Controls of Dynamic and Static Stress Changes and Aseismic Slip on Delayed Earthquake Triggering: Application to the 2019 Ridgecrest Earthquake Sequence

Jeena Yun[1], Alice-Agnes Gabriel[1,2], Dave A. May[1], and Yuri Fialko[1]

[1]Scripps Institution of Oceanography, University of California San Diego, La Jolla, CA, USA
[2]Department of Earth and Environmental Sciences, Ludwig-Maximilians Universität München, Munich, Germany

Key Points:

- Simulations of stress perturbations due to the M_w 5.4 foreshock predict a clock advance of the mainshock of several hours.
- Instantaneous triggering does not occur unless stress perturbation is a large fraction of strength excess during quasi-static nucleation.
- The sign of stress perturbation in areas of accelerating slip controls the advance versus delay of the mainshock.

Corresponding author: Jeena Yun, j4yun@ucsd.edu

Abstract

Dynamic earthquake triggering often involves a time delay relative to the peak stress perturbation. In this study, we investigate the physical mechanisms responsible for delayed triggering. We compute detailed spatiotemporal changes in dynamic and static Coulomb stresses at the 2019 M_w 7.1 Ridgecrest mainshock hypocenter, induced by the M_w 5.4 foreshock, using 3D dynamic rupture models. The computed stress changes are used to perturb 2D quasi-dynamic models of seismic cycles on the mainshock fault governed by rate-and-state friction. We explore multiple scenarios with varying hypocenter depths, perturbation amplitudes and timing, and different evolution laws (aging, slip, and stress-dependent). Most of the perturbed cycle models show a mainshock clock advance of several hours. Instantaneous triggering occurs only if the peak stress perturbation is comparable to the strength excess during quasi-static nucleation. While both aging and slip laws yield similar clock advances, the stress-dependent aging law results in a systematically smaller clock advance. The sign of the stress perturbation in regions of accelerating slip controls whether the mainshock is advanced or delayed. Mainshocks can be triggered even when the future mainshock hypocenter is within a stress shadow, due to stress transfer from the foreshock sequence. Our results imply that the Ridgecrest mainshock fault was already on the verge of runaway rupture prior to the M_w 5.4 foreshock. These results highlight the contribution of both foreshocks and aseismic deformation to earthquake triggering and emphasize the importance of considering the physics of fault-system-wide processes when assessing triggering potential.

Plain Language Summary

Earthquakes can be triggered by stress changes induced by seismic waves from other earthquakes. These triggered events often exhibit a delay relative to the arrival time of the seismic waves. For example, the 2019 M_w 7.1 Ridgecrest, CA, mainshock occurred several hours after a nearby M_w 5.4 foreshock. The physical mechanism behind such delayed triggering remains unclear. In this study, we use computer simulations to explore the physical mechanisms responsible for delayed triggering. We compute detailed time-dependent stress changes at the Ridgecrest mainshock hypocenter caused by the M_w 5.4 foreshock and compare the timing of the mainshock in models with and without stress perturbation, for different scenarios. These results show that in most cases the perturbed mainshock occurs several hours earlier than it would without the perturbation. The clock advancement or delay depends on whether the stress change in regions of accelerating fault slip favors rupture. Even when stress changes at the future mainshock hypocenter do not favor rupture, stress transfer from the foreshock sequence can still trigger mainshocks. We infer that the Ridgecrest mainshock fault was ready to rupture. These findings emphasize the important role of foreshock sequences and aseismic deformation in earthquake triggering.

1 Introduction

Some earthquakes may be encouraged by other earthquakes, a phenomenon called earthquake triggering (e.g., Freed, 2005; Hill & Prejean, 2015; Stein, 1999). Earthquake triggering has been documented using seismic and geodetic observations at various distances from the source, both in the near-field (within one or two fault lengths; e.g., Bosl & Nur, 2002; Hudnut et al., 1989; King et al., 1994; Parsons & Dreger, 2000) and far-field (e.g., DeSalvio & Fan, 2023; Gomberg et al., 2001; Hill et al., 1993). Earthquake triggering has also been observed in laboratory experiments (e.g., Dong et al., 2022; Farain & Bonn, 2024; Y. Jin et al., 2021). One of the widely used frameworks to explain earthquake triggering considers changes in Coulomb failure stress (ΔCFS; Caskey & Wesnousky, 1997; Harris & Simpson, 1992; King et al., 1994; Z. Jin et al., 2022). Slip on a fault can permanently alter the stress field, either promoting or inhibiting failure on surrounding

faults. The static ΔCFS is a linear combination of permanent changes in shear stress and effective normal stress on a given 'receiver' fault. The magnitude and sign of ΔCFS indicate whether a fault is moved closer to failure. A region with positive static ΔCFS is considered to have an elevated likelihood of failure and is often well correlated with an increased rate of aftershocks, although there are notable exceptions (e.g., Hardebeck & Harris, 2022).

However, not all earthquakes appear to be triggered by static ΔCFS . Some presumably triggered earthquakes occur in regions with negative ΔCFS (stress shadow; Felzer & Brodsky, 2005) and at considerable distances from the causal earthquakes (e.g., Gomberg, 1996). The magnitude of static stress changes decreases rapidly with distance, becoming negligible at teleseismic distances (Árnadóttir et al., 2004; Gomberg et al., 2001). The concept of dynamic triggering considers changes in stress and/or strength due to passing seismic waves, which can produce an order of magnitude higher ΔCFS compared to static stress changes (Felzer & Brodsky, 2006; Kilb et al., 2000). Dynamic triggering may possibly explain the asymmetry in aftershock distributions due to rupture directivity (Kilb et al., 2000) and the occurrence of aftershocks within static stress shadows (Hardebeck & Harris, 2022). Additionally, dynamically triggered earthquakes often occur in geothermal fields or volcanic regions (e.g., Brodsky & Prejean, 2005), suggesting an important role of pore fluids interacting with faults.

While some dynamically triggered earthquakes occur at the time of the largest stress perturbation during the passage of seismic waves, a time delay between the largest perturbation and triggered earthquakes is frequently observed (e.g., Belardinelli et al., 1999; Dong et al., 2022; Guo et al., 2024; Shelly et al., 2011). For example, the July 2019 M_w 7.1 Ridgecrest earthquake was preceded by multiple foreshocks, including the two largest events of M_w 6.4 and M_w 5.4 (Jia et al., 2020; Meng & Fan, 2021; Ross et al., 2019). The M_w 5.4 foreshock occurred only 16.2 hours before the mainshock, and the hypocenters of the two earthquakes were separated by only about 3 km (USGS, 2017). Previous studies showed that the nucleation site of the M_w 7.1 Ridgecrest mainshock likely experienced significant dynamic stress changes of several MPa due to the foreshocks(e.g., Z. Jin & Fialko, 2020; Taufiqurrahman et al., 2023). Another example is the February 2023 Kahramanmaraş, Turkey M_w 7.8-7.7 earthquake doublet, which exhibited a time difference of about 9 hours between the two earthquakes, with a large dynamic stress perturbation on the M_w 7.7 earthquake fault plane induced by the M_w 7.8 earthquake (Gabriel et al., 2023; Jia et al., 2023). Given the spatiotemporal proximity of the causal and triggered large earthquakes, it is important to understand why apparently large stress perturbations fail to instantaneously trigger faults that are presumably already on the verge of runaway rupture and what factors control delayed triggering.

Several hypotheses have been proposed to explain the observed time delay in dynamic earthquake triggering, including changes in frictional contacts (Parsons, 2005), aseismic slip triggered by dynamic (Árnadóttir et al., 2004; Shelly et al., 2011) or static (Barbot et al., 2009; Wang & Fialko, 2014) stress changes, variations in pore pressure or fluid diffusion (Elkhoury et al., 2006; Gomberg et al., 2001), granular flow (Farain & Bonn, 2024; Johnson & Jia, 2005), and subcritical crack growth (Atkinson, 1984). Recently, Dong et al. (2022) observed delayed dynamic triggering in laboratory experiments. They infer a slow rupture phase and an increased critical slip distance near the P-wave perturbation, indicating a contribution of aseismic slip and changes in frictional contacts to delayed dynamic triggering.

Insights into the mechanics of earthquake triggering can be obtained from numerical modeling. Rate-and-state friction is a widely adopted constitutive law that describes the non-linear response of rock friction as a function of slip velocity and the state of the interface (Dieterich, 1979; Ruina, 1983). Single-degree-of-freedom spring slider models have provided useful insights into time-dependent slip histories and the sensitivity of the nucleation time in response to static or dynamic stress perturbations (Dieterich, 1994;

Gomberg et al., 1997; Perfettini et al., 2001; Mitchell et al., 2015). More complex rate-and-state models incorporating multiple earthquake sequences (i.e., seismic cycle models) have enhanced the understanding of the effects of external stress perturbations on the temporal evolution of fast and slow slip instabilities (e.g., Kostka & Gallovič, 2016; D. Li & Gabriel, 2024; Perfettini et al., 2003a, 2003b; Tymofyeyeva et al., 2019; Wei et al., 2018).

Despite considerable progress, many aspects of the physical mechanisms underlying earthquake triggering and delay remain unresolved. While far-field triggering is most likely dynamic in nature, distinguishing between the effects of static and dynamic triggering in the near-field is challenging. In the near-field, van der Elst and Brodsky (2010) estimated that dynamic strain accounts for the occurrence of 15 % - 60 % of magnitude 3 - 5.5 earthquakes, and Hardebeck and Harris (2022) estimated that ~ 34 % of all aftershocks are driven by dynamic stress changes. However, these studies relied on order-of-magnitude estimates of dynamic strain to quantify the effects of dynamic triggering. Although some previous studies have explored the effects of static (Dublanchet et al., 2013; Kaneko & Lapusta, 2008; Perfettini et al., 2003a) and dynamic (Gomberg et al., 1997; Perfettini et al., 2001, 2003b) stress changes individually, the combined static and dynamic effects remain poorly understood.

Also, existing models of dynamic triggering typically rely on simplified stress histories to estimate the triggering response. For example, dynamic stress perturbations are often modeled as a single pulse or harmonic function (Ader et al., 2014; Perfettini et al., 2003b; Luo & Liu, 2019). A notable exception is Wei et al. (2018), who computed a detailed time series of ΔCFS inferred from a kinematic slip model, but neglected variations of ΔCFS with depth. While these simplified stress histories might be appropriate approximations for far-field triggering or near-surface processes, they fall short of capturing the complexities of near-field triggering mechanics. A comprehensive understanding of near-field triggering requires considering the detailed history of stress perturbation throughout the full seismogenic depth range.

The emergence of earthquake dynamic rupture and seismic cycle simulations that efficiently utilize high-performance computing (HPC) provides new opportunities to address existing knowledge gaps (e.g., Taufiqurrahman et al., 2023; Uphoff et al., 2023). High-accuracy 3D dynamic rupture simulations enable the computation of realistic histories of seismic stress perturbations, allowing the exploration of the combined contributions of static and dynamic stress changes. Similarly, HPC-empowered seismic cycle simulations can incorporate more realistic parameters that are closer to those observed in laboratory experiments and allow extensive exploration of the parameter space. Additionally, the increased computational capabilities facilitate volume-discretized methods (Erickson & Dunham, 2014; Liu et al., 2020; Pranger, 2020; Thakur et al., 2020; Uphoff et al., 2023), which can require high computational costs in terms of both storage and time-to-solution.

In this study, we investigate the physical factors and processes governing potential triggering relationships between the 2019 Ridgecrest M_w 5.4 foreshock and the M_w 7.1 mainshock. We record detailed spatiotemporal stress changes on the mainshock fault plane caused by the M_w 5.4 foreshock, considering a range of fault geometries and varying moment release rates using 3D dynamic rupture simulations (Sections 2.1 and 3.1). These stress perturbations are applied to a suite of quasi-dynamic seismic cycle models described in a companion paper (Yun et al, 2025), denoted YGMF1 hereafter. The unperturbed models represent the reference fault slip history on the mainshock fault. We extensively explore the change in timing of the mainshock (i.e., mainshock 'clock change') across different stress perturbation models, target mainshock depths, times intervals between perturbation and mainshock, amplitudes of stress perturbations, and state variable evolution laws (Sections 3.2 and 3.3). We compare the correlation of the mainshock clock change with various physical factors, such as peak slip rate, static ΔCFS, and peak dynamic ΔCFS,

to identify the controlling mechanisms behind the mainshock clock change. We find that the spatial distribution of depth-dependent static ΔCFS and aseismic deformation significantly affects the mainshock clock change (Section 4.3). This work proposes a novel framework for evaluating the combined effect of static and dynamic stress changes on near-field triggering and suggests a deterministic approach to estimating triggering potential. Additionally, we highlight the contributions of static stress change and background deformation in earthquake triggering and advocate for an integrative approach to assessing triggering potential.

2 Methods

2.1 Dynamic Rupture Simulations

We compute the coseismic spatiotemporal evolution of stress changes near the mainshock hypocenter location caused by the M_w 5.4 foreshock using 3D dynamic rupture simulations. To this end, we use the open-source dynamic rupture and seismic wave propagation simulation software *SeisSol* (Dumbser & Käser, 2006; Pelties et al., 2014), which is optimized for HPC infrastructure (Heinecke et al., 2014; Krenz et al., 2021; Uphoff et al., 2017) and has been applied to model rupture dynamics in various tectonic contexts (e.g., Biemiller et al., 2022; Ulrich et al., 2019). We include both foreshock and mainshock faults within a 3D domain (Fig. 1a). In this model setup, the mainshock fault plane serves as the receiver plane, recording the dynamic and static stresses induced by the foreshock.

The foreshock rupture plane is modeled as a square fault with dimensions of 3 km by 3 km, centered at a depth of 7 km (USGS, 2017). We consider two dip angles, vertical and NW70° dip (USGS, 2017), to account for possible uncertainties in the fault dip estimation. To nucleate the earthquake, we prescribe a frictionally weak circular patch with a radius of 250 m at the center of the foreshock rupture plane.

The receiver mainshock fault extends from the free surface to a depth of 24 km, with a width of 3 km, and is centered at the M_w 7.1 mainshock epicenter location (USGS, 2017). We model scenarios using four different mainshock fault strikes (320°, 330°, 340°, and 350°) to cover a range of the average strike angles obtained from finite fault inversions of the M_w 7.1 mainshock (320°; Z. Jin & Fialko, 2020; Jia et al., 2020) and focal mechanisms (340°; SCEDC, 2013; Z. Jin & Fialko, 2020). Allowing for variations in the strike and dip of either fault accounts for uncertainties in the relative geometries of the two faults. Since we use eight different combinations of mainshock fault strikes and foreshock fault dips, the minimum distance between the two faults varies between 1303 m and 116 m. For models with a dipping foreshock fault, the horizontal extent of the mainshock fault is slightly reduced by 20 m (330°) or 500 m (320°) to prevent the two faults from intersecting. However, this variability in horizontal extent does not affect the stress change estimates, as we focus on the stress changes along a profile beneath the mainshock epicenter.

We embed both faults in a 3D velocity model (CVMS4.26.M01; Lee et al., 2014; Small et al., 2017, 2022). We use a stress-free boundary condition for the flat free surface (at zero depth) and absorbing boundary conditions for all remaining model boundaries. The spatial discretization of dynamic rupture simulations must be sufficient to resolve the width of the process zone (Day et al., 2005; Ramos et al., 2022). On-fault, we use a uniform element size of 25 m for the foreshock. This discretization adequately resolves the median cohesive zone width of about 200 m on the foreshock fault (Wollherr et al., 2018). For the mainshock fault, we use an element size of 80 m. This model resolves the seismic wavefield up to frequencies of 6.9 Hz between the two faults. Away from the fault, we gradually coarsen the unstructured tetrahedral mesh to element sizes of up to 1.5 km at the boundaries of our computational domain. The meshes used in this

study contain 1.8 to 2.3 million elements and require ∼500 CPU hours on average on the supercomputer SuperMUC-NG for each 15-second simulation.

All dynamic rupture model parameters used in this study are summarized in Table 1. We use a linear slip-weakening friction law (Andrews, 1976; Ida, 1972; Palmer & Rice, 1973) where the fault strength τ_s is defined as

$$\tau_s = C_0 + \sigma_n \left(f_s - \frac{f_s - f_d}{D_{LSW}} \min(S, D_{LSW}) \right), \tag{1}$$

with the frictional cohesion C_0, the effective normal stress σ_n, the static and dynamic friction f_s and f_d, respectively, and the slip-weakening distance for the linear slip-weakening law D_{LSW}. We vary the combination of dynamic friction f_d and critical distance D_{LSW} to obtain models with different rupture characteristics (Table 1).

We assign a Cartesian initial stress tensor $\boldsymbol{\sigma}$ for the entire domain (Table 1). As a result, the initial normal and shear stresses on each fault vary depending on the fault orientation. For the foreshock fault, which is contained within the $xz-$plane, the initial normal stress is $\sigma_n^0 = \boldsymbol{\sigma}_{yy}$, and the initial shear stress $\tau_0 = \boldsymbol{\sigma}_{xy}$. The prestress level and the frictional fault strength can be characterized by the seismic parameter or relative strength parameter S (Andrews, 1976), which represents the ratio of the frictional strength excess to the maximum possible dynamic stress drop,

$$S = \frac{f_s \sigma_n^0 - \tau_0}{\tau_0 - f_d \sigma_n^0}, \tag{2}$$

where $f_s \sigma_n^0$ and $f_d \sigma_n^0$ are the static and dynamic strength, respectively. Smaller static and dynamic friction coefficients are assigned within the nucleation patch, resulting in an S ratio of -0.56, which gradually increases outside the patch towards the fault boundary (Fig. 1b).

From the stress changes recorded on the mainshock fault plane, we compute the time evolution of ΔCFS, which includes both static and dynamic stress changes, as follows:

$$\Delta\mathrm{CFS}(z,t) = \hat{\tau}(z,t) - f\hat{\sigma}_n(z,t) \tag{3}$$

where z is depth, $t \in [0\ s, 15\ s]$ is time, $f = 0.4$ is the friction coefficient, and $\hat{\sigma}_n$ and $\hat{\tau}$ are the normal and along-strike shear stress changes with respect to the initial conditions. The peak dynamic ΔCFS at a certain depth then becomes $\max_t \Delta\mathrm{CFS}(z,t)$, and the static ΔCFS at a certain depth is $\Delta\mathrm{CFS}\ (z, 15\ \mathrm{s})$. Since models with varying dip angles and moment rate functions yield slightly different total moments, we scale all stress estimates by a factor of $M_{5.4}/M_0$ where $M_{5.4}$ is the total moment expected for a magnitude 5.4 earthquake on the modeled foreshock fault, and M_0 is the total moment obtained from each model.

2.2 Reference Seismic Cycle Simulations

A companion paper YGMF1 explores the role of various heterogeneities on the slip complexity in quasi-dynamic simulations of seismic cycles on a 2D vertical strike-slip fault governed by the rate-and-state friction law, using the open-source software *Tandem* (Uphoff et al., 2023). YGMF1 also compares slip patterns obtained from two state evolution laws, the aging law (Dieterich, 1979):

$$\frac{d\theta}{dt} = 1 - \frac{\|\boldsymbol{V}\|\theta}{D_{RS}}, \tag{4}$$

and the slip law (Ruina, 1983):

$$\frac{d\theta}{dt} = -\frac{\|\boldsymbol{V}\|\theta}{D_{RS}} \ln\left(\frac{\|\boldsymbol{V}\|\theta}{D_{RS}}\right), \tag{5}$$

where $\|\boldsymbol{V}\|$ is the Euclidean norm of the slip rate vector $\boldsymbol{V}$, θ is the state variable, and D_{RS} is the characteristic state evolution distance.

In this study, we use the most complex model considered in YGMF1 (model A2 that assumes the aging law; see Figs. S1 and S2a) as the reference model of slip history on the 2019 Ridgecrest mainshock fault without stress perturbation. This model features cascades of ruptures with various sizes and hypocenter depths as well as spontaneous slow slip events (SSE). We also use models S10 (Fig. S2b) and A10 (Fig. S2c) from YGMF1 to compare the triggering response of different evolution laws. All seismic cycle input parameters used in this study are summarized in Table 2.

We consider an additional state evolution law that can capture the immediate response of the rock strength as a response to a sudden change in normal stress (e.g., Boettcher & Marone, 2004; Linker & Dieterich, 1992; Pignalberi et al., 2024). The effect of external normal stress perturbations is taken into account by adding a stress-dependent term to the classic state evolution laws. For example, the stress-dependent aging law takes the form of:

$$\frac{d\theta}{dt} = 1 - \frac{\|\boldsymbol{V}\|\theta}{D_{RS}} - \alpha\frac{\theta}{b}\frac{\dot{\sigma}_n}{\sigma_n}, \tag{6}$$

where b is the rate-and-state parameters governing the evolution effect, $\dot{\sigma}_n$ is the time derivative of normal stress, and α is the scaling factor that can vary from 0 to the static friction coefficient (Boettcher & Marone, 2004; Wei et al., 2018). We use $\alpha = 0.3$ (Boettcher & Marone, 2004; Richardson & Marone, 1999). The stress-dependent aging law takes effect only under external stress perturbations, as normal stress remains constant in 2D anti-plane models.

Following YGMF1, we define 'system-size earthquake' as an event that ruptures the entire seismogenic zone (rupture length greater than 10 km), while all other events are denoted 'partial rupture events'.

2.3 Combining Dynamic Rupture and Seismic Cycle Simulations

To estimate the triggering response of the mainshock nucleation site to stress changes imposed by the foreshock, we perturb the seismic cycle models (Section 2.2) using stress histories calculated from the dynamic rupture simulation (Section 2.1). The main processing steps are as follows (Fig. 2):

1. Run 3D dynamic rupture models rupturing the foreshock fault and record the normal ($\hat{\sigma_n}$) and shear stress ($\hat{\tau}$) perturbations across the (locked) mainshock fault beneath the mainshock epicenter (Section 2.1; Fig. 2b).
2. Run a 2D seismic cycle model and obtain N cycles using either the aging law or the slip law. We refer to these models as 'unperturbed' reference models (black line in Fig. 2a).
3. Among the N cycles of the unperturbed seismic cycle model, choose one cycle with a system-size earthquake. The selected system-size earthquake will be called a 'target mainshock'. Identify the time of occurrence for the target mainshock, t_u.
4. Restart and run the cycling experiment from time $t = t_u - t_g$ where t_g is the time interval between the start of the perturbation (corresponding to the time of the M_w 5.4 foreshock) and the mainshock. Unless otherwise noted, t_g is set to 16.2 h, the time interval between the M_w 5.4 foreshock and the M_w 7.1 mainshock in the 2019 Ridgecrest earthquake sequence (USGS, 2017). During this stage, the time-dependent normal ($\hat{\sigma}_n$) and shear ($\hat{\tau}$) stress changes on the mainshock fault simulated in the dynamic rupture simulations (Section 2.1) are added to those of the unperturbed seismic cycle model ($\tau(z,t)$ & $\sigma_n(z,t)$) at each time step, yielding the perturbed normal stress (σ_n^p) and shear stress (τ^p):

$$\tau^p(z,t) = \tau(z,t) + \hat{\tau}(z,t)$$

$$\sigma_n^p(z,t) = \sigma_n(z,t) + \hat{\sigma}_n(z,t).$$

This phase will be denoted as the 'perturbation period', which lasts 15 s. During this stage, we use a fixed time step of 0.01 s to match the time interval of the dynamic rupture simulation outputs.

5. After the perturbation ends (i.e., $t > t_u - t_g + 15$ s) keep the static stress changes:

$$\tau^0(z) = \tau^0(z) + \hat{\tau}(z, t_f)$$

$$\sigma_n^0(z) = \sigma_n^0(z) + \hat{\sigma}_n(z, t_f),$$

where $t_f = t_u - t_g + 15$ s is the final time of the perturbation period. Continue running the seismic cycle simulation until a system-size earthquake occurs, and record the time of this event, t_p (blue line in Fig. 2a). This model is referred to as a 'perturbed' model.

6. Calculate the time difference between the system-size earthquakes with and without the perturbation: $\Delta t = t_u - t_p$. Δt is a measure for the triggering response. A positive Δt indicates that the perturbed system-size earthquake (mainshock) occurs earlier than in the unperturbed model, indicating a clock advance. A negative Δt indicates a mainshock clock delay.

Incorporating the stress-dependent aging law (Eq. (6)) requires a slight modification during the perturbation period (i.e., step 4 above):

1. Repeat steps 1 - 3 as outlined above.
2. During the perturbation period ($t \in [t_u - t_g, t_u - t_g + 15s]$), apply the stress-dependent aging law. The stressing rate during this perturbation ($\dot{\sigma_n^p}$) depends solely on the external stress perturbation ($\hat{\sigma}_n$):

$$\begin{aligned}\dot{\sigma}_n^p(z,t) &= \dot{\sigma}_n(z,t) + \dot{\hat{\sigma}}_n(z,t) \\ &= \dot{\sigma}_n^0(z) + \dot{\hat{\sigma}}_n(z,t) \\ &= \dot{\hat{\sigma}}_n(z,t)\,,\end{aligned}$$

since the background normal stress in the seismic cycle simulation (σ_n^0) remains constant over time (i.e., $\dot{\sigma}_n^0(z) = 0$). Then, Eq. (6) becomes:

$$\frac{d\theta}{dt} = G(\|\boldsymbol{V}\|, \theta) - \alpha \frac{\theta}{b} \frac{\dot{\sigma_n^p}}{\sigma_n^p} = G(\|\boldsymbol{V}\|, \theta) - \alpha \frac{\theta}{b} \frac{\dot{\hat{\sigma_n}}}{\sigma_n + \hat{\sigma_n}},$$

where $G(\|\boldsymbol{V}\|, \theta) = 1 - \frac{\|\boldsymbol{V}\|\theta}{D_{RS}}$. Aside from the state variable evolution law, everything else is the same as step 4 in the previously described procedure.

3. For $t > t_u - t_g + 15$ s, switch the state variable evolution law back to the aging law and keep the constant static stress change. Repeat steps 5 - 6 in the previously described procedure to obtain Δt.

3 Results

3.1 Dynamic and Static Stress Change Estimation

The 3D dynamic rupture simulations well capture the dynamics of the M_w 5.4 foreshock along the mainshock fault. Figure 3 shows examples of spatiotemporal evolutions of the ΔCFS across the mainshock fault with 340° strike, assuming different foreshock fault dips and rupture characteristics. The dynamic stress transfer mediated by body waves and reflections from the free surface is clearly observed. The peak dynamic ΔCFS values fall between 0.4 MPa and 2 MPa (Fig. S3a), consistent with the previous estimate by Z. Jin and Fialko (2020) based on a point source approximation. The static ΔCFS values are generally on the order of kilopascals (Figs. S3c-d). The sign of the static ΔCFS

changes from negative in the middle of the seismogenic zone (between 5 km and 10 km) to positive at smaller depths (< 5 km) and greater depths (> 10 km), reflecting the 3D nature of the respective stress field.

The rupture characteristics of the M_w 5.4 foreshock (Fig. 1c) mostly affect the arrival time and the amplitude of the peak dynamic ΔCFS, while having a negligible effect on the pattern of static ΔCFS (left vs. right columns of Fig. 3). We explore varying combinations of f_d and D_{LSW} to obtain two distinctive dynamic rupture characteristics that differ in their timing of the peak energy release (Fig. 1c): one set of models nucleates and releases all its energy immediately (denoted 'fast initiation' hereafter), while the others nucleate slowly, with pronounced runaway rupture initiating after 0.5 s (denoted 'slow initiation' hereafter). The slow initiation model features two episodes of moment release: one at the initial, prescribed time of rupture initiation and a second at the point of spontaneous runaway rupture. This resembles the two subevents with a 0.8 s time interval constrained from apparent source time functions of the M_w 5.4 foreshock (Meng & Fan, 2021). The difference in moment release rate is well reflected in the spatiotemporal patterns of ΔCFS . Slow initiation models show delayed arrivals of the peak dynamic ΔCFS with reduced amplitudes (Fig. S3a) compared to the fast initiation models. The reduced amplitude is likely caused by the energy distribution to each subevent in the slow initiation models.

The mainshock fault strike systematically affects the amplitude of the peak dynamic ΔCFS and the static ΔCFS, while the foreshock fault dip affects the seismic radiation, altering the arrival time, depth, and amplitude. More northerly strike angles systematically decrease the amplitude of the peak dynamic ΔCFS and the static ΔCFS (Fig. S3). Although the foreshock fault dip does not significantly affect the peak dynamic ΔCFS values, the dipping foreshock fault produces a stronger contrast between the positive and negative static ΔCFS values (Fig. S3c-d). The vertical foreshock fault produces near-symmetric wave propagation with respect to a depth of $\sim$ 7 km, whereas the dipping foreshock fault shows asymmetric propagation (top vs. bottom rows of Fig. 3). This apparent asymmetry is caused by the asymmetric arrival of the strong dynamic ΔCFS pulse due to the rotation of the radiation field in the dipping foreshock fault models, although the actual rupture speed is similar for various depths. The rotation of the radiation field also makes the depth of the peak dynamic ΔCFS smaller (except for the 350° strike).

Throughout the remainder of this study, we divide the stress perturbation models into four classes defined by the combination of the foreshock fault dip and the rupture characteristics: the vertical foreshock fault and the fast initiation model (VFI), the vertical foreshock fault and the slow initiation model (VSI), the dipping foreshock fault and the fast initiation model (DFI), and the dipping foreshock fault and the slow initiation model (DSI). Therefore, we have 16 dynamic rupture models in total, combining the four model classes with four mainshock strike angles.

3.2 Triggering Responses: Aging Law

We perturb the aging law reference model (A2 model, see YGMF1) following the procedure outlined in Section 2.3. We consistently obtain several hours of target mainshock clock advance ($\Delta t > 0$) for all considered cases (Fig. 4). For example, we select various target mainshocks with hypocenter depths ranging from 4.34 km to 7.82 km while fixing the stress perturbation from the dynamic rupture model with the vertical foreshock fault, slow initiation, and 340° mainshock fault strike (denoted "VSI, 340° strike" model), to explore the effect of target mainshock selection on the estimated triggering response. The observed clock advance ranges from 4.5 h to 6.1 h.

Next, we apply various stress models to a fixed target mainshock (event 282 at 7.82 km depth; Fig. S1a) and observe time advances of several hours (4.1 h to 5.6 h) for all considered combinations of fault geometry and rupture characteristics. We repeat the pro-

cess with different fixed target mainshocks (e.g., event 120 at 6.5 km depth; event 88 at 4.38 km depth), and the overall pattern of several hours of clock advance remains consistent.

Given the consistent behavior observed across all combinations of the perturbation model and target mainshock depths, we explore the effect of the timing of the perturbation (i.e., t_g). We test seven different values for t_g (10 yr, 1 yr, 30 h, 20 h, 16.2 h, 5 h, and 1 h) and perturb a fixed combination of the target mainshock (event 88 at 4.38 km depth) and stress perturbation model (VSI, 340° strike; Fig. 5). The mainshock clock is advanced for all explored timings of perturbation. The modeled Δt decreases as t_g decreases (Fig. 5b). However, we do not observe instantaneous triggering even when the perturbation is applied closer to the unperturbed target mainshock time (e.g., $t_g = 1$ h).

We further examine the control of t_g on the mainshock clock change by defining the 'closeness to instantaneous triggering' as $\Delta t/t_g$, a quantity designed to become 1 when the mainshock is triggered instantaneously (squares in Fig. S4). The closeness to instantaneous triggering varies non-linearly for different t_g and does not exhibit a clear trend with varying t_g values. This contrasts with previous simulation results with static ΔCFS perturbations showing a systematic convergence toward the instantaneous triggering curve as t_g decreases (e.g., Gallovič, 2008; Perfettini et al., 2003a). This implies that applying the stress perturbation later in the unperturbed earthquake cycle does not guarantee more rapid nucleation, likely due to the complexity in our models.

Earthquake triggering may also depend on the amplitude of the stress perturbation (e.g., Wei et al., 2018). To explore the effect of the amplitude of the perturbing stress changes, we scale the amplitude of the stress perturbation by a factor ranging from 1 to 30 and perturb a given target mainshock (event 88). The amplification results in a wide range of the peak dynamic ΔCFS at the given target mainshock hypocenter location (4.38 km), from 0.5 MPa to 17.5 MPa. For smaller amplification factors (1, 2, 3, and 5), the mainshock clock is advanced but we do not observe instantaneous triggering. The magnitude of clock advance is systematically increased from 6.1 h to 11.9 h as the amplitude of the perturbing stress change increases.

The target mainshock is not triggered instantaneously, even when the stress perturbation is amplified by a factor of 10, yielding a peak dynamic ΔCFS of 5.8 MPa at the expected hypocenter depth (Fig. 6a). This peak dynamic ΔCFS value is equivalent to 27 % of the excess strength during the quasi-static nucleation ($\tau - f_0\sigma_n = 21.4$ MPa for $\sigma_n = 53$ MPa at the nucleation site). Instead, a new partial rupture event that would not have occurred with the absence of perturbation is triggered soon after the perturbation (new event 1 in Fig. 6a), followed by a smaller partial rupture event (new event 2 in Fig. 6a), forming a new sequence that does not culminate in a system-size earthquake. A system-size earthquake occurs several months after the sequence at a slightly shallower depth, eventually delaying the time by 74 days compared to the unperturbed model. However, since the sequence that leads to the mainshock is completely altered, we do not consider the new system-sized event as a delay of the target mainshock but rather consider it as a new event not observed in the reference model.

The instantaneous triggering of a system-size earthquake occurs when the stress perturbation is amplified by a factor of 30, resulting in a peak dynamic ΔCFS of 17.5 MPa at the mainshock hypocenter depth (Fig. 6b). This peak dynamic ΔCFS value corresponds to 82 % of the excess strength during the quasi-static nucleation. We consider this event as an example of dynamic triggering since it nucleates ~ 2.5 s after the start of perturbation, which corresponds with the arrival of the largest dynamic stress. The depth of the nucleation also matches that of the peak dynamic stress change.

Throughout the exploration with the aging law reference model (A2 model), we persistently obtain a mainshock clock advance. To understand the underlying physical mech-

anisms, we examine the correlation of the clock advance with five key physical parameters (Fig. 4): peak dynamic ΔCFS and static ΔCFS at the depth of maximum slip during the perturbation period (i.e., at $z_{max} = \text{argmax}_z\, \delta(z)$ for slip δ), peak slip, peak slip rate, and work per distance (W; Eq. (7)) along the entire fault.

We define work per distance W as the work density integrated over the entire fault:

$$W = \int_0^{L_f} \int_0^{\Delta\delta(z)} \Delta\tau(z,\delta)\, d\delta dz, \tag{7}$$

where δ is slip, $\Delta\delta$ and $\Delta\tau$ are the net slip and shear stress change during the perturbation period, respectively. Although W includes all VW and VS regions, the contribution of creep in VS regions ($V \sim 10^{-9}$ m/s) to W is minor compared to that in VW regions ($V \sim 10^{-6}$ m/s). The W metric well captures the net energy gain or loss due to the applied stress perturbation along the fault. This metric measures the combined effect of external stress change and inherent slip along the entire fault. We compute the Pearson correlation coefficient R between Δt and each parameter for a quantitative comparison.

The clock advances from our models show a strong correlation with both peak dynamic ΔCFS and static ΔCFS values, showing R values of 0.86 and 0.94, respectively. Both parameters show a positive, almost linear, relationship with the clock advance. In contrast, the peak slip, the peak slip rate, and the work per distance did not show a strong correlation with the estimated clock advance ($R \leq 0.53$). However, it is worth noting that all W values are positive for all clock advance models. As will be discussed in more detail in Section 4.3, the sign of the W value effectively predicts whether the mainshock will advance or delay as a response to the given stress perturbation.

Note that we measure both ΔCFS values at z_{max} instead of the hypocenter depth in the unperturbed models. This choice is made to fully reflect the ongoing aseismic slip at the time of perturbation in our models, mostly in the form of afterslip of the preceding foreshocks (see Figs. 9a & 9b). We will discuss more about this choice in Section 4.5.

3.3 Triggering Responses: Other Evolution Laws

In the previous section, the models with aging law consistently predict the clock advance of the next large event regardless of the choice of event, stress perturbation model, and timing of perturbation, unless the amplitude of perturbing stress is significantly elevated to produce instantaneous triggering. In this section, we explore triggering responses from other state evolution laws.

Although adding the stress-dependent term in the evolution law (i.e., the last term in Eq. (6)) is expected to make the models more realistic, it is still poorly understood how this stress-dependency affects the state variable evolution on a fault with a complex seismic and aseismic slip history and in turn, how it would affect the triggering response on the fault. Thus, we estimate the triggering response with stress-dependent aging law, following the procedure outlined in Section 2.3, and compare the results with those from the aging law reference model (Section 3.2). The stress-dependent aging law and aging law reference model take the same unperturbed model (i.e., A2 model), but differ in that the stress-dependent term is applied during the perturbation period for the stress-dependent aging law models. We again obtain mainshock clock advances (i.e., $\Delta t > 0$) of several hours when using the stress-dependent aging law, but the Δt estimates are systematically smaller compared to the aging law reference model (Fig. 7). For example, a given combination of target mainshock (event 282 at 7.82 km depth) and the stress perturbation model (VSI, 340° strike) yields $\Delta t = 4.5$ h when perturbing the aging law reference model while $\Delta t = 3.7$ h is obtained using the stress-dependent aging law (Fig. 7a). The decreased magnitude of clock advance in stress-dependent aging law is robustly ob-

tained for all five tested cases with different target events and stress perturbation models (Fig. 7b).

The reduction of clock advance can be well explained in the framework of work per distance (W). With the stress-dependent term, the evolution of the state variable and the slip rate during the perturbation period resembles that of the external stress perturbation, leaving a depth-dependent static change in both variables. Therefore, tracking the change in variable at a single depth cannot fully explain the systematic decrease in Δt. We rather compute the W values from the stress-dependent law models, which reflect integrated effect along the entire fault, and obtain systematically lower W values compared to the aging law reference models (Fig. 7c). Since models using different evolution laws are perturbing the same target mainshock using the same stress perturbation, the reduction in W originates from the amount of slip at regions under higher ΔCFS values. Integration of the state variable in Eq. (6) leads to a minor decrease in slip in the stress-dependent law models, thus causing slightly smaller advances of the time of mainshock. This result emphasizes the importance of an integrative approach to assess the effects of external stress perturbation.

Next, we explore whether using the slip law (Eq. (5)) significantly alters the triggering response, since the slip law may facilitate triggering compared to the aging law owing to its smaller nucleation size. We perturb the slip law reference model (S10 model) with different stress perturbation models and obtain a similar pattern of clock advance of several hours, ranging from 6 h to 8 h. We cannot explore the effect of hypocenter depth since the slip law reference model produces a repetitive sequence with a single hypocenter depth (6.92 km) for system-size events. The clock advance of 6 to 8 h is comparable to that of 5 to 9 h estimated from the aging law reference model using a system-size event with a similar depth of 6.5 km. However, we cannot directly compare the Δt value between the slip law reference model and the aging law reference model due to their different parameter setups.

For a better comparison, we perturb the A10 model with different stress perturbation models, and surprisingly, we consistently obtain mainshock clock delays (i.e., $\Delta t < 0$), instead of advances. To understand the key control of clock advance versus delay, we investigate the five key parameters examined in Figure 4 for both clock advance and clock delay models (Fig. S5). We observe that the static ΔCFS value and W value exhibit a clear distinction between the clock advance models and the clock delay models. All clock delay models from the A10 model show negative values for both parameters, in contrast to all clock advance models, which show positive values (Figs. S5b & e). The notable contrast in the static ΔCFS value and W value implies a strong control of the combined effect of the static ΔCFS and background aseismic slip along the entire fault on the mainshock clock change. We discuss this combined effect in detail in Section 4.3.

The only deviation between the sign of W and the sign of Δt occurs when the perturbation is applied well before the target mainshock (i.e., larger t_g). We obtain a mainshock clock delay of ~ 13 yr when we increase t_g to 30 yr, unlike the clock advances obtained from smaller t_g values (Fig. S6). Then, the estimated W value is very small but positive, an unexpected outcome for a model with a mainshock clock delay. Using $t_g = 30$ yr, the perturbation is applied before the first transient in a sequence of SSEs occurring in the deeper part of the seismogenic zone, preceding the target foreshock-mainshock sequence. This perturbation triggers a new SSE, which ultimately delays the target mainshock's onset. This implies that the external energy applied at $t_g = 30$ yr is insufficient to affect the nucleation of the foreshock-mainshock sequence but instead is consumed in initiating an additional aseismic transient. The unpredictable behavior associated with the complex SSE sequence emphasizes the importance of considering aseismic processes in the context of longer seismic cycle history.

In addition, we find a decrease of Δt value when using the stress-dependent aging law to perturb the A10 models. For example, we obtain 6 h of time delay (i.e., $\Delta t = -6$ h) when perturbing target mainshock 18 in the A10 model (Fig. S2c) using the VSI stress perturbation model with the mainshock strike orientation of 340°. When assuming the stress-dependent aging law during the perturbation period, the time delay increases to 6.5 h (i.e., $\Delta t = -6.5$ h). This result suggests that the stress-dependent term systematically decreases Δt value, regardless of its sign.

4 Discussion

4.1 Lack of Instantaneous Triggering

Throughout this study, we persistently observe a lack of instantaneous triggering. In Section 3.2, we find that instantaneous triggering does not occur even for small values of t_g and that the proximity to instantaneous triggering is unpredictable. Some studies suggest that a larger perturbing stress amplitude leads to a more rapid convergence toward instantaneous triggering as t_g decreases (Gallovič, 2008; Gomberg et al., 1998; Perfettini et al., 2003a, 2003b). To analyze such amplitude dependency, we repeat the analysis detailed in Section 3.2 with a stress perturbation amplitude elevated by a factor of 5 (resulting in a peak stress change of ∼3 MPa at the expected target hypocenter depth; triangles in Fig. S4). As expected, the overall proximity to instantaneous triggering increases with elevated amplitudes. However, the proximity to instantaneous triggering systematically decreases with smaller t_g values, indicating less efficient triggering when the perturbation occurs later in the cycle. The non-monotonic response of Δt for varying t_g may be explained as a combined contribution from transient (larger Δt value when applied later in the cycle) and static (smaller Δt value when applied later in the cycle) stress changes, as suggested by Gomberg et al. (1998). These analyses with varying t_g demonstrate that the timing of the perturbation is not a crucial factor in instantaneous triggering.

In our model parameterization, instantaneous triggering occurs only when the peak amplitude of stress perturbation at the unperturbed mainshock hypocenter depth is elevated to 17.5 MPa (30-times elevated model; Fig. 6b). We identify instantaneous triggering as dynamically triggered based on the occurrence time and hypocentral depth, which coincide with the arrival of the peak dynamic ΔCFS . The amplitude required for instantaneously triggered rupture in this study (17.5 MPa) is comparable to the additional prestress level required to dynamically nucleate the Ridgecrest mainshock after the M_w 6.4 foreshock (18 MPa), estimated from a realistic sequence of 3D dynamic rupture simulations (Taufiqurrahman et al., 2023). The required peak stress change amplitude of a few tens of MPa is also consistent with the dynamic triggering threshold inferred from peak seismic velocities (Gomberg et al., 2001). This amplitude (17.5 MPa) is slightly less than, but comparable to, the steady-state-to-peak stress change of 20.4 MPa produced by the unperturbed model. This implies that the amplitude of the stress perturbation is expected to be comparable to the excess strength during the quasi-static nucleation for an instantaneous dynamic triggering to occur. Because the excess strength scales with the effective normal stress, this may explain why dynamically triggered earthquakes are mostly observed in geothermal areas (Aiken & Peng, 2014; Brodsky & Prejean, 2005; Hirose et al., 2011; Husen et al., 2004), where the effective normal stress may be locally low due to the presence of over-pressurized fluids. The triggering stress required in the perturbed model is somewhat lower (< 90 %) compared to the strength excess, indicating that the passage of seismic waves may additionally affect the effective fault strength.

We find that a peak dynamic ΔCFS of moderately large amplitude (∼ 5.8 MPa at the unperturbed hypocenter depth) is capable of triggering partial ruptures which alter the stress distribution along the fault, subsequently leading to an entirely new sequence

of earthquakes following the perturbation (Section 3.2; Fig. 6a). From a seismic hazard perspective, the models presented here may imply that an earthquake is less likely to be triggered immediately by another earthquake unless a sufficiently high stress is applied. However, a significantly strong perturbation may affect the occurrence of smaller earthquakes, causing changes in the timing and location of nucleation of the next large earthquake in a highly non-linear, complex way.

4.2 Which is Dominant in Earthquake Triggering: Static or Dynamic Stress Changes?

Identifying the roles of static and dynamic stress changes in earthquake triggering is important for seismic hazard assessment, specifically in the aftermath of large earthquakes. We aim to understand the relative contribution of each process. So far, we present models containing both dynamic and static components of ΔCFS and provide insights into their combined impact on the mainshock clock change.

We now compare how the Δt estimates change when we perturb using only the dynamic component of the ΔCFS or only the static component. First, we separate the dynamic and static components of the ΔCFS from the "VSI, 340° strike" stress perturbation model by tapering out the early ($t < 10$ s) or late ($t < 10$ s) part of the computed time series of dynamic stress perturbations due to the M_w 5.4 foreshock (Fig. S7).

In Figure 8, we compare the triggering response from dynamic-only and static-only models with that from the original stress perturbation model, which includes both dynamic and static components. When both components are included, we obtain a mainshock clock advance of 4.5 h. In contrast, the mainshock clock advances only by a few seconds (3.9 s) when we perturb with the dynamic-only perturbation model. The static-only perturbation model almost fully reproduces the mainshock clock advance of 4.5 h. The Δt estimates of the original model and static-only model differ by only 1.4 s. The dominance of static ΔCFS is robust when tested with different sets of target mainshocks and stress perturbation models. Thus, we conclude that static ΔCFS is more effective in altering the timing of a future mainshock in the current model setup.

The dominance of the static stress change in earthquake triggering was suggested in previous studies as well. High-precision earthquake catalogs reveal a lower triggering threshold for static stress change compared to the dynamic stress change (Gomberg et al., 2001) or a strong size-to-distance relationship of aftershocks (van der Elst & Shaw, 2015). Also, a delayed change in seismicity rate, particularly a delayed decrease in seismicity rate, can be well explained by the static stress transfer (Kroll et al., 2017; Toda et al., 2012). In numerical simulations with rate-and-state friction law, a higher triggering potential of the static ΔCFS compared to the dynamic ΔCFS of the same amplitude is reported for fast and slow earthquakes (Belardinelli et al., 2003; Gomberg et al., 1998; Luo & Liu, 2019; Yoshida et al., 2020).

However, the limited contribution from the dynamic ΔCFS in our models cannot fully explain the frequent observation of dynamic triggering, particularly in the far field. The lack of dynamic triggering in this study might be related to the short duration ($<$ 5 s) of the dynamic ΔCFS used in this study (Katakami et al., 2020; Wei et al., 2018). Additional weakening mechanisms that are not considered in this study, such as pore pressure changes, thermal pressurization, localization of brittle deformation, or off-fault damage, may play a crucial role in facilitating dynamic triggering (e.g., Brodsky et al., 2003; Elkhoury et al., 2006; Gabriel et al., 2024; Zhu et al., 2020).

Another mechanism that may contribute to the complexity of earthquake triggering is the cumulative stress transfer from multiple foreshocks. We observe a systematic shortening of the duration of the modeled cascading foreshock-mainshock sequence as a result of perturbation. For example, the duration of the foreshock-mainshock sequence

(i.e., time from the leading foreshock to the system-size earthquake) in one of the sequences in the unperturbed aging law reference model is 1,166 s, which becomes 411 s when it is perturbed (Fig. S8). Similar behavior has been shown in models with a rough fault surface, where creep was accelerated in areas of low effective normal stress due to foreshocks (Cattania & Segall, 2021). This shortening of the sequence implies that the superposition of perturbations from multiple foreshocks might significantly advance the mainshock occurrence time. While this study only considers the stress changes inferred from the closest M_w 5.4 foreshock, the 2019 Ridgecrest mainshock was accompanied by multiple foreshocks, including the largest M_w 6.4 foreshock (e.g., Meng & Fan, 2021; Ross et al., 2019; Shelly, 2020). Although a single foreshock's perturbation may not be sufficient to dynamically trigger the mainshock, it might be possible to dynamically trigger the mainshock if the fault is sufficiently weakened due to prior seismicity.

4.3 What Controls the Mainshock Clock Change?

We investigate the dominant factors controlling the sign of the Δt estimate in the models presented here. First, to confirm that the mainshock clock change in the complex sequences of seismic and aseismic events cannot be fully explained by a simple analytic solution, we compare the change in time to instability (defined as $t_i = t_g - \Delta t$) measured from our simulations to that predicted from a 1D spring-slider solution (Fig. S9; Dieterich, 1994). We do not follow the exact formula but rather adopt the concept that an increase in stress may lead to an increase in slip rate and a reduction of the time to instability, acknowledging that the complex model setup in this study and the 1D spring slider solution are not directly comparable.

We apply the perturbation at $t_i = 16.2$ h before the target mainshock (event 282). After the perturbation using the "VSI, 340° strike" stress model, we measure a t_i of 11.7 h. The perturbation causes a quasi-constant increase in the slip rate of 4.8×10^{-8} m/s. Tracking the time in the unperturbed model when this increased slip rate is reached yields a much shorter time to instability (t_{D94}) of 2.7 h. The deviation of time to instability from the analytical solution has been documented for complex models, particularly for those involving a rheological transition from VW to VS (Kaneko & Lapusta, 2008), agreeing well with our models with multiple VW-to-VS transitions along the fault (Fig. S1c). The large discrepancy between these two estimates indicates that simple analytic solutions may not be suitable for predicting the triggering response on natural faults with complex earthquake and slow-slip transient history.

To discuss the question of what may control the mainshock clock change on a complex fault, we compare models that show clock advance and clock delay (Fig. 9). The clock advance and delay are obtained by perturbing target mainshocks at similar hypocentral depths of 4.38 km and 3.7 km in the aging law reference model (A2) and the A10 model, respectively, using the same stress perturbation (VSI, 340° strike). The perturbed aging law reference model yields a clock advance of 6 h (Fig. 9a), while the perturbed A10 model yields a mainshock clock delay of 6 h (Fig. 9b).

The key difference between these two cases lies in the depth extent of the ongoing aseismic slip at the time of the perturbation. The clock delay model shows a wider zone of aseismic slip ranging from ∼7 km to 15 km, while the clock advance model shows a narrower zone of aseismic slip confined near ∼11 km depth. This difference arises from the month-long foreshock sequence in the A10 model, although the two models share the same t_g of 16.2 h.

We recall that the static stress shadow occurs between 5 km and 10 km depth, overlapping with the depth extent of the aseismic slip in the clock delay model but not in the clock advance model (Fig. 9c). Since the perturbation does not induce significant slip, the ongoing aseismic slip controls the net amount of work done by each fault (i.e., δ in Eq. (7)). In all of our models, if the fault slips within the static stress shadow, W is neg-

ative, delaying the next earthquake (Fig. S5e). Conversely, in the clock advance model, W is positive, promoting the onset of the next earthquake.

To probe the robustness of this behavior, we perturb the same event in the aging law reference model with a much smaller t_g of 2 min, the time at which the afterslip from foreshocks is extended to the static stress shadow. Despite the proximity to the unperturbed event time, we observe a clock delay of 82 s, accompanied by a negative W value. This suggests that the complex interplay between background deformation and external stress perturbation governs the advancement and delay of a future large event.

We conduct two additional sets of simulations to verify that these findings are not dependent on the specific choice of parameters used in this study. In one of the two model setups, a lower loading velocity of 3.2×10^{-11} m/s is used (Fig. S10a), and in the other model, a fractal distribution with different minimum (30 m; order of L_∞) and maximum (order of 10 km; seismogenic zone width) limiting wavelengths is used (Fig. S10b). Both models involve foreshock-mainshock sequences connected by afterslip but with a different recurrence interval (from $\sim$ 76 yr in higher V_{pl} to $\sim$ 1915 yr in lower V_{pl}) and spatial pattern of afterslip. For a diverse combination of target mainshocks in both models and different stress perturbations, we obtain several hours of time advance when W is positive, while we obtain several days of time delay when W is negative. Thus, we conclude that the control of the sign of the static ΔCFS under regions of active aseismic slip on the mainshock clock advance and delay is not restricted to the specific set of parameters used in Section 3.

We find that the change in the mainshock clock is mostly controlled by the aseismic transfer of energy instead of the direct change from the perturbation itself. We explore how the stress perturbation changes the fault friction evolution by plotting a phase diagram (Fig. 10; Belardinelli et al., 2003; Dublanchet et al., 2013; Rice & Tse, 1986). We find that the fault is neither significantly brought closer to nor farther from the steady state during the perturbation period (pink lines in Fig. 10). Instead, the perturbed evolution curve deviates from the unperturbed evolution curve before the start of the foreshock-mainshock sequence (i.e., shallow SSE period; Fig. 10a) and during the foreshocks (Figs. 10b-c). During the mainshock, however, the evolution of friction in the perturbed and unperturbed models appears comparable (Fig. 10d). We observe similar behavior in several different scenarios, including the same target mainshock and stress perturbation pair with stress-dependent friction law and the clock delay model. The phase diagram suggests that foreshocks and aseismic slip can accommodate the changes induced by external perturbations, allowing the mainshock to follow a nearly identical limiting cycle.

These results highlight the crucial role of the interaction between external stress perturbations and ongoing background slip in earthquake triggering in complex earthquake sequences with realistic stress perturbations. The contribution of aseismic processes on earthquake triggering has also been suggested by previous studies (e.g., Cho et al., 2009; Gallovič, 2008; Inbal et al., 2023; Kostka & Gallovič, 2016).

4.4 Implications for the 2019 Ridgecrest Earthquake Sequence

The model results presented in this study may provide insights into key features observed in the 2019 Ridgecrest sequence. First, our results suggest that the foreshock sequence likely moved the 2019 Ridgecrest mainshock fault closer to failure and advanced its timing. Taufiqurrahman et al. (2023) inferred a ΔCFS increase of hundreds of kilopascals due to the M_w 6.4 foreshock at all depths near the Ridgecrest mainshock hypocenter. In the framework of W, this uniform increase in ΔCFS results in a positive W value regardless of the depth extent of background aseismic slip, likely advancing the clock of the mainshock rupture. This may suggest that the Ridgecrest mainshock fault is likely close to a runaway rupture at the time of the M_w 5.4 foreshock (Chen et al., 2020; Goldberg et al., 2020; S. Li et al., 2020; Pope & Mooney, 2020).

The analysis with varying t_g in Section 3.2 supports the idea that the mainshock fault was on the verge of runaway rupture at the time of the M_w 5.4 foreshock. For $t_g =$ 30 h (pink line in Fig.5), the model yields $t_i =\sim$ 15 h, comparable to the observed 16.2 h interval between the M_w 5.4 foreshock and the mainshock. This t_g value corresponds to 0.005 % of the $\sim$ 76 yr recurrence interval, suggesting the M_w 5.4 foreshock occurred in the final stage of the mainshock fault cycle.

Despite the mainshock fault being near failure, the M_w 5.4 foreshock did not immediately trigger a runaway rupture. This may be resembled by the lack of instantaneous triggering in our models, where for realistic stress perturbation amplitudes, the mainshock is not triggered immediately regardless of the source characteristic of the foreshock. Based on these results, a plausible explanation for the non-immediate triggering of the M_w 5.4 foreshock may be the insufficient amplitude of the stress perturbation.

In addition, the analysis using different stress perturbation amplitudes (Section 3.2) may provide insights into why the M_w 7.1 mainshock occurred on a relatively quiet fault. If the M_w 6.4 foreshock induced a large stress change relative to the quasi-static strength of the mainshock fault, it may have considerably altered the sequence on the mainshock fault. As shown in the example of moderately large amplitude perturbation (i.e., Fig. 6a), multiple partial ruptures can be triggered, cumulatively shortening a mainshock's recurrence interval and thus causing earlier mainshock rupture (Fig. S8).

4.5 Implications for Earthquakes within Stress Shadows

Classic Coulomb failure theory (e.g., Reasenberg & Simpson, 1992) predicts that 'stress shadows' (Harris & Simpson, 1996, 1998) move faults away from failure. However, numerous aftershocks, including large-magnitude events, occur within these regions (Felzer & Brodsky, 2005; Hori & Kaneda, 2001), complicating seismic hazard assessment. Several mechanisms have been suggested to explain these earthquakes occurring within a stress shadow region, including dynamic stress transfer, errors in Coulomb stress change calculations, rapid stress relaxation, and small-scale heterogeneities in background stress or fault geometry (Hardebeck & Harris, 2022; Hill et al., 1993; Hori & Kaneda, 2001; Marsan, 2006).

In this study, static ΔCFS often show negative values, even in cases when the mainshock clock advances, if measured at the target mainshock hypocenter depth in the unperturbed models (Fig. S11). The mainshock clock advances in regions of negative ΔCFS resemble earthquakes occurring within stress shadows.

These modeled mainshock clock advances within stress shadows are driven by stress transfer from foreshock sequences and/or aseismic slip. We show that the mainshock clock is largely controlled by the net energy gain or loss across the slipping fault due to external stress perturbations (W), governed by complex stress-slip interaction across different parts of the fault (Section 4.3). Even when a hypocenter locally experiences negative ΔCFS, the interplay between background aseismic slip and external stress perturbations could promote an earthquake, if the entire fault gained energy under the external stress perturbation. This mechanism may account for earthquakes occurring within stress shadows.

In addition, since both background aseismic slip and external stress perturbations are highly depth-dependent (Fig. 9c), focusing on a specific depth to assess the triggering potential might be misleading. We suggest that evaluating the response of the entire fault (e.g., through W analysis) may be required. Unfortunately, this is problematic in the case of natural faults, since a detailed knowledge of the in situ distribution of rate-and-state friction parameters is not readily available. This presents a significant challenge for deterministic models of earthquake triggering.

5 Conclusions

We combine dynamic rupture simulations and seismic cycle simulations to estimate the triggering response of the 2019 M_w 7.1 Ridgecrest mainshock to the stress perturbation from the M_w 5.4 foreshock. Detailed spatiotemporal stress changes near the mainshock nucleation site are computed using 3D dynamic rupture simulations, accounting for various fault geometries (mainshock fault strike and foreshock fault dip) and foreshock rupture dynamics.

Perturbing the seismic cycle models using the dynamic and static stress changes from the dynamic rupture simulations consistently results in a mainshock clock advance of several hours in most cases. Aging and slip law models show comparable mainshock clock advances, while stress-dependent aging law models exhibit a systematic reduction in clock advance.

Instantaneous triggering occurs only when the peak ΔCFS at the unperturbed hypocenter depth is increased to 17.5 MPa, comparable to excess strength during the quasi-static nucleation. The timing of the perturbation has little impact on instantaneous triggering or the mainshock clock change. In some cases, triggering is less efficient when the perturbation is applied later in the cycle.

We find a dominant influence of static ΔCFS on the mainshock clock change. Models perturbed using only the static component of stress change closely reproduce the mainshock clock change seen in models with both dynamic and static components, whereas the dynamic ΔCFS component alone results in a minor clock advance of only a few seconds.

We explain the mainshock clock advance and delay across all explored cases by the sign of the static ΔCFS in areas of accelerating slip, quantified by the W metric. Additionally, we find that a mainshock can be promoted if the entire fault gains energy under the stress perturbation (i.e., positive W), even when the future mainshock hypocenter depth is in a local static stress shadow. This is driven by a complex stress transfer from foreshock sequences and/or aseismic slip, suggesting a possible mechanism for earthquakes occurring within stress shadows

Finally, we infer that the M_w 6.4 foreshock of the 2019 Ridgecrest sequence likely moved the mainshock fault significantly closer to failure, based on the positive W value expected from the uniform increase of ΔCFS near the Ridgecrest mainshock hypocenter.

These results highlight the critical role of foreshock sequences and aseismic deformation in earthquake triggering and emphasize the importance of considering the physics of fault-system-wide, short- and long-term processes when assessing triggering potential.

Table 1. Parameters for the 3D dynamic rupture simulation using *SeisSol*. VFI: vertical foreshock fault, fast initiation; VSI: vertical foreshock fault, slow initiation; DFI: dipping foreshock fault, fast initiation; DSI: dipping foreshock fault, slow initiation.

Symbol	Parameter	Value			
		VFI	VSI	DFI	DSI
D_{LSW}	Critical slip-weakening distance	0.1 m	0.25 m	0.1 m	0.25 m
C_0	Frictional cohesion	0.2 MPa			
f_d	Dynamic friction coefficient				
	On nucleation patch	0.3743	0.3343	0.3328	0.2735
	On foreshock fault	0.471	0.431	0.4295	0.3702
	On mainshock fault	1000			
f_s	Static friction coefficient				
	On nucleation patch	$0.4433 - 0.4869$			
	On foreshock fault	$0.5841 - 0.7$			
	On mainshock fault	1000			
$\boldsymbol{\sigma}$	Initial stress tensor				
	Normal components ($\boldsymbol{\sigma}_{xx}$, $\boldsymbol{\sigma}_{yy}$, $\boldsymbol{\sigma}_{zz}$)	120 MPa			
	Along-strike shear component ($\boldsymbol{\sigma}_{xy}$)	70 MPa			
	Along-dip shear components ($\boldsymbol{\sigma}_{yz}$, $\boldsymbol{\sigma}_{xz}$)	0 MPa			

Table 2. Parameters used in the seismic cycle models using *Tandem*. Parameters a, D_{RS}, and σ_n^0 show their average value, as these parameters include fractal heterogeneity. A2: 'A'ging law model with $\overline{D_{RS}} = 2$ mm, S10: 'S'lip law model with $\overline{D_{RS}} = 10$ mm, A10: 'A'ging law model with $\overline{D_{RS}} = 10$ mm.

Symbol	Parameter	Value
$\overline{a}$	Rate-and-state parameter, direct effect	Variable (see Fig. S1c)
b	Rate-and-state parameter, evolution effect	0.019
$\overline{D_{RS}}$	Characteristic state evolution distance	2 mm (A2) 10 mm (S10 & A10)
f_0	Reference coefficient of friction	0.6
V_0	Reference slip rate	10^{-6} m/s
V_{init}	Initial slip rate	10^{-9} m/s
V_{pl}	Plate loading rate	10^{-9} m/s
$\overline{\sigma_n^0}$	Background effective normal stress	50 MPa (see Fig. S1b)
τ^0	Background shear stress	10 - 30 MPa
μ	Bulk shear modulus	20 GPa
ν	Poisson's ratio	0.25
W	Seismogenic zone width*	$\sim$ 10 km
L_f	Fault length	24 km

* May slightly vary due to fractal heterogeneity (see Fig. S1).

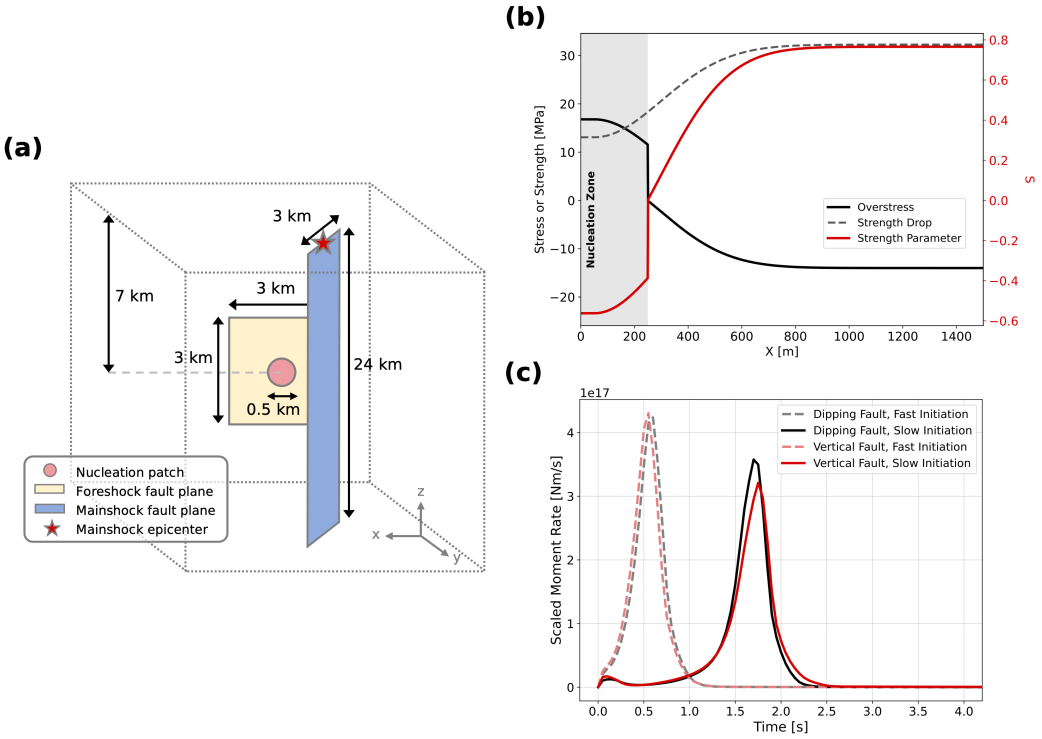

Figure 1. (a) Sketch of the model geometry for the 3D dynamic rupture simulation using *SeisSol*. The foreshock fault (yellow), mainshock fault (blue), and circular nucleation patch (pink) are shown. The red star denotes the location of the 2019 M_w 7.1 Ridgecrest mainshock epicenter. The sketch is not to scale with respect to depth (the z-axis). (b) An example of the prestress conditions used to nucleate the M_w 5.4 foreshock in the vertical foreshock fault and the slow initiation (VSI) model. The overstress (black line), the relative strength parameter S (Eq. (2); red line), and the strength drop (grey dashed line) are shown along a profile across the foreshock plane from its center to its edge. The grey shaded area indicates the extent of the nucleation patch. (c) Moment rate functions for the four classes of dynamic rupture models, classified by the combination of rupture characteristics (dashed lines for fast initiation and solid lines for slow initiation) and the dip of the foreshock fault (red hues for vertical foreshock fault and black hues for dipping foreshock fault). The moment rates are scaled by the expected moment from an M_w 5.4 earthquake (i.e., $M_{5.4}$).

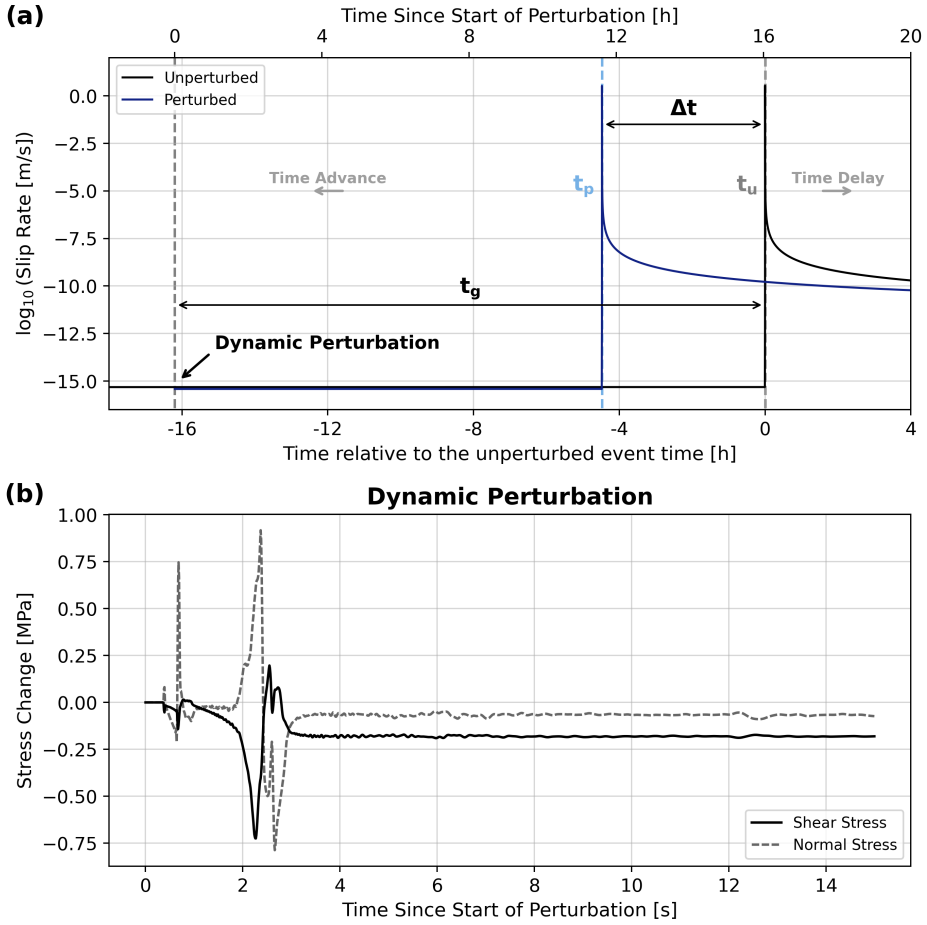

Figure 2. Illustration of the process for estimating the triggering response (Section 2.3). (a) Slip rate evolution of the unperturbed model (black) and the perturbed model (dark blue) at the mainshock hypocenter depth in the unperturbed model (7.82 km). Grey and light blue dashed lines indicate the time of the unperturbed (t_u) and perturbed (t_p) system-size earthquakes, respectively. The vertical arrow marks the timing of the applied dynamic perturbation, while the horizontal arrows represent the clock advance (Δt) and the time interval between the perturbation and the unperturbed mainshock time (t_g). (b) The applied dynamic stress changes at the depth of the unperturbed target mainshock hypocenter. The solid line represents the change in shear stress ($\hat{\tau}$), while the dashed line shows the change in normal stress ($\hat{\sigma_n}$). This example is generated by perturbing target mainshock event 282 (Fig. S2a) in the reference aging law seismic cycle model using the dynamic stress perturbation from the dynamic rupture model with the vertical foreshock fault, slow initiation (VSI) with 340° strike orientation of the mainshock fault.

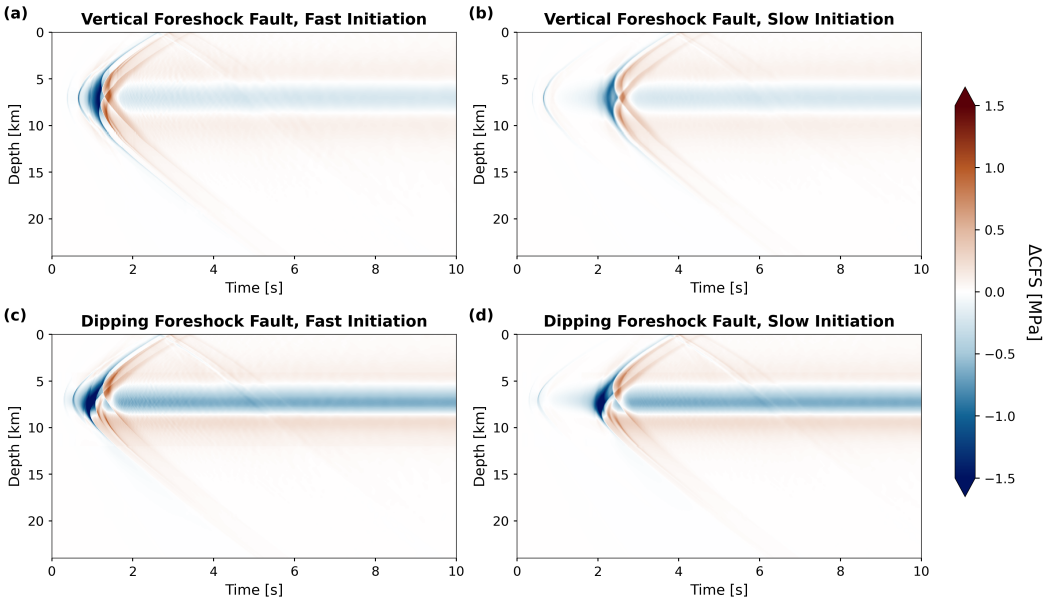

Figure 3. Spatiotemporal evolution of ΔCFS along the mainshock fault in 3D dynamic rupture models for (a) VFI, (b) VSI, (c) DFI, and (d) DSI models. All four models assume a mainshock fault strike of 340°. (VFI: vertical foreshock fault, fast initiation; VSI: vertical foreshock fault, slow initiation; DFI: dipping foreshock fault, fast initiation; DSI: dipping foreshock fault, slow initiation.)

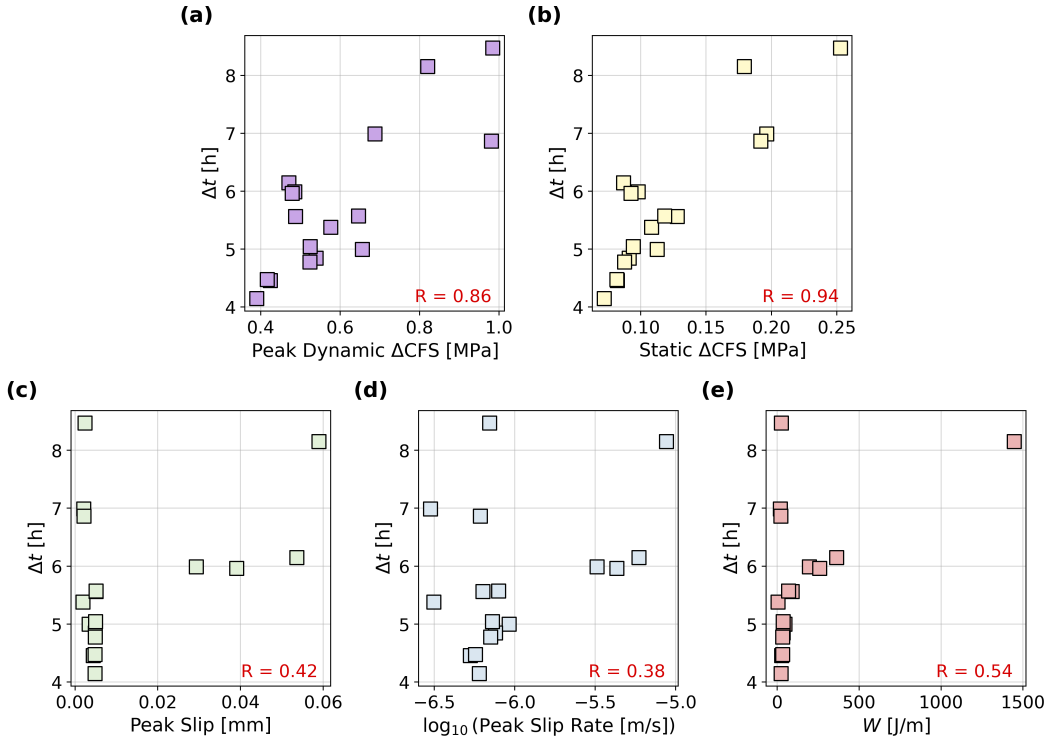

Figure 4. Correlation between the mainshock clock change (Δt) and various physical parameters obtained from all explored cases with the aging law reference model: (a) peak dynamic ΔCFS , (b) static ΔCFS , (c) peak slip, (d) peak slip rate, and (e) work per distance, W (Eq. (7)). All five parameters are estimated during the 15 s perturbation period. The ΔCFS values are measured at a depth corresponding to the maximum aseismic slip during the perturbation period in each simulation (i.e., z_{max}), while the other three parameters are measured along the entire fault. The Pearson correlation coefficient R is shown in the bottom right corner of each panel.

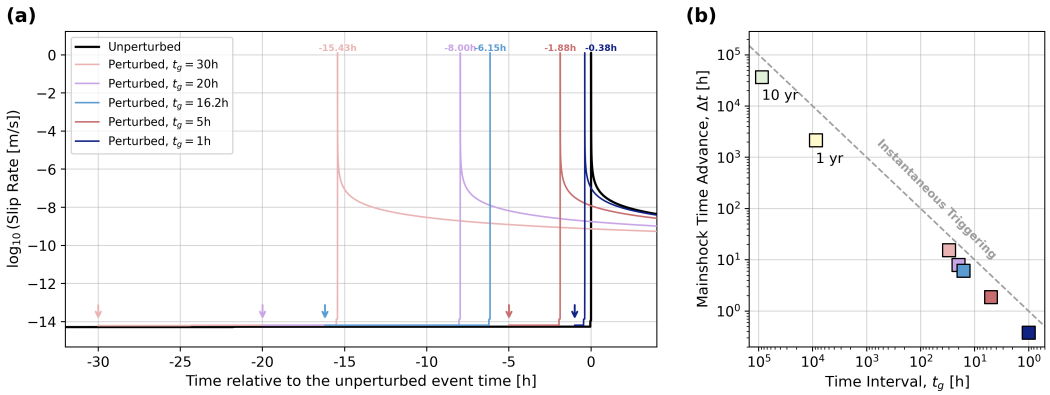

Figure 5. Comparison of triggering responses for different perturbation timings (t_g). (a) Slip rate at the mainshock hypocenter depth in the unperturbed model (4.38 km), for varying t_g values, ranging from 10 yr (light green) to 1 h (dark blue). Vertical arrows mark the timing of the applied dynamic perturbation for each t_g. (b) Relationship between the mainshock clock change (Δt) and the timing of perturbation. The grey dashed line indicates the expected Δt values for instantaneous triggering. Panels (a) and (b) share the same color scheme for each t_g. These examples are generated by perturbing target mainshock event 88 (4.38 km; Fig. 9a) in the reference aging law seismic cycle model using the stress perturbation from the dynamic rupture model with a vertical foreshock fault, slow initiation (VSI), and a 340° strike orientation of the mainshock fault.

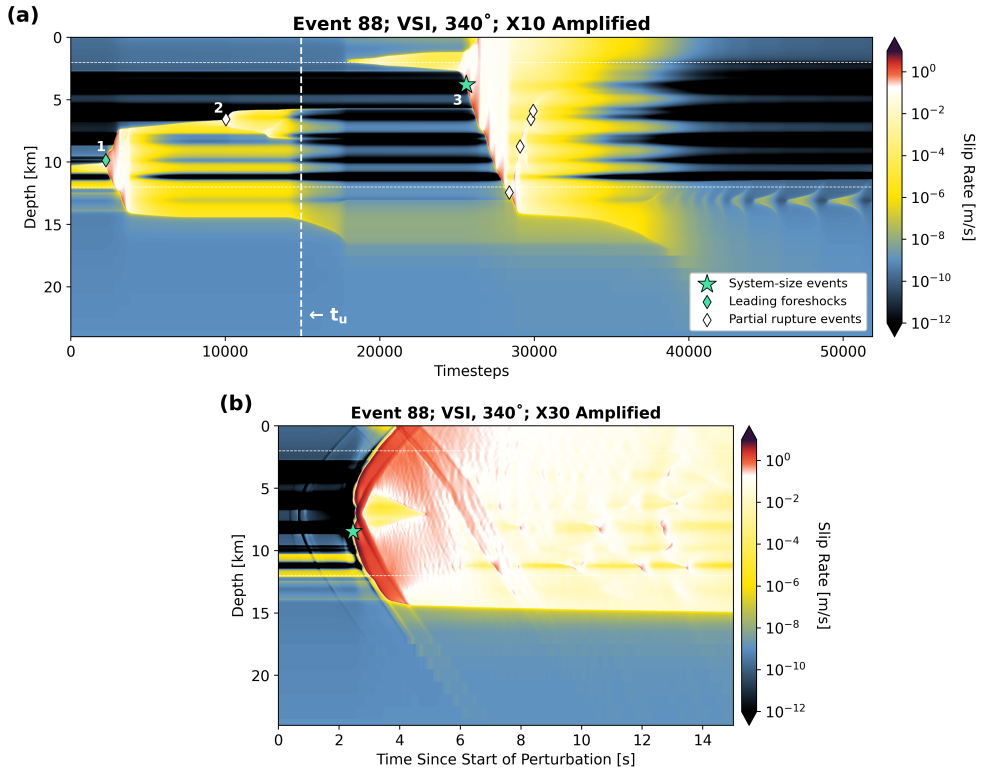

Figure 6. Spatiotemporal evolution of slip rate after applying stress perturbations with scaled amplitudes. (a) Result of the 10-times amplified stress model, where new events 1 and 2 occur 22 min and 1.6 h after the initiation of the perturbation, respectively. A new system-size earthquake (new event 3) occurs approximately 74 days later than the target mainshock in the unperturbed model. (b) Result of the 30-times amplified stress model, where a system-size earthquake is triggered $\sim$ 2.5 s after the start of the perturbation. Green stars, green diamonds, and white diamonds indicate the hypocenter locations of system-size earthquakes, leading foreshocks, and partial rupture events, respectively. Both stress perturbation models are scaled versions of the stress perturbation from the dynamic rupture model with a vertical foreshock fault, slow initiation (VSI), and a 340° strike orientation of the mainshock fault. These examples are generated by perturbing target mainshock event 88 (4.38 km; Fig. 9a) in the reference aging law seismic cycle model.

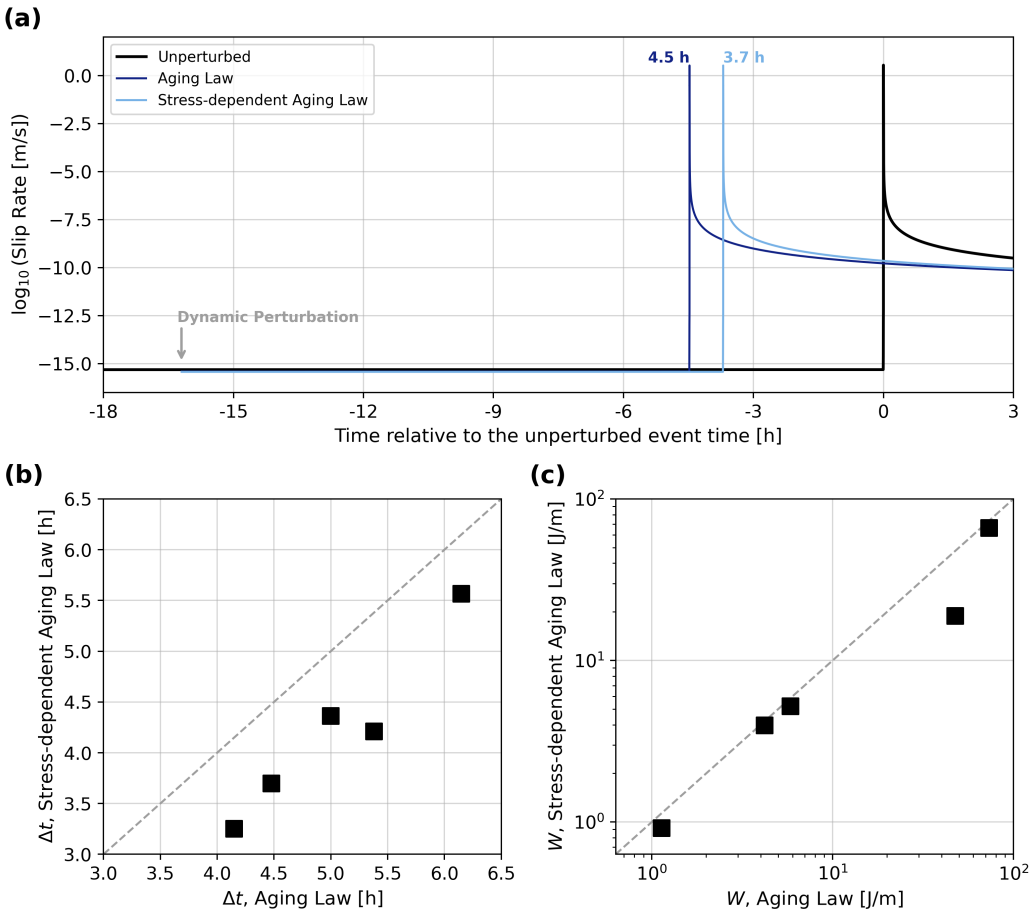

Figure 7. Comparison of seismic cycle models using the aging law (Eq. (4)) versus the stress-dependent aging law (Eq. (6)) during the perturbation period. (a) Slip rate at the mainshock hypocenter (7.82 km) in the unperturbed model (black) and perturbed models with the aging law (dark blue) and the stress-dependent aging law (light blue). This example perturbs target event 282 (Fig. S2a) using a dynamic rupture model with vertical foreshock fault, slow initiation (VSI), and 340° strike orientation of the mainshock fault. (b-c) Comparison of the mainshock clock changes (Δt, panel b) and the work per distance values (W, panel c) produced by both models. The grey dashed lines in both panels indicate a 1-to-1 relationship. Systematically smaller Δt and W values are obtained when using the stress-dependent aging law.

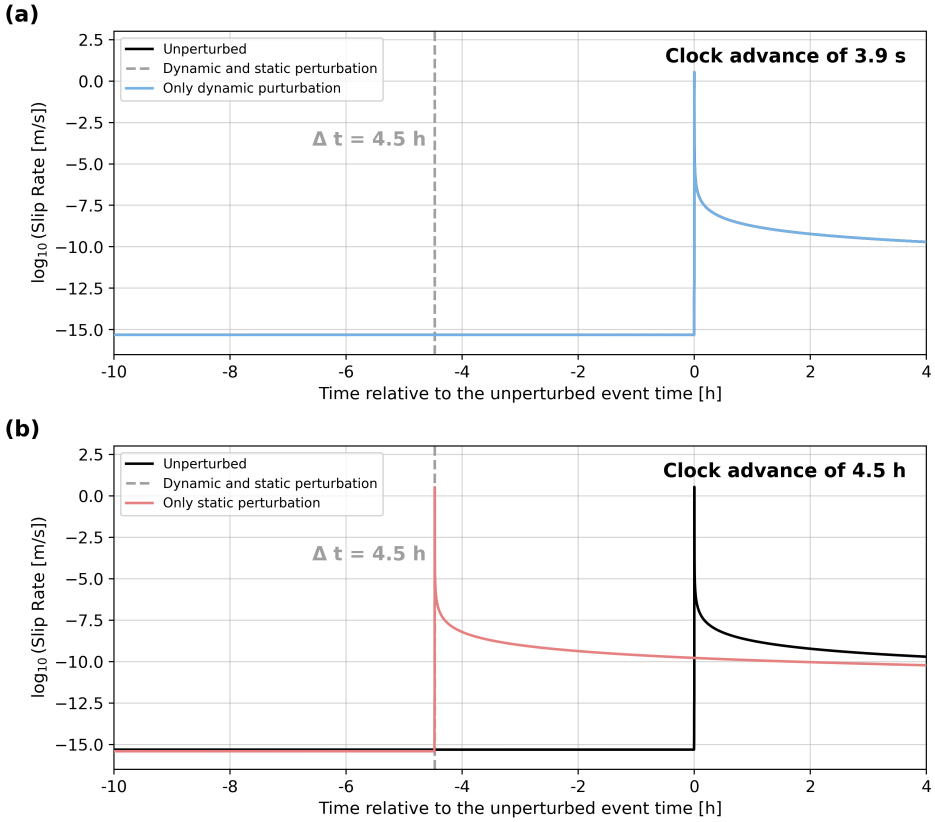

Figure 8. Comparison of the evolution of slip rate when perturbed by both dynamic and static components of ΔCFS (grey) with the slip rate when perturbed by (a) only the dynamic component of ΔCFS (see Fig. S7a) and (b) only the static component of ΔCFS (see Fig. S7b). The black line in both panels shows the slip rate evolution of the unperturbed model. These examples are generated by perturbing target mainshock event 282 (7.82 km; Fig. S2a) in the reference aging law seismic cycle model using the stress perturbation from the dynamic rupture model with a vertical foreshock fault, slow initiation (VSI), and a 340° strike orientation of the mainshock fault.

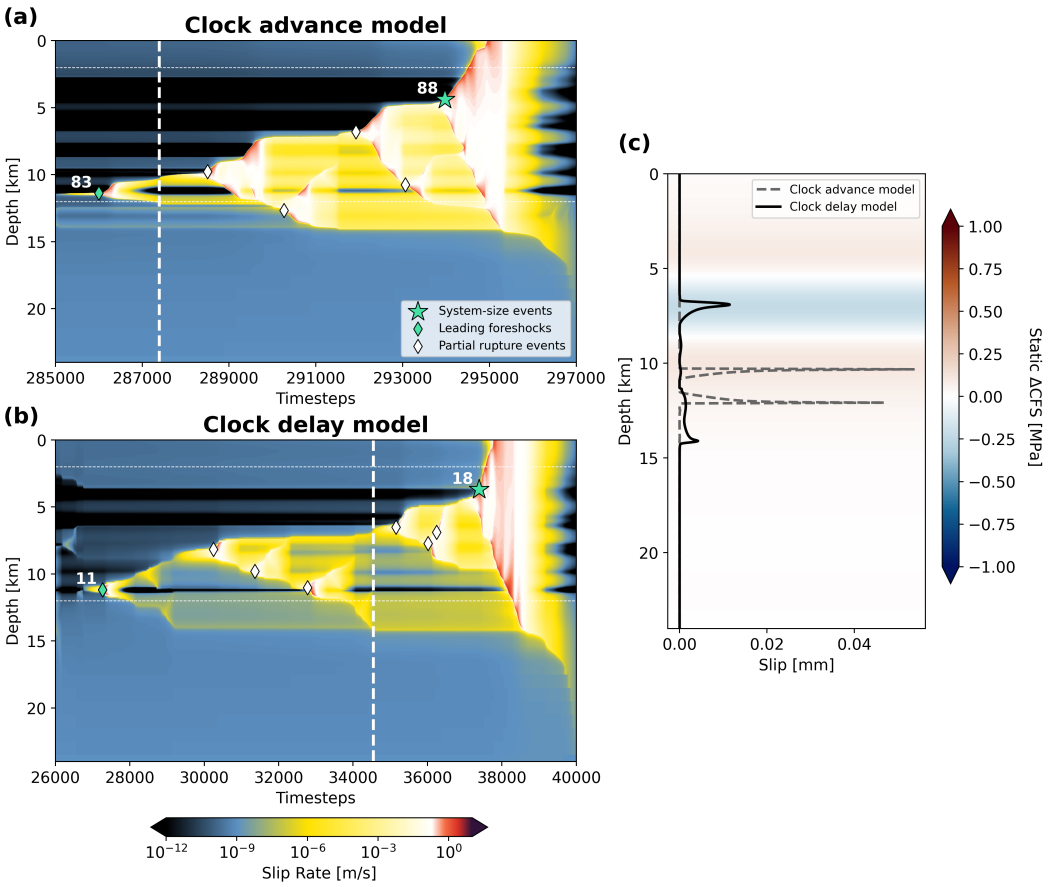

Figure 9. (a-b) Comparison of the spatiotemporal evolution of slip rate for models with (a) mainshock clock advance (aging law reference model; target mainshock event 88) and (b) mainshock clock delay (A10 model; target mainshock event 18). Both models are perturbed using the same stress perturbation (VSI, 340° strike mainshock fault orientation). The white dashed line in both panels indicates the time when the dynamic perturbation is applied. Green stars, green diamonds, and white diamonds indicate the hypocenter locations of system-size earthquakes, leading foreshocks, and partial rupture events, respectively. (c) Net slip during the perturbation period for the clock advance (dashed lines) and clock delay (solid) models overlaying the static ΔCFS along the entire fault. In the clock advance model, the maximum slip during the perturbation period occurs predominantly under positive static ΔCFS , while in the clock delay model, it occurs predominantly in the static stress shadow. (VSI: vertical foreshock fault, slow initiation.)

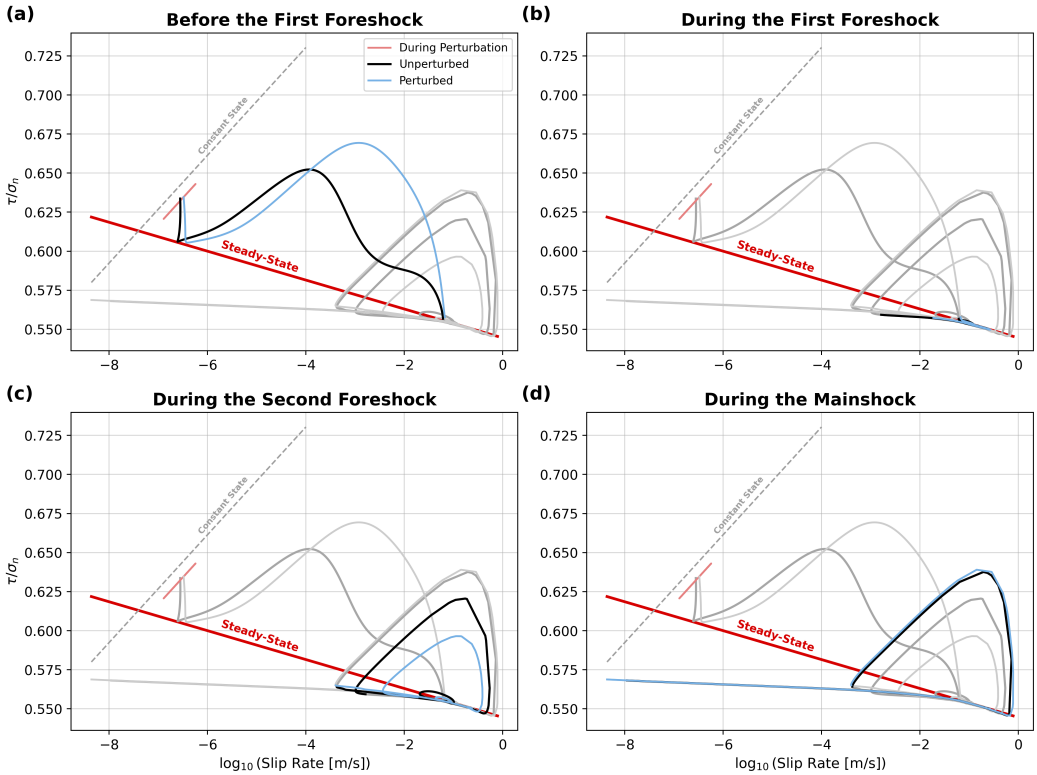

Figure 10. Phase diagram comparing the evolution of friction (shear stress over normal stress) as a function of slip rate for unperturbed model (black) and perturbed model (blue). The scenario perturbs event 282 (Fig. S2a) in the aging law reference model using the stress perturbation from the dynamic rupture model with a vertical foreshock fault, slow initiation (VSI), and a 340° strike orientation of the mainshock fault. For clarity, the diagram is divided into four stages: (a) before the first foreshock when shallow SSEs are dominant, (b) during the first foreshock (event 280 in Fig. S2a), (c) during the second foreshock (event 281 in Fig. S2a), and (d) during the system-size earthquake (i.e., mainshock, event 282 in Fig. S2a). The red solid line indicates the steady state, and the grey dashed line indicates the constant state variable contour. The incomplete cycle in panel (a) represents the shallow SSEs preceding the foreshock-mainshock sequence while panels (b) through (d) show well-developed limiting cycles of each earthquake. Friction and slip rate are measured at a depth corresponding to the maximum aseismic slip during the perturbation period ($z_{max} = 3.44$ km).

6 Open Research

All data required for reproducing the *SeisSol* dynamic rupture models and *Tandem* seismic cycle models can be downloaded from the Zenodo repository, [redacted]. The open-source software *SeisSol* is available at `https://github.com/SeisSol/SeisSol`. We use *SeisSol* commit tag #e6ef661 in the master branch. The open-source software *Tandem* is available at `https://github.com/TEAR-ERC/tandem`. We use dmay/seas-checkpoint branch (commit #1dc36db; `https://github.com/TEAR-ERC/tandem/tree/dmay/seas-checkpoint`) for aging law simulations and jyun/state-law branch (commit #5d5c63f; `https://github.com/TEAR-ERC/tandem/tree/jyun/state laws`) for slip law simulations. The location, timing, and focal mechanism of the 2019 Ridgecrest M_w 7.1 and M_w 5.4 earthquakes are retrieved from the U.S. Geological Survey Advanced National Seismic System Comprehensive Earthquake Catalog (ANSS ComCat) webpage (USGS, 2017, last accessed on 25 Aug, 2024).

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Supporting Information for "Controls of Dynamic and Static Stress Changes and Aseismic Slip on Delayed Earthquake Triggering: Application to the 2019 Ridgecrest Earthquake Sequence"

Jeena Yun[1], Alice-Agnes Gabriel[1,2], Dave A. May[1], and Yuri Fialko[1]

[1]Scripps Institution of Oceanography, University of California San Diego, La Jolla, CA, USA

[2]Department of Earth and Environmental Sciences, Ludwig-Maximilians Universität München, Munich, Germany

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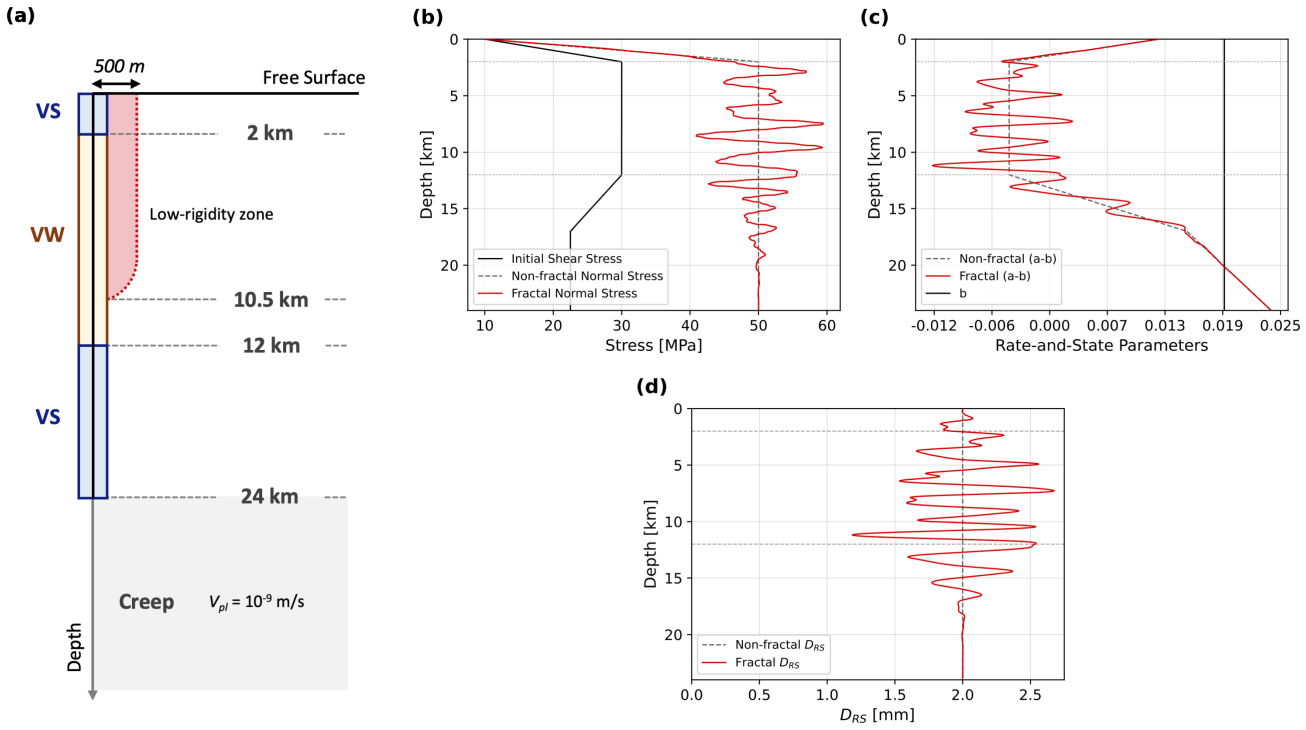

Figure S1. (from Yun et al., 2025) (a) Sketch of the model geometry for the seismic cycle simulations using *Tandem*. The rate-and-state fault (black vertical line) includes a central velocity-weakening zone (yellow) surrounded by shallow and deep velocity-strengthening zones (blue). The bottom creep zone governed by the constant loading rate (V_{pl}) is shaded in grey. The red-shaded area indicates the spatial extent of a low-rigidity fault zone. As the model represents a perfectly symmetric vertical strike-slip fault, we model only one side of the domain. (b-d) Self-affine fractal distributions of (b) initial effective normal stress, (c) rate-and-state parameters, and (d) characteristic state evolution distance, that parameterize the aging law reference model (A2 model; see Section 2.1 in the main text). The fractal distributions of all three parameters share the same limiting wavelengths of $\lambda_{min} = 500$ m and $\lambda_{max} = 2.5$ km.

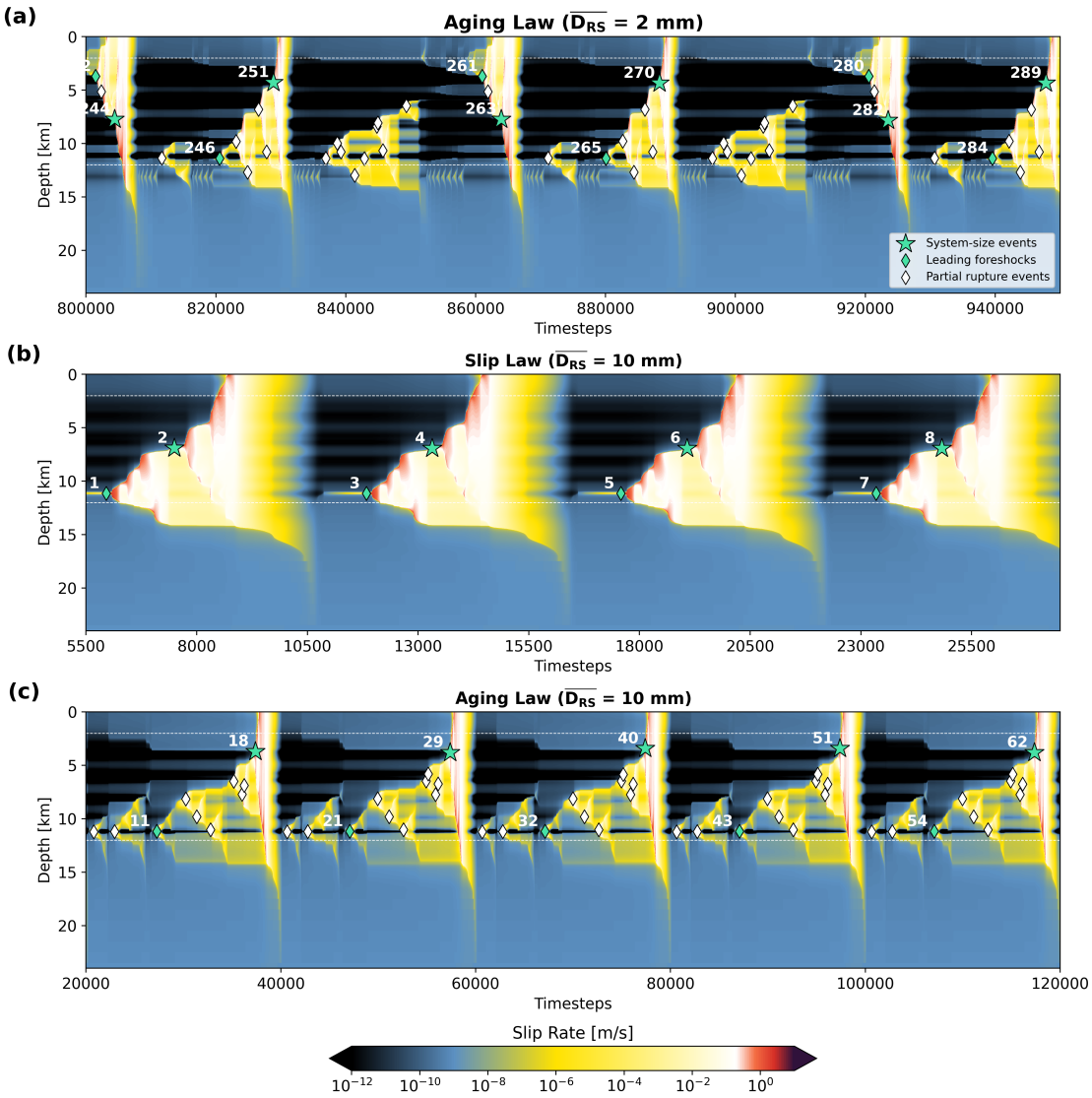

Figure S2. Spatiotemporal evolution of slip rate of reference seismic cycle models used in this study. (a) Reference aging law seismic cycle model (A2 model), showing the period between 2,317 yr and 2,681 yr of simulation time. (b) Reference slip law seismic cycle model (S10 model) and (c) the equivalent aging law model (A10 model). See Section 2.1 in the main text for detailed model descriptions. Event numbering starts from a non-zero value since we only show the spun-up phase of the models, i.e., after 200 yr of simulation time. Green stars, green diamonds, and white diamonds indicate the hypocenter locations of system-size earthquakes, leading foreshocks, and partial rupture events, respectively.

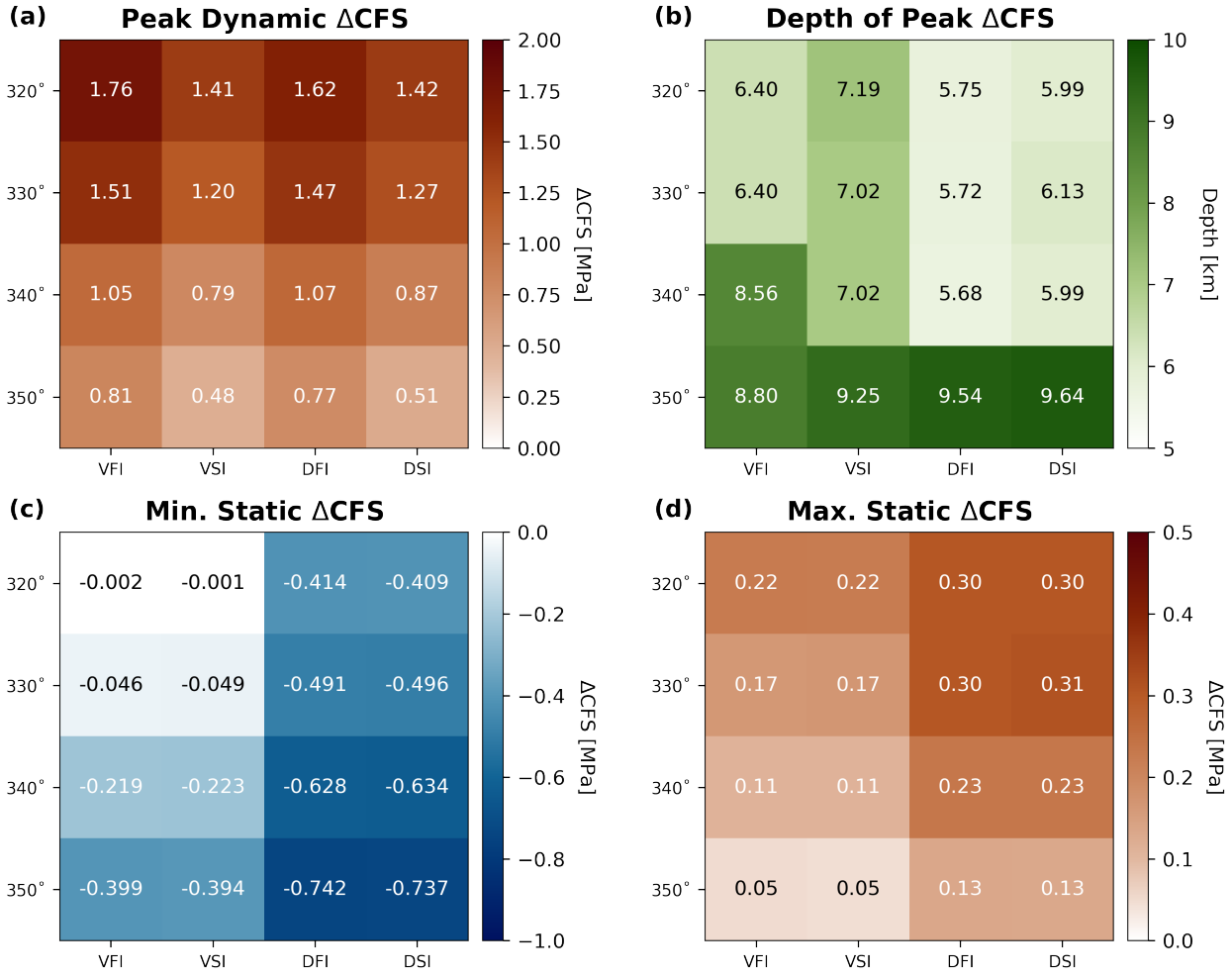

Figure S3. Summary of key values obtained from all 3D dynamic rupture models: (a) peak dynamic ΔCFS , (b) depth corresponding to the peak dynamic ΔCFS , (c) minimum static ΔCFS and (d) maximum static ΔCFS . (VFI: vertical foreshock fault, fast initiation; VSI: vertical foreshock fault, slow initiation; DFI: dipping foreshock fault, fast initiation; DSI: dipping foreshock fault, slow initiation.)

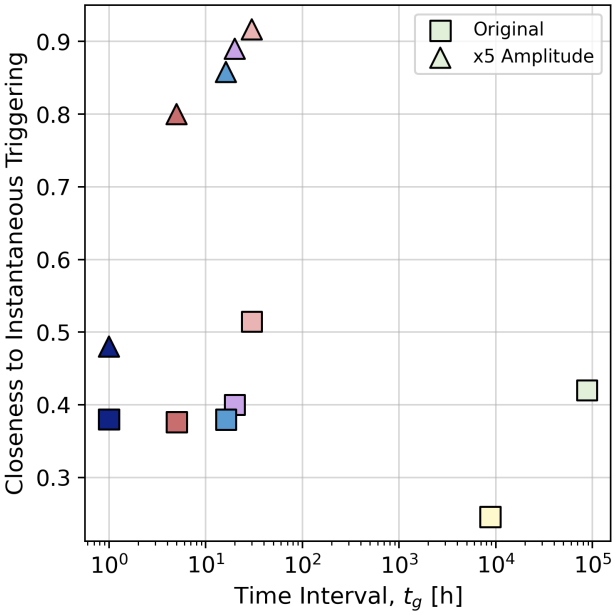

Figure S4. Closeness to instantaneous triggering (see Section 3.2 in the main text) for different perturbation timings (t_g). The squares represent the same seismic cycle simulations shown in Figure 5 in the main text while the triangles represent the seismic cycle simulations perturbing the same target event with 5-times amplified stress perturbation. The color scheme is identical to that in Figure 5 in the main text.)

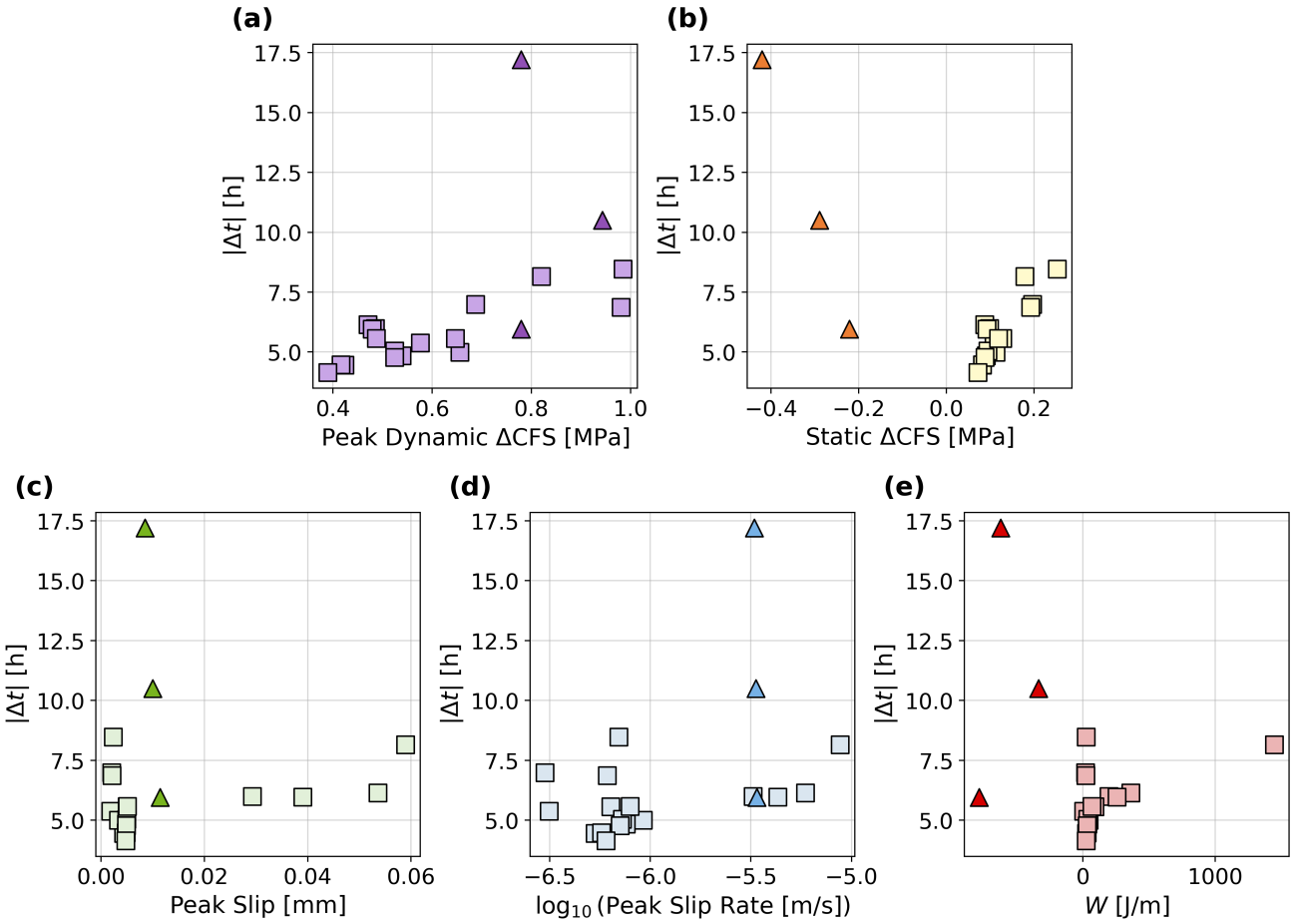

Figure S5. Same as Figure 4 in the main text (squares), but including clock delay models (triangles). For clarity, the absolute value of the mainshock clock change ($|\Delta t|$) is shown in the y-axis. A clear distinction between the clock advance models (squares) and the clock delay models (triangles) is observed in static ΔCFS (panel b) and work per distance, W (panel e).

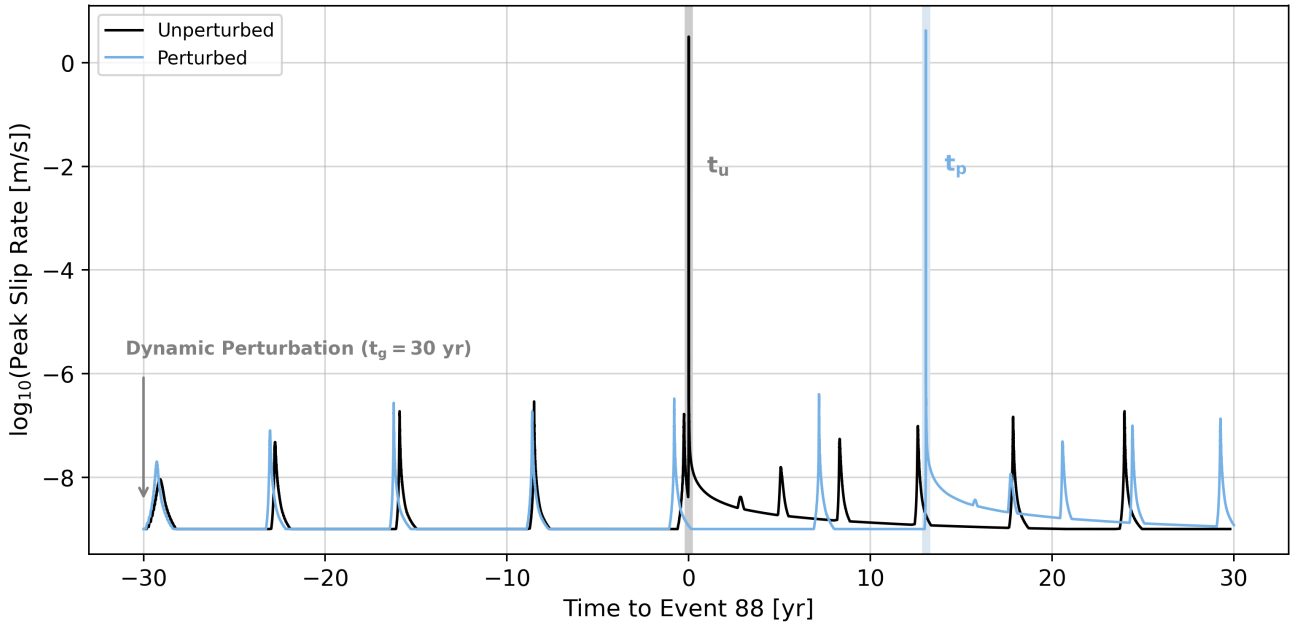

Figure S6. Peak slip rate of the unperturbed model (black) and perturbed model (blue) with $t_g = 30$ yr (grey arrow), showing ~ 13 yr delay of the mainshock. The example simulation shown here is identical to that in Figure 5 in the main text.

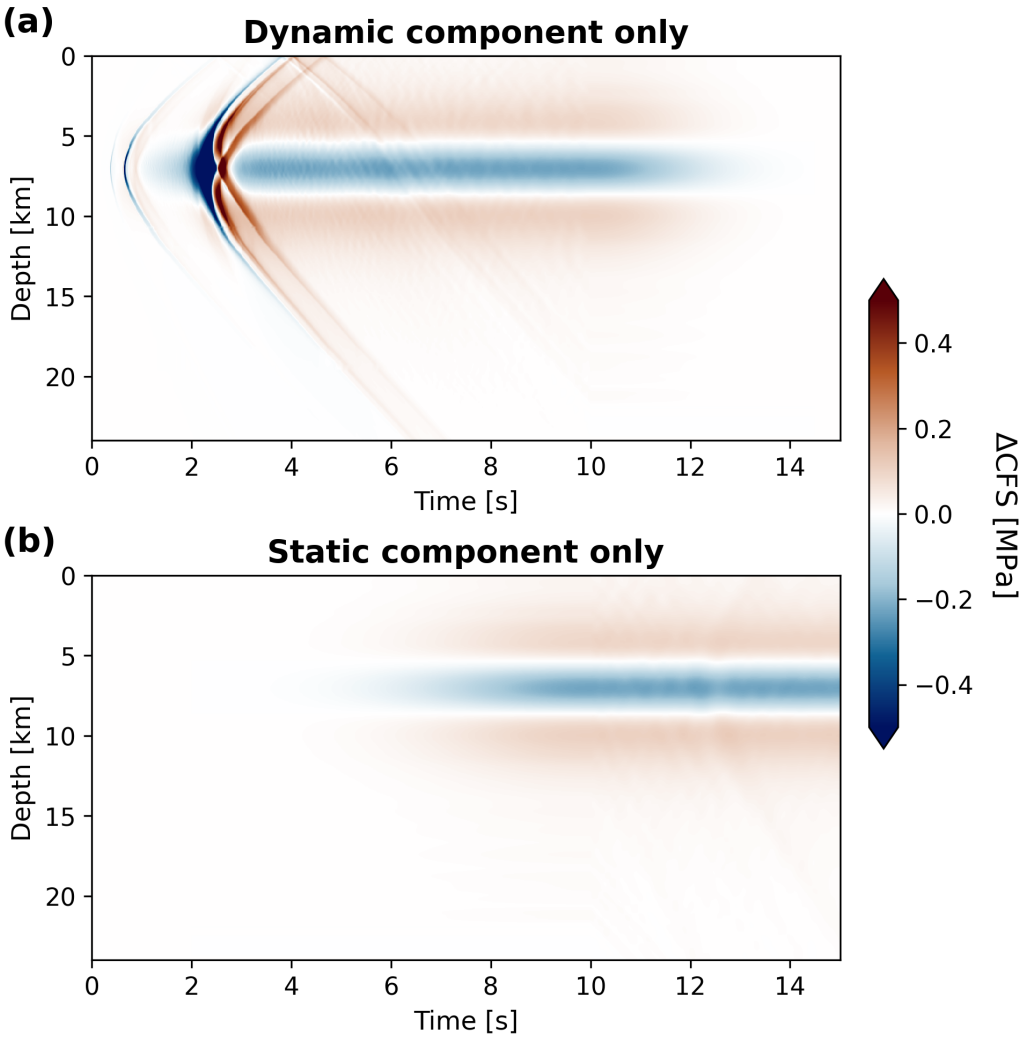

Figure S7. Spatiotemporal evolution of ΔCFS along the mainshock fault in 3D dynamic rupture models for models with (a) only the dynamic component of ΔCFS and (b) only the static component of ΔCFS . Panels (a) and (b) are utilized to generate perturbed seismic cycle models shown in Figures 8a and 8b in the main text, respectively.

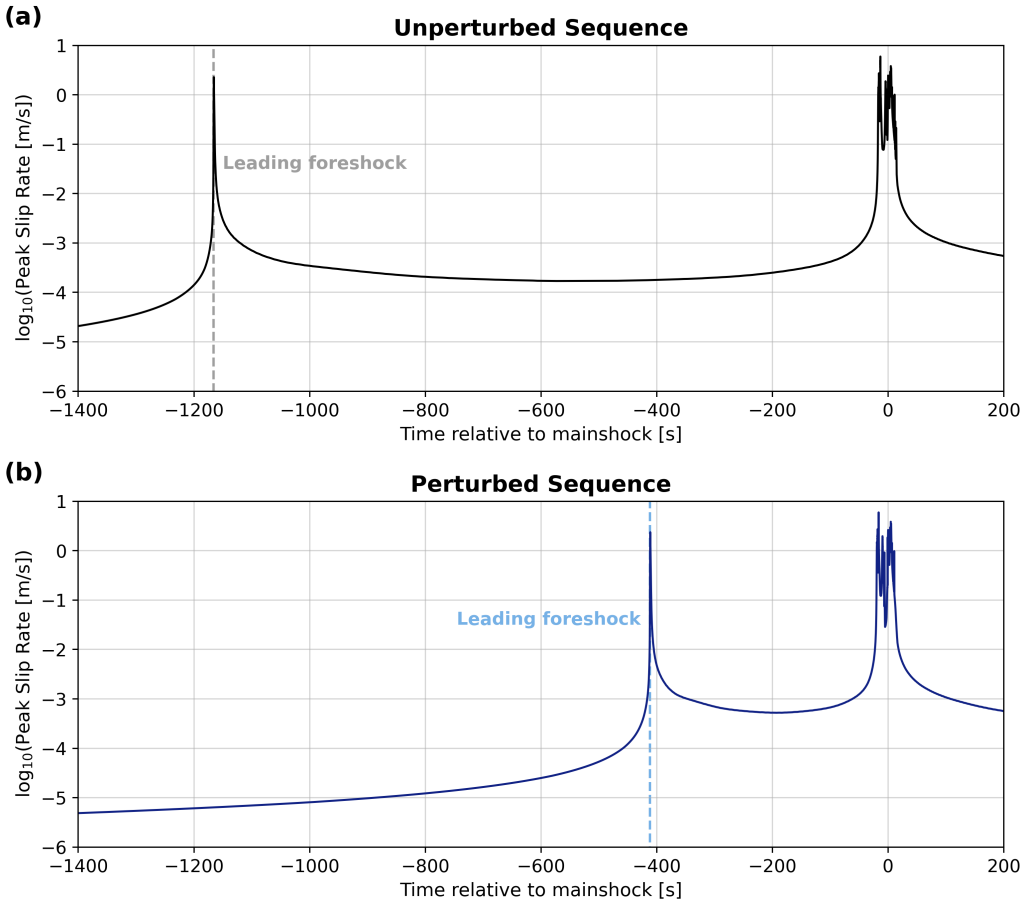

Figure S8. Shortening of the duration of the cascading foreshock-mainshock sequence in the seismic cycle model. Peak slip rate evolution of (a) the unperturbed model and (b) the perturbed model. The time from the leading foreshock (dashed lines) to the mainshock (zero in x-axis) reduces from 1,166 s in the unperturbed sequence (a) to 411 s in the perturbed sequence (b). This example is generated by perturbing event 120 (at 6.5 km depth) in the reference aging law seismic cycle model using the stress perturbation from the dynamic rupture model with the vertical foreshock fault, slow initiation (VSI) with 340° strike orientation of the mainshock fault.

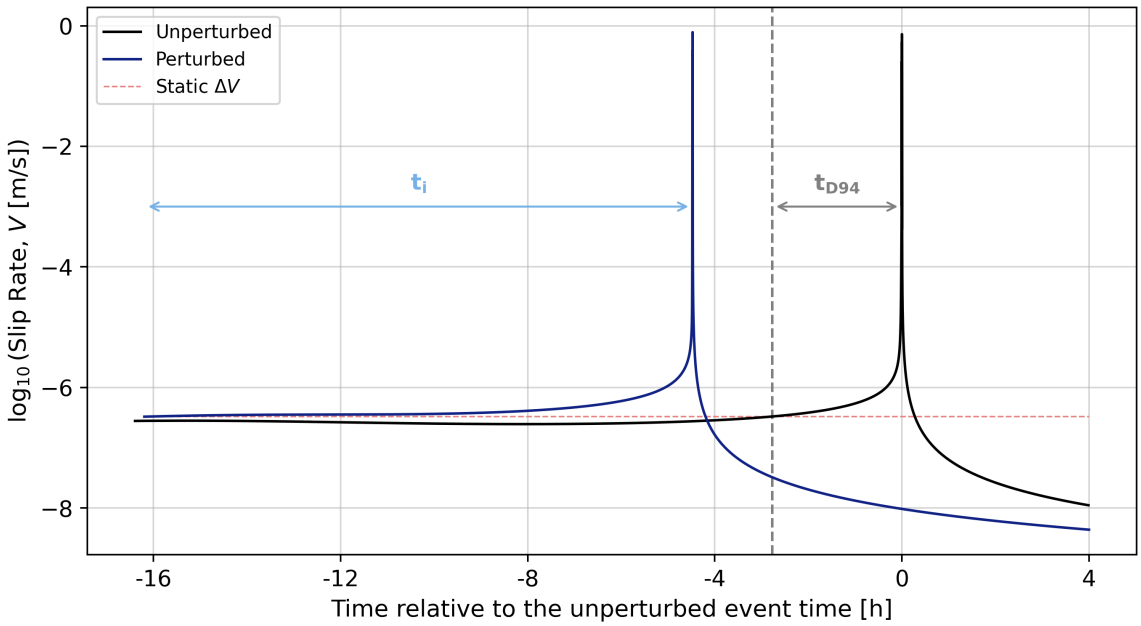

Figure S9. Comparison of time to instability measured from our seismic cycle simulation (t_i, blue arrow) to that predicted from a 1D spring-slider solution (t_{D94}, grey arrow; Dieterich, 1994). Slip rate evolution of the unperturbed model (black) and the perturbed model (dark blue) is obtained at a depth corresponding to the maximum aseismic slip during the perturbation period in each simulation ($z_{max} = 3.44$ km). The pink dotted line shows the quasi-constant increase in slip rate due to the perturbation and the grey dashed line marks the time when the slip rate in the unperturbed model reaches the increased slip rate. This example is generated by perturbing target mainshock event 282 (at 7.82 km depth; Fig. S2a) using the dynamic stress perturbation from the dynamic rupture model with the vertical foreshock fault, slow initiation (VSI) with 340° strike orientation of the mainshock fault.

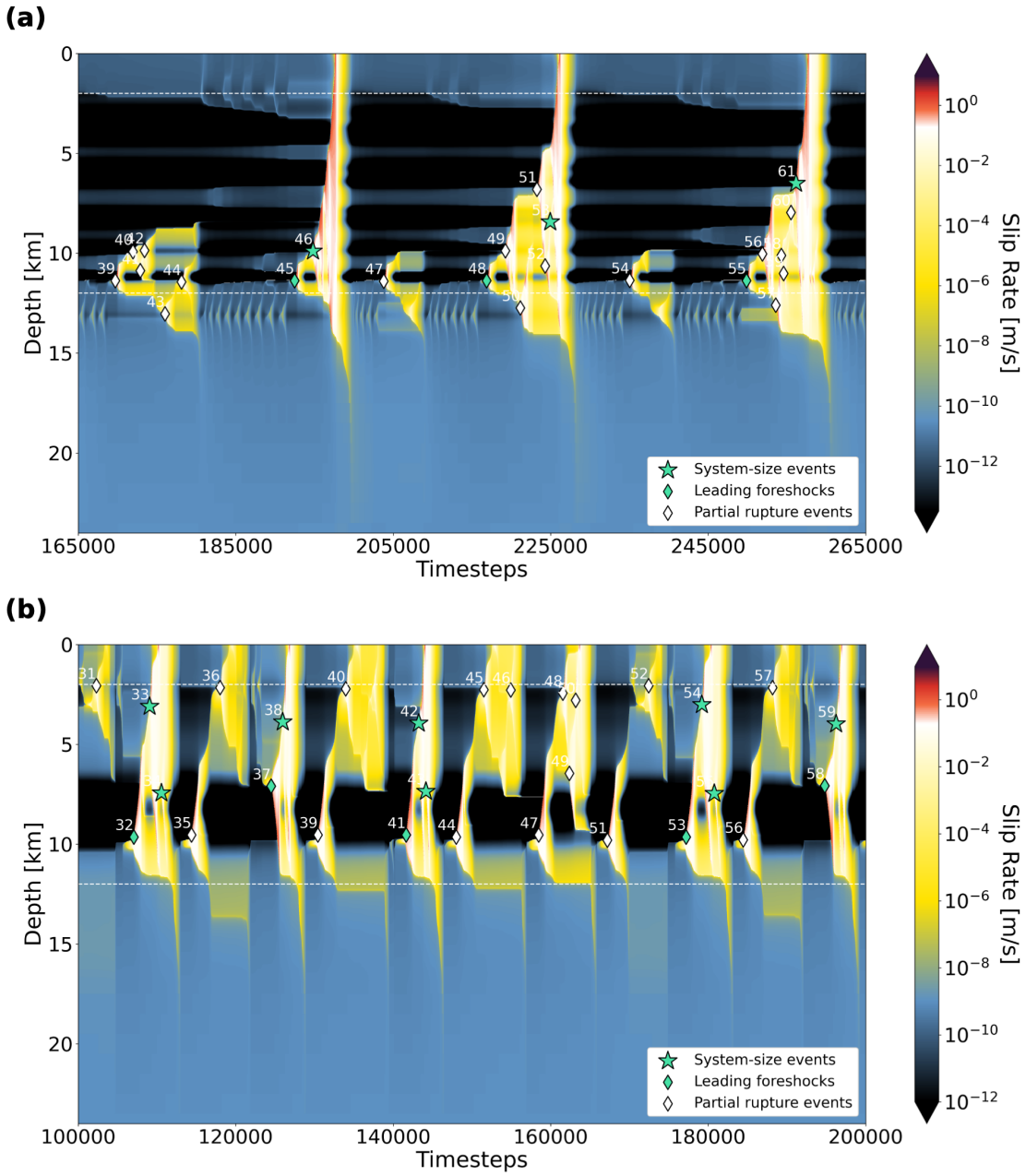

Figure S10. Spatiotemporal evolution of slip rate for seismic cycle models with different parameterization. (a) Seismic cycle model with $V_{pl} = 3.2 \times 10^{-11}$ m/s, showing the period between 11,520 yr and 19,880 yr of simulation time. (b) Seismic cycle model with fractal heterogeneity in all three parameters using limiting bandwidths of $\lambda_{min} = 30$ m and $\lambda_{max} = 10$ km, showing the period between 338 yr and 710 yr of simulation time. The color scheme and marker usage are identical to those in Figure S2.

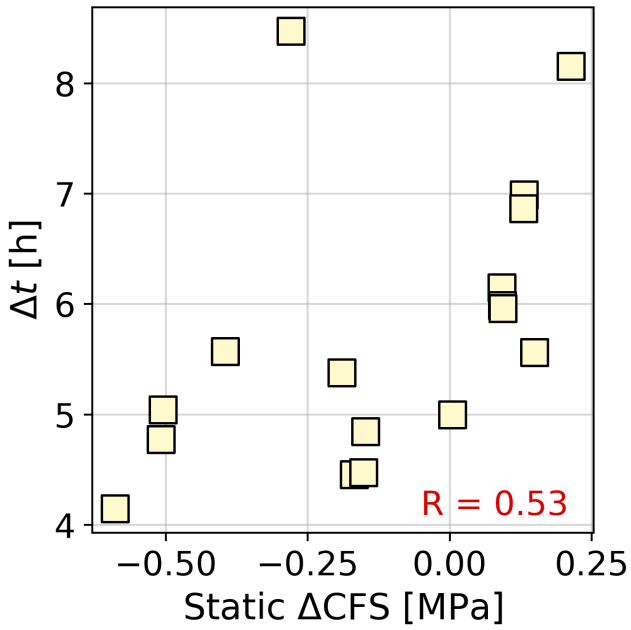

Figure S11. Same as Figure 4b in the main text, but measured at the target hypocenter depth in each unperturbed model. Note negative static ΔCFS values even for mainshock clock advance models (i.e., $\Delta t > 0$).