# SWMManywhere: A Global-scale Workflow for Generation and Sensitivity Analysis of Synthetic Urban Drainage Models

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# 10 Statement

- 11 The submitted version on EarthArXiv is a non-peer reviewed preprint. This manuscript has,
- 12 however, been submitted for peer review in the Journal of Hydrology. Subsequent versions
- 13 of this manuscript may have slightly different content. If accepted, the final version of this
- 14 manuscript will be available via the 'Peer-reviewed Publication DOI' link on the right-hand
- 15 side of this webpage.

#### 16 Highlights

- SWMManywhere can synthesise an urban drainage network model anywhere in the
   world
- SWMManywhere is a parameterised approach for customising the synthesised
   network
- 21 We use sensitivity analysis to investigate uncertainty of network synthesis
- We find significant interaction between parameters, suggesting an ensemble
   approach
- Parameters controlling surface observable network elements are most sensitive

## 25 Abstract

26 Continual improvements in publicly available global geospatial datasets provide an 27 opportunity for deriving urban drainage networks and simulation models of these networks 28 (UDMs) worldwide. We present SWMManywhere, which leverages such datasets for 29 generating synthetic UDMs and creating a Storm Water Management Model for any urban 30 area globally. SWMManywhere's highly modular and parameterised approach enables 31 significant customisation to explore hydraulicly feasible network configurations. Key novelties 32 of our workflow are in network topology derivation that accounts for combined effects of 33 impervious area and pipe slope. We assess SWMManywhere by comparing pluvial flooding, 34 drainage network outflows, and design with known networks. The results demonstrate high 35 quality simulations are achievable with a synthetic approach even for large networks. Our 36 extensive sensitivity analysis shows that the locations of manholes, outfalls, and underlying 37 street network are the most sensitive parameters. We find widespread sensitivity across all 38 parameters without clearly defined values that they should take, thus, recommending an 39 uncertainty driven approach to synthetic drainage network modelling. This study showcases 40 significant potential of SWMManywhere for research and industry applications to provide 41 drainage network models in urban areas where traditional approaches are impractical.

#### 42 **1** Introduction

43 Urban drainage models (UDMs) are representations of land and pipes that can be simulated 44 with hydraulic models such as Storm Water Management Model (SWMM) (Rossman, 2010). 45 UDMs are essential for managing stormwater, preventing flooding, and ensuring the 46 sustainability of urban water systems (Butler and Davies, 2004). UDM simulations capture 47 the behaviour of drainage networks under various rainfall scenarios, enabling planners to 48 design effective infrastructure and mitigate risks (Bach et al., 2014). However, the 49 development of UDMs typically requires extensive infrastructure records on the connectivity. 50 geometric properties, and elevations of underground pipes (Bach et al., 2020; Chahinian et 51 al., 2019). In cases where these records are unavailable, whether due to ownership issues 52 or simply that they do not exist, the expense of creating a UDM becomes significant because 53 of costly surveying requirements. To forgo this expense, it may be preferrable to synthesise 54 a UDM based on the underlying information governing the placement and sizing of drainage 55 pipes, most generally, surface elevation, building locations, and road locations (Chegini and 56 Li, 2022).

57 The earliest methods to create synthetic UDM exploited the fractal nature of a drainage 58 network and, while simulations were not tested, demonstrated that the broad statistical 59 properties of the network, i.e., distribution of flow path lengths, could be estimated (Ghosh et 60 al., 2006). When road network and elevation data were incorporated, the accuracy of 61 synthesised UDMs improved and simulations approached those of a real UDM for the same locale (Blumensaat et al., 2012). Generally, UDM synthesis involves three main tasks: 62 63 delineating surface characteristics, deriving network topology, and hydraulic design, each of 64 which will be reviewed below.

First, surface characteristics, hereafter referred to as sub-catchments, quantify the spatial
distribution of stormwater drainage from impervious areas to manholes. Sub-catchment
delineation has received the least attention in UDM synthesis literature and most commonly
follows a watershed delineation approach (Blumensaat et al., 2012; Warsta et al., 2017). The

69 drained impervious area within a delineated sub-catchment is typically calculated from the 70 area covered by roads and buildings (Mair et al., 2017; Chegini and Li, 2022). However, 71 another simpler method is to assign impervious areas to drain to a nearest manhole (Reyes-72 Silva et al., 2023). Both methods require identification of manholes, highlighted as critical 73 future work in Blumensaat et al., (2012), but has received little attention since (Bertsch et al., 74 2017; Chahinian et al., 2019). We place sub-catchment delineation and manhole 75 identification as the first tasks to perform during UDM synthesis, since network topology and 76 hydraulic design should account for the impervious area contributing to a given pipe.

77 Second, network topology describes the spatial layout of a UDM, connectivity of pipes, and 78 connectivity of the sub-catchments to UDM, i.e., through manholes. Network topology is 79 typically derived by asserting that pipes follow roads, thus dramatically reducing the 80 dimensionality of deriving network topology (Mair et al., 2017; Xu et al., 2021). An efficient 81 network that visits all manholes without redundant pipes can be derived using a shortest 82 path-based algorithm. This algorithm minimizes the total graph cost, with each edge (i.e., a 83 plausible pipe) assigned an individual cost that represents some penalty associated with 84 retaining that edge. Chahinian et al. (2019) provide a detailed exploration minimising costs 85 based on pipe length, pipe adjacent angle, and slope, and highlighting the importance of 86 slope as a cost. Reyes-Silva et al. (2023) derive the UDM by applying the minimum 87 spanning tree (MST) to a full street network to minimise the number of pipes. This approach, 88 however, does not inherently consider slope in the deriving network topology step since MST 89 is only applicable to undirected networks, instead gravitational slope along pipes is enforced 90 as a postprocessing correction. A minimum spanning arborescence is an alternative 91 approach to solve such a problem for a directed network (Ray and Sen, 2024; Tarjan, 1977), 92 although has not yet been demonstrated in UDM synthesis. Furthermore, an additional cost 93 to be minimised that has not been tested in the literature is the need to minimise the 94 impervious contributing area to a given pipe and thus more evenly distribute flow throughout

95 the network, much in the manner of the original proposed fractals for network topology96 (Ghosh et al., 2006).

97 Third, hydraulic design refers to the selection of pipe diameter, invert levels, and other pipe 98 hydraulic parameters in a synthetic UDM, which typically follows local standards (Chegini 99 and Li, 2022; Duque et al., 2022; Reyes-Silva et al., 2023). Duque et al. (2022), present a 100 methodology for designing sanitary sewer networks by starting from the most upstream 101 pipes, iteratively working downstream, and designing each pipe by minimising the costs 102 subject to the feasibility of design constraints; such an approach could be equally valid for a 103 UDM. In cases where the impervious contributing area of a given pipe has been 104 synthesised, a Rational Method could be applied for determining pipe size. A variety of more 105 extensive global optimisation methods exist for hydraulic design to both minimise costs (e.g., 106 Sun et al., (2011)), or calibrate to observations (e.g., Huang et al., (2022); Sytsma et al., 107 (2022)). However, these calibration studies highlight the inherent equifinality in parameter 108 selection, thus suggesting the uncertainties in such a high dimensionality problem may 109 outweigh any 'optimal' algorithm.

Because UDM synthesis requires a hydraulic design, equifinality must also be inherent to UDM synthesis. We argue that this has been under-recognised in existing UDM synthesis, primarily because of a lack of data and the absence of an automated, end-to-end workflow to assess the impact of parameter selection. A reader may observe results from the supplement of Duque et al., (2022), which demonstrates that small changes in their grid scale for the synthesis algorithm can generate dramatically different sanitary sewer networks.

An equally valid line of inquiry is, therefore, to examine UDM synthesis with sensitivity
analysis to quantify the importance of various factors in generating more realistic networks
(Pianosi et al., (2016). Sensitivity analysis provides verification by revealing ranges of
'behavioural' parameter values that produce acceptable model outputs, thus informing
application of UDM synthesis in data-sparse regions. Additionally, it reveals the dominant

122 controls and key processes governing UDM synthesis by quantifying the relative importance 123 of different parameters. In turn, revealing where uncertainty reduction may be most 124 beneficial. We do not assume that accurate UDM synthesis is possible in every location 125 using solely building, road, and elevation data, particularly given the complexities involved in 126 the gradual expansion of a UDM (Rauch et al., 2017). However, it is impractical to improve 127 UDM synthesis by capturing every possible element involved in network evolution. Instead, 128 sensitivity analysis provides an objective way to guide improvement; prioritising 129 measurements and processes that relate to the most sensitive parameters.

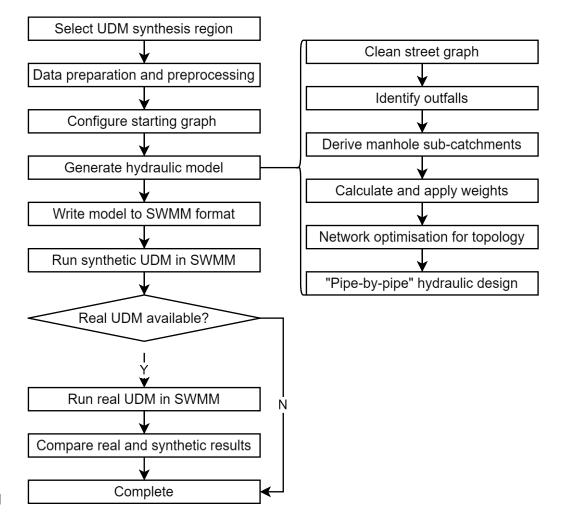
130 Continual improvements in development and accessibility of remote sensing and open 131 geospatial data at global scale facilitates applicability of UDM synthesis in many locations. 132 Chegini et al., (2022), demonstrate an approach that can perform network topology and the 133 dimensioning part of hydraulic design anywhere in the continental United States. Montalvo et 134 al., (2024) implement the UDM synthesis algorithm presented by Reves-Silva et al., (2023), 135 in a GIS tool, however this approach does not acquire/process the necessary geospatial 136 data nor is it open-source at time of writing. We believe that a global tool, that is open-137 source, and tailored to accommodate the uncertainty inherent in the UDM synthesis problem 138 would be of great value to the urban drainage community. Such a tool would enable 139 hydrodynamic method developers to bypass the reproducibility crisis (Stagge et al., 2019; 140 Hutton et al., 2016), by demonstrating their tools on an unlimited suite of UDMs synthesised 141 in cities worldwide, improving on the entirely theoretical test suites that presently exist 142 (Möderl et al., 2011, 2009; Sweetapple et al., 2018). Furthermore, it would contribute 143 towards better representation of urban environments in the regional hydrological cycle, 144 which is a critical and under-represented component of such applications (Coxon et al., 145 2024).

In this paper we present a workflow, called SWMManywhere, to synthesise UDMs anywhere
in the world. We show its versatility by applying it to multiple case studies (i.e. sewer
systems of different sizes in two different countries) and to facilitate its global usage we

149 deploy it as an open-source Python tool (Dobson et al., 2024a) with extensive 150 documentation (SWMManywhere documentation, 2024). SWMManywhere provides a 151 parameterised and easy to customise approach for UDM synthesis which allows us to 152 perform sensitivity analysis of synthesised UDMs. We ensure SWMManywhere responds to 153 the need for worldwide application by using open global datasets and including the retrieval 154 and preprocessing of these datasets as part of the algorithm. The methods implemented in 155 SWMManywhere also include a variety of technical novelties in the field of UDM synthesis, 156 including use of a minimum spanning arborescence to derive topology, enabling 157 minimisation of contributing area during this process, and implementing Duque et al., 158 (2022)'s pipe-by-pipe design method for urban drainage networks.

# 159 2 Methodology

160 A high-level overview of our proposed SWMManywhere workflow is shown in Figure 1.



### 162 Figure 1: Overview of the SWMManywhere workflow.

163 We present an end-to-end workflow for UDM synthesis and comparison against a real UDM, 164 if available, anywhere in the world. A key barrier to UDM synthesis identified in literature is 165 difficulty in setting up a hydraulicly correct model, thus we specify data acquisition and 166 preprocessing in the workflow. The 'generate hydraulic model' step, is the key step that 167 should ultimately create sub-catchments, a network topology, and hydraulic designs of pipes 168 that together fully describe the synthesised drainage network. Such a drainage network, i.e., 169 the synthetic UDM, will be valid for simulation in a widely used software for design and 170 analysis of drainage networks, such as SWMM, enabling studying different precipitation 171 events and inspecting state variables such as pipe flows and pluvial flooding. In Section 2.1, 172 we describe the theory and processes in our workflow, also explaining how it can be 173 customised with parameter choices and additional processes to vary the nature of the 174 synthesised UDM.

175 A key hypothesis that must underlie any synthetic UDM approach is that results may be valid 176 in places where a real UDM is not available or not trusted. Because we observed the 177 sensitivity to parameter selection in previous UDM synthesis literature, we intentionally 178 specify SWMManywhere to be highly parameterised and customisable. We use sensitivity 179 analysis on these parameters to demonstrate how they impact synthesised networks. In 180 Section 2.2, we describe how sensitivity analysis can guide the use of SWMManywhere in 181 areas where parameters cannot be estimated a priori based on field data and provide a 182 deeper understanding of UDM synthesis. We apply this analysis to eight UDMs in two different locations. 183

184 We discuss UDM synthesis using graph theory terminology:

A graph represents the UDM, consisting of nodes (manholes) that are connected by
 edges (pipes). The graph can be either undirected or directed, indicating that
 connections are between two nodes (undirected) or from one node to another
 (directed). Pipes are undirected since head may drive uphill flow, however, treating

the graph as directed enables better description of preferential flow paths and is also
the format required by SWMM, SWMManywhere makes use of both directed and
undirected graphs.

In graph theory, a subgraph refers to a sub-selection of the graph and is called a
 connected component if every node is in the subgraph reachable from every other
 node within that subgraph. Connected components are used in SWMManywhere to
 describe a collection of manholes and pipes that drain to a common outfall.

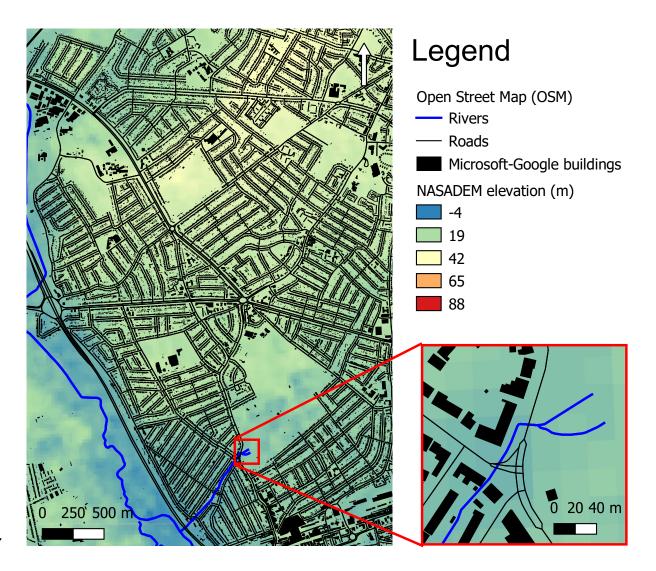
196 The topology of the graph captures the overall arrangement and relationships of 197 nodes and edges and can be thought of as the pipe layout in a UDM. The edges can 198 have costs, for example length, which may be minimised by shortest path algorithms 199 to minimise flow routes. Flow routes should be minimised in any drainage network to 200 drain the catchment as efficiently as possible, preventing the accumulation of water 201 and flooding of manholes. A minimum spanning tree is a subgraph that connects all 202 nodes with the minimum possible total edge cost for an undirected graph, a minimum 203 spanning arborescence is the same for a directed graph, thus these represent the 204 most cost-efficient pipe layouts that may exist for a given area. We will refer to a 205 graph of potential pipe-carrying edges as the street graph, while the optimised layout 206 is the UDM topology.

207 2.1 SWMManywhere

#### 208 2.1.1 Data and preparation

Our SWMManywhere approach uses datasets that are of sufficient level of detail to be used in global application: road locations, river locations, elevation, and building footprints. We stress that these datasets, in particular road locations and building footprints, vary in quality from location to location, thus, the downloaded data for a given case study should always be inspected carefully. Additionally, we enable manually sourced, higher quality data for input, if available, as described in the online documentation (SWMManywhere documentation,

- 215 2024). The default datasets are visualised for one of our case studies in Figure 2, and
- 216 described in further detail in this section.



217

218 Figure 2: Visualisation of downloaded data in the Cran Brook, UK. See main text for citations.

Assuming pipes can only exist in pre-specified plausible locations will dramatically reduce the dimensionality of the shortest-path UDM topology derivation. Thus, we assume that pipes can only exist in certain locations, typically streets due to the common validity of this assumption (Mair et al., 2017). In addition, paved streets constitute one of the key impervious surfaces which must be drained in a UDM. Rivers are also downloaded as these are potential outfall locations of the drainage network, described in further detail in Section

<sup>219</sup> Streets and rivers

226 2.1.2. OpenStreetMap (OSM) provides street and river data worldwide and is used in this227 study.

# 228 Impervious areas

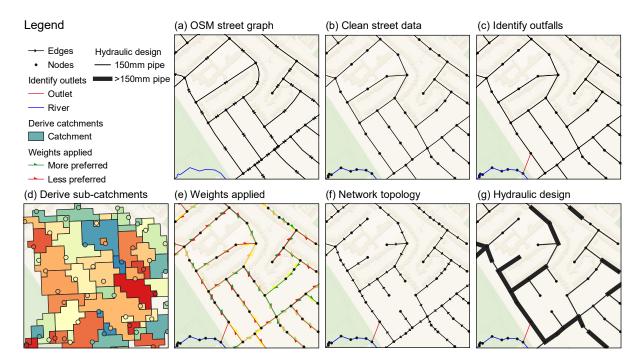
229 To calculate the impervious area of a sub-catchment, and thus enable runoff generation, we 230 use road locations, their number of lanes, which are contained within OSM, and building 231 footprints. Recent advances in machine learning have enabled identification of building 232 perimeters from high-resolution satellite data worldwide. Two large datasets, provided by 233 Google and by Microsoft, are now combined and available at (Google-Microsoft Open 234 Buildings, 2024). Both datasets use convolutional neural networks to classify pixels as 235 buildings (Tan and Le, 2019; Sirko et al., 2021) and custom methods to polygonise these 236 pixels into buildings (Sirko et al., 2021; Computer generated building footprints for the United 237 States, 2024). The authors would note that, although global, this dataset has varying quality 238 in different regions due to the nature of the training data that was used and resolution of 239 satellite imagery. Although other impervious surfaces besides roads and buildings, such as 240 car parks, that must be drained in a UDM are common, we could not identify global datasets 241 describing these, and thus consider them currently outside the scope of this study.

#### 242 Elevation

Elevation data, in the format of a Digital Elevation Model (DEM), is essential to delineate manhole sub-catchments, to calculate the slope along edges, and to identify if there are paths in the street graph that should not be ignored, for example, those at that span different hydrological catchments. We use NASADEM, which is a publicly available radar-based global DEM at 30m resolution (Crippen et al., 2016), from Microsoft Planetary Computer (Source et al., 2022). Although higher resolutions around 2m are recommended for UDM (Arrighi and Campo, 2019), such datasets do not yet exist openly at global scales.

# 250 2.1.2 Pipe network generation

- 251 A key innovation of our approach is to iteratively process a street graph and gradually
- transform it into a UDM with full hydraulic design. These processes must take a graph and
- 253 return a graph. The key tasks that they perform are summarised in Figure 3, discussed
- further in this section and used for the experiments in this paper.



- Figure 3: Visualisation of key iterations to the graph as different processes are applied. Catchments (D) are coloured by the manhole that they drain to.
- 258 Table 1 lists all tuneable parameters of our proposed workflow, with reasonable default
- values for these parameters and their ranges provided in the online documentation
- 260 (SWMManywhere documentation, 2024). We carry out an extensive sensitivity analysis (see
- 261 Section 2.2) to identify any behavioural ranges of these parameters and identify their relative
- 262 importance in UDM synthesis.

Table 1: SWMManywhere user adjustable parameters that are tested in sensitivity analysis for this work, a full list
 of parameters is available in the online documentation (SWMManywhere documentation, 2024). If the variable is
 described differently from its use in the software to improve clarity, the software term is indicated in brackets.

GROUP	VARIABLE	KEY
SYSTEM DESCRIPTION	node merge distance	pNM
(MANHOLES AND OUTFALLS)	outfall length	pOL
	max street length	pXS
	river buffer distance	pRB
TOPOLOGY DERIVATION	chahinian slope scaling	pSS
	chahinian angle scaling	pAS
	length scaling	pLS
	contributing area scaling	pCS
	chahinian slope exponent	pSE
	chahinian angle exponent	pAE
	length exponent	pLE
	contributing area exponent	pCE
HYDRAULIC DESIGN	max filling ratio (max fr)	pFR
	min v	pMV
	max v	pXV
	min depth	pMD
	max depth	рХD
	design precipitation (precipitation)	pDP

266

# 267 Data cleaning and manhole identification

As explained in Section 2.1.1, OpenStreetMap (OSM) is the default data source for obtaining 268 269 street and river graphs. However, the raw OSM data are not directly suitable for UDM 270 generation, so we perform a variety of data cleaning operations to create a more suitable 271 graph for UDM synthesis, as illustrated in Figure 3a-b. The first significant process in data 272 cleaning is enforcing a maximum edge length, splitting edges that are longer than max street 273 length parameter (pXS, Table 1). The second is merging of nodes, which joins nodes 274 together if they are within a specified distance of each other (node merge distance, pNM). 275 These two processes jointly control where manholes are located along edges and the 276 frequency with which they occur. The final significant task in data cleaning is buffering street 277 paths in proportion to the number of lanes to create a shapefile of impervious street area. 278 The remainder of processing in this stage is perfunctory, performing tasks such as ensuring 279 consistent geometries, a consistent identification scheme, removing parallel edges, and

converting the directed street graph to an undirected graph (as a pipe may flow in a directionopposite to road travel).

#### 282 Sub-catchment outline and surface characteristics

We begin the sub-catchment delineation, by first burning the road network into the DEM of 283 284 an urban area. This burning process is a common practice in UDM sub-catchment 285 representation (Gironás et al., 2010) and involves lowering the elevation of grid cells in the 286 DEM that contain roads. Then, we hydrologically condition the DEM by breaching 287 depressions (Lindsay, 2016a). Upon conditioning the DEM, we compute the flow direction, 288 using the D8 method (O'Callaghan and Mark, 1984), and slope. Because our workflow 289 includes generation of a SWMM model, a sub-catchment width parameter is required. We 290 follow the approach proposed by InfoWorks (Subcatchment Data Fields (InfoWorks), 2024) 291 to compute the width of a sub-catchment based on the radius of a circle with area equal to 292 the area of the sub-catchment.

#### 293 Outfall identification

294 Another key feature of a UDM is outfall locations. The first step in identifying outfalls requires 295 assessing the topology of the graph to ensure its hydrologic feasibility (Seo and Schmidt, 296 2013; Li and Willems, 2020). To achieve this, we remove edges that cross the boundaries of 297 hydrological catchments (defined as the largest non-overlapping drainage basins in the 298 study region), because these are unlikely to carry a pipe. Then, we identify potential outfall 299 locations by assuming that outfalls may only exist within a specified distance of a river (river 300 buffer distance, pRB). Although other factors such as environmental considerations affect 301 selection of the outfall location, in this study, we only account for the vicinity of water bodies. 302 We incorporate the relative construction cost of outfalls in our workflow, by assigning weights 303 to the identified outfall locations based the length of the pipe that connects the network to 304 the river (outfall length, pOL). If no potential outfalls are identified the node with the lowest 305 elevation is used as the outfall. On the other hand, in cases where multiple plausible outfalls

are identified, we retain them all at this step and determine the outfall during the networktopology derivation step.

#### 308 Calculating weights and network topology

The network topology can be derived as a minimisation problem of overall graph cost. This minimisation should start with a graph of potential edges (i.e., the graph up to this point) and return a directed graph that visits all nodes (manholes), minimising overall graph cost, without retaining redundant edges (pipes), which is also referred to as a minimum spanning arborescence (MSA).

314 The first step to take in network topology derivation is to identify how each edge contributes 315 to the overall graph cost. As identified by Chahinian et al., (2019), it is plausible that each of 316 pipe length, pipe slope and pipe adjacent angle (the angle at which two joining pipes meet) 317 are important to consider for minimisation. We further propose that the total contributing area 318 carried by pipes in the derived network should also be minimised. As with *ibid.*, these factors 319 do not necessarily contribute to the overall graph cost symmetrically or proportionally. For 320 example, while both negative slopes and overly steep positive slopes are penalised, the 321 penalisation on negative slopes increases with slope more sharply than for positive slopes, 322 because the former becomes hydraulically impractical more quickly than the latter. It is not 323 apparent which of these factors (slope, angle, area, and length) are more important to 324 minimise than others and so we combine each factor to be varied, as in *ibid*. We deviate 325 from *ibid.* by assigning both a linear and exponential scaling parameter to each factor (rather 326 than solely linear), enabling high customisation of how overall graph cost is calculated (i.e., 327 parameters in the topology derivation group). We calculate each individual factor, apply 328 scaling parameters, and sum these into an overall cost for each edge in the graph, 329 producing a graph such as that visualised in Figure 3e.

The network topology is then derived using an implementation based on the shortest-path
algorithm proposed by Tarjan (1977), to find the MSA of the graph. The algorithm starts from

332 a designated "waste" node that all potential outfall locations are connected to, either directly 333 or through river paths, thus enabling all connected component subgraphs to be handled in a 334 single pass. The algorithm initializes a priority queue with the waste node's incoming edges, 335 sorted by their costs. At each step, the minimum cost edge is extracted from the priority 336 queue. If the node it leads to is not already included in the arborescence being constructed, 337 that node and edge are added to the arborescence. The node is marked with its parent, and 338 any edges incoming to that node are added to the priority queue. This process continues 339 until all nodes are included in the arborescence. The final arborescence represents the UDM 340 network topology, where the selected edges correspond to the pipe segments that must be 341 hydraulically designed.

342 Hydraulic design

Duque et al., (2022), propose a "pipe-by-pipe" method to design sanitary sewer network pipes, the method starts at the most upstream pipes, designing each pipe in terms of diameter and depth under a set of design constraints (see *hydraulic design* group), and continues iterating downstream. They demonstrate that this method is comparable to an optimal dynamic programming-based approach, although is significantly more efficient. We adapt the pipe-by-pipe approach to make it suitable for a SWMManywhere approach:

Rather than deriving the design flow from household waste generation, we use a
 Rational method that calculates the design flow as the entire impervious area in sub catchments upstream of the pipe being designed multiplied by a *design precipitation*,
 *pDP*, amount.

Inspection of any large real UDM will commonly reveal pipes travelling in an uphill
 direction, as measured by surface elevation. Wherever possible the pipe's elevation
 will be such that they flow downhill despite the surface elevation, however there is no
 guarantee that any hydraulically feasible design will exist. Because Duque et al.
 (2022) derive network topology using hydrological flow paths a feasible design will
 always exist, however this is not the case for SWMManywhere, which uses streets

for pipe locations and accounts for factors besides slope during network topology
derivation. To accommodate this, we include a surcharge feasibility constraint, which
allows a pipe to be designed for flow under surcharge, provided this is the only way
to reach a feasible hydraulic design.

To provide better performance, we assess all designs for a pipe rather than selecting
 the first feasible design. The selected design first aims to satisfy feasibility
 constraints, and if no feasible design exists, picking the most feasible design. It then
 minimises depth, diameter, and excavation cost, as calculated in Duque et al. (2022).

367 The final product is a fully described UDM, complete with sub-catchments and hydraulic368 designs, thus sufficient to be simulated in software such as SWMM.

369 2.1.3 Measuring effectiveness of UDM synthesis

370 The question of 'how realistic is a synthesised UDM' is most sensibly assessed by 371 comparing synthesised results against a real UDM. UDM synthesis in a sensitivity analysis 372 context requires understanding why we see the results that we see. Thus, an extensive suite 373 of allowable performance metrics is provided covering a variety of different measures and 374 variables, see Table 2 for a list of the metrics used in this study. We define metrics that 375 measure performance for different elements of UDM synthesis. System description metrics 376 assess the synthesised UDM in terms of properties that describe infrastructure, topology 377 metrics investigate the layout of the graph, and design metrics assess the derived diameter 378 of pipes. Furthermore, the UDM is simulated in SWMM and thus simulated flow, and flooding 379 can also be compared.

CATEGORY	MEASURE	VARIABLE	KEY
SYSTEM DESCRIPTION	relerror	length	mRL
	relerror	npipes	mRP
	relerror	nmanholes	mRM
TOPOLOGY	deltacon0	-	mD0
	laplacian distance	-	mLD
	vertex edge distance	-	mVD
	kstest	edge betweenness	mKE
	kstest	node betweenness	mKN
DESIGN	relerror	diameter	mRD
	kstest	diameter	mKD
SIMULATION	nse	flow	mNQ
	kge	flow	mKQ
	relerror	flow	mRQ
	nse	flooding	mNF
	kge	flooding	mKF
	relerror	flooding	mRF

Comparing flow and/or flooding simulations is typical in the UDM synthesis literature (Reyes-381 382 Silva et al., 2023; Blumensaat et al., 2012). We create a timeseries of total flooded volume to 383 assess flooding simulation performance across the entire network. Meanwhile, flows are 384 assessed at the system outfall, as with (Blumensaat et al., 2012). However, unlike existing 385 literature, which assumes that the outfall locations of the network being synthesised are 386 known, we do not make this assumption, as this information is not globally available. 387 Instead, we identify where synthetic manholes fall inside sub-catchments of the real network. 388 From these classified manholes it identifies the most commonly represented outfall, and sub-389 selects only that connected component for comparison purposes.

Because the reasons for performing sensitivity analysis are to understand how parameterschange behaviours in UDM synthesis, the most common measure of performance we use is

the relative error (*relerror* measure in Table 2, equation 1), which is simple to understand
and provides directionality in terms of over/under estimation,

$$relerror = \frac{mean(synthetic) - mean(real)}{mean(real)}$$
(1),

where *synthetic* is the synthetic UDM data to be compared against the *real* data. We omit a conventional *time* component of the metric because the same equation can equally be used for timeseries or design properties (such as average diameter) alike. In cases of comparing flow or flooding timeseries, we also include the Nash-Sutcliffe Efficiency and Kling-Gupta Efficiency, because these are commonly used and so will provide users who are familiar with them a more nuanced grasp of the synthetic UDM's performance.

A further set of measures that can be used for synthetic networks are those that test the
topological similarity of the derived vs real network, we implement a variety of those
presented in existing literature (Wills and Meyer, 2020; Chegini and Li, 2022), see *topology*category in Table 2.

#### 404 2.1.4 Implementation

405 SWMManywhere is a highly modular workflow and in this study, we implement it in Python 406 and publish it as an open-source tool (Dobson et al., 2024a). We note that the workflow is 407 general and can be implemented in any other programming language. In our implementation 408 of SWMManywhere the minimal required user input is the bounding box of the target urban 409 area, and all remaining steps Figure 1 are automated. The bounding box should be provided 410 in terms of latitudes and longitudes in WGS 84 geographic coordinate system (EPSG:4326). 411 SWMManywhere will reproject all downloaded data into the Universal Transverse Mercator 412 (UTM) coordinate system. UTM uses a coordinate system with metre as its unit, and thus 413 can provide accurate distance and area calculations in contrast to WGS 84. The UTM is split

into zones and the zone ultimately used in a SWMManywhere run is calculated based on theUTM zone of the bounding box.

416 As we described in Section 2.1.2 the most complex step in the workflow is the pipe network 417 generation, i.e., iteratively applying various graph operations to the initial graph street to 418 generate the final UDM. These operations, referred to in our implementation as graph 419 functions, have a variety of parameters that need to be specified, as listed in Table 1. 420 Considering the importance of graph functions and to accommodate flexibility in applying 421 them, our implementation allows adding, removing, or changing their order without modifying 422 the code. Structuring code into graph functions enable easy reuse of code, customisation, 423 and introduction of new processing steps. Graph functions are wrapped in a class for 424 validation, enabling SWMManywhere to identify if a set of graph functions to be applied is 425 valid a priori. Graph functions are stored in a registry object to enable easy access. We 426 provide a description of all graph functions in the documentation online (SWMManywhere 427 documentation, 2024). However, users may also customise the selection and order of graph 428 functions, or create new ones, as described in the online documentation, to fit their 429 requirements.

430 Processes or operations described in Sections 2.1.1 and 2.1.2 that are used by but not431 implemented natively within the tool are described in Table 3.

432 Table 3: List of tools for specific tasks in our SWMManywhere implementation.

DEM CONDITIONING	Whitebox	(Lindsay, 2016b)
FLOW DIRECTION CALCULATIONS	Whitebox	(Lindsay, 2016b)
SUB-CATCHMENT DELINEATION FROM	PyFlwDir	(Eilander, 2022)
FLOW DIRECTIONS		
SUB-CATCHMENT SLOPE	PyFlwDir	(Eilander, 2022)
CALCULATION		
OSM DATA RETRIEVAL	OSMnx	(Boeing, 2017)
GRAPH OPERATIONS	Networkx	(Hagberg et al., 2008)

#### TASK

#### SOFTWARE REFERENCE

#### 433

434 To accommodate ease of use for a wide range of users with different levels of programming experience, we provide a command-line interface (CLI) for the software. More experienced 435 436 users can take advantage of the modularity of SWMManywhere for more advanced 437 customisation of the workflow. The CLI works with a configuration file that enables a user to 438 change parameter values and functionality. The minimal essential requirements that this file 439 must contain are a project name, a base directory, and a bounding box. The configuration 440 file provides a centralised location to perform customisations including changing the 441 selection/ordering of graph functions, changing parameter values (see Table 1), file locations 442 of a real network to compare against (see Section 2.1.3) and which metrics to calculate (see 443 Table 2), a starting graph if not using downloaded street data, and any running settings for 444 the SWMM simulation. A variety of online tutorials explain the procedure to make such 445 customisations.

SWMManywhere provides a capability to write simple SWMM model files (typically with a
.inp file extension) that have been synthesised via the various graph functions used. It also
provides a wrapper of the PySWMM software (McDonnell et al., 2020), which enables calling
the SWMM software and interacting with its simulations from Python. Thus, in addition to the

450 UDM synthesis, writing, running, and calculating metrics if real network information exists451 are carried out during the command line call.

Precipitation data is frequently identified as a critical factor in UDM simulations (Ochoa-Rodriguez et al., 2015), however, there are currently no open global datasets that provide the high frequency monitoring needed to drive these models and so precipitation must be user-provided if deviating from the default storm provided as part of the tool.

456 2.2 Sensitivity analysis

457 Sensitivity analysis is used to examine how output variations can be attributed to input 458 variations, typically expressed as sensitivity indices for each model parameter (Pianosi et al., 459 2016). While popular reviews in the environmental sciences define sensitivity analysis as 460 specific to model input/outputs (Saltelli et al., 2008, 2019; Pianosi et al., 2016), it can equally 461 be applied to any generic parameterised workflow, such as SWMManywhere. As defined in 462 Table 1, there are a wide variety of parameters that must be selected, many of which do not 463 have values that could be easily measured or derived, and thus are useful candidates for 464 sensitivity analysis.

465 In general, it is recognised that, to robustly conduct sensitivity analysis, a global method 466 should be used, and the variability of the calculated indices should be checked to ensure 467 that the number of samples is sufficient (Saltelli et al., 2019). Because of the presumed high 468 level of dependency in the SWMManywhere workflow (for example, hydraulic design 469 depends entirely on network topology, which in turn depends on outfall and manhole 470 identification), we also calculate second order indices to better capture interactions between parameters (Herman and Usher, 2017). To implement sensitivity analysis for 471 472 SWMManywhere, we use the SALib software (Herman and Usher, 2017), which provides a 473 variety of global methods for sampling parameter ranges and calculating sensitivity indices 474 natively in Python. In this study we use the Sobol method (Sobol, 1993) due to its 475 widespread use and recognised robustness of results providing that a sufficient number of 476 samples can be investigated (Pianosi et al., 2016). 18 parameters are sampled, indicated in

Table 1, and 16 metrics, Table 2, are evaluated. Thus, the overall approach is to perform
parameter sampling, run SWMManywhere with the parameters of each sample, calculate the
performance metrics between the synthesised and real UDMs, and calculate sensitivity
indices.

Sobol sensitivity analysis that includes second order interactions with SALib requires takingsamples equal to,

$$N = n * (2m + 2) \tag{2},$$

483 where N is the total number of samples (or SWMManywhere calls), m is the number of 484 parameters, and *n* is the number of Sobol sequence samples to generate (preferably a power of 2). In this experiment we set n to  $2^{10}$  (1024), m is 18, resulting in N of 38912. As 485 demonstrated in Pianosi et al., (2016), this many evaluations ( $m \times 1000$ ) are towards the 486 487 upper limit of what is found in the literature. We take this opportunity to note a further benefit 488 of sensitivity analysis in the context of SWMManywhere as a global tool, which is that testing 489 it under such a large and diverse range of parameters further guarantees robustness of the 490 software implementation in locations not tested.

# 491 **3 Case studies**

492 In this study, we evaluate our proposed workflow by comparing the SWMM simulation 493 results obtain from using the synthetic UDM with those of the real UDM for the Cran Brook, 494 London, UK (Babovic and Mijic, 2019). We then perform sensitivity analysis in other 495 locations to examine the transferability of results and parameters. We use seven UDMs 496 around the town of Bellinge, Denmark, as delineated by Farina et al., (2023). These data 497 were selected because they are openly available and demonstrate results over a wide range 498 of scales (Pedersen et al., 2021). The properties of the case study networks are presented in 499 Table 4.

#### 500 Table 4: Summary of networks tested and their properties

Network	Number of	Number of	Impervious
	nodes	edges	percentage
Cran Brook	6931	6965	27
Bellinge 1	142	150	36
Bellinge 2	118	117	33
Bellinge 3	52	51	25
Bellinge 4	46	45	32
Bellinge 5	45	46	40
Bellinge 6	36	35	32
Bellinge 7	15	14	34

501

502 A key feature of many UDM is the presence of hydraulic structures such as weirs, orifices, 503 storages, or pumps. There is extensive evidence from the sewer network simplification 504 literature that capturing and parameterising these structures is critical towards reproducing 505 the behaviour of the real network (Thrysøe et al., 2019; Dobson et al., 2022). However, 506 SWMManywhere currently does not attempt to estimate the locations or hydraulic properties 507 of any such structures. We acknowledge that this could be a significant limitation and hope 508 to add this behaviour in future work. In this paper, we replace the hydraulic structures and 509 storage nodes in the real models with simple and uniform nodes to better assess the 510 SWMManywhere workflow as designed. Furthermore, the hydraulic properties of sub-511 catchments (specifically, the Manning's roughness coefficient and depression storage of 512 both impervious and pervious areas) are a significant source of uncertainty and typically 513 calibrated or set arbitrarily (Deletic et al., 2012), thus we set these at the same values for all 514 networks to ensure comparability.

515 The precipitation event we use to demonstrate SWMManywhere is the largest storm in the 516 openly available Bellinge data (Pedersen et al., 2021).

517 Workflow evaluations were performed on the Imperial College High Performance Computing 518 facilities (see Acknowledgements). Hardware used was typically AMD EPYC 7742 (128 519 cores, 1TB RAM per node), although this varied based on availability. On one of these 520 machines, for a single workflow evaluation in the Cran Brook case study, downloading and 521 data preprocessing takes ten seconds (except for buildings, which are national datasets and 522 so download speeds will vary significantly depending on the country), evaluating graph 523 functions and writing the UDM to SWMM format takes around two minutes (deriving sub-524 catchments and deriving network topology are the slowest individual steps at 20 seconds 525 each), simulation in SWMM takes eight minutes, and evaluating metrics takes two minutes 526 (dominated by the K-S test for node betweenness, mKN which took over one minute). Run 527 times for all Bellinge case studies were dramatically quicker owing to the far smaller UDM 528 sizes.

529 The code used to perform this experiment and results required to reproduce the figure 530 results in Section 4 are openly shared in a separate repository (Dobson et al., 2024b).

# 531 4 Results

#### 532 4.1 Proof-of-concept examination

We focus this section on a synthesised model selected from our sensitivity analysis sampling (Section 4.2) that performed well across a range of metrics to assess SWMManywhere's ability to generate a high-quality UDM and raise methodological points of interest. Figure 4 plots a flow and flooding timeseries and diameter, elevation, slope, and travel time distributions for the Cran Brook network to provide a detailed comparison of the real and synthetic UDM.

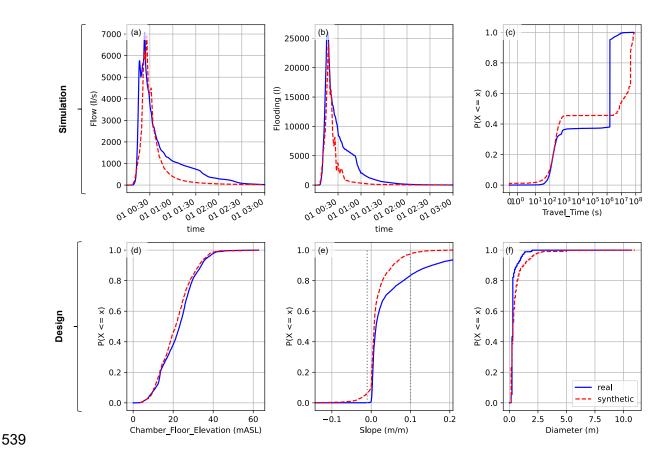


Figure 4: Demonstration plot of a high performance synthetic UDM. Red dashed lines represent synthetic data,
while solid blue represents the real UDM simulations. Grey lines on the slope plot (e) show the target design
range.

543 Figure 4a shows flow at the network outfall, while Figure 4b shows the total flooded volume 544 across the network. We see that the maximum values of both are captured with accuracy, however, the falling limb for both recedes more quickly in the synthetic network than in the 545 546 real UDM simulations. The synthetic network has consistently larger diameters (Figure 4f) 547 than the real, while chamber floor elevations (Figure 4d) are well matched. Synthetic pipe 548 slopes (Figure 4e) are lower, although we observe that these are primarily within the grey 549 dashed lines which show the target design range (Chahinian et al., 2019). The average 550 travel time from each node to the outfall (Figure 4c) shows distinctively different patterns 551 across the distribution, with a good match for the quickest third of nodes, the synthetic UDM 552 quicker for the middle third (because of the larger diameters), and the real UDM quicker for 553 the slowest third. Although not shown, the total runoff from manhole sub-catchments in both

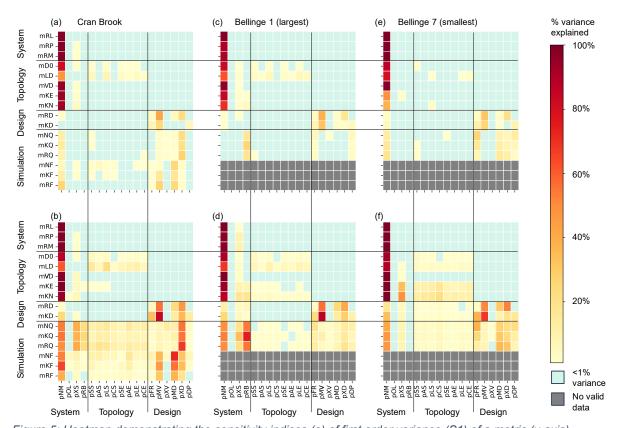
the real and synthetic models is within 2% of each other, which is true for all synthesisedUDMs.

556 4.2 Sensitivity analysis, Cran Brook

557 SWMManywhere parameters, see Table 1, were sampled using a Sobol sampling scheme,

see Section 2.2, to enable a global sensitivity analysis using the Sobol method. The findings

- of this analysis for Cran Brook, the sensitivity indices, are presented in Figure 5a-b. Two
- other locations (Figure 5 c-f) are discussed in Section 4.2, with other locations in full
- 561 presented in Supplemental Figure S1.



562 563 564 565 566 567 568

Figure 5: Heatmap demonstrating the sensitivity indices (a) of first order variance (S1) of a metric (y-axis) attributable to a parameter (x-axis) based on simulations in the Cran Brook network, (b) of total variance (ST) attributable to a parameter based on simulations in the Cran Brook network. Red indicates more sensitive and yellow less sensitive. Blue indicates less than 1% variance explained. (c, d, e, f), shows equivalent of (a) and (b) respectively, but for the Bellinge 1 and Bellinge 7 networks. Grey indicates no sensitivity indices could be calculated because no flooding occurred.

- 569 In Figure 5 we show the first order variance (S1) of each metric (as listed in Table 2)
- 570 attributable to each parameter (Figure 5a), and the total variance (ST) attributable (Figure
- 571 5b). We see that sensitivity is widespread, with every parameter exhibiting at a total variance
- 572 attributable of >1% for at least one metric. We also see that sensitivity is overwhelmingly

573 occurring through interactions (i.e., sensitivities present in Figure 5b but not in Figure 5a), 574 with some notable exceptions: *node merge distance (pNM), minimum velocity (pMV),* 575 *minimum* (pMD) and *maximum chamber depth (pXD)*. First order sensitivity indicates that 576 the parameter is sensitive regardless of other parameter values, *pMV* and *pNM* are evidently 577 dominant in their influence on pipe design while *pNM* is discussed below. Second order 578 variance indices were also calculated, but not included because their confidence intervals 579 were prohibitively large.

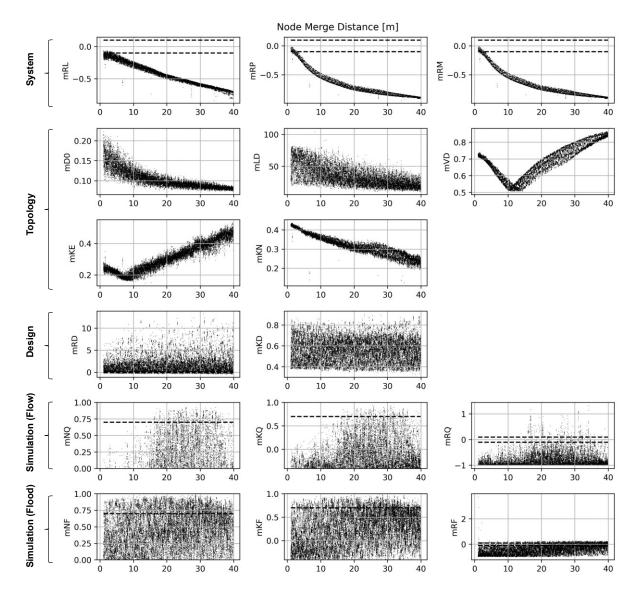
Across metrics the *node merge distance* is the most sensitive parameter, impacting both system description metrics (top rows), topology metrics (middle rows), and simulation metrics (bottom rows). It is a sensitive parameter because it interacts with three key elements in SWMManywhere:

- It influences manhole placement, which is also impacted by *max street length* (*pXS*,
  another sensitive parameter).
- It impacts which nodes can drain to where, which is also impacted by *river buffer distance* (*pRB*, another sensitive parameter).

It can significantly alter how the road layout is translated into potential pipes, which
 no other parameter does. For example, two adjacent roads running parallel may not
 have a driving connection between them, and thus no potential pipe may span them,
 but if these nodes are merged then a pipe could span them.

592 In addition to the dominance of these three parameters (node merge distance, max street 593 *length* and *river buffer distance*), we see many other intuitively appropriate sensitivities. 594 System metrics are sensitive to system parameters, topological metrics to topological 595 parameters, and design metrics to design parameters. We also find that flow simulation 596 metrics are sensitive to parameters relating to network topology, indicating that topology is 597 primarily influencing the global behaviour of the UDM. In contrast, we see that flood 598 simulation metrics are more sensitive to design parameters, indicating that design is 599 primarily influencing the local behaviour of the UDM.

We provide a specific examination of *node merge distance*, selected because it is the most sensitive parameter, to illustrate how SWMManywhere can be used to provide a detailed parametric exploration. We plot the parameter value of *node merge distance* against each metric value for all sampled points in Figure 6. We see clear evidence of first order sensitivity in line with those reported in Figure 5a-b.



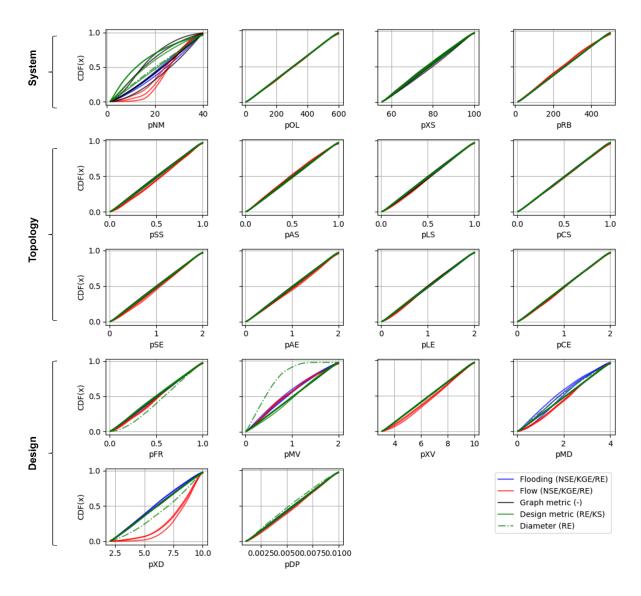
605

Figure 6: Node merge distance parameter value plotted against all evaluated performance metrics. Based on simulations in the Cran Brook network. Panels showing NSE or KGE are clipped at 0.0 and -0.41 respectively, which indicates the performance of taking the mean value of observations as the simulation. Dashed lines for KGE, NSE, relative error indicate a region of 'behavioural' performance, that is, values >0.7 (KGE, NSE) or within +/- 0.1 (relative error).

Figure 6 indicates some evidence of identifiable parameter values, e.g., we observe that the

612 node merge distance should fall around 25m for the simulation flow metrics. However, this

- value can vary depending on which metric is used, for example, System metrics (*mRL*, *mRP*,
  and *mRM*) and some topology metrics (*mVD*, *mKE*, *mKN*) indicate better performance when *node merge distance* is around 0-15m.
- 616 It can be more informative to investigate whether parameters are identifiable using a
- 617 Gaussian kernel density estimate (KDE), which can be used to create a cumulative density
- 618 function for each parameter and can be weighted by different metrics. For example, in Figure
- 619 7, top left panel (*pNM*), weighting the KDE by flow simulations (red lines), we can see that
- 620 75% of the distribution indicates that *node merge distance* should be greater than 20m,
- agreeing with Figure 6. The KDE plots further highlight identifiability for a range of other
- 622 parameters, however, as with *node merge distance*, in most cases there can be
- 623 disagreement depending on which metric is used for weighting.



624

625 Figure 7: Gaussian KDE cumulative density functions for parameters, weighted by different metrics evaluated on 626 the Cran Brook network. Metrics are grouped by colour to highlight different behaviours.

- 627 4.3 Sensitivity analysis, other locations
- In Figure 5 c-f we show the sensitivity analysis results for the Bellinge 1 and 7 networks,
- 629 which are the largest and smallest networks in the Bellinge dataset, respectively. Results for
- the other Bellinge UDMs are shown in Supplemental Figure S1, although do not
- 631 meaningfully differ from the observations below.
- 632 In general, we see many similarities between the two analyses, including high sensitivity of
- 633 *node merge distance*, more sensitivity occurring through interactions (Figure 5 c and e) than
- 634 in first order (Figure 5 d and f). In contrast, we see less significance of network topology
- 635 parameters across all metrics, which we can likely be attributed to smaller sizes of both

Bellinge networks are comparing to the Cran Brook network resulting in availability of fewer
topological configurations, thus less significance in terms of impacting metrics. We note that
no indices for flooding metrics could be calculated because the network did not experience
flooding under the precipitation timeseries used.

640 In Figure 8 we show the KDE estimates of parameter distributions for each network,

641 weighted by the NSE flow metric (*mNQ*). In contrast to Figure 7, we see stronger agreement

642 across networks than across metrics for weighting. For example, *max fr (pXF), precipitation* 

643 (*pDP*), max depth (*pXD*), tend towards aligned parameter distributions across most

644 networks. Despite this, we also see some sensitive parameters with less agreement across

645 networks. For example, *min v (pMV), max street length (pXS),* and *node merge distance* 

646 (*pNM*) have unaligned but identifiable parameter values. We also see that many parameters

647 do not have clearly defined distributions for most networks but do for one/few. For example,

648 *river buffer distance* appears to have a clearly defined distribution for Cran Brook and

649 Bellinge 2, while no other networks do. We do not see clear parameter distributions for

650 network topology parameters, despite their sensitivity demonstrated in Figure 5.

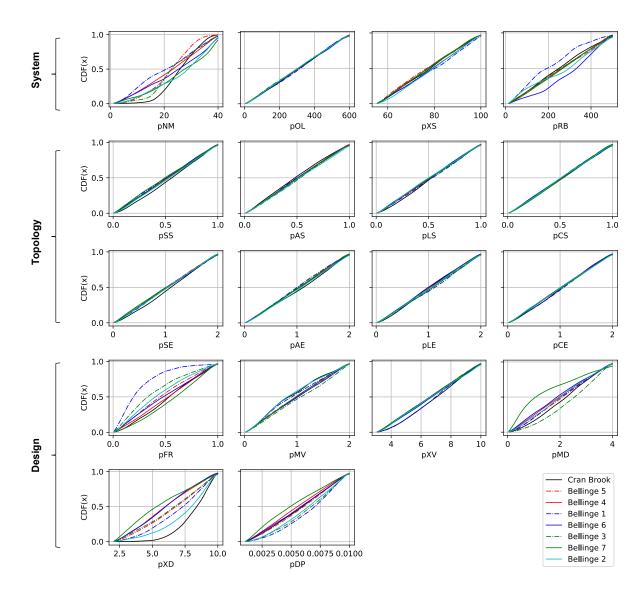


Figure 8: Gaussian KDE cumulative density function for parameters for each location. Weighted by outfall flow
 NSE.

- 654 **5 Discussion**
- 655 5.1 Development of SWMManywhere
- In this study, we provide new insight into the intricacies of UDM synthesis through
- application of our proposed SWMManywhere workflow and performing extensive sensitivityanalysis.
- 659 We demonstrate in Figure 4 that reasonable simulations are achievable, with NSE values of
- >0.7 for both outfall flow and flooding, Figure 6. The implementation based on Duque et. al.,
- 661 (2022)'s pipe-by-pipe method results in high efficiency UDMs, although we observe that the

synthesised UDMs are perhaps too efficient as they drain the network too quickly, see flow and flood simulations in Figure 4. This finding suggests that inefficiencies seen in the real network reflect the additional constraints not captured by data sources that we employ in our workflow, for example, incremental construction of the network (Rauch et al., 2017). Despite such shortcomings, we recommend that sensitivity analysis is a necessary precursor to introducing any further complexity.

668 The sensitivity analysis results, Figure 5, show widespread and intuitively sensible sensitivity 669 of all parameters, including those introduced as technical innovations of this paper: enabling 670 slope inclusion within the MSA and contributing area as a factor in the network topology 671 derivation (pSS, pCS, pSE, pCE). We also highlight the dominant sensitivity of node merge 672 distance (pNM), which influences manhole locations, outfall locations, and underlying street 673 graph preprocessing. Manhole locations are well established to be important factors 674 (Chahinian et al., 2019; Blumensaat et al., 2012), while to our knowledge this is the first 675 UDM synthesis study that treats outfall locations as an explicit unknown. The importance of 676 the underlying street graph that *node merge distance* controls is intuitively sensible, as a 677 UDM synthesis can only ever be as good as the potential pipe-carrying locations that it 678 begins with. These findings indicate a promising outlook for UDM synthesis, as manhole 679 locations, outfall locations, and the street graph are all surface elements whose estimation 680 will only improve with improved satellite imagery and machine learning. Furthermore, in 681 cases where SWMManywhere is to be applied to a local area, surveying these surface 682 elements is likely to be far less costly than a below-ground network survey.

683 5.2 Transferability of SWMManywhere

A key motivation for performing sensitivity analysis is in identifying behavioural parameter ranges. In an ideal case, behavioural parameter ranges align across metrics and locations, thus implying that parameter choices are good under any condition. Figure 7 and Figure 8 demonstrate that we do not see clear evidence of this for either metrics or locations respectively. Figure 5 demonstrates that parameters are generally sensitive through

689 interactions, rather than through first order effects, which limits the ability to provide clear 690 advice on behavioural ranges. Although second order effects were calculated, the 691 confidence intervals were such that no conclusions could be drawn, and we estimate that 692 multiple magnitudes more samples would be required to provide definitive results, which is 693 outside the scope of this paper, but future work may investigate. Parameters that have high 694 first order sensitivity provide some clear advice, for example, node merge distance values 695 should be between 20m-35m to provide good flow simulation metrics in a variety of 696 locations. However, the dominant finding on parameter transferability is that the panacea of 697 arriving to a single 'correct' UDM through a synthesis approach is false. Indeed, we believe 698 that widespread findings of equifinality in hydraulic calibration of real UDMs, (Huang et al., 699 2022; Sytsma et al., 2022) supports that the idea of having a single 'correct' UDM that is 700 based on survey information (rather than synthesis) is also false. We propose that data 701 uncertainty will remain a fundamental element of UDM, synthetic or otherwise, for the 702 foreseeable future.

703 We therefore advocate for an approach to UDM that is uncertainty driven. Rather than 704 narrowly focussing on aligning synthetic with real UDMs, a synthetic UDM may most 705 appropriately be considered one hypothesis for the underlying system. Further 706 developments to SWMManywhere should thus seek to synthesise UDMs that are plausible 707 hypotheses, possibly through a more iterative approach that refines the UDM based on 708 simulation data only, for example, by assessing SWMM continuity errors. In a no field data 709 setting, the focus could shift to, for example, various climate scenarios or future urban 710 development, to study an ensemble of plausible UDMs and explore their likely outcomes. If 711 such studies would prohibitively increase simulation time, a range of network complexity 712 reduction techniques have been demonstrated for UDMs (Farina et al., 2023; Palmitessa et 713 al., 2022), including as part of an uncertainty ensemble approach (Dobson et al., 2022; 714 Thrysøe et al., 2019).

715 To ensure that our proposed workflow is applicable at the global scale, we have deliberately 716 avoided some data, for example design regulations or a higher resolution DEM, that are 717 commonly available at national scales. In local applications, however, we do recommend 718 exploring utilising the best quality data available and adapting the underlying datasets or 719 parameter assumptions, which our SWMManywhere implementation supports. Nevertheless, 720 we caution that this may not provide the certainty that one might expect. For example, as our 721 KDE parameter estimates demonstrate in Bellinge, Denmark (Figure 8), design regulations, 722 which are parameters that are country and region specific, do not show agreement across 723 UDMs in the same locale.

724 5.3 Outlook and limitations

725 The modular graph function-based architecture of SWMManywhere makes it easy to extend 726 or customise, thus we hope that it may become a centralised location for the synthetic UDM 727 community. We see a variety of potential improvements that may be introduced to increase 728 the realism of synthesised UDMs, although we stress the importance of performing 729 sensitivity analysis before investing time in creating complicated customisations. In addition 730 to better identification of surface elements described above, other surface factors such as 731 hydraulic structures are well established to play a dominant role in UDM behaviour (Thrysøe 732 et al., 2019; Dobson et al., 2022). SWMManywhere does not attempt to synthesise these 733 structures, and they are omitted from the analysis performed in this paper. However, 734 structures such as weirs may be identifiable from satellite imagery, while including pumps 735 may form an additional element in the network topology derivation, as has been 736 demonstrated for sanitary sewer networks (Khurelbaatar et al., 2021). 737 An immediate extension to the behaviour of SWMManywhere that we are exploring is 738 around water quality. Recent literature demonstrates the feasibility of quantifying urban 739 pollution deposition on roads (Revitt et al., 2022), which could be included as an optional 740 extension, thus providing the much-needed transport element to link deposition with in-river 741 pollution. We anticipate that a key difficulty of such an approach would be in identifying

742 validation data, since sampling water quality at urban drainage outfalls during a storm is 743 dangerous to do in person. For example, while the English Environment Agency's 744 harmonised water quality sampling database contains over 60 million pollution sample 745 records since 2000 (Open water quality archive datasets (WIMS), 2024), just 0.4% are of 746 urban drainage outfalls, and only 25% of these have occurred since 2010, reflecting the 747 diminishing focus on non-compliance monitoring observed across England (Dobson et al., 748 2021). Further improvements towards capturing water quality may also focus on 749 representing combined or misconnected systems, linking with the synthetic sanitary sewer 750 network literature (Duque et al., 2022).

751 A clear limitation of the case studies demonstrated in this paper is that they are based in 752 temperate and wealthy European countries, this is particularly problematic when considering 753 that street graph and building footprint data uncertainty will be more significant in nearly any 754 other type of region. We reached out to a variety of urban drainage modellers in both 755 industry and research but were not able to extend our case study selection further and 756 instead identified a significant paucity of publicly available reliable SWMM models. While the 757 SWMM website hosts a variety of useful example models, these aim to build understanding 758 about representing different elements of drainage networks, rather than providing a suite of 759 real test cases. Ultimately, SWMManywhere and other synthetic UDM tools will not be 760 trusted at global scales until they have been demonstrated on a wide variety of case studies. 761 Thus, we call for collaborators who can either share their SWMM models openly or are 762 willing to demonstrate SWMManywhere for their models to reach out that we may create a 763 more robust demonstration of UDM synthesis and verify that understandings created are 764 sustainable.

## 765 6 Conclusion

In this paper we present a workflow, SWMManywhere, that can synthesise an urban
drainage network model (UDM) and simulate it in SWMM, anywhere globally. We test the

parameters of SWMManywhere using sensitivity analysis to understand the dominant
 processes involved in synthesising UDMs. Our results revealed three key findings:

The SWMManywhere workflow can synthesize high quality UDM at a range of spatial
 scales. The parameters that can be used to tune SWMManywhere behave in
 intuitively sensible ways, verifying its implementation.

- We find that parameters controlling surface elements such as manhole locations,
  street layout, and network outfalls are the most sensitive, and thus should be the key
  focus of uncertainty reduction. Encouragingly, the identification of these elements is
  also the most likely to improve in the foreseeable future.
- 3. UDM synthesis is sensitive to all parameters and these parameters primarily
- influence outputs through second order or higher interactions, revealing UDM
- synthesis to be a more complex process than previously recognised. Additionally, we
- recommend that an ensemble approach would be appropriate for practical
- applications to more appropriately reflect the inherent uncertainty of the underlyingsystem.

We hope that the urban drainage community will use SWMManywhere to further explore the
complexity of UDM synthesis, develop robust interventions in areas without existing UDM
data, and do so in a more open and reproducible scientific environment.

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#### 799 8 Data availability statement

- 800 The software implementation of SWMManywhere is an open-source repository available at
- 801 https://github.com/ImperialCollegeLondon/SWMManywhere (last accessed 2024-10-11). The
- 802 documentation for SWMManywhere can be found at
- 803 https://imperialcollegelondon.github.io/SWMManywhere/ (last accessed 2024-10-11). The
- 804 results of the paper's experiments and code to perform sensitivity analysis and plots is
- 805 available at https://github.com/barneydobson/swmmanywhere paper (last accessed 2024-
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