# **Predictive modeling of seismic wave fields: Learning the trans-** <sup>1</sup> **fer function using encoder-decoder networks** <sup>2</sup>

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## **Abstract:** <sup>7</sup>

Wouldn't it be beneficial if we could predict the time series at a seismic station even if the station no longer 8 exists? In geophysical data analysis, this capability would enhance our ability to study and monitor seismic events 9 and seismic noise, particularly in regions with incomplete station coverage or where stations are temporarily offline. 10 This study introduces a novel adaption of encoder-decoder networks from the subfield of Deep Learning, modified 11 to predict the development of seismic wave fields between two seismic stations. Using one-dimensional time series 12 measurements, our algorithm aims to learn and predict signal transformations between the two stations by 13 approximating the transfer function. Initially, we evaluate this proof of concept in a simplified controlled setting 14 using synthetic data, before we incorporate field data gathered at a seismic exploration site in an area containing 15 several roads, wind turbines, oil pump jacks and railway traffic. Across diverse scenarios, the model demonstrates 16 proficiency in learning the transfer function among various seismic station configurations. Particularly, it achieves 17 high accuracy in predicting a majority of seismic wave phases across different datasets. Diverging significantly from 18 encoder-decoder networks that estimate time series forecasts by analysing historical trends, our approach places 19 greater emphasis on the wave propagation between nearby locations. Thereby, the analysis incorporates both phase 20 and amplitude information and provides a new approach to approximate the transfer function relying on Machine 21 Learning techniques. The gained knowledge enables to reconstruct data from missing, offline, or defunct stations in 22 the context of temporary seismic arrays or exclude non-relevant data for denoising. 23

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## **1. INTRODUCTION** <sup>28</sup>

Signal recording and processing hold significant importance across a range of scientific disciplines, including the field 29 of geophysics. Capturing and analyzing various types of signals, such as seismic waves, electromagnetic waves, and 30 gravity anomalies, enables the understanding of the Earth's subsurface and its geological characteristics. As waves 31 propagate through the Earth, their interaction with geological structures, such as sediment layers or fault lines, af- 32 fects the recorded signals and leads to changes in the wave's propagation characteristics. Deploying seismic stations 33 enables the measurement of signals and the derivation of insights regarding the subsurface characteristics and na- 34 ture of the area.  $35$ 

In seismic analysis, understanding these measurements involves the identification of different wave types, along 36 with analyzing frequency spectra, amplitude variations, phase shifts, and other wave properties (**M. Bath, 1973**; **Rost** 37 **and Thomas, 2002**; **Barnes, 2007**). While many of these signal components deliver valuable information and are es- 38 sential for seismic investigations, there are also parts known as seismic noise that introduce more complexity to the 39 data interpretation process. Natural sources such as wind or ocean waves, atmospheric disturbances, or geological 40 activities, as well as artificial sources including human activities and industrial operations, emit noise signals in vari- 41 ous frequency bands and contribute to seismic measurements. In order to interpret measurements and mitigate the 42 influence of undesired signals on the results, understanding the relationship between input and output within a 43 given physical system is essential (**Walden and White, 1998**; **Kawakami and Oyunchimeg, 2003**). The transfer func- 44 tion, denoting this relationship, holds significance across multiple disciplines, including the field of seismology. For  $\frac{45}{10}$ instance, the relation between the ground motion and the recorded seismogram is named instrument response 46 (**Havskov and Alguacil, 2016**; **Lindsey et al., 2020**), while the relationship between ground motions at different 47 points is called Greens function (**Snieder, 2004**; **Sabra et al., 2005**; **Sergeant et al., 2020**). However, estimating the 48 transfer function in seismology can be complex due to the interaction of varying subsurface structures, variability in 49 seismic wave propagation, noise and instrumentation limitations leading to complex coupled systems of differential 50 equations. 51

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Machine Learning has emerged as a widespread methodology in geophysical data analysis, providing an advanced  $52$ alternative to conventional seismic analysis methods for uncovering relationships within seismic data. Multiple fields 53 including seismic exploration (**Helmy et al., 2010**; **Li et al., 2019**; **Tariq et al., 2021**) and seismology (**Li et al., 2018**; 54 **Xie et al., 2020**; **Mousavi and Beroza, 2023**) employ Machine Learning methods to characterize seismic data and de- 55 tect and classify relevant characteristics and patterns within the data*.* One fundamental architecture in the subfield 56 of Deep Learning (**LeCun et al., 2015**) are encoder-decoder networks, which provide the opportunity to learn and 57 extract dependencies between data across input and output domains. In seismic and seismological applications, en- 58 coder-decoder networks play a crucial role for tasks like denoising (**M. Saad and Chen, 2020**; **Knispel et al., 2022**; **Yin** 59 **et al., 2022**) or interpretation (**Wu et al., 2019**; **Zhang et al., 2021**). 60

In this paper, we introduce an adaptation of encoder-decoder networks to learn the relationship between seismic 61 wave fields recorded at two different locations. By using one dimensional time series from a fixed seismic station as 62 input and the measurements from a nearby seismic station as target, we aim for the network to learn the alterations 63 that the signal undergoes between the two stations. Through this approach, we want to demonstrate that a modifi- 64 cation of the encoder-decoder architecture is capable of learning data characteristics that closely resemble the prin- 65 ciple of the transfer function within the setup of two seismic stations. While the foundation of the concept originates 66 from the established practice of detecting and learning patterns and structures of and within time series data (**Mal-** 67 **hotra et al., 2016**; **Badrinarayanan et al., 2017**; **Du et al., 2020**; **Beveren et al., 2023**), our approach focuses more on 68 the parts that influence the propagation of waves between nearby locations. Thereby, the analysis incorporates both 69 phase and amplitude information and provides a new approach to approximate the transfer function using Machine  $\frac{70}{20}$ Learning techniques. By considering phase information, our approach distinguishes from Wiener prediction filters. 71

We will guide through this study by introducing the encoder-decoder network setup and the most important metrics 72 for this specific use case (Section [2\)](#page-3-0) first. Following this, Section [3](#page-6-0) outlines the characteristics of the measurement 73 region and provides an overview of the selected seismic stations and data. Section [4](#page-10-0) will involve evaluating the find- 74 ings across different scenarios and datasets before discussing (Sectio[n 5\)](#page-17-0) and drawing conclusions on the potentials 75 and limitations of the presented method (Section [6\)](#page-21-0). The state of the state of the presented method (Section 6).

#### <span id="page-3-0"></span>**2. NEURAL NETWORK SETUP** <sup>77</sup>

The methodology employed in this study follows the overall aim of testing the feasibility of a network that is able to 78 learn the transfer properties between two seismic stations. We make use of an encoder-decoder architecture in a 79 supervised fashion and train it by using input data from a fixed reference station A and target data from a second 80 station B [\(Figure 1,](#page-4-0) top). The form of the network traces the traditional U-Net shape (**Ronneberger et al., 2015**; **Zhu** 81 **and Beroza, 2019**; **Zhong et al., 2022**; **Li et al., 2022**) while an equal amount of convolutional and deconvolutional 82 blocks defines its structure. Each block consists of a convolutional layer, a batch normalization layer and an activation 83 layer. Furthermore, we use a dropout layer after each block to prevent overfitting by randomly setting a fraction of 84 input units to zero during training. To make sure that every input connects to every output, we extend the architecture 85 by a dense layer in the latent space bottleneck. To enable the direct transfer of information from the encoder to the 86 decoder, we introduce skip connections between the respective convolutional and deconvolutional blocks. The depth 87 of the network is five, while we use hyperbolic tangens as final activation layer in each of the individual use cases 88 introduced in Sectio[n 3.](#page-6-0) As an outcome of the learning process from the input to the target data, the network delivers 89 a prediction that ideally resembles the shape of the target data[. Figure 1](#page-4-0) illustrates the schematic network architecture 90 subdivided into the use of input and target data, the encoder part, the latent space, and the decoder part. 91



<span id="page-4-0"></span>**Figure 1.** Simplified visualization of the network architecture consisting of an encoder and decoder part. Data from 94 seismic station A serve as input, while data from another seismic station B provide the target data. Skip connections 95 (olive dashed lines) link corresponding convolutional and deconvolutional blocks. Within the encoder, each block con- 96 sists of a Convolutional layer (Conv), Batch Normalization (BN) and an Activation layer. A dropout layer follows almost 97 every block. Within the decoder, each block with dropout layer complements by an Upsampling layer. 98

To assess the model performance, we select different metrics to evaluate the similarity between the predicted  $(\hat{y})$  and 99 the observed value (y). In order to optimize the model during the training process of the algorithm, the error between 100 the model prediction and the actual target data is estimated using the Huber loss function implemented by Keras 101 **(Chollet and others, 2015**). The Huber loss *l* (Eq. (1)) combines the mean squared error (MSE) and the mean absolute 102 error (MAE) with  $\partial$  defining the threshold for the transition from quadratic to linear components of the loss. This 103 helps the Huber loss function to be robust to outliers in the data. 104

$$
l(y,\hat{y}) = \begin{cases} \frac{1}{2}(y-\hat{y})^2 & \text{for } |y-\hat{y}| \leq \theta \\ \frac{\partial}{\partial (|y-\hat{y}|-\frac{1}{2}\partial) \text{for } |y-\hat{y}| > \partial \end{cases}
$$
(1) 107

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To evaluate the performance of the model and the goodness of its prediction after training is finished, we select two 106

metrics to independently assess both amplitude and phase fit, and subsequently consider them in equal measure for 108 an overall indication of the model quality. The model of the model of the model of the model quality.

In order to assess the degree of similarity between the target and prediction time series, one evaluation metric of 110 choice is the normalized cross-correlation function. This function measures the similarity between the two time series 111 based on the displacement of one relative to the other and normalizes by the overall standard deviation. While phase 112 shift in seismology denotes the time displacement of a waveform, we employ this metric to emphasize the temporal 113 alignment between the two signals. Assuming a good model and thus an accurate prediction, we expect both signals 114 to be identical and align well without any offset. Under this assumption, we compute the cross-correlation without 115 shifting samples and determine the cross-correlation coefficient at time zero. By doing so, a value of 1 indicates a 116 strong positive similarity, -1 indicates an anti-correlation, and 0 reflects no relationship between the two time series. 117 Assessing the cross-correlation on the entire time series as well as in smaller segments of about 10.24s helps in deter- 118 mining the quality of the results in detail. 119

Classifying the amplitude differences between the predicted and the actual target values, the Root Mean Squared 120 Error (RMSE) quantifies the accuracy of a model while being sensitive to the magnitude of errors. Thereby, the RMSE 121 indicates how far the predicted value deviates from the target value. Employing RMSE as the second evaluation metric 122 aids in comparing the amplitudes of the actual target data with those predicted by the model. It defines as shown in 123 Eq. 2, where n represents the total number of data points and i refers to the  $i<sup>th</sup>$  observation. With increasing 124 errors, the RMSE score tends to rise linearly, indicating that a smaller value corresponds to a closer alignment between 125 the model's predictions and the actual data. Thereby, RMSE shares units with the actual target values. 126

$$
RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i)^2}
$$
 (2)

While the Huber loss is estimated as part of the model training process to enhance the models understanding of the 127 data iteratively, cross-correlation coefficients and RMSEs are calculated post-training. Estimating both provides a com- 128 prehensive approach to quantify the model's predictive capability of how well it captures the phases and amplitudes 129 of the target data. Thereby, we do not combine the metrics numerically, but rather use them to comprehend the 130 quality of the results. 131

## <span id="page-6-0"></span>**3. DATA AND PROCESSING** <sup>132</sup>

In order to demonstrate the viability of the proposed method in capturing the relationship between two seismic sta- 133 tions, we will employ one-dimensional time series measurements, starting with the exploration of synthetic data. With 134 this, we aim to validate the viability of the general approach in a controlled setting, before we proceed to analyze field 135 data gathered during a seismic exploration campaign. The matrix of the set of t

## **Synthetic data** 137



#### **Field data** 153

To evaluate the applicability of the proposed method across various data scenarios, we employ not only synthetic 154 data but also incorporate field data gathered at a seismic exploration campaign conducted by the OMV E&P GmbH in 155 the Vienna basin, Austria. The array setup consisted of in total 4907 seismic stations, each tooled with either 12 or 156 24 geophones (vertical components), and spaced with an interstation distance of approximately 200m [\(Figure 2\(](#page-8-0)a)). 157 The measurement period comprises a total duration of about four weeks during March and April 2019 using a sam- 158 pling rate of 100 Hz. Major and minor roads surround and intersect the region, and a railway line runs along its 159 southern boundary. In addition to these sources of seismic signals, wind turbines and oil pump jacks appear through-<br>160 out the region [\(Figure 2\(](#page-8-0)a)). The wind parks Prottes-Ollersdorf and Grossengersdorf are situated northeast and 161 southwest within the array, while the wind park Deutsch-Wagram is located on its southwestern boundary. Oil pump 162 jacks position in various setups, ranging from individual placements to small clusters and larger groupings within the 163 array. Ocean noise reaches the stations predominantly from the northwest direction. **Schippkus et al., 2022** provide 164 another detailed description of the array used in this study. The authors explore the impact of an isolated noise 165 source within the framework of seismic interferometry using the same dataset. Furthermore, a detailed description 166 of the study area offering background information on the present industry and additional potential sources of noise 167 is given by **Schippkus et al., 2020**. While using a different array than the one in this study, the authors provide de- 168 tailed insights into the source characteristics of the region by examining spectrograms and power spectral densities. 169

For the model training, we select three station pairs within the southwestern quarter of the array. The choice of sta- 170 tion pairs thereby depends on the respective area conditions in terms of wind turbine and oil pump jack distribution 171 and the distances of these sources to the stations. We successively enhance complexity between the scenarios by 172 increasing the number of surrounding noise sources and consider their spatial proximity to the stations. We evaluate 173 the close vicinity of a wind park in absence of other sources, as well as configurations with and without a wind tur-<br>174 bine positioned directly between the stations. [Figure 2\(](#page-8-0)b) shows the three scenarios and their surrounding noise 175 sources. The first station pair F1 situates at the western edge of the array in an area surrounded by fields. The wind 176 park Grossengersdorf is located in the southwestern vicinity of the stations, having its closest wind turbine east of 177

the stations in about ~110m to the target station and ~250m to the reference station. Situated more towards the 178 center of the array, the second station pair F2 encircles by wind turbines and oil pump jacks, appearing either indi- 179 vidually or in smaller groups. With a distance of ~55m to the reference station and about ~125 m to the target sta- 180 tion, a single wind turbine locates between the stations. For the third station pair F3, the number of surrounding 181 sources further increases, particularly witnessing a greater number of oil pump jacks in close proximity to the sta-<br>182 tions. In contrast to the other station combinations, there is no wind turbine directly next to the stations in this case. 183 The closest wind turbine is located at a distance of about  $\sim$ 440m, while the nearest oil pump jack is  $\sim$ 950m away. To 184 ensure an appropriate and consistent amount of training and testing data, we limit the measurement of each station 185 to a period of two days. The same state of two days and the same state of two days and the same state of two days  $186$ 



<span id="page-8-0"></span>**Figure 2.** Geometry of the experiment and synthetic setups. (a) Map of the study area northeast of Vienna, where 188 seismic stations are positioned with an interstation distance of approximately 200  $m$ . The chosen pairs of analysed 189 stations are indicated by colored boxes (olive, cyan, dark blue). (b) Detailed view of the three chosen station pairs F1, 190 F2, and F3 from the array deployment. The plot's border color corresponds to its location on the map. (c) Configuration 191 of synthetically generated station pairs S1 and S2 with surrounding sources. 192

#### **3.1 Data processing and model training** <sup>193</sup>

Prior to starting the training of models for each of the datasets, it is essential to perform pre-processing on the data, 194 as it directly impacts the network's ability to learn accurately. In addition to filtering the data below 10Hz using a 195 Butterworth low-pass filter, data preparation for both synthetic and field data includes the alignment of all ampli-<br>196 tudes to the same range through data scaling. For the synthetic data, we implement normalization to consistently 197 scale the data within the range of [-1, 1]. Given the data generation process, we expect only minimal variations 198 within the data, thus eliminating the need for independent centering and scaling using standard scaling methods. 199 With regard to the variety of sources influencing the characteristics of the field data, we anticipate greater variations 200 in range and distribution within this dataset. Therefore, we combine both standard scaling and normalization to ac- 201 count for these variations. Initially, standard scaling is applied to center the data around zero and standardize its de- 202 viation to one, followed by normalization to adjust the data to fit within the range of [-1, 1]. Before scaling, we allo-<br>203 cate 80% of the data to the training set and 20% to the testing set. Additionally, 20% of the training data is automati- 204 cally determined as the validation set during model training. To ensure successful model training, it is important to 205 provide a sufficient amount of training and testing examples. To do so, we divide the overall time series of two days 206 into chunks of 10.24 seconds each, while each chunk corresponds to 1024 samples based on a sampling rate of 100 207 Hz. Like this, we receive 13.500 chunks for training and 3.375 chunks for testing. In the following, we will refer to 208 these chunks as traces. 209

We train our encoder-decoder model using pre-processed input traces from reference station A and provide the 210 traces from station B as the target we aim to predict. This way, we obtain a unique model for each station pair that 211 outputs predictions based on the individual dataset provided. Subsequently, we compute relevant metrics between 212 the target and prediction to assess the model performance. Following architectural investigations, we empirically 213 determine the optimal network depth by analyzing accuracy, convergence and model performance on a sample of 214 the data before starting model trainings. In order to capture the complexity of the data and avoid overfitting, we use 215 a network depth of five layers. Figure 1 shows the schematic layout of the network having five convolutional and 216

deconvolutional blocks. We train our models with a learning rate of  $10^{-4}$  for 1500 epochs each, as further training 217 beyond this point does not significantly improve performance. 218

## <span id="page-10-0"></span>**4. RESULTS** <sup>219</sup>

Following the training phase, we evaluate the models by calculating the Root Mean Square Error (RMSE) and cross- 220 correlation coefficient (CC) between the target data and the corresponding model prediction. We assess both met-<br>221 rics on the overall target time series of two days, and on smaller segments of it. To facilitate the analysis of results 222 and improve the visual representation, we analyze our results within output segments that are half the size (512  $223$ samples) of the training and testing traces. When the model captures all relevant transfer features from the data, its 224 predictions will accurately correspond with the unseen target data. To scrutinize the results in terms of positive and 225 negative amplitude deviations, we visualize each sample of the entire target time series against the model prediction 226 by density plots [\(Figure 3\(](#page-12-0)d)). In order to comprehend the correlation dynamics across the whole dataset, we further 227 estimate correlation coefficients for each window of 512 samples without any shift and visualize their distribution 228 through a histogram [\(Figure 3\(](#page-12-0)e)). Going into further detail, we will analyze a representative example trace [\(Figure](#page-12-0) 229 [3\(](#page-12-0)b)) for each scenario along with its corresponding prediction, correlation coefficient and input data [\(Figure 3\(](#page-12-0)a)) 230 from the model training. To understand how the cross-correlation coefficient evolves throughout the data, we link 231 each section of the trace to its corresponding correlation coefficient, as shown in [Figure 3\(](#page-12-0)c). For this, we compute 232 these correlation coefficients using moving intervals of 20-sample windows with a 10-sample offset and visualize the 233 results. 234

## **4.1 Synthetic data** <sup>235</sup>

[Figure 3](#page-12-0) illustrates the results for the two scenarios of synthetic data. For the single source case S1 [\(Figure 3\(](#page-12-0)a)-(e)), 236 the model prediction closely aligns with the actual target data [\(Figure 3\(](#page-12-0)b)), showing the algorithm's general capabil- 237 ity to predict the transfer properties in a very simplified setup. Metrics support this observation, validating the accu- 238 racy of predictions and the presence of minimal errors by a small RMSE value of 0.04. While the majority of value 239 pairs cluster around the ideal case of correct amplitude predictions as indicated by the dotted purple line i[n Figure](#page-12-0) 240 [3\(](#page-12-0)d), some segments show significant deviations, highlighting instances where the prediction does not align with the 241 target values. The overall cross-correlation coefficient of 0.90, as shown in [Figure 3\(](#page-12-0)e), reflects the predominance of 242 good fits, though it moderates by the occurrence of some less accurate predictions. The histogram shows, that a ma- 243 jority of traces display a correlation coefficient close to one, while another distinct cluster is observed around zero. 244 We attribute the latter cluster, observed around zero, to the random noise introduced in the data, which adds varia-<br>245 bility but does not necessarily indicate a systematic relationship. Consequently, the predictions do not align with the 246 target, leading to CCs near zero. This observation is confirmed by the analysis of CCs in smaller windows [\(Figure 3\(](#page-12-0)c)), 247 which indicate strong correlations when predicting the wavelet at given travel time, whereas the correlations of ran-<br>248 dom noise components are significantly lower. 249

The presence of 19 sources surrounding the stations (S2[, Figure 3\(](#page-12-0)f)-(j)) introduces increased variability to the data,  $250$ evident in the time series as overlapping signals with varying amplitudes [\(Figure 3\(](#page-12-0)g)). While certain segments of the  $251$ target trace align with the model predictions [\(Figure 3\(](#page-12-0)g)), other parts reveal disparities in either amplitude or the 252 general shape of the wavelet. The overall correlation coefficient of 0.34 [\(Figure 3\(](#page-12-0)j)), along with the RMSE of 0.13 253 [\(Figure 3\(](#page-12-0)i)) highlights larger differences in the similarity of the time series compared to the single source case S1. 254 However, the given overall correlation coefficient of 0.34 indicates a predominantly positive correlation, implying 255 that the model is able to approach a modest similarity between its predictions and the target data. The analysis of 256 the correlation coefficients for individual traces [\(Figure 3\(](#page-12-0)j)) reveals characteristics of Gaussian-like distribution, with 257 the majority of values concentrated between 0.1 and 0.4, and some traces reaching an upper limit near 0.8 and a 258 lower limit around -0.4. Analysing the kind of differences between the target and predictions [\(Figure 3\(](#page-12-0)i)) demon- 259 strates a slightly tilted elliptical shape of amplitude mismatch around the center indicating that amplitudes are more 260 commonly underestimated than overestimated. 261



<span id="page-12-0"></span>Figure 3. Results of the model analysis for two synthetic data scenarios (S1, top - dashed grey box; S2, bottom - solid 263 grey box) using Root Mean Square Error (RMSE) and cross-correlation coefficient (CC) across the entire target time 264 series and within traces. The light grey line represents the input data  $((a), (f))$ , orange and blue lines denote the target 265 and network prediction respectively ((b), (g)). The density plots ((d), (i)) show the network prediction of the target 266 against the actual target data, while the dotted purple line visualizes the ideal best-fit line for the regression. Single 267 grey points ((c), (h)) depict cross-correlation coefficients for 20-sample sections beneath the corresponding example 268 trace. Histograms ((e), (j)) show correlation coefficients for windows of 512 samples each. The black marker highlights 269 the overall correlation coefficient of the entire time series given in the text box. 270



**4.2 Field data** <sup>279</sup>

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[Figure 4](#page-16-0) depicts the outcomes for the three field data scenarios. Beginning with the first station pair located at the 280 array's edge near a wind park (F1[, Figure 4\(](#page-16-0)a)-(e)), the model prediction closely aligns with the actual target data in 281 various segments [\(Figure 4\(](#page-16-0)b)). While we observe positive and negative deviations in amplitudes between target and 282 prediction in several parts of the trace, the prediction of phases exhibits accurate matches with the target time se- 283 ries. [Figure 4\(](#page-16-0)c) confirms this observation, as the correlation coefficients for the majority of trace subparts cluster 284 near one, highlighting the model's accuracy in predicting phase information. With an overall correlation coefficient 285 of 0.75, the concentration of individual correlation coefficients [\(Figure 4\(](#page-16-0)e)) is mostly within the positive range of 0  $286$ to 1, having its peak strength at a high correlation value of around 0.8. A cluster of values around 0.75 characterizes 287 the central tendency of the dataset and emphasizes further the models ability to make predictions of similarity to 288 the target data. Besides, there is another notable peak around -0.58 and -0.78, likely attributable to data gaps pre-<br>289 sent in this dataset leading to inaccurate predictions in the negative range. Evident from the elliptical shape, the 290 density plot [\(Figure 4\(](#page-16-0)d)) reveals positive and negative mismatches of amplitudes along the dotted purple best-fit 291 line. Thus, both positive and negative amplitude predictions display tendencies of overfitting and underfitting, re-<br>292 flecting some variability in the model's capacity to accurately estimate amplitude values. The RMSE reflects this with 293



While wind turbines are already in close proximity to the stations in the first case F1, the distance further halves for 297 the second scenario F2 ([\(Figure 4\(](#page-16-0)f)-(j)), where a wind turbine is located directly between both stations. Although the 298 overall correlation coefficient of 0.77 [\(Figure 4\(](#page-16-0)j)) is nearly identical to the one of the previous example, there are 299 visual differences regarding the data itself and the model outcomes leading to variations in the results. Examining 300 the example trace [\(Figure 4\(](#page-16-0)g)), the predicted phases largely correspond with those of the target data again. The pre-<br> $301$ dominance of correlation coefficients close to one supports this observation [\(Figure 4\(](#page-16-0)h)), although minor or nega- 302 tive coefficients occur occasionally. However, the amplitude predictions again exhibit greater variances compared to 303 the targets. While the RMSE for the selected trace is 0.06, the global RMSE measures at 0.08 [\(Figure 4\(](#page-16-0)i)), indicating 304 more accurate amplitude predictions for this station pair compared to case F1. This is also evident when looking at 305 the distribution of values around the purple dotted best-fit line of the plot. Similar to the initial example, the analysis 306 reveals a tendency to both over fit and under fit, affecting the accuracy of predictions for both positive and negative 307 amplitude values. However, the dataset predominantly consists of smaller values, leading to reduced variability and 308 a narrower range of data dispersion. Following this, the individual correlation coefficients of traces [\(Figure 4\(](#page-16-0)j)) not 309 only approximate a nearly Gaussian distribution again but also display increased steepness, indicating a tighter clus- 310 tering of values around the mean. 311

The third station pair, F3, unique among the combinations as it lacks a wind turbine in direct proximity to the sta- 312 tions, leads to an overall correlation coefficient of 0.58, as shown in [Figure 4\(](#page-16-0)o). Although the overall correlation co- 313 efficient represents a decrease relative to those found in earlier field data examples, the amplitude deviations, char- 314 acterized by an RMSE of 0.10, lie within an intermediate range compared to the observations from the prior two 315 cases. In this instance, as shown i[n Figure 4\(](#page-16-0)n), the comparison of target and predicted amplitudes reveals an ellipti- 316 cal shape again. However, the ellipse appears more circular in comparison to previous cases, suggesting that it repre- 317 sents an intermediate scenario in terms of the spread and steepness. Additionally, there is the same tendency of 318 over- and underestimation as in previous scenarios. The analysis of the model's performance on the example trace 319 [\(Figure 4\(](#page-16-0)l)) shows disparities between the target and predicted values in certain intervals, whereas other sections 320 align well. Correlation coefficients, derived from 20-sample segments of the example trace [\(Figure 4\(](#page-16-0)m)), confirm  $321$ this impression: values near one mirror precise phase predictions or moderate amplitude fits, while values at or be- 322 low zero point to negative predictions. The analysis of correlation coefficients for trace windows [\(Figure 4\(](#page-16-0)o)) reveals 323 that most bins lie within the positive range of 0.2 to 0.8, while we identify one large peak above 0.9. This indicates 324 the presence of a generally positive linear relationship between input features and the models output predictions,  $325$ affirming the model's effectiveness in detecting data patterns to a certain degree. 326

All three field data examples exhibit moderate to strong linear correlation, providing predictions that resemble the 327 actual target to a high degree. In this regard, both the visual assessment and the evaluation metrics surpass the per- 328 formance of the second synthetic example S2, which mirrors comparable environmental conditions of having 329 sources distributed around the stations. However, the field data examples do not achieve the level of accuracy seen 330 in the perfect synthetic case S1, suggesting that the performance of field data models ranges somewhere between 331 these two extremes. Physically, we also expect the source regime to be a hybrid between single source and evenly 332 distributed sources, with a tendency towards a few significant sources.  $333$ 



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<span id="page-16-0"></span>Figure 4 Results on the comparative analysis (cf. [Figure 3\)](#page-12-0) for three field data scenarios (F1 top, F2 middle, F3 bottom). 336 Plots provide insights into the examination of correlation dynamics, magnitude deviations, and distribution patterns 337 using Root Mean Square Error (RMSE) and cross-correlation coefficient (CC) for evaluation. The results for this dataset 338 follow the same evaluation criteria and presentation as in [Figure 3.](#page-12-0) The frame color of the box indicates the corre- 339 sponding scenario. 340

#### <span id="page-17-0"></span>**5. DISCUSSION** <sup>341</sup>

The model architecture described in this study shows the capability to predict the transfer properties, in our case the  $342$ 1D time series, between two seismic stations in different source-station-setups. Employing diverse scenarios of both 343 synthetic data [\(Figure 3\)](#page-12-0) as a controlled environment, and field data [\(Figure 4\)](#page-16-0), representing real-world conditions,  $344$ delivers a comprehensive proof of concept across different datasets. Overall, the models demonstrate strong predic- 345 tive performance, particularly in predicting the phase of the wave field more reliably than its amplitude, as demon-<br>346 strated by both synthetic [\(Figure 3\)](#page-12-0) and field data examples [\(Figure 4\)](#page-16-0). While the models manage the novel scenario 347 of differing input and target data effectively, further optimization by fine-tuning various factors, such as hyperpa- 348 rameters, could affect the algorithms performance even further (**Weerts et al., 2020**; **Yang and Shami, 2020**; 349 **Bakhashwain and Sagheer, 2021**).  $350$ 

Particularly evident in the scenario S1 (Figure 3(a)-(e)), the model training benefits significantly by considering only a  $351$ single source from one direction and random noise, representing an idealized scenario. This simplification yields fa- 352 vourable results, underscoring the network's general ability to learn a given relationship in a controlled setting. Mov- 353 ing to scenario S2, the approach handles a higher level of complexity introduced by simultaneous inputs from multi- 354 ple directions. Despite these challenges, the algorithm maintains a decent level of performance, as evident by the 355 mean correlation coefficient (CC) of 0.34. When comparing the performance of this second synthetic example S2  $356$ [\(Figure 3\(](#page-12-0)f)-(j)) with that of the field data models, all results from the field data exceed the performance observed in 357 S2 with CCs of 0.58, 0.75 and 0.77. Although scenario S2 may seem initially favourable due to the uniform energy  $358$ propagation from the synthetic sources, the observed performance improvement in the field data is likely driven by 359 the unique characteristics of different sources around the array, such as wind turbines, oil pumps or roads. Despite 360 similarities in source distributions between the two setups, our field data do not exhibit the extreme conditions of 361 S2, demonstrating the robustness and practical applicability of our approach in more natural and realistic scenarios. 362



In addition to the equal distribution of energy for each source in the synthetic data scenarios, the inconsistent and 371 repeated activation of these sources may fail to generate learnable characteristics in the dataset. The absence of 372 pattern-like attributes introduces challenges for the algorithms learning process, as they represent essential relation- 373 ships within the data that models are trained to learn and utilize. While this could potentially create challenges with 374 our synthetic data, the situation shifts with the nature of sources present in the field data, which exhibit consistent 375 and repetitive signals. Given the distribution of surrounding sources in the field data examples [\(Figure 2](#page-8-0) (b)), we ac- 376 count for the presence of wind turbines at various distances in each scenario. **Neuffer et al., 2019** demonstrate that 377 wind turbines show directional characteristics with wind-dependent specific patterns. Anticipating these sources to 378 introduce distinct patterns by the propagation of similar signals, we expect them to provide valuable input to the  $379$ model training and enhance its predictive accuracy. Given that our results improve when wind turbines are in close 380 proximity to the stations, the presence of such noise sources appears to resemble the characteristics of a single 381 source and thus positively influences the model's performance.  $382$ 

While it is evident that consistently emitting sources such as wind turbines positively impact our results, it is not im-<br>383 mediately clear why we observe stronger accuracy across various datasets in the prediction of phases, while our 384 models preferentially underestimate amplitudes [\(Figure 3,](#page-12-0) [Figure 4\)](#page-16-0). Given that neither the area of investigation nor 385 the characteristics of the sources and stations indicate any physical phenomena that could account for these devia- 386 tions, it appears that there are no evident physical processes to explain this behaviour. Consequently, we will focus 387 our investigation on the data as well as the architecture and parameters of the models as potential cause. The fun- 388 damental nature of encoder-decoder networks, particularly autoencoders and the ones used for sequence-to-se- 389 quence learning, aims to capture and reconstruct patterns in the data. However, these networks learn to prioritize 390 certain characteristics of the data based on their architecture, parameters and data attributes. Upon visually inspect- 391 ing our data, it becomes apparent that the spacing between phases of our time series appears to be relatively con- 392 sistent. This can be attributed to two key factors: the application of filtering and the dominance of a relatively nar-<br>393 row frequency band in the remaining frequencies. While this is true for the phases, amplitudes vary between high 394 and low values and span from positive to negative, which poses a greater challenge for the model to learn the data 395 properties. Besides the architecture of encoder-decoder networks and the quality of training data, the choice of pa- 396 rameters like learning rate, batch size and loss function can affect the model performance, yet demands additional 397 research for a comprehensive understanding. The search of the search of the search for a comprehensive understanding.

Although it is not obvious to us why amplitudes are preferentially underestimated, many seismological applications 399 rely entirely on the phases of seismograms. Our models reliably predict the phase of seismic noise. For instance,  $400$ phases from seismic waves are essential for determining arrival times of different waves, which help to locate earth- 401 quake epicentres and understand Earth's internal properties. In addition, phase-based investigations, such as ambi- 402 ent noise tomography and seismic interferometry, predominantly rely on phase information to extract subsurface 403 details. As highlighted by **Bensen et al., 2007**, ambient noise data processing involves steps like cross-correlation and 404 temporal stacking, which are inherently phase-dependent, and the accurate measurement of dispersion curves,  $405$ which utilize phase and group speeds. Seismic interferometry, for example, involves the cross-correlation of seismic 406 recordings at different stations, allowing researchers to reconstruct the Green's function between two points using 407 phase information. This highlights that while our amplitude predictions may be less precise, the critical phase infor-<br>408 mation remains robust and useful for various seismological analyses.  $409$ 

In general, choosing an encoder-decoder architecture suits the requirements of the given problem, as it is able to  $410$ capture complex relationships and generalizes well to unseen data. Traditionally, this approach is used to predict 411 future values of time series based on historical trends, using past data as input to forecast subsequent values within 412 the same series. Using it with input data from one seismic station and target data from another seismic station 413 thereby diverges from this conventional application as well as from classical autoencoders. While autoencoders aim 414 to learn a compressed representation of the input data, the proposed architecture extends this approach to learn 415 and predict the relationship between data from distinct stations. In other words, our model learns the propagation 416 of complex wave fields between the stations. This allows to model spatial and temporal dependencies between seis- 417 mic data relying on the phase and amplitude information of the signals. One might draw parallels between this ap- 418 proach and Wiener prediction filters (**Chen et al., 2006**; **Chandra et al., 2014**), which also aim to capture dependen- 419 cies within signal data. However, it is important to note that Wiener prediction filters primarily deal with the auto-<br>420 correlation of signals, focusing on their power spectrum without considering phase information. Wiener filtering as- 421 sumes non-deterministic signals, which contradicts seismic signals known for their deterministic nature, such as re- 422 flections from layered structures. In contrast, our method comprehensively accounts for the dynamic, non-linear  $423$ interactions and phase information essential for accurately modeling wave propagation in seismology. 424

To advance our approach from the proof-of-concept stage described herein to concrete applications, several aspects 425 will likely need to be addressed. These could encompass technical and structural enhancements that include the im-<br>426 provement of data quality, fine-tuning of hyperparameters or the accuracy of amplitude predictions. Additionally, 427 we might consider adjustments to the synthetic data generation process to better resemble conditions encountered 428 in field environments with multiple ambient noise sources. Future studies might also delve into how the geograph- 429 ical and spatial configuration of sources and receivers impacts the results. Given the differences in model perfor-<br>430 mance in predicting phases and amplitudes, experimenting with different model architectures and parameters could 431 further be advantageous. By implementing these modifications to the model setup and understanding influences on 432 the results in detail, we can further refine the overall performance and robustness of our approach. 433

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## <span id="page-21-0"></span>**6. CONCLUSION** <sup>436</sup>

In this study, we have successfully presented and tested an adaption of encoder-decoder networks to predict the 437 transfer function of seismic wave fields, between two seismic stations. By introducing one-dimensional time series 438 data from a fixed seismic station as the input to the network and data from a nearby station as the target, our ap-<br>439 proach effectively learns the transfer function between the locations. Initially tested with synthetic data, the ap- 440 proach was validated further with field data from a seismic exploration campaign. Employing a range of scenarios 441 with varying surrounding conditions – from a controlled environment with synthetic data to field data including sev-<br> eral sources of ambient noise - we demonstrate a broad proof of concept. 443

Our findings confirm that our approach effectively predicts the wave field recorded as time series at a seismic station 444 using input from a neighbouring seismic station, resulting in machine learning models with varying degrees of accu- 445 racy. Notably, our models not only achieve high precision in predicting the phases of seismic waves but also perform 446 adequately in estimating amplitudes, demonstrating significant potential for the field of geophysical research. This 447 makes our approach particularly valuable for applications requiring precise seismic isolation or compensation, such 448 as active vibration isolation in photolithography, semiconductor manufacturing, and 3D-microfabrication (**Kerber et** 449 **al., 2007**; **Kim et al., 2009**). It is also highly relevant for projects like the Einstein Telescope (**Punturo et al., 2010**; 450 Harms et al., 2022), where extremely sensitive gravitational wave detections need to be free from seismic distur-<br>451 bances. Additionally, our approach also opens up the potential for the novel concept of virtual seismic arrays. 452

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