SWMManywhere: A Global-scale Workflow for Generation and Sensitivity Analysis of Synthetic Urban Drainage Models

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11 Statement

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- 14 of this manuscript may have slightly different content. If accepted, the final version of this
- 15 manuscript will be available via the 'Peer-reviewed Publication DOI' link on the right-hand
- 16 side of this webpage.

17 Highlights

- SWMManywhere can synthesise an urban drainage network model anywhere in the
 world
- SWMManywhere is a parameterised approach for customising the synthesised
 network
- 22 We use sensitivity analysis to investigate uncertainty of network synthesis
- We find significant interaction between parameters, suggesting an ensemble
 approach
- 25 Parameters controlling surface observable network elements are most sensitive

26 Abstract

27 Continual improvements in publicly available global geospatial datasets provide an 28 opportunity for deriving urban drainage networks and simulation models of these networks 29 (UDMs) worldwide. We present SWMManywhere, which leverages such datasets for 30 generating synthetic UDMs and creating a Storm Water Management Model for any urban 31 area globally. SWMManywhere's highly modular and parameterised approach enables 32 significant customisation to explore hydraulicly feasible network configurations. Key novelties 33 of our workflow are in network topology derivation that accounts for combined effects of 34 impervious area and pipe slope. We assess SWMManywhere by comparing pluvial flooding, 35 drainage network outflows, and design with known networks. The results demonstrate high 36 quality simulations are achievable with a synthetic approach even for large networks. Our 37 extensive sensitivity analysis shows that the locations of manholes, outfalls, and underlying street network are the most sensitive parameters. We find widespread sensitivity across all 38 39 parameters without clearly defined values that they should take, thus, recommending an 40 uncertainty driven approach to synthetic drainage network modelling. This study showcases 41 significant potential of SWMManywhere for research and industry applications to provide 42 drainage network models in urban areas where traditional approaches are impractical.

43 **1** Introduction

44 Urban drainage models (UDMs) are representations of land and pipes that can be simulated 45 with hydraulic models such as Storm Water Management Model (SWMM) (Rossman, 2010). 46 UDMs are essential for managing stormwater, preventing flooding, and ensuring the 47 sustainability of urban water systems (Butler and Davies, 2004). UDM simulations capture 48 the behaviour of drainage networks under various rainfall scenarios, enabling planners to 49 design effective infrastructure and mitigate risks (Bach et al., 2014). However, the 50 development of UDMs typically requires extensive infrastructure records on the connectivity. 51 geometric properties, and elevations of underground pipes (Bach et al., 2020; Chahinian et 52 al., 2019). In cases where these records are unavailable, whether due to ownership issues 53 or simply that they do not exist, the expense of creating a UDM becomes significant because 54 of costly surveying requirements. To forgo this expense, it may be preferrable to synthesise 55 a UDM based on the underlying information governing the placement and sizing of drainage 56 pipes, most generally, surface elevation, building locations, and road locations (Chegini and 57 Li, 2022).

58 The earliest methods to create synthetic UDM exploited the fractal nature of a drainage 59 network and, while simulations were not tested, demonstrated that the broad statistical 60 properties of the network, i.e., distribution of flow path lengths, could be estimated (Ghosh et 61 al., 2006). When road network and elevation data were incorporated, the accuracy of 62 synthesised UDMs improved and simulations approached those of a real UDM for the same 63 locale (Blumensaat et al., 2012). Generally, UDM synthesis involves three main tasks: 64 delineating surface characteristics, deriving network topology, and hydraulic design, each of 65 which will be reviewed below.

First, surface characteristics, hereafter referred to as sub-catchments, quantify the spatial
distribution of stormwater drainage from impervious areas to manholes. Sub-catchment
delineation has received the least attention in UDM synthesis literature and most commonly
follows a watershed delineation approach (Blumensaat et al., 2012; Warsta et al., 2017). The

70 drained impervious area within a delineated sub-catchment is typically calculated from the 71 area covered by roads and buildings (Mair et al., 2017; Chegini and Li, 2022). However, 72 another simpler method is to assign impervious areas to drain to a nearest manhole (Reyes-73 Silva et al., 2023). Both methods require identification of manholes, highlighted as critical 74 future work in Blumensaat et al., (2012), but has received little attention since (Bertsch et al., 75 2017; Chahinian et al., 2019). We place sub-catchment delineation and manhole 76 identification as the first tasks to perform during UDM synthesis, since network topology and 77 hydraulic design should account for the impervious area contributing to a given pipe.

78 Second, network topology describes the spatial layout of a UDM, connectivity of pipes, and 79 connectivity of the sub-catchments to UDM, i.e., through manholes. Network topology is 80 typically derived by asserting that pipes follow roads, thus dramatically reducing the 81 dimensionality of deriving network topology (Mair et al., 2017; Xu et al., 2021). An efficient 82 network that visits all manholes without redundant pipes can be derived using a shortest 83 path-based algorithm. This algorithm minimizes the total graph cost, with each edge (i.e., a 84 plausible pipe) assigned an individual cost that represents some penalty associated with 85 retaining that edge. Chahinian et al. (2019) provide a detailed exploration minimising costs 86 based on pipe length, pipe adjacent angle, and slope, and highlighting the importance of 87 slope as a cost. Reyes-Silva et al. (2023) derive the UDM by applying the minimum 88 spanning tree (MST) to a full street network to minimise the number of pipes. This approach, 89 however, does not inherently consider slope in the deriving network topology step since MST 90 is only applicable to undirected networks, instead gravitational slope along pipes is enforced 91 as a postprocessing correction. A minimum spanning arborescence is an alternative 92 approach to solve such a problem for a directed network (Ray and Sen, 2024; Tarjan, 1977), 93 although has not yet been demonstrated in UDM synthesis. Furthermore, an additional cost 94 to be minimised that has not been tested in the literature is the need to minimise the impervious contributing area to a given pipe and thus more evenly distribute flow throughout 95

96 the network, much in the manner of the original proposed fractals for network topology97 (Ghosh et al., 2006).

98 Third, hydraulic design refers to the selection of pipe diameter, invert levels, and other pipe 99 hydraulic parameters in a synthetic UDM, which typically follows local standards (Chegini 100 and Li, 2022; Duque et al., 2022; Reyes-Silva et al., 2023). Duque et al. (2022), present a 101 methodology for designing sanitary sewer networks by starting from the most upstream 102 pipes, iteratively working downstream, and designing each pipe by minimising the costs 103 subject to the feasibility of design constraints; such an approach could be equally valid for a 104 UDM. In cases where the impervious contributing area of a given pipe has been 105 synthesised, a Rational Method could be applied for determining pipe size. A variety of more 106 extensive global optimisation methods exist for hydraulic design to both minimise costs (e.g., 107 Sun et al., (2011)), or calibrate to observations (e.g., Huang et al., (2022); Sytsma et al., 108 (2022)). However, these calibration studies highlight the inherent equifinality in parameter 109 selection, thus suggesting the uncertainties in such a high dimensionality problem may 110 outweigh any 'optimal' algorithm.

Because UDM synthesis requires a hydraulic design, equifinality must also be inherent to UDM synthesis. We argue that this has been under-recognised in existing UDM synthesis, primarily because of a lack of data and the absence of an automated, end-to-end workflow to assess the impact of parameter selection. A reader may observe results from the supplement of Duque et al., (2022), which demonstrates that small changes in their grid scale for the synthesis algorithm can generate dramatically different sanitary sewer networks.

An equally valid line of inquiry is, therefore, to examine UDM synthesis with sensitivity analysis to quantify the importance of various factors in generating more realistic networks (Pianosi et al., (2016). Sensitivity analysis provides verification by revealing ranges of 'behavioural' parameter values that produce acceptable model outputs, thus informing application of UDM synthesis in data-sparse regions. Additionally, it reveals the dominant

123 controls and key processes governing UDM synthesis by quantifying the relative importance 124 of different parameters. In turn, revealing where uncertainty reduction may be most 125 beneficial. We do not assume that accurate UDM synthesis is possible in every location 126 using solely building, road, and elevation data, particularly given the complexities involved in 127 the gradual expansion of a UDM (Rauch et al., 2017). However, it is impractical to improve 128 UDM synthesis by capturing every possible element involved in network evolution. Instead, 129 sensitivity analysis provides an objective way to guide improvement; prioritising 130 measurements and processes that relate to the most sensitive parameters.

131 Continual improvements in development and accessibility of remote sensing and open 132 geospatial data at global scale facilitates applicability of UDM synthesis in many locations. 133 Chegini et al., (2022), demonstrate an approach that can perform network topology and the 134 dimensioning part of hydraulic design anywhere in the continental United States. Montalvo et 135 al., (2024) implement the UDM synthesis algorithm presented by Reyes-Silva et al., (2023), 136 in a GIS tool, however this approach does not acquire/process the necessary geospatial 137 data nor is it open-source at time of writing. We believe that a global tool, that is open-138 source, and tailored to accommodate the uncertainty inherent in the UDM synthesis problem 139 would be of great value to the urban drainage community. Such a tool would enable 140 hydrodynamic method developers to bypass the reproducibility crisis (Stagge et al., 2019; 141 Hutton et al., 2016), by demonstrating their tools on an unlimited suite of UDMs synthesised 142 in cities worldwide, improving on the entirely theoretical test suites that presently exist 143 (Möderl et al., 2011, 2009; Sweetapple et al., 2018). Furthermore, it would contribute 144 towards better representation of urban environments in the regional hydrological cycle, 145 which is a critical and under-represented component of such applications (Coxon et al., 146 2024).

In this paper we present a workflow, called SWMManywhere, to synthesise UDMs anywhere
in the world. We show its versatility by applying it to multiple case studies (i.e. sewer
systems of different sizes in two different countries) and to facilitate its global usage we

150 deploy it as an open-source Python tool (Dobson et al., 2024a) with extensive 151 documentation (SWMManywhere documentation, 2024). SWMManywhere provides a 152 parameterised and easy to customise approach for UDM synthesis which allows us to perform sensitivity analysis of synthesised UDMs. We ensure SWMManywhere responds to 153 154 the need for worldwide application by using open global datasets and including the retrieval and preprocessing of these datasets as part of the algorithm. The methods implemented in 155 156 SWMManywhere also include a variety of technical novelties in the field of UDM synthesis, 157 including use of a minimum spanning arborescence to derive topology, enabling 158 minimisation of contributing area during this process, and implementing Duque et al., 159 (2022)'s pipe-by-pipe design method for urban drainage networks.

160 2 Methodology

161 A high-level overview of our proposed SWMManywhere workflow is shown in Figure 1.



163 Figure 1: Overview of the SWMManywhere workflow.

164 We present an end-to-end workflow for UDM synthesis and comparison against a real UDM, if available, anywhere in the world. A key barrier to UDM synthesis identified in literature is 165 166 difficulty in setting up a hydraulicly correct model, thus we specify data acquisition and 167 preprocessing in the workflow. The 'generate hydraulic model' step, is the key step that 168 should ultimately create sub-catchments, a network topology, and hydraulic designs of pipes 169 that together fully describe the synthesised drainage network. Such a drainage network, i.e., 170 the synthetic UDM, will be valid for simulation in a widely used software for design and 171 analysis of drainage networks, such as SWMM, enabling studying different precipitation 172 events and inspecting state variables such as pipe flows and pluvial flooding. In Section 2.1, 173 we describe the theory and processes in our workflow, also explaining how it can be 174 customised with parameter choices and additional processes to vary the nature of the 175 synthesised UDM.

176 A key hypothesis that must underlie any synthetic UDM approach is that results may be valid 177 in places where a real UDM is not available or not trusted. Because we observed the 178 sensitivity to parameter selection in previous UDM synthesis literature, we intentionally 179 specify SWMManywhere to be highly parameterised and customisable. We use sensitivity 180 analysis on these parameters to demonstrate how they impact synthesised networks. In 181 Section 2.2, we describe how sensitivity analysis can guide the use of SWMManywhere in 182 areas where parameters cannot be estimated a priori based on field data and provide a 183 deeper understanding of UDM synthesis. We apply this analysis to eight UDMs in two 184 different locations.

185 We discuss UDM synthesis using graph theory terminology:

A graph represents the UDM, consisting of nodes (manholes) that are connected by
 edges (pipes). The graph can be either undirected or directed, indicating that
 connections are between two nodes (undirected) or from one node to another
 (directed). Pipes are undirected since head may drive uphill flow, however, treating

the graph as directed enables better description of preferential flow paths and is also
the format required by SWMM, SWMManywhere makes use of both directed and
undirected graphs.

In graph theory, a subgraph refers to a sub-selection of the graph and is called a
 connected component if every node is in the subgraph reachable from every other
 node within that subgraph. Connected components are used in SWMManywhere to
 describe a collection of manholes and pipes that drain to a common outfall.

The topology of the graph captures the overall arrangement and relationships of 197 198 nodes and edges and can be thought of as the pipe layout in a UDM. The edges can 199 have costs, for example length, which may be minimised by shortest path algorithms 200 to minimise flow routes. Flow routes should be minimised in any drainage network to 201 drain the catchment as efficiently as possible, preventing the accumulation of water 202 and flooding of manholes. A minimum spanning tree is a subgraph that connects all 203 nodes with the minimum possible total edge cost for an undirected graph, a minimum 204 spanning arborescence is the same for a directed graph, thus these represent the 205 most cost-efficient pipe layouts that may exist for a given area. We will refer to a 206 graph of potential pipe-carrying edges as the street graph, while the optimised layout 207 is the UDM topology.

208 2.1 SWMManywhere

209 2.1.1 Data and preparation

Our SWMManywhere approach uses datasets that are of sufficient level of detail to be used in global application: road locations, river locations, elevation, and building footprints. We stress that these datasets, in particular road locations and building footprints, vary in quality from location to location, thus, the downloaded data for a given case study should always be inspected carefully. Additionally, we enable manually sourced, higher quality data for input, if available, as described in the online documentation (SWMManywhere documentation,

- 216 2024). The default datasets are visualised for one of our case studies in Figure 2, and
- 217 described in further detail in this section.



218

219 Figure 2: Visualisation of downloaded data in the Cran Brook, UK. See main text for citations.

Assuming pipes can only exist in pre-specified plausible locations will dramatically reduce the dimensionality of the shortest-path UDM topology derivation. Thus, we assume that pipes can only exist in certain locations, typically streets due to the common validity of this assumption (Mair et al., 2017). In addition, paved streets constitute one of the key impervious surfaces which must be drained in a UDM. Rivers are also downloaded as these are potential outfall locations of the drainage network, described in further detail in Section

²²⁰ Streets and rivers

227 2.1.2. OpenStreetMap (OSM) provides street and river data worldwide and is used in this228 study.

229 Impervious areas

230 To calculate the impervious area of a sub-catchment, and thus enable runoff generation, we 231 use road locations, their number of lanes, which are contained within OSM, and building 232 footprints. Recent advances in machine learning have enabled identification of building 233 perimeters from high-resolution satellite data worldwide. Two large datasets, provided by 234 Google and by Microsoft, are now combined and available at (Google-Microsoft Open 235 Buildings, 2024). Both datasets use convolutional neural networks to classify pixels as 236 buildings (Tan and Le, 2019; Sirko et al., 2021) and custom methods to polygonise these 237 pixels into buildings (Sirko et al., 2021; Computer generated building footprints for the United 238 States, 2024). The authors would note that, although global, this dataset has varying quality 239 in different regions due to the nature of the training data that was used and resolution of 240 satellite imagery. Although other impervious surfaces besides roads and buildings, such as 241 car parks, that must be drained in a UDM are common, we could not identify global datasets describing these, and thus consider them currently outside the scope of this study. 242

243 Elevation

Elevation data, in the format of a Digital Elevation Model (DEM), is essential to delineate manhole sub-catchments, to calculate the slope along edges, and to identify if there are paths in the street graph that should not be ignored, for example, those at that span different hydrological catchments. We use NASADEM, which is a publicly available radar-based global DEM at 30m resolution (Crippen et al., 2016), from Microsoft Planetary Computer (Source et al., 2022). Although higher resolutions around 2m are recommended for UDM (Arrighi and Campo, 2019), such datasets do not yet exist openly at global scales.

251 2.1.2 Pipe network generation

A key innovation of our approach is to iteratively process a street graph and gradually
transform it into a UDM with full hydraulic design. These processes must take a graph and
return a graph. The key tasks that they perform are summarised in Figure 3, discussed
further in this section and used for the experiments in this paper.



- Figure 3: Visualisation of key iterations to the graph as different processes are applied. Catchments (D) are
 coloured by the manhole that they drain to.
- 259 Table 1 lists all tuneable parameters of our proposed workflow, with reasonable default
- 260 values for these parameters and their ranges provided in the online documentation
- 261 (SWMManywhere documentation, 2024). We carry out an extensive sensitivity analysis (see
- 262 Section 2.2) to identify any behavioural ranges of these parameters and identify their relative
- 263 importance in UDM synthesis.

Table 1: SWMManywhere user adjustable parameters that are tested in sensitivity analysis for this work, a full list of parameters is available in the online documentation (SWMManywhere documentation, 2024). If the variable is described differently from its use in the software to improve clarity, the software term is indicated in brackets.

GROUP	VARIABLE	KEY
SYSTEM DESCRIPTION	node merge distance	pNM
(MANHOLES AND OUTFALLS)	outfall length	pOL
	max street length	pXS
	river buffer distance	pRB
TOPOLOGY DERIVATION	chahinian slope scaling	pSS
	chahinian angle scaling	pAS
	length scaling	pLS
	contributing area scaling	pCS
	chahinian slope exponent	pSE
	chahinian angle exponent	pAE
	length exponent	pLE
	contributing area exponent	рСЕ
HYDRAULIC DESIGN	max filling ratio (max fr)	pFR
	min v	рМV
	max v	рХV
	min depth	pMD
	max depth	рХD
	design precipitation (precipitation)	pDP

267

268 Data cleaning and manhole identification

269 As explained in Section 2.1.1, OpenStreetMap (OSM) is the default data source for obtaining 270 street and river graphs. However, the raw OSM data are not directly suitable for UDM 271 generation, so we perform a variety of data cleaning operations to create a more suitable 272 graph for UDM synthesis, as illustrated in Figure 3a-b. The first significant process in data 273 cleaning is enforcing a maximum edge length, splitting edges that are longer than max street 274 length parameter (pXS, Table 1). The second is merging of nodes, which joins nodes 275 together if they are within a specified distance of each other (node merge distance, pNM). 276 These two processes jointly control where manholes are located along edges and the 277 frequency with which they occur. The final significant task in data cleaning is buffering street paths in proportion to the number of lanes to create a shapefile of impervious street area. 278 279 The remainder of processing in this stage is perfunctory, performing tasks such as ensuring 280 consistent geometries, a consistent identification scheme, removing parallel edges, and

converting the directed street graph to an undirected graph (as a pipe may flow in a directionopposite to road travel).

283 Sub-catchment outline and surface characteristics

284 We begin the sub-catchment delineation, by first burning the road network into the DEM of 285 an urban area. This burning process is a common practice in UDM sub-catchment 286 representation (Gironás et al., 2010) and involves lowering the elevation of grid cells in the 287 DEM that contain roads. Then, we hydrologically condition the DEM by breaching 288 depressions (Lindsay, 2016a). Upon conditioning the DEM, we compute the flow direction, 289 using the D8 method (O'Callaghan and Mark, 1984), and slope. Because our workflow 290 includes generation of a SWMM model, a sub-catchment width parameter is required. We 291 follow the approach proposed by InfoWorks (Subcatchment Data Fields (InfoWorks), 2024) 292 to compute the width of a sub-catchment based on the radius of a circle with area equal to 293 the area of the sub-catchment.

294 Outfall identification

295 Another key feature of a UDM is outfall locations. The first step in identifying outfalls requires 296 assessing the topology of the graph to ensure its hydrologic feasibility (Seo and Schmidt, 297 2013; Li and Willems, 2020). To achieve this, we remove edges that cross the boundaries of 298 hydrological catchments (defined as the largest non-overlapping drainage basins in the 299 study region), because these are unlikely to carry a pipe. Then, we identify potential outfall 300 locations by assuming that outfalls may only exist within a specified distance of a river (river buffer distance, pRB). Although other factors such as environmental considerations affect 301 302 selection of the outfall location, in this study, we only account for the vicinity of water bodies. 303 We incorporate the relative construction cost of outfalls in our workflow, by assigning weights 304 to the identified outfall locations based the length of the pipe that connects the network to 305 the river (outfall length, pOL). If no potential outfalls are identified the node with the lowest 306 elevation is used as the outfall. On the other hand, in cases where multiple plausible outfalls

307 are identified, we retain them all at this step and determine the outfall during the network308 topology derivation step.

309 Calculating weights and network topology

The network topology can be derived as a minimisation problem of overall graph cost. This minimisation should start with a graph of potential edges (i.e., the graph up to this point) and return a directed graph that visits all nodes (manholes), minimising overall graph cost, without retaining redundant edges (pipes), which is also referred to as a minimum spanning arborescence (MSA).

315 The first step to take in network topology derivation is to identify how each edge contributes 316 to the overall graph cost. As identified by Chahinian et al., (2019), it is plausible that each of 317 pipe length, pipe slope and pipe adjacent angle (the angle at which two joining pipes meet) 318 are important to consider for minimisation. We further propose that the total contributing area 319 carried by pipes in the derived network should also be minimised. As with *ibid.*, these factors 320 do not necessarily contribute to the overall graph cost symmetrically or proportionally. For 321 example, while both negative slopes and overly steep positive slopes are penalised, the 322 penalisation on negative slopes increases with slope more sharply than for positive slopes, 323 because the former becomes hydraulically impractical more quickly than the latter. It is not 324 apparent which of these factors (slope, angle, area, and length) are more important to 325 minimise than others and so we combine each factor to be varied, as in *ibid*. We deviate 326 from *ibid.* by assigning both a linear and exponential scaling parameter to each factor (rather 327 than solely linear), enabling high customisation of how overall graph cost is calculated (i.e., 328 parameters in the topology derivation group). We calculate each individual factor, apply 329 scaling parameters, and sum these into an overall cost for each edge in the graph, 330 producing a graph such as that visualised in Figure 3e.

The network topology is then derived using an implementation based on the shortest-path
algorithm proposed by Tarjan (1977), to find the MSA of the graph. The algorithm starts from

333 a designated "waste" node that all potential outfall locations are connected to, either directly 334 or through river paths, thus enabling all connected component subgraphs to be handled in a 335 single pass. The algorithm initializes a priority queue with the waste node's incoming edges, 336 sorted by their costs. At each step, the minimum cost edge is extracted from the priority 337 queue. If the node it leads to is not already included in the arborescence being constructed, 338 that node and edge are added to the arborescence. The node is marked with its parent, and 339 any edges incoming to that node are added to the priority queue. This process continues 340 until all nodes are included in the arborescence. The final arborescence represents the UDM 341 network topology, where the selected edges correspond to the pipe segments that must be 342 hydraulically designed.

343 Hydraulic design

Duque et al., (2022), propose a "pipe-by-pipe" method to design sanitary sewer network pipes, the method starts at the most upstream pipes, designing each pipe in terms of diameter and depth under a set of design constraints (see *hydraulic design* group), and continues iterating downstream. They demonstrate that this method is comparable to an optimal dynamic programming-based approach, although is significantly more efficient. We adapt the pipe-by-pipe approach to make it suitable for a SWMManywhere approach:

Rather than deriving the design flow from household waste generation, we use a
 Rational method that calculates the design flow as the entire impervious area in sub catchments upstream of the pipe being designed multiplied by a *design precipitation, pDP,* amount.

Inspection of any large real UDM will commonly reveal pipes travelling in an uphill
 direction, as measured by surface elevation. Wherever possible the pipe's elevation
 will be such that they flow downhill despite the surface elevation, however there is no
 guarantee that any hydraulically feasible design will exist. Because Duque et al.
 (2022) derive network topology using hydrological flow paths a feasible design will
 always exist, however this is not the case for SWMManywhere, which uses streets

for pipe locations and accounts for factors besides slope during network topology
derivation. To accommodate this, we include a surcharge feasibility constraint, which
allows a pipe to be designed for flow under surcharge, provided this is the only way
to reach a feasible hydraulic design.

To provide better performance, we assess all designs for a pipe rather than selecting
 the first feasible design. The selected design first aims to satisfy feasibility
 constraints, and if no feasible design exists, picking the most feasible design. It then

minimises depth, diameter, and excavation cost, as calculated in Duque et al. (2022).

368 The final product is a fully described UDM, complete with sub-catchments and hydraulic 369 designs, thus sufficient to be simulated in software such as SWMM.

370 2.1.3 Measuring effectiveness of UDM synthesis

367

371 The question of 'how realistic is a synthesised UDM' is most sensibly assessed by 372 comparing synthesised results against a real UDM. UDM synthesis in a sensitivity analysis 373 context requires understanding why we see the results that we see. Thus, an extensive suite 374 of allowable performance metrics is provided covering a variety of different measures and 375 variables, see Table 2 for a list of the metrics used in this study. We define metrics that 376 measure performance for different elements of UDM synthesis. System description metrics 377 assess the synthesised UDM in terms of properties that describe infrastructure, topology 378 metrics investigate the layout of the graph, and design metrics assess the derived diameter 379 of pipes. Furthermore, the UDM is simulated in SWMM and thus simulated flow, and flooding 380 can also be compared.

381 Table 2: List of metrics implemented in SWMManywhere

CATEGORY	MEASURE	VARIABLE	KEY
SYSTEM DESCRIPTION	relerror	length	mRL
	relerror	npipes	mRP
	relerror	nmanholes	mRM
TOPOLOGY	deltacon0	-	mD0
	laplacian distance	-	mLD
	vertex edge distance	-	mVD
	kstest	edge betweenness	mKE
	kstest	node betweenness	mKN
DESIGN	relerror	diameter	mRD
	kstest	diameter	mKD
SIMULATION	nse	flow	mNQ
	kge	flow	mKQ
	relerror	flow	mRQ
	nse	flooding	mNF
	kge	flooding	mKF
	relerror	flooding	mRF

Comparing flow and/or flooding simulations is typical in the UDM synthesis literature (Reves-382 383 Silva et al., 2023; Blumensaat et al., 2012). We create a timeseries of total flooded volume to 384 assess flooding simulation performance across the entire network. Meanwhile, flows are 385 assessed at the system outfall, as with (Blumensaat et al., 2012). However, unlike existing literature, which assumes that the outfall locations of the network being synthesised are 386 387 known, we do not make this assumption, as this information is not globally available. 388 Instead, we identify where synthetic manholes fall inside sub-catchments of the real network. 389 From these classified manholes it identifies the most commonly represented outfall, and sub-390 selects only that connected component for comparison purposes.

Because the reasons for performing sensitivity analysis are to understand how parameterschange behaviours in UDM synthesis, the most common measure of performance we use is

the relative error (*relerror* measure in Table 2, equation 1), which is simple to understandand provides directionality in terms of over/under estimation,

$$relerror = \frac{mean(synthetic) - mean(real)}{mean(real)}$$
(1),

where *synthetic* is the synthetic UDM data to be compared against the *real* data. We omit a conventional *time* component of the metric because the same equation can equally be used for timeseries or design properties (such as average diameter) alike. In cases of comparing flow or flooding timeseries, we also include the Nash-Sutcliffe Efficiency and Kling-Gupta Efficiency, because these are commonly used and so will provide users who are familiar with them a more nuanced grasp of the synthetic UDM's performance.

A further set of measures that can be used for synthetic networks are those that test the
topological similarity of the derived vs real network, we implement a variety of those
presented in existing literature (Wills and Meyer, 2020; Chegini and Li, 2022), see *topology*category in Table 2.

405 2.1.4 Implementation

406 SWMManywhere is a highly modular workflow and in this study, we implement it in Python 407 and publish it as an open-source tool (Dobson et al., 2024a). We note that the workflow is 408 general and can be implemented in any other programming language. In our implementation 409 of SWMManywhere the minimal required user input is the bounding box of the target urban 410 area, and all remaining steps Figure 1 are automated. The bounding box should be provided 411 in terms of latitudes and longitudes in WGS 84 geographic coordinate system (EPSG:4326). 412 SWMManywhere will reproject all downloaded data into the Universal Transverse Mercator 413 (UTM) coordinate system. UTM uses a coordinate system with metre as its unit, and thus 414 can provide accurate distance and area calculations in contrast to WGS 84. The UTM is split

into zones and the zone ultimately used in a SWMManywhere run is calculated based on theUTM zone of the bounding box.

417 As we described in Section 2.1.2 the most complex step in the workflow is the pipe network 418 generation, i.e., iteratively applying various graph operations to the initial graph street to 419 generate the final UDM. These operations, referred to in our implementation as graph 420 functions, have a variety of parameters that need to be specified, as listed in Table 1. 421 Considering the importance of graph functions and to accommodate flexibility in applying them, our implementation allows adding, removing, or changing their order without modifying 422 423 the code. Structuring code into graph functions enable easy reuse of code, customisation, 424 and introduction of new processing steps. Graph functions are wrapped in a class for 425 validation, enabling SWMManywhere to identify if a set of graph functions to be applied is 426 valid a priori. Graph functions are stored in a registry object to enable easy access. We 427 provide a description of all graph functions in the documentation online (SWMManywhere 428 documentation, 2024). However, users may also customise the selection and order of graph 429 functions, or create new ones, as described in the online documentation, to fit their 430 requirements.

431 Processes or operations described in Sections 2.1.1 and 2.1.2 that are used by but not432 implemented natively within the tool are described in Table 3.

433 Table 3: List of tools for specific tasks in our SWMManywhere implementation.

DEM CONDITIONING	Whitebox	(Lindsay, 2016b)
FLOW DIRECTION CALCULATIONS	Whitebox	(Lindsay, 2016b)
SUB-CATCHMENT DELINEATION FROM	PyFlwDir	(Eilander, 2022)
FLOW DIRECTIONS		
SUB-CATCHMENT SLOPE	PyFlwDir	(Eilander, 2022)
CALCULATION		
OSM DATA RETRIEVAL	OSMnx	(Boeing, 2017)
GRAPH OPERATIONS	Networkx	(Hagberg et al., 2008)

TASK

SOFTWARE REFERENCE

434

435 To accommodate ease of use for a wide range of users with different levels of programming 436 experience, we provide a command-line interface (CLI) for the software. More experienced 437 users can take advantage of the modularity of SWMManywhere for more advanced 438 customisation of the workflow. The CLI works with a configuration file that enables a user to 439 change parameter values and functionality. The minimal essential requirements that this file 440 must contain are a project name, a base directory, and a bounding box. The configuration 441 file provides a centralised location to perform customisations including changing the 442 selection/ordering of graph functions, changing parameter values (see Table 1), file locations 443 of a real network to compare against (see Section 2.1.3) and which metrics to calculate (see 444 Table 2), a starting graph if not using downloaded street data, and any running settings for 445 the SWMM simulation. A variety of online tutorials explain the procedure to make such 446 customisations.

SWMManywhere provides a capability to write simple SWMM model files (typically with a
.inp file extension) that have been synthesised via the various graph functions used. It also
provides a wrapper of the PySWMM software (McDonnell et al., 2020), which enables calling
the SWMM software and interacting with its simulations from Python. Thus, in addition to the

451 UDM synthesis, writing, running, and calculating metrics if real network information exists452 are carried out during the command line call.

Precipitation data is frequently identified as a critical factor in UDM simulations (OchoaRodriguez et al., 2015), however, there are currently no open global datasets that provide
the high frequency monitoring needed to drive these models and so precipitation must be
user-provided if deviating from the default storm provided as part of the tool.

457 2.2 Sensitivity analysis

458 Sensitivity analysis is used to examine how output variations can be attributed to input 459 variations, typically expressed as sensitivity indices for each model parameter (Pianosi et al., 460 2016). While popular reviews in the environmental sciences define sensitivity analysis as 461 specific to model input/outputs (Saltelli et al., 2008, 2019; Pianosi et al., 2016), it can equally 462 be applied to any generic parameterised workflow, such as SWMManywhere. As defined in 463 Table 1, there are a wide variety of parameters that must be selected, many of which do not 464 have values that could be easily measured or derived, and thus are useful candidates for 465 sensitivity analysis.

In general, it is recognised that, to robustly conduct sensitivity analysis, a global method 466 467 should be used, and the variability of the calculated indices should be checked to ensure 468 that the number of samples is sufficient (Saltelli et al., 2019). Because of the presumed high 469 level of dependency in the SWMManywhere workflow (for example, hydraulic design 470 depends entirely on network topology, which in turn depends on outfall and manhole 471 identification), we also calculate second order indices to better capture interactions between 472 parameters (Herman and Usher, 2017). To implement sensitivity analysis for 473 SWMManywhere, we use the SALib software (Herman and Usher, 2017), which provides a 474 variety of global methods for sampling parameter ranges and calculating sensitivity indices 475 natively in Python. In this study we use the Sobol method (Sobol, 1993) due to its 476 widespread use and recognised robustness of results providing that a sufficient number of 477 samples can be investigated (Pianosi et al., 2016). 18 parameters are sampled, indicated in

Table 1, and 16 metrics, Table 2, are evaluated. Thus, the overall approach is to perform
parameter sampling, run SWMManywhere with the parameters of each sample, calculate the
performance metrics between the synthesised and real UDMs, and calculate sensitivity
indices.

Sobol sensitivity analysis that includes second order interactions with SALib requires takingsamples equal to,

$$N = n * (2m + 2) \tag{2},$$

where N is the total number of samples (or SWMManywhere calls), m is the number of 484 parameters, and *n* is the number of Sobol sequence samples to generate (preferably a 485 power of 2). In this experiment we set n to 2^{10} (1024), m is 18, resulting in N of 38912. As 486 demonstrated in Pianosi et al., (2016), this many evaluations (m^* 1000) are towards the 487 upper limit of what is found in the literature. We take this opportunity to note a further benefit 488 489 of sensitivity analysis in the context of SWMManywhere as a global tool, which is that testing 490 it under such a large and diverse range of parameters further guarantees robustness of the 491 software implementation in locations not tested.

492 **3 Case studies**

493 In this study, we evaluate our proposed workflow by comparing the SWMM simulation 494 results obtain from using the synthetic UDM with those of the real UDM for the Cran Brook, 495 London, UK (Babovic and Mijic, 2019). We then perform sensitivity analysis in other 496 locations to examine the transferability of results and parameters. We use seven UDMs 497 around the town of Bellinge, Denmark, as delineated by Farina et al., (2023). These data were selected because they are openly available and demonstrate results over a wide range 498 499 of scales (Pedersen et al., 2021). The properties of the case study networks are presented in 500 Table 4.

501 Table 4: Summary of networks tested and their properties

Network	Number of	Number of	Impervious
	nodes	edges	percentage
Cran Brook	6931	6965	27
Bellinge 1	142	150	36
Bellinge 2	118	117	33
Bellinge 3	52	51	25
Bellinge 4	46	45	32
Bellinge 5	45	46	40
Bellinge 6	36	35	32
Bellinge 7	15	14	34

502

503 A key feature of many UDM is the presence of hydraulic structures such as weirs, orifices, 504 storages, or pumps. There is extensive evidence from the sewer network simplification 505 literature that capturing and parameterising these structures is critical towards reproducing 506 the behaviour of the real network (Thrysøe et al., 2019; Dobson et al., 2022). However, 507 SWMManywhere currently does not attempt to estimate the locations or hydraulic properties 508 of any such structures. We acknowledge that this could be a significant limitation and hope 509 to add this behaviour in future work. In this paper, we replace the hydraulic structures and 510 storage nodes in the real models with simple and uniform nodes to better assess the 511 SWMManywhere workflow as designed. Furthermore, the hydraulic properties of sub-512 catchments (specifically, the Manning's roughness coefficient and depression storage of 513 both impervious and pervious areas) are a significant source of uncertainty and typically 514 calibrated or set arbitrarily (Deletic et al., 2012), thus we set these at the same values for all 515 networks to ensure comparability.

516 The precipitation event we use to demonstrate SWMManywhere is the largest storm in the 517 openly available Bellinge data (Pedersen et al., 2021).

518 Workflow evaluations were performed on the Imperial College High Performance Computing 519 facilities (see Acknowledgements). Hardware used was typically AMD EPYC 7742 (128 520 cores, 1TB RAM per node), although this varied based on availability. On one of these 521 machines, for a single workflow evaluation in the Cran Brook case study, downloading and 522 data preprocessing takes ten seconds (except for buildings, which are national datasets and 523 so download speeds will vary significantly depending on the country), evaluating graph 524 functions and writing the UDM to SWMM format takes around two minutes (deriving sub-525 catchments and deriving network topology are the slowest individual steps at 20 seconds 526 each), simulation in SWMM takes eight minutes, and evaluating metrics takes two minutes 527 (dominated by the K-S test for node betweenness, mKN which took over one minute). Run 528 times for all Bellinge case studies were dramatically quicker owing to the far smaller UDM 529 sizes.

530 The code used to perform this experiment and results required to reproduce the figure 531 results in Section 4 are openly shared in a separate repository (Dobson et al., 2024b).

532 4 Results

533 4.1 Proof-of-concept examination

We focus this section on a synthesised model selected from our sensitivity analysis sampling (Section 4.2) that performed well across a range of metrics to assess SWMManywhere's ability to generate a high-quality UDM and raise methodological points of interest. Figure 4 plots a flow and flooding timeseries and diameter, elevation, slope, and travel time distributions for the Cran Brook network to provide a detailed comparison of the real and synthetic UDM.



Figure 4: Demonstration plot of a high performance synthetic UDM. Red dashed lines represent synthetic data,
while solid blue represents the real UDM simulations. Grey lines on the slope plot (e) show the target design
range.

544 Figure 4a shows flow at the network outfall, while Figure 4b shows the total flooded volume 545 across the network. We see that the maximum values of both are captured with accuracy, 546 however, the falling limb for both recedes more quickly in the synthetic network than in the 547 real UDM simulations. The synthetic network has consistently larger diameters (Figure 4f) 548 than the real, while chamber floor elevations (Figure 4d) are well matched. Synthetic pipe 549 slopes (Figure 4e) are lower, although we observe that these are primarily within the grey 550 dashed lines which show the target design range (Chahinian et al., 2019). The average 551 travel time from each node to the outfall (Figure 4c) shows distinctively different patterns 552 across the distribution, with a good match for the quickest third of nodes, the synthetic UDM 553 quicker for the middle third (because of the larger diameters), and the real UDM quicker for the slowest third. Although not shown, the total runoff from manhole sub-catchments in both 554

the real and synthetic models is within 2% of each other, which is true for all synthesisedUDMs.

557 4.2 Sensitivity analysis, Cran Brook

558 SWMManywhere parameters, see Table 1, were sampled using a Sobol sampling scheme, 559 see Section 2.2, to enable a global sensitivity analysis using the Sobol method. The findings 560 of this analysis for Cran Brook, the sensitivity indices, are presented in Figure 5a-b. Two

other locations (Figure 5 c-f) are discussed in Section 4.2, with other locations in full

562 presented in Supplemental Figure S1.



563 564 565 566 567 568 569

Figure 5: Heatmap demonstrating the sensitivity indices (a) of first order variance (S1) of a metric (y-axis)
attributable to a parameter (x-axis) based on simulations in the Cran Brook network, (b) of total variance (ST)
attributable to a parameter based on simulations in the Cran Brook network. Red indicates more sensitive and
yellow less sensitive. Blue indicates less than 1% variance explained. (c, d, e, f), shows equivalent of (a) and (b)
respectively, but for the Bellinge 1 and Bellinge 7 networks. Grey indicates no sensitivity indices could be
calculated because no flooding occurred.

- 570 In Figure 5 we show the first order variance (S1) of each metric (as listed in Table 2)
- 571 attributable to each parameter (Figure 5a), and the total variance (ST) attributable (Figure
- 572 5b). We see that sensitivity is widespread, with every parameter exhibiting at a total variance
- 573 attributable of >1% for at least one metric. We also see that sensitivity is overwhelmingly

574 occurring through interactions (i.e., sensitivities present in Figure 5b but not in Figure 5a), 575 with some notable exceptions: *node merge distance (pNM), minimum velocity (pMV),* 576 *minimum* (pMD) and *maximum chamber depth (pXD)*. First order sensitivity indicates that 577 the parameter is sensitive regardless of other parameter values, *pMV* and *pNM* are evidently 578 dominant in their influence on pipe design while *pNM* is discussed below. Second order 579 variance indices were also calculated, but not included because their confidence intervals 580 were prohibitively large.

Across metrics the *node merge distance* is the most sensitive parameter, impacting both system description metrics (top rows), topology metrics (middle rows), and simulation metrics (bottom rows). It is a sensitive parameter because it interacts with three key elements in SWMManywhere:

- 585 It influences manhole placement, which is also impacted by *max street length* (*pXS*,
 586 another sensitive parameter).
- 587 It impacts which nodes can drain to where, which is also impacted by *river buffer* 588 *distance* (*pRB*, another sensitive parameter).

It can significantly alter how the road layout is translated into potential pipes, which
 no other parameter does. For example, two adjacent roads running parallel may not
 have a driving connection between them, and thus no potential pipe may span them,
 but if these nodes are merged then a pipe could span them.

593 In addition to the dominance of these three parameters (node merge distance, max street 594 length and river buffer distance), we see many other intuitively appropriate sensitivities. 595 System metrics are sensitive to system parameters, topological metrics to topological 596 parameters, and design metrics to design parameters. We also find that flow simulation 597 metrics are sensitive to parameters relating to network topology, indicating that topology is 598 primarily influencing the global behaviour of the UDM. In contrast, we see that flood 599 simulation metrics are more sensitive to design parameters, indicating that design is 600 primarily influencing the local behaviour of the UDM.

We provide a specific examination of *node merge distance*, selected because it is the most sensitive parameter, to illustrate how SWMManywhere can be used to provide a detailed parametric exploration. We plot the parameter value of *node merge distance* against each metric value for all sampled points in Figure 6. We see clear evidence of first order sensitivity in line with those reported in Figure 5a-b.





Figure 6: Node merge distance parameter value plotted against all evaluated performance metrics. Based on
simulations in the Cran Brook network. Panels showing NSE or KGE are clipped at 0.0 and -0.41 respectively,
which indicates the performance of taking the mean value of observations as the simulation. Dashed lines for
KGE, NSE, relative error indicate a region of 'behavioural' performance, that is, values >0.7 (KGE, NSE) or within
+/- 0.1 (relative error).

Figure 6 indicates some evidence of identifiable parameter values, e.g., we observe that the

613 node merge distance should fall around 25m for the simulation flow metrics. However, this

- value can vary depending on which metric is used, for example, System metrics (*mRL, mRP,*and *mRM*) and some topology metrics (*mVD, mKE, mKN*) indicate better performance when *node merge distance* is around 0-15m.
- 617 It can be more informative to investigate whether parameters are identifiable using a
- 618 Gaussian kernel density estimate (KDE), which can be used to create a cumulative density
- 619 function for each parameter and can be weighted by different metrics. For example, in Figure
- 620 7, top left panel (*pNM*), weighting the KDE by flow simulations (red lines), we can see that
- 621 75% of the distribution indicates that *node merge distance* should be greater than 20m,
- agreeing with Figure 6. The KDE plots further highlight identifiability for a range of other
- 623 parameters, however, as with *node merge distance*, in most cases there can be
- 624 disagreement depending on which metric is used for weighting.



625

Figure 7: Gaussian KDE cumulative density functions for parameters, weighted by different metrics evaluated on
 the Cran Brook network. Metrics are grouped by colour to highlight different behaviours.

- 628 4.3 Sensitivity analysis, other locations
- In Figure 5 c-f we show the sensitivity analysis results for the Bellinge 1 and 7 networks,
- 630 which are the largest and smallest networks in the Bellinge dataset, respectively. Results for
- the other Bellinge UDMs are shown in Supplemental Figure S1, although do not
- 632 meaningfully differ from the observations below.
- 633 In general, we see many similarities between the two analyses, including high sensitivity of
- 634 node merge distance, more sensitivity occurring through interactions (Figure 5 c and e) than
- 635 in first order (Figure 5 d and f). In contrast, we see less significance of network topology
- 636 parameters across all metrics, which we can likely be attributed to smaller sizes of both

Bellinge networks are comparing to the Cran Brook network resulting in availability of fewer
topological configurations, thus less significance in terms of impacting metrics. We note that
no indices for flooding metrics could be calculated because the network did not experience
flooding under the precipitation timeseries used.

In Figure 8 we show the KDE estimates of parameter distributions for each network,

642 weighted by the NSE flow metric (*mNQ*). In contrast to Figure 7, we see stronger agreement

643 across networks than across metrics for weighting. For example, max fr (pXF), precipitation

644 (*pDP*), max depth (*pXD*), tend towards aligned parameter distributions across most

645 networks. Despite this, we also see some sensitive parameters with less agreement across

646 networks. For example, *min v (pMV), max street length (pXS),* and *node merge distance*

647 (*pNM*) have unaligned but identifiable parameter values. We also see that many parameters

648 do not have clearly defined distributions for most networks but do for one/few. For example,

649 *river buffer distance* appears to have a clearly defined distribution for Cran Brook and

Bellinge 2, while no other networks do. We do not see clear parameter distributions for

network topology parameters, despite their sensitivity demonstrated in Figure 5.



Figure 8: Gaussian KDE cumulative density function for parameters for each location. Weighted by outfall flow
 NSE.

- 655 5 Discussion
- 656 5.1 Development of SWMManywhere
- 657 In this study, we provide new insight into the intricacies of UDM synthesis through
- application of our proposed SWMManywhere workflow and performing extensive sensitivityanalysis.
- 660 We demonstrate in Figure 4 that reasonable simulations are achievable, with NSE values of
- >0.7 for both outfall flow and flooding, Figure 6. The implementation based on Duque et. al.,
- 662 (2022)'s pipe-by-pipe method results in high efficiency UDMs, although we observe that the

synthesised UDMs are perhaps too efficient as they drain the network too quickly, see flow and flood simulations in Figure 4. This finding suggests that inefficiencies seen in the real network reflect the additional constraints not captured by data sources that we employ in our workflow, for example, incremental construction of the network (Rauch et al., 2017). Despite such shortcomings, we recommend that sensitivity analysis is a necessary precursor to introducing any further complexity.

669 The sensitivity analysis results, Figure 5, show widespread and intuitively sensible sensitivity 670 of all parameters, including those introduced as technical innovations of this paper: enabling 671 slope inclusion within the MSA and contributing area as a factor in the network topology 672 derivation (pSS, pCS, pSE, pCE). We also highlight the dominant sensitivity of node merge 673 distance (pNM), which influences manhole locations, outfall locations, and underlying street 674 graph preprocessing. Manhole locations are well established to be important factors 675 (Chahinian et al., 2019; Blumensaat et al., 2012), while to our knowledge this is the first 676 UDM synthesis study that treats outfall locations as an explicit unknown. The importance of 677 the underlying street graph that node merge distance controls is intuitively sensible, as a 678 UDM synthesis can only ever be as good as the potential pipe-carrying locations that it 679 begins with. These findings indicate a promising outlook for UDM synthesis, as manhole 680 locations, outfall locations, and the street graph are all surface elements whose estimation 681 will only improve with improved satellite imagery and machine learning. Furthermore, in 682 cases where SWMManywhere is to be applied to a local area, surveying these surface 683 elements is likely to be far less costly than a below-ground network survey.

684 5.2 Transferability of SWMManywhere

A key motivation for performing sensitivity analysis is in identifying behavioural parameter ranges. In an ideal case, behavioural parameter ranges align across metrics and locations, thus implying that parameter choices are good under any condition. Figure 7 and Figure 8 demonstrate that we do not see clear evidence of this for either metrics or locations respectively. Figure 5 demonstrates that parameters are generally sensitive through

690 interactions, rather than through first order effects, which limits the ability to provide clear 691 advice on behavioural ranges. Although second order effects were calculated, the 692 confidence intervals were such that no conclusions could be drawn, and we estimate that 693 multiple magnitudes more samples would be required to provide definitive results, which is 694 outside the scope of this paper, but future work may investigate. Parameters that have high 695 first order sensitivity provide some clear advice, for example, node merge distance values 696 should be between 20m-35m to provide good flow simulation metrics in a variety of 697 locations. However, the dominant finding on parameter transferability is that the panacea of 698 arriving to a single 'correct' UDM through a synthesis approach is false. Indeed, we believe 699 that widespread findings of equifinality in hydraulic calibration of real UDMs, (Huang et al., 700 2022; Sytsma et al., 2022) supports that the idea of having a single 'correct' UDM that is 701 based on survey information (rather than synthesis) is also false. We propose that data 702 uncertainty will remain a fundamental element of UDM, synthetic or otherwise, for the 703 foreseeable future.

704 We therefore advocate for an approach to UDM that is uncertainty driven. Rather than 705 narrowly focussing on aligning synthetic with real UDMs, a synthetic UDM may most 706 appropriately be considered one hypothesis for the underlying system. Further 707 developments to SWMManywhere should thus seek to synthesise UDMs that are plausible 708 hypotheses, possibly through a more iterative approach that refines the UDM based on 709 simulation data only, for example, by assessing SWMM continuity errors. In a no field data 710 setting, the focus could shift to, for example, various climate scenarios or future urban 711 development, to study an ensemble of plausible UDMs and explore their likely outcomes. If 712 such studies would prohibitively increase simulation time, a range of network complexity 713 reduction techniques have been demonstrated for UDMs (Farina et al., 2023; Palmitessa et 714 al., 2022), including as part of an uncertainty ensemble approach (Dobson et al., 2022; 715 Thrysøe et al., 2019).

716 To ensure that our proposed workflow is applicable at the global scale, we have deliberately 717 avoided some data, for example design regulations or a higher resolution DEM, that are 718 commonly available at national scales. In local applications, however, we do recommend 719 exploring utilising the best quality data available and adapting the underlying datasets or 720 parameter assumptions, which our SWMManywhere implementation supports. Nevertheless, 721 we caution that this may not provide the certainty that one might expect. For example, as our 722 KDE parameter estimates demonstrate in Bellinge, Denmark (Figure 8), design regulations, 723 which are parameters that are country and region specific, do not show agreement across 724 UDMs in the same locale.

725 5.3 Outlook and limitations

726 The modular graph function-based architecture of SWMManywhere makes it easy to extend 727 or customise, thus we hope that it may become a centralised location for the synthetic UDM 728 community. We see a variety of potential improvements that may be introduced to increase 729 the realism of synthesised UDMs, although we stress the importance of performing 730 sensitivity analysis before investing time in creating complicated customisations. In addition 731 to better identification of surface elements described above, other surface factors such as 732 hydraulic structures are well established to play a dominant role in UDM behaviour (Thrysøe 733 et al., 2019; Dobson et al., 2022). SWMManywhere does not attempt to synthesise these 734 structures, and they are omitted from the analysis performed in this paper. However, 735 structures such as weirs may be identifiable from satellite imagery, while including pumps 736 may form an additional element in the network topology derivation, as has been 737 demonstrated for sanitary sewer networks (Khurelbaatar et al., 2021). 738 An immediate extension to the behaviour of SWMManywhere that we are exploring is 739 around water quality. Recent literature demonstrates the feasibility of quantifying urban 740 pollution deposition on roads (Revitt et al., 2022), which could be included as an optional 741 extension, thus providing the much-needed transport element to link deposition with in-river pollution. We anticipate that a key difficulty of such an approach would be in identifying 742

743 validation data, since sampling water quality at urban drainage outfalls during a storm is 744 dangerous to do in person. For example, while the English Environment Agency's 745 harmonised water quality sampling database contains over 60 million pollution sample 746 records since 2000 (Open water quality archive datasets (WIMS), 2024), just 0.4% are of 747 urban drainage outfalls, and only 25% of these have occurred since 2010, reflecting the diminishing focus on non-compliance monitoring observed across England (Dobson et al., 748 749 2021). Further improvements towards capturing water quality may also focus on 750 representing combined or misconnected systems, linking with the synthetic sanitary sewer 751 network literature (Duque et al., 2022).

752 A clear limitation of the case studies demonstrated in this paper is that they are based in 753 temperate and wealthy European countries, this is particularly problematic when considering 754 that street graph and building footprint data uncertainty will be more significant in nearly any 755 other type of region. We reached out to a variety of urban drainage modellers in both 756 industry and research but were not able to extend our case study selection further and 757 instead identified a significant paucity of publicly available reliable SWMM models. While the 758 SWMM website hosts a variety of useful example models, these aim to build understanding 759 about representing different elements of drainage networks, rather than providing a suite of 760 real test cases. Ultimately, SWMManywhere and other synthetic UDM tools will not be 761 trusted at global scales until they have been demonstrated on a wide variety of case studies. 762 Thus, we call for collaborators who can either share their SWMM models openly or are 763 willing to demonstrate SWMManywhere for their models to reach out that we may create a 764 more robust demonstration of UDM synthesis and verify that understandings created are 765 sustainable.

766 6 Conclusion

In this paper we present a workflow, SWMManywhere, that can synthesise an urban
drainage network model (UDM) and simulate it in SWMM, anywhere globally. We test the

parameters of SWMManywhere using sensitivity analysis to understand the dominant
 processes involved in synthesising UDMs. Our results revealed three key findings:

The SWMManywhere workflow can synthesize high quality UDM at a range of spatial
 scales. The parameters that can be used to tune SWMManywhere behave in
 intuitively sensible ways, verifying its implementation.

- We find that parameters controlling surface elements such as manhole locations,
 street layout, and network outfalls are the most sensitive, and thus should be the key
 focus of uncertainty reduction. Encouragingly, the identification of these elements is
 also the most likely to improve in the foreseeable future.
- 3. UDM synthesis is sensitive to all parameters and these parameters primarily
- influence outputs through second order or higher interactions, revealing UDM
- synthesis to be a more complex process than previously recognised. Additionally, we
- recommend that an ensemble approach would be appropriate for practical
- applications to more appropriately reflect the inherent uncertainty of the underlyingsystem.

We hope that the urban drainage community will use SWMManywhere to further explore the complexity of UDM synthesis, develop robust interventions in areas without existing UDM data, and do so in a more open and reproducible scientific environment.

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800 8 Data availability statement

- 801 The software implementation of SWMManywhere is an open-source repository available at
- 802 <u>https://github.com/ImperialCollegeLondon/SWMManywhere</u> (last accessed 2024-10-11). The
- 803 documentation for SWMManywhere can be found at
- 804 <u>https://imperialcollegelondon.github.io/SWMManywhere/</u> (last accessed 2024-10-11). The
- 805 results of the paper's experiments and code to perform sensitivity analysis and plots is
- 806 available at https://github.com/barneydobson/swmmanywhere_paper (last accessed 2024-
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