)
98 shows the trend intercept method produces the highest correlations with ECS, especially in the
99 early years. Close examination of Fig. 2a reveals the model time series with the trend intercept
100 removed are tightly clustered in the early years, and then diverge in later years roughly in
101 proportion to their climate sensitivities.

102 Note that the post-Pinatubo years of 1992-93 in Fig. 2b have a maximum correlation of all
103 methods, with a 1992 correlation of 0.77, versus only 0.34 using the first 30 years as a baseline,
104 and 0.62 using the first year. This shows the strength of the CMIP6 models’ temperature
105 response to the 1991 eruption of Mt. Pinatubo is well correlated with the models’ climate
106 sensitivities, but only if an appropriate baseline is subtracted from the data. This is an example of
107 how the choice of a baseline impacts conclusions drawn from the model data.

108 It must be emphasized that the trend intercept method of comparing time series does not
109 exaggerate the trend differences between the various models – the trends (linear regression-
110 computed slopes) remain unchanged no matter how the time series are plotted. What it does is
111 fully reveal on a graph how those trend differences evolve through time, in individual years,
112 without obscuring the differences through forcing the most rapidly warming models to have the
113 coolest temperatures in the early years.

114 **3 Conclusions**

115 Various methods have been used to compare temperature time series from climate models and
116 observational datasets, but little attention has been given to what methods are the best for both
117 qualitative and quantitative comparisons. While the long-term trends computed through linear
118 regression are arguably the single best quantitative metric of the strength of global warming, the
119 graphical relationship between various time series can be manipulated depending upon how the
120 biases between datasets are removed. For example, this issue impacts the question of how well
121 time series of observed temperatures fall within the envelope of many climate models’

122 projections of temperature in recent decades. This has societal importance since it affects both
123 public perception and policymaking which depend upon assessments of climate model accuracy.

124 The trend intercept method presented here most fully reveals the time evolving warming signal,
125 especially early in a time series when the warming signal is small compared to both the size of
126 baseline adjustments to the data and noise in the data. It is recommended that the proposed
127 method be the standard when the goal is to fully reveal, without obscuration, the temperature
128 differences between various climate models and observational datasets over time.

129 **Acknowledgments**

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133 **Data Availability Statement**

134 The CMIP6 climate model data are publicly available from the KNMI Climate Explorer website.
135 An Excel (Microsoft Corporation, 2018) spreadsheet with the model data and calculations used in
136 the paper is available at <https://github.com/roywspencer-nsstc/plotting>
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