

1 **Internal Oscillations of Tropical Mesoscale Convective Disturbances**

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23 **Abstract**

24 In real-world observations, long-lived tropical mesoscale convective disturbances
25 (MCDs) often exhibit quasi-periodic variations in precipitation and cloudiness on time
26 scales of tens of hours. Previous studies suggested that these variations are mainly
27 induced by external forcings such as the diurnal cycle of insolation. However, some
28 studies showed evidence that tropical MCDs can display quasi-periodic behavior even
29 without external forcings. In this study, a suite of idealized convection-permitting
30 simulations is used to examine the evolution of a mesoscale atmospheric column after
31 an initial pulse of heating. It is demonstrated that the heated column not only radiates
32 inertia-gravity waves that perturb its environment, but itself continues to oscillate with
33 consequences for subsequent local convection. By comparing simulations with linear
34 wave theory, it is suggested that this oscillation is an inertia-gravity oscillation. This
35 study indicates that convectively coupled internal oscillations may constitute a
36 fundamental component of the life cycle of observed long-lived tropical MCDs.

37

38 **1. Introduction**

39 Mesoscale convective disturbances (MCDs) are frequently observed in Earth's
40 tropical regions. These disturbances typically encompass or are associated with systems
41 like mesoscale convective systems, tropical depressions, tropical cyclones (TCs), and
42 monsoon low-pressure systems (LPSs), with sizes ranging from hundreds to thousands
43 of kilometers. These convective systems not only play a crucial role in the water and
44 energy cycles within the tropics, but also significantly impact our social and economic
45 activities (e.g., Nesbitt et al. 2000; Emanuel 2018; Houze 2018). However, the
46 mechanisms driving the evolution of these systems remain incompletely understood.

47 In real-world observations and numerical simulations, long-lived tropical MCDs
48 often interact with external forcings and demonstrate significant periodicity in
49 precipitation, cloudiness and convective heating. A typical example is the occurrence
50 of large-scale, westward-propagating convective disturbances with periods of
51 approximately 2 days in the equatorial western Pacific (e.g., Takayabu 1994; 1996).
52 Studies indicated that this 2-day period of convection is forced by the propagation of
53 equatorial waves with wavelengths of around 2000 to 4000 km (e.g., Haertel and
54 Johnson 1998; Wheeler et al. 2000; Haertel and Kiladis 2004). Another example is the
55 diurnal cycle of convection over the tropical ocean. In the nighttime, the absence of
56 shortwave heating cools the troposphere, which fosters convection by increasing
57 relative humidity and enhancing convective instability. Conversely, convection is
58 inhibited during the daytime due to strong shortwave heating in the free-troposphere
59 (e.g., Gray and Jacobson 1977; Fingerhut 1978). This diurnal cycle of convection is
60 robust in nearly all types of tropical MCDs, particularly in those with longer lifetimes,
61 such as TCs (e.g.; Browner et al. 1977; Dunion et al. 2014; Wu et al. 2015).

62 However, in many idealized simulations without external forcing, tropical MCDs
63 also exhibit pronounced quasi-periodic variations. For instance, in many idealized TC
64 genesis simulations, which lack both the diurnal insolation cycle and lateral boundary
65 forcing, significant quasi-periodic pulses of the disturbance can often be seen (e.g.,
66 Nolan 2007; Nicholls and Montgomery 2013; Yang and Tan 2020). Some studies

67 suggested that this behavior may be a model artifact resulting from the use of doubly
68 periodic boundary conditions, wherein gravity waves can return to their source and
69 trigger new convection (e.g., Nolan, 2007). Nonetheless, in simulations with very large
70 domains or damping lateral boundary conditions, quasi-periodic variation of the TC
71 disturbances still occurs (e.g., Li et al. 2006; Nicholls 2015). Similarly, quasi-periodic
72 variations can also be seen in idealized simulations of monsoon LPSs (e.g., Diaz and
73 Boos, 2021a, b). These results suggest that the quasi-periodic behavior of tropical
74 MCDs are not solely attributable to external forcing, but may also be internally
75 generated.

76 The aim of this work is to determine whether a tropical MCD could internally
77 generate quasi-periodic behaviors and, if so, to identify the mechanisms underlying
78 those behaviors. The rest of the paper is organized as follows: Section 2 introduces the
79 simulation details. Section 3 briefly analyzes the internal quasi-periodic behavior in
80 full-physics simulations. Section 4 provides evidence for the critical role of low-level
81 buoyancy in determining the precipitation. Section 5 demonstrates that the inertia-
82 gravity oscillation is responsible for the quasi-periodic behavior of low-level buoyancy
83 and precipitation. Finally, Section 6 offers a discussion and summary.

84

85 **2. Full-physics simulation design**

86 In this work, we use idealized numerical simulations to investigate the internal
87 oscillations of tropical MCDs. The numerical model employed is the WRF version 4.6.0
88 (Skamarock et al., 2019). The model domain extends to an altitude of 27 km, with the
89 upper third consisting of a sponge layer (Klemp and Lilly 1978). There are 50 vertical
90 levels, with 10 levels located below 1 km height. The initial sounding is derived from
91 Jordan (1958), which is a typical tropical sounding commonly used in simulations.

92 The simulations cover a horizontal domain size of $1800 \text{ km} \times 1800 \text{ km}$, with a
93 horizontal resolution of 3 km. To rule out the effects of gravity waves propagating back
94 to their sources, the best way should be using open lateral boundary conditions so that
95 gravity waves can radiate out of the domain. However, in our preliminary simulations
96 (not shown), adopting open lateral boundary condition leads to a drastic drying of the

97 domain, with the domain-mean moisture content decreasing by 40% in the first 3 days.
 98 This is probably because open boundary condition allows water vapor to escape out of
 99 the domain. Therefore, we still use doubly periodic lateral boundary condition, but add
 100 a sponge layer at the lateral boundaries of the domain (e.g., Li et al., 2006). This sponge
 101 layer is 180 km wide at the lateral boundaries, with the diffusion coefficient set to 1000
 102 times the model's predicted value (based on a 1.5-order TKE closure). The simulations
 103 maintain a fixed sea surface temperature SST of 302.15 K and a constant solar radiation
 104 of 350 W m^{-2} with no diurnal cycle. The Thompson microphysics scheme (Thompson
 105 et al., 2004) and the RRTMG radiation scheme (Iacono et al. 2008) are implemented in
 106 the simulations. The boundary layer (BL) scheme is YSU, coupled with the revised
 107 Monin–Obukhov surface-layer scheme (Hong et al. 2006).

108 All simulations initiate with a moist anomaly characterized by enhanced humidity
 109 at the center of the domain. This moist anomaly has a radius of 150 km and a height of
 110 3 km (starting at the surface), with the water vapor mixing ratio inside set to be 110%
 111 (horizontally uniform) of the initial sounding value. We conduct three simulations with
 112 Coriolis parameter set to 10^{-4} s^{-1} (CTLF10), $5 \times 10^{-5} \text{ s}^{-1}$ (CTLF05) and 0 s^{-1} (CTLF0),
 113 respectively (Table 1). All the simulations are run for 72 hours, and results are output
 114 every 2 hours. In the following analysis, we will mainly focus on the results in CTLF10,
 115 and the results in the other two experiments will be briefly compared.

116
 117

Table 1 Descriptions of full-physics experiments.

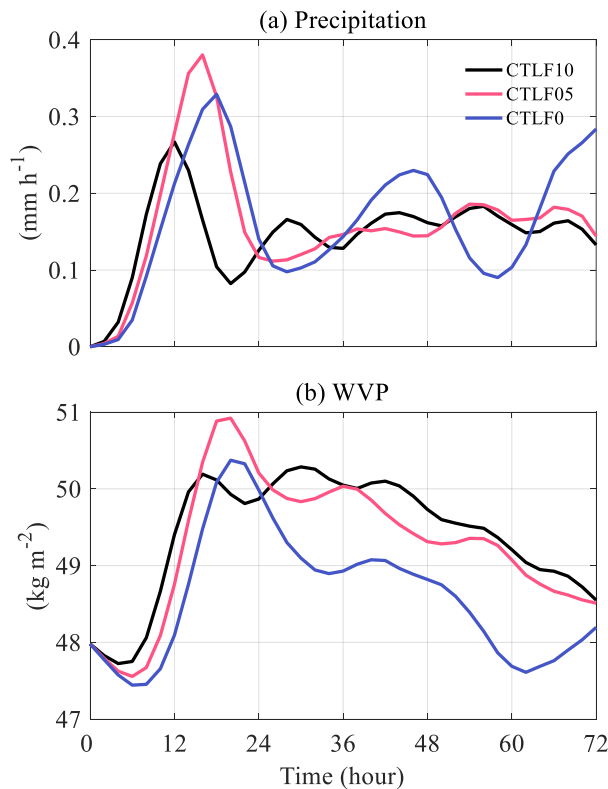
Name	Description
CTLF10	An 1800 km×1800 km full-physics simulation with Coriolis parameter set to be $1 \times 10^{-4} \text{ s}^{-1}$. The lateral boundary condition is double periodic, with a damping layer of 180 km wide.
CTLF05	As CTLF10, with Coriolis parameter set to be $5 \times 10^{-5} \text{ s}^{-1}$.
CTLF0	As CTLF10, without Coriolis force.

118

119 **3. Internal oscillation of tropical MCDs**

120 The time series of the precipitation rate in the disturbed region (defined to be the
 121 inner 150 km radii of the disturbance) of the three simulations are shown in Fig. 1a. All

122 three simulations exhibit a significant quasi-periodic pulsing in precipitation. The range
 123 of the quasi-periodic precipitation variations is approximately 0.08 to 0.15 mm h⁻¹,
 124 representing about 30% (CTLF10) to 50% (CTLF0) of the mean precipitation. In
 125 contrast, the precipitation pulsing observed in real-world Atlantic tropical cyclones
 126 (TCs) is approximately 0.3 mm h⁻¹ (Wu et al., 2015), which constitutes roughly 10%
 127 of the mean precipitation. Therefore, the pulsing observed in the ‘CTL’ simulations
 128 may be larger than real-world analogues. The pulsing periods in CTF10, CTF05 and
 129 CTF0 are around 15 hours, 18 hours and 28 hours (the period is defined as the time
 130 lag between the first and the last precipitation peaks divided by the number of cycles),
 131 respectively, indicating a noticeable increase in the period as the Coriolis parameter
 132 decreases. We further conduct sensitivity simulations based on CTF10 to examine the
 133 influence of domain size on the pulsing period. As shown in Fig. A1, variations in
 134 domain size do not have a discernible effect on the pulsing period, which suggests that
 135 the gravity wave return mechanism, as proposed in previous studies (e.g., Nolan, 2007),
 136 is unlikely to be responsible for the observed pulsing. The water vapor path (WVP) in
 137 the disturbance region also shows a significant pulsing signal, which is almost in phase
 138 with the precipitation (Fig. 1b).



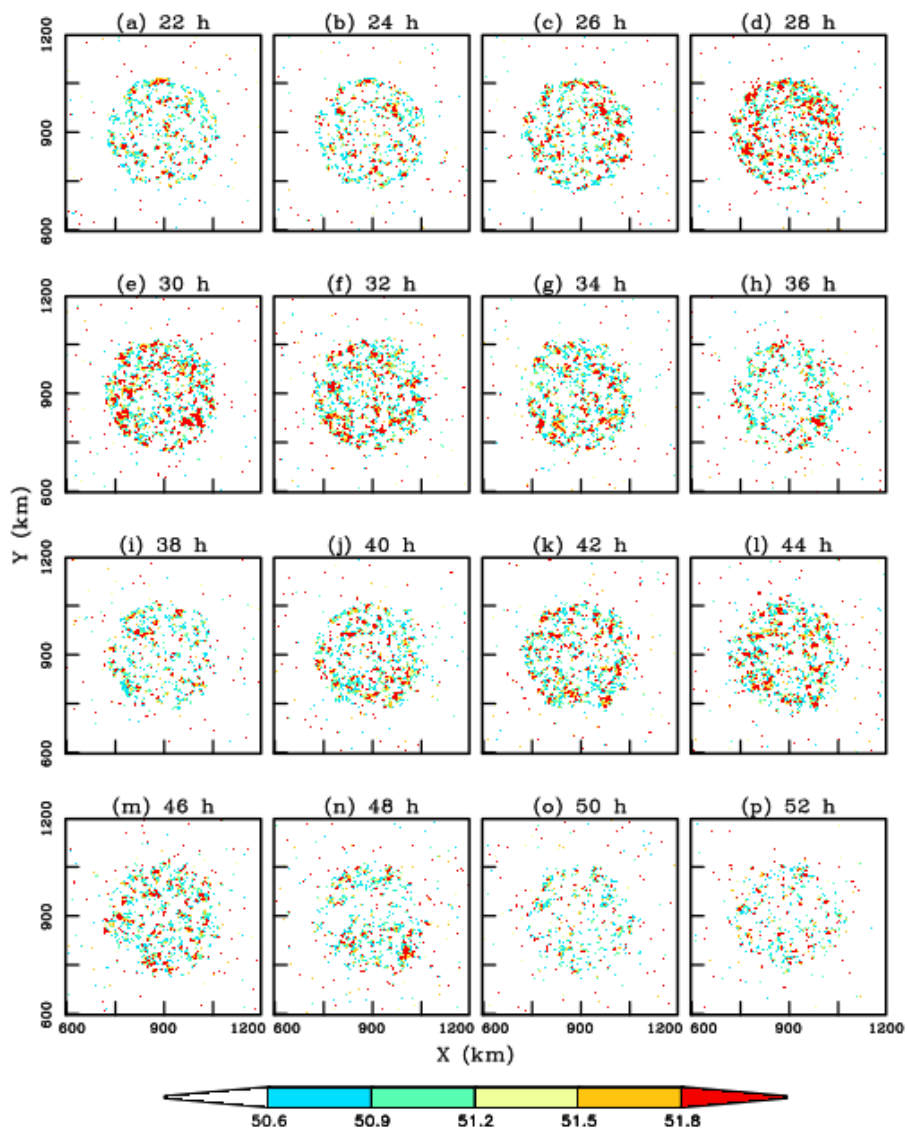
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140 **Fig.1** Time series of (a) precipitation rate (mm h^{-1}) and (b) water vapor path (kg m^{-2})
141 over the inner 150 km radii of the disturbance in CTLF10 (black), CTLF05 (red), and
142 CTLF0 (blue).

143

144 To confirm that this quasi-periodic pulsing is physically meaningful rather than a
145 result of model noise, we present plane views of WVP from 22 h to 52 h in CTLF10
146 (Fig. 2). In Fig. 2, the WVP shows clear variations, mainly confined to the initially
147 disturbed area. The WVP has an increasing trend from 22-28 h and 38-44 h, and a
148 decreasing trend from 30-36h and 46-52h, consistent with the variation of WVP shown
149 in Fig. 1b.

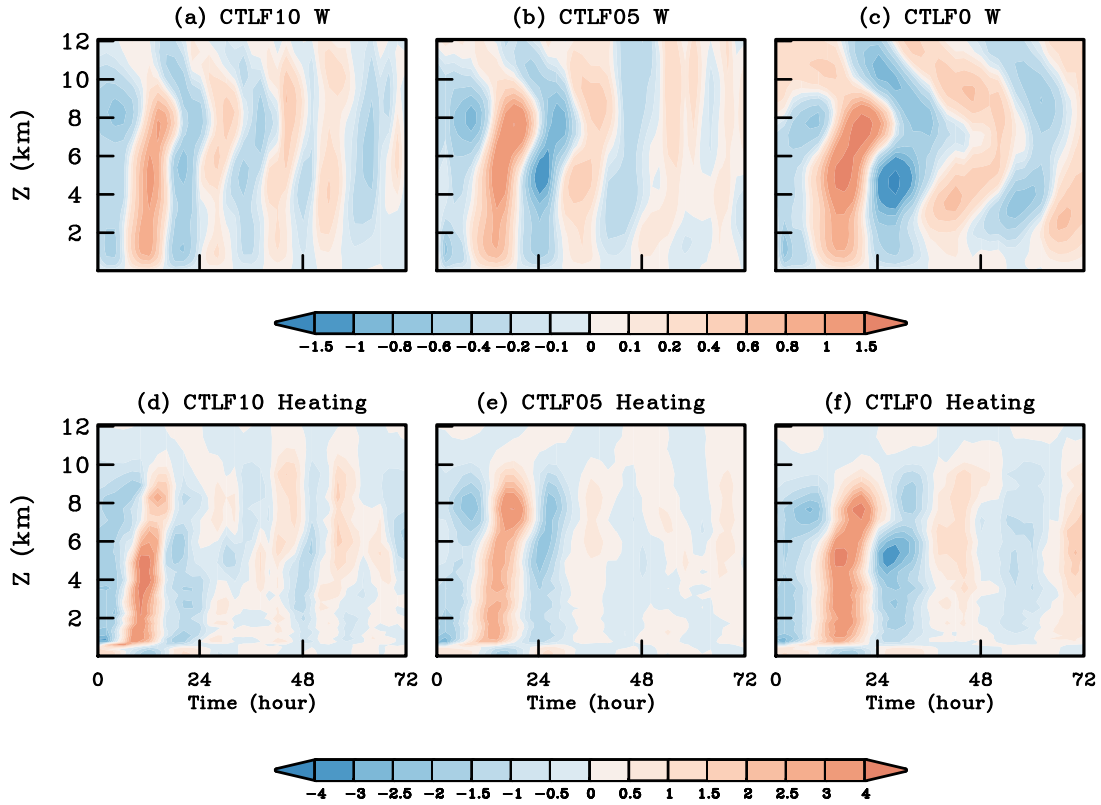
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152 **Fig. 2** Plane views of water vapor path (kg m^{-2}) from 22 h to 52 h in CTLF10.

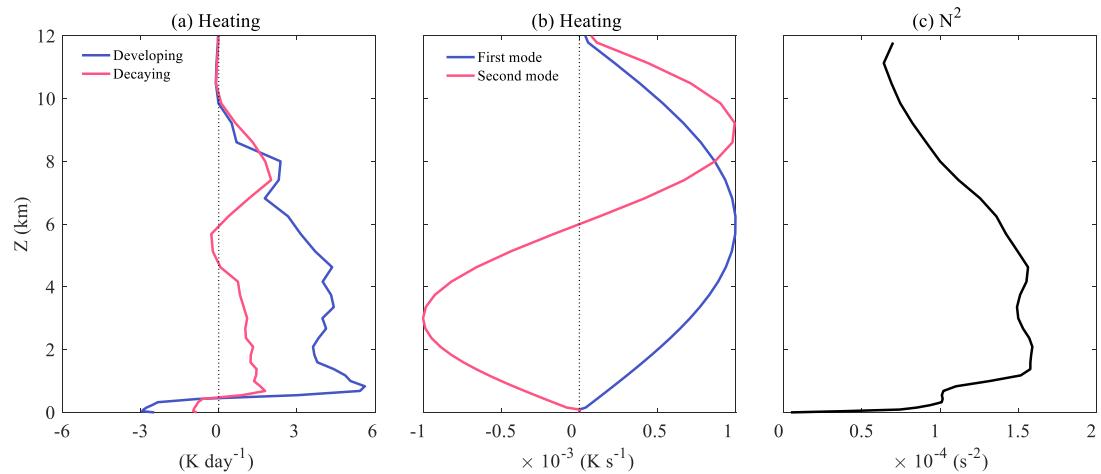
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154 We also present time-height plots of vertical velocity and diabatic heating averaged
155 over the disturbed area during the whole simulation. Given that the disturbed columns
156 exhibit a systematic warming trend at upper levels and an elevated convective top
157 throughout the entire 3-day simulation period (Fig. A2), we use a moving average
158 method to filter out variations longer than 30 hours. The filtered variables exhibit clear
159 periodic features in the central column of the domain (where the disturbance was
160 initiated with the initial moisture anomaly) across all simulations (Fig. 3). Based on the
161 results after filtering, we define periods with positive mass-weighted vertical integrated
162 vertical velocity as the convectively active stages, and those with negative column-
163 integrated vertical velocity as the convectively suppressed stages. In CTLF10, the first
164 active stage occurs from 6 h to 16 h. The mean latent heating profile shows a vertical
165 half-wavenumber structure in the free-troposphere (above the BL top). Unlike the first
166 baroclinic mode observed in real-world scenarios (e.g., Haertel and Kiladis 2004;
167 Houze, 2018), the latent heating here exhibits a bottom-heavy structure, with its
168 maximum around 1 km altitude (Fig. 4a). The first suppressed stage occurs from 16 h
169 to 24 h, during which latent heating is significantly weaker compared to the developing
170 stage. In this stage, the heating displays a more complicated vertical structure,
171 characterized by heating from the BL top to 4.4 km, cooling from 4.4 km to 5.8 km,
172 and additional heating from 5.8 to 10 km height (Fig. 4a). Although the peak heating
173 occurs in the upper troposphere, the vertical structure in the suppressed stage does not
174 clearly resemble the stratiform (wavenumber-one) structure seen in previous studies
175 (e.g., Haertel and Kiladis 2004; Houze, 2018).



177

178 **Fig. 3** Time-height plot of (a) vertical velocity (cm s^{-1}) and (d) diabatic heating
 179 (K day^{-1}) in CTLF10, with signals longer than 30 hours filtered out. All the variables
 180 are averaged in the inner 150 km radii of the domain. (b), (e) and (c), (f) are for CTLF05
 181 and CTLF0, respectively.

182



183

184

185 **Fig. 4** Vertical profiles of (a) the latent heating profiles averaged in the first active (blue)
 186 and suppressed (red) stage of CTLF10, (b) the first (blue) and second (red) diabatic

187 heating mode (K s^{-1}) used in the dry simulations, and (c) the N^2 (s^{-2}) averaged in the
188 initial 2 hours over the disturbed area.

189

190 In this first suppressed stage, subsidence occurs in the lower levels of the disturbed
191 column, extending from 6 km down to the surface (Fig. A2a). This downward motion
192 and the associated drying (between hours 16-24; Figs. 1b & 3) might be expected to
193 inhibit subsequent convection at the same location (e.g., Houze, 1982; Houze, 2018).
194 However, deep convection is reinvigorated after 24 hours, and the initially disturbed
195 column repeats this cycle of active and suppressed convection over the next several
196 days (Figs. 1 & 3). A similar pattern is seen in CTLF05 and CTLF0, although the
197 periods of the cycles differ (Figs. 1 & 3).

198 The occurrence of quasi-periodic convection raises two questions: What
199 mechanisms facilitate the recovery of deep convection following the downward motion
200 in the disturbed air column? Additionally, what determines the period of the cycle? We
201 will address these questions in the next two sections.

202

203 **4. Convective recovery: the role of low-level buoyancy**

204 To understand the recovery of convection after the suppressed stage in the disturbed
205 column, we need to understand the evolution of the variables that determine convective
206 activity. Previous studies have demonstrated that low-level buoyancy plays a crucial
207 role in determining precipitation in tropical MCDs (e.g., Ahmed and Neelin 2018;
208 Ahmed et al. 2020). Following Ahmed et al. (2020), the low-level buoyancy of an
209 entraining convective plume can be approximated as:

$$210 \quad B_{low} = g(w_1 \frac{\theta_{eBL} - \theta_{el}^*}{\theta_{el}^*} - w_2 \frac{\theta_{el}^* - \theta_{el}}{\theta_{el}^*}), \quad (1)$$

211 in which θ_{eBL} is the BL averaged θ_e , θ_{el} is the θ_e averaged in the lower free-
212 troposphere, and θ_{el}^* is the saturation θ_e in the lower free-troposphere. The first term
213 on the right-hand side of Eq. (1) can be interpreted as an approximate measure of the
214 undilute plume buoyancy based on BL properties and lower free-tropospheric

215 temperature, and the second term measures the influence of lower free-tropospheric
 216 subsaturation on the plume via entrainment. The coefficients w_1 and w_2 are the weights
 217 of the two processes, which can be expressed as:

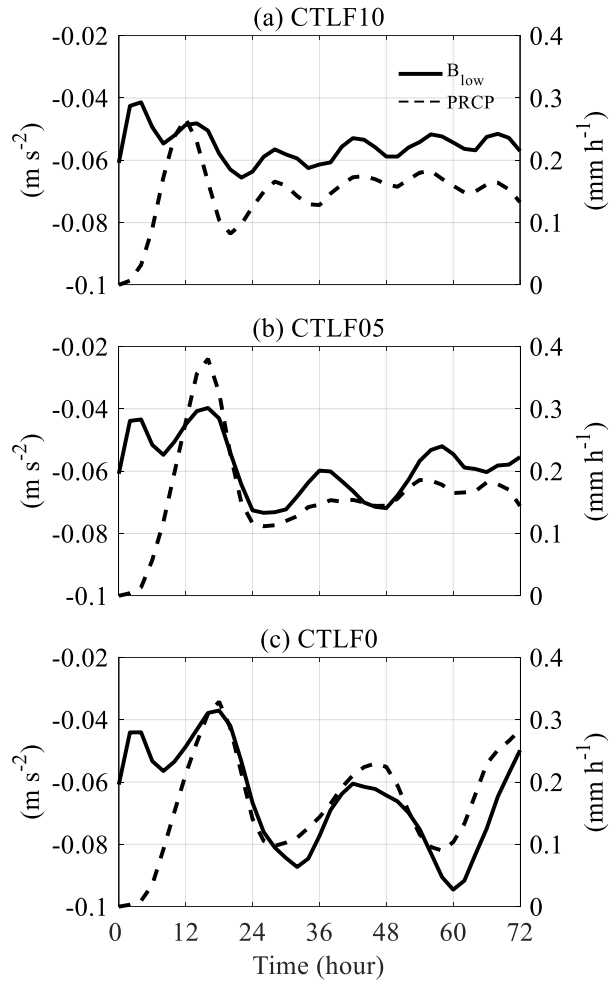
$$218 \quad w_1 = \frac{\Delta p_{BL}}{\Delta p_L} \ln\left(\frac{\Delta p_{BL} + \Delta p_L}{\Delta p_{BL}}\right),$$

$$219 \quad w_2 = 1 - w_1.$$

220 In this study, the BL and the low-level troposphere are defined as the layer below 900
 221 hPa and the layer between 900 hPa and 500 hPa, respectively. With this definition, w_1
 222 and w_2 are 0.4 and 0.6, respectively, but we follow parts of Ahmed et al. (2020) and
 223 henceforth use $w_1 = w_2 = 0.5$ to estimate the low-level buoyancy. All vertically averaged
 224 variables in Eq. (1) are density weighted.

225 The time evolution of B_{low} in the ‘CTL’ simulations is shown in Fig. 5. Except
 226 for the last 12 hours in ‘CTLF05’, the evolution of B_{low} is generally in phase and
 227 strongly correlated with precipitation in the disturbance region in all three simulations
 228 after 12 h. For comparison, plane views of B_{low} from 22 to 54 h in CTLF10 are also
 229 presented in Fig. 6. It is evident that the most significant variations in B_{low} occur in
 230 the central column that was initially disturbed, which generally retains its size, shape,
 231 and location throughout the simulation. B_{low} shows an increasing trend from 22-28 h
 232 and 38-44 h, and a decreasing trend from 30-36h and 46-52h, consistent with the
 233 variations of precipitation and B_{low} shown in Fig. 5a.

234



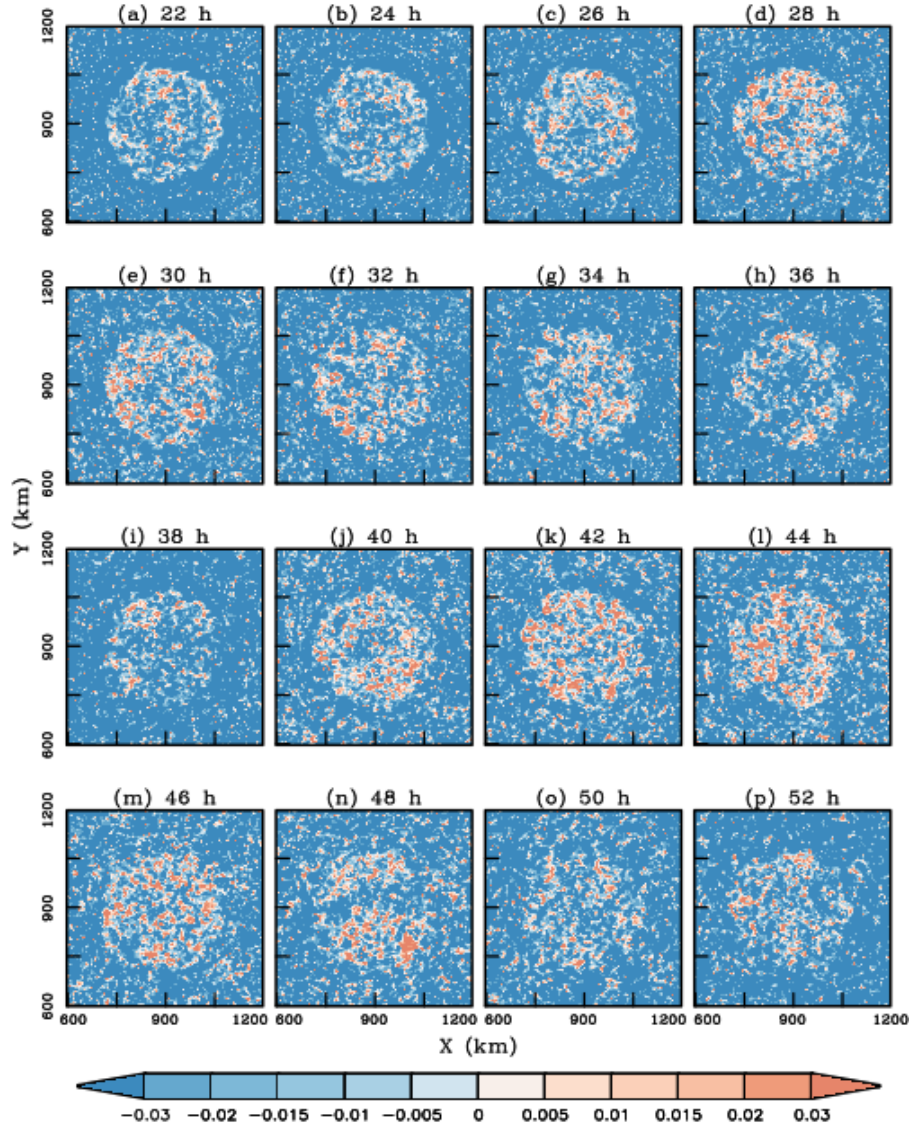
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236 **Fig. 5** Time series of low-level buoyancy (solid, m s^{-2}) and precipitation rate

237 (dashed, mm h^{-1}) over the inner 150 km radii of the disturbance in (a) CTLF10, (b)

238 CTLF05, and (c) CTLF0.

239



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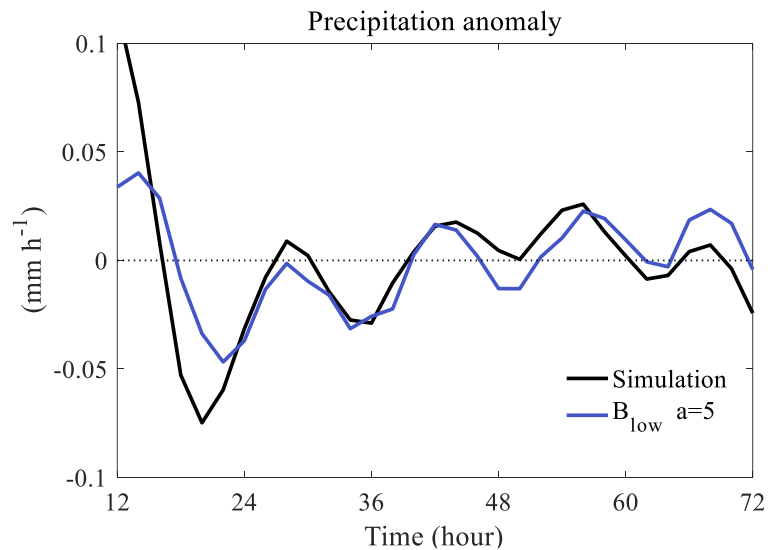
241 **Fig. 6** Plan views of B_{low} (m s^{-2}) from 22 h to 52 h in CTLF10. We add a constant value
 242 of 0.05 to make B_{low} in the disturbance region around 0.

243

244 To further investigate whether the evolution of B_{low} quantitatively reflects
 245 precipitation changes, we reference the P- B_{low} relationship established in Ahmed et al.
 246 (2020, their Fig. 2) and find that sensitivity of $a=5$ (mm h^{-1}) (m s^{-2}) $^{-1}$ provides an
 247 approximate fit in our simulations¹. Here, we calculate the precipitation anomaly using

¹ Ahmed et al. (2020) found larger sensitivities of precipitation to buoyancy ($a=20$ (mm h^{-1}) (m s^{-2}) $^{-1}$) than what we use here, but those were for positive buoyancies. In our simulations the precipitation occurs at weakly negative buoyancies, which is consistent with the smaller sensitivity

248 the variation of B_{low} in CTLF10, and compare it with the temporal precipitation
 249 anomaly from 0-72 h in CTLF10. As shown in Fig. 7, the temporal precipitation
 250 anomalies estimated from buoyancy variations are a close match to the explicitly
 251 simulated precipitation. This further validates the use of low-level buoyancy as a means
 252 of quantitatively understanding the evolution of convection in the disturbed column.
 253 Nonetheless, it is important to recognize that while B_{low} correlates well with
 254 precipitation, the absolute values do not always align. For instance, at 44 hours, B_{low}
 255 in CTLF0 is lower than in CTLF10, yet the precipitation in CTLF0 is greater (Fig. 5).
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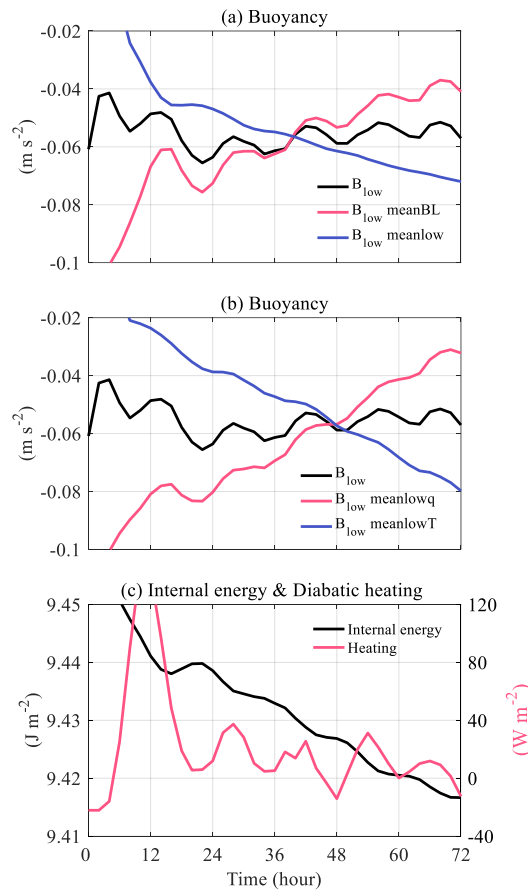


257
 258 **Fig. 7** Time series of temporal precipitation anomaly (mm h^{-1}) from 12-72 h in the
 259 disturbance in CTLF10 (black) and the precipitation anomaly estimated with low-level
 260 buoyancy (blue).

261
 262 The above analysis indicates that, following the decay of the initial pulse of
 263 precipitating convection, the recovery of low-level buoyancy is critical to the recovery
 264 of deep convection and precipitation. According to equation (1), there are three factors
 265 controlling the low-level buoyancy: the BL θ_e , the temperature in the lower free-

we use here.

266 troposphere, and water vapor mixing ratio (q_v) in the lower free-troposphere. A higher
 267 BL θ_e , a larger lower free-tropospheric humidity, or a colder lower free-tropospheric
 268 temperature produce an increased B_{low} . To identify which factor dominates the
 269 evolution of B_{low} , we calculate B_{low} in CTLF10 again but substitute the BL θ_e with
 270 its temporal mean from 0-72 h. Fixing the BL θ_e in Eq. (1) introduces a systematic
 271 trend in B_{low} for the duration of the simulation, but retains significant pulsing in B_{low}
 272 (Fig. 8a). However, when the temperature and moisture variation in the lower free-
 273 troposphere is removed using the same method, the pulsing signal in B_{low} greatly
 274 diminishes (Fig. 8a). This indicates that for B_{low} to recover, it is the lower free-
 275 troposphere that matters most.
 276



277

278 **Fig. 8** (a) Time series of the original B_{low} ($m\ s^{-2}$) in CTLF10 (black), B_{low} calculated

279 with a 0-72 h temporal mean BL variables ($B_{\text{low_meanBL}}$, red), and B_{low} calculated
280 with 0-72 h temporal mean lower free-tropospheric variables ($B_{\text{low_meanlow}}$, blue) in
281 CTLF10. (b) Time series of the original B_{low} in CTLF10 (black), B_{low} calculated
282 with a 0-72 h temporal mean lower free-troposphere q_v ($B_{\text{low_meanlow}q}$, red), and B_{low}
283 calculated with a 0-72 h temporal mean lower free-troposphere temperature
284 ($B_{\text{low_meanlow}T}$, blue) in CTLF10. (c) Time series of lower free-tropospheric mass-
285 weighted internal energy (black, J m^{-2}) and diabatic heating (red, W cm^{-2}) in CTLF10.
286

287 We further investigate which characteristics in the lower free-troposphere are most
288 significant in influencing the pulsing of B_{low} . We recalculated B_{low} in CTLF10 by
289 substituting the free-tropospheric temperature and water vapor with their temporal
290 means from 0 to 72 hours. The results indicate that the pulsing of B_{low} is controlled
291 mostly by the temperature in the lower free-troposphere (Fig. 8b; the variance of the
292 detrended $B_{\text{low_meanlow}T}$ line in Fig. 8b is about one-third the variance of the
293 detrended $B_{\text{low_meanlow}q}$ line). This suggests that the variation of low-level
294 temperature plays a primary role in the variation of B_{low} , and in turn, the variation in
295 precipitation.

296 In this section, we demonstrated that the oscillation of deep convection and
297 precipitation could be explained by the oscillation of low-level buoyancy, which is
298 primarily influenced by variations in the lower free-tropospheric temperature. However,
299 the mechanisms causing these temperature variations remain unclear. Previous
300 theoretical studies have argued that diabatic cooling in the lower free-troposphere by
301 stratiform convection can produce a decrease of lower free-tropospheric temperature
302 following deep convective heating (e.g., Mapes 2000; Kuang 2008b). However, in our
303 simulations, the diabatic cooling caused by stratiform precipitation is relatively weak.
304 In some cases, there is even no discernible diabatic cooling in the lower free-
305 troposphere (e.g., CTLF05, Fig. A2e). Furthermore, Fig. 8c generally shows an out-of-

306 phase relationship (in a signal that is admittedly noisy) between temperature anomalies
 307 and diabatic heating anomalies, with multiple instances of positive temperature
 308 tendency anomalies occurring while diabatic heating anomalies are negative. This
 309 suggests that the decrease of lower free-tropospheric temperature during the oscillation
 310 is not directly caused by diabatic cooling of a stratiform heating structure. In the
 311 following section, we will explore the occurrence of cooling in the lower free-
 312 troposphere and the recovery of buoyancy from the perspective of adiabatic processes.

313

314 **5. Recovery of Buoyancy: an inertia-gravity oscillation**

315 In this section, we conduct a series of simulations without latent heating (or cooling),
 316 termed ‘Dry’, to investigate the recovery of buoyancy in tropical MCDs after the
 317 suppressed stage (Table 2). These simulations have a domain size of 3000 km × 3000
 318 km with open lateral boundary conditions. Additionally, there is no radiation or
 319 microphysics parameterization. The other settings remain consistent with the ‘CTL’
 320 series.

321

322

Table 2 Descriptions of dry experiments.

Name	Description
Dry_Active	A 3000 km×3000 km simulation forced with the heating profile averaged in the active stage of CTLF10. There is no microphysics or radiation parameterization, and the open lateral boundary condition is used. The other settings are as in CTLF10.
Dry_Suppressed	As in Dry_Active, but forced with the heating profile averaged in the suppressed stage.
Dry2_F10	As in Dry_suppressed, but forced with the stratiform heating profile shown in Fig. 6b.
Dry2_F05	As in Dry2_F10, but with Coriolis parameter set to be $5 \times 10^{-5} \text{ s}^{-1}$.
Dry2_F0	As in Dry2_F10, but without Coriolis forcing.
Dry1_F10	As in Dry2_F10, but forced with a deep convective heating profile shown in Fig. 6b.
Dry1_F05	As in Dry1_F10, but with Coriolis parameter set to be $5 \times 10^{-5} \text{ s}^{-1}$.
Dry1_F0	As in Dry1_F10, but without Coriolis force.

323

324 We first test the response of the disturbed column to heating in the convectively

325 active (Dry_active) and suppressed (Dry_suppressed) stage, as defined in section 3
 326 (Fig. 5a). In all the dry simulations, the imposed diabatic heating is maintained for two
 327 hours, followed by an additional 46 hours of simulation. In both Dry_active and Dry_
 328 suppressed, the diabatic heating produces subsequent damped oscillations of multiple
 329 variables including B_{low} (Figs. 9 and 10a).

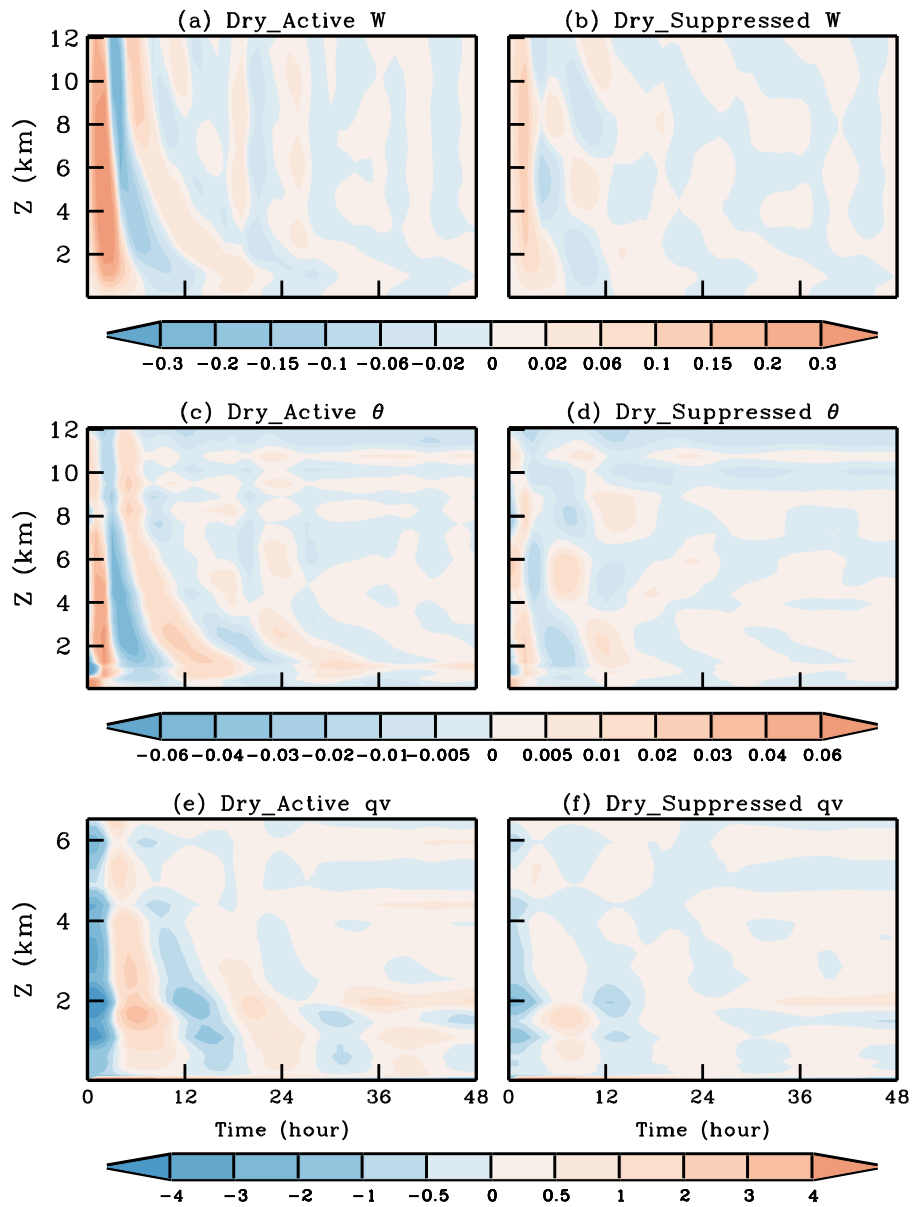
330 The purpose of the full-physics ‘CTL’ simulations is to show that, even when
 331 initiated from a simple moist bubble, the resulting MCD can show a pulsing signal.
 332 However, the heating profiles shown in Fig. 4 are highly atypical of real-world
 333 conditions. In real-world observations, tropical MCDs usually exhibit a half-
 334 wavenumber vertical structure during the development of deep convection, and a
 335 wavenumber-one vertical structure during the decay of deep convection (e.g., Haertel
 336 and Kiladis 2004; Houze 2018). To better understand the mechanism of the oscillation
 337 and to draw closer connections to real-world scenarios, we conduct a second set of dry
 338 simulations forced by a vertical wavenumber-one heating structure (‘Dry2’; Table 1).

339 The heating structure in the ‘Dry2’ simulations is given as follows:

$$Q(r, z) = \begin{cases} Q_0 \sin(2\pi z/H - \pi) \cos(\pi r/2R) & (z < H \text{ and } r < R) \\ 0 & (z \geq H \text{ or } r \geq R) \end{cases} \quad (2)$$

340 In Eq. (2), r and z represent radius and height, respectively. H and R are the maximum
 341 height and radius of the heating, which are 12 km and 150 km, respectively. Q_0 is the
 342 magnitude of the heating, which is set to be 0.001 K s^{-1} . This heating has a typical
 343 second baroclinic mode (stratiform heating profile) in the vertical direction (Fig. 4b),
 344 which also decays sinusoidally with radius. The magnitude of the heating is chosen to
 345 be roughly 20 times stronger than the diabatic heating in the developing phase of the
 346 full-physics model (Fig. 4a) to both better match diabatic heating values in observed
 347 real-world synoptic systems and obtain a better signal-to-noise ratio (simulations using
 348 a weaker forcing with magnitude of $1 \times 10^{-4} \text{ K s}^{-1}$ produces qualitatively similar results).

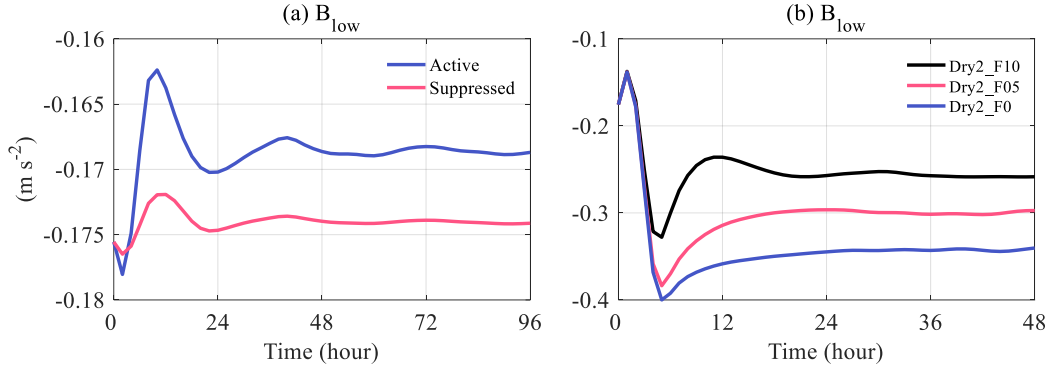
349



350

351 **Fig. 9** The time-height plot of (a) vertical velocity (cm s^{-1}), (c) temporal potential
 352 temperature anomaly (K), and (e) temporal q_v anomaly (g kg^{-1}), all averaged in the inner
 353 150 km radii of the central column in Dry_Active. (b), (d) and (f) are the corresponding
 354 variables for Dry_Suppressed.

355



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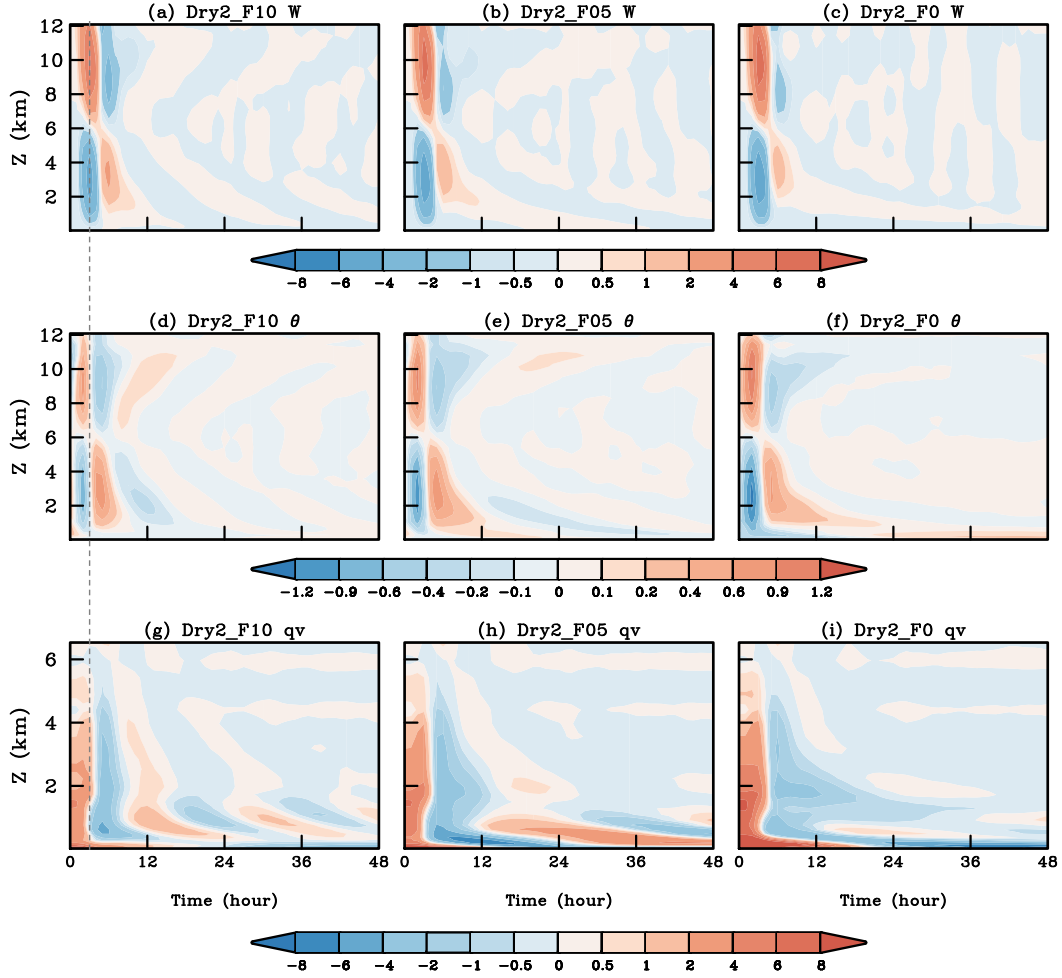
357 **Fig. 10** (a) Time series of B_{low} (m s^{-2}) in Dry_Active (blue) and Dry_Suppressed (red).

358 (b) Time series of B_{low} (m s^{-2}) in Dry2_F10 (black), Dry2_F05 (red), and Dry2_F0

359 (blue).

360

361 The immediate response of the air column in Dry2_F10 to the heating is
 362 characterized by upward motion above 6 km and downward motion below 6 km (Fig.
 363 10a). Although these vertical motions may induce adiabatic cooling at upper levels and
 364 warming at lower levels, they are insufficient to offset the diabatic heating and cooling
 365 over such a short time frame. Consequently, warm and cold anomalies develop at 9 km
 366 and 3 km, respectively, during the initial hours (Fig. 11d). Additionally, the vertical
 367 motion redistributes water vapor, with subsidence over the first several hours inducing
 368 a drying tendency at lower levels. Note that both potential temperature and q_v exhibit
 369 stronger vertical variations than temporal variations. To better isolate the temporal
 370 oscillations of interest, we remove the time-mean vertical profile from both fields in
 371 Fig. 11, so a secular drying trend over the course of the simulation yields a moist
 372 anomaly during the initial few hours that decays in response to the subsidence.



373

374 **Fig. 11** The time-height plot of (a) vertical velocity (cm s^{-1}), (d) temporal potential
 375 temperature anomaly (K), and (g) temporal q_v anomaly (g kg^{-1}), all averaged in the inner
 376 150 km radii of the domain in Dry2_F10. (b), (e), (h) and (c), (f), (i) are for Dry2_F05
 377 and Dry2_F0, respectively. The vertical dashed line marks the moment that the vertical
 378 velocity in the lower free-troposphere reaches the first minimum, indicating that the
 379 temperature and q_v anomaly is 1/4 period behind the vertical velocity.

380

381 Although the diabatic heating ceases after 2 hours, the response of vertical motion
 382 persists for a significantly longer duration. The evolution of temperature and q_v lags the
 383 vertical velocity by one-fourth of the oscillation period, suggesting that vertical motion
 384 is the driving force behind the changes in temperature and q_v . The subsidence in the
 385 lower free-troposphere further results in warming and drying at lower levels, which
 386 decreases low-level buoyancy that would be expected to suppress convection in a

387 simulation with latent heating (Fig. 10b). However, the vertical motion reverses 6 hours
388 after model initialization (4 hours after the cessation of the diabatic forcing), resulting
389 in a cooler and moister lower troposphere that enhances B_{low} (Fig. 10b). In fact, the
390 vertical motion undergoes periodic sign changes, leading to oscillations in temperature
391 and q_v (Figs. 11a, d, & g), and, in turn, B_{low} (Fig. 10b). In Dry2_F05 and Dry2_F0, we
392 also find similar oscillations (Figs. 10b & 11). The oscillation period increases as the
393 Coriolis parameter decreases, consistent with the results of the full-physics simulations
394 (Fig. 1). It is important to note that in all the dry simulations, the oscillation period
395 varies with altitude (Fig. 11), characterized by shorter periods throughout most of the
396 troposphere and longer periods in the upper troposphere and the lowest kilometer (here
397 the period is defined as the time between the first two same-signed vertical velocity
398 extrema). This vertical structure of the period also corresponds to an increase in vertical
399 wavenumber over time (Fig. 11).

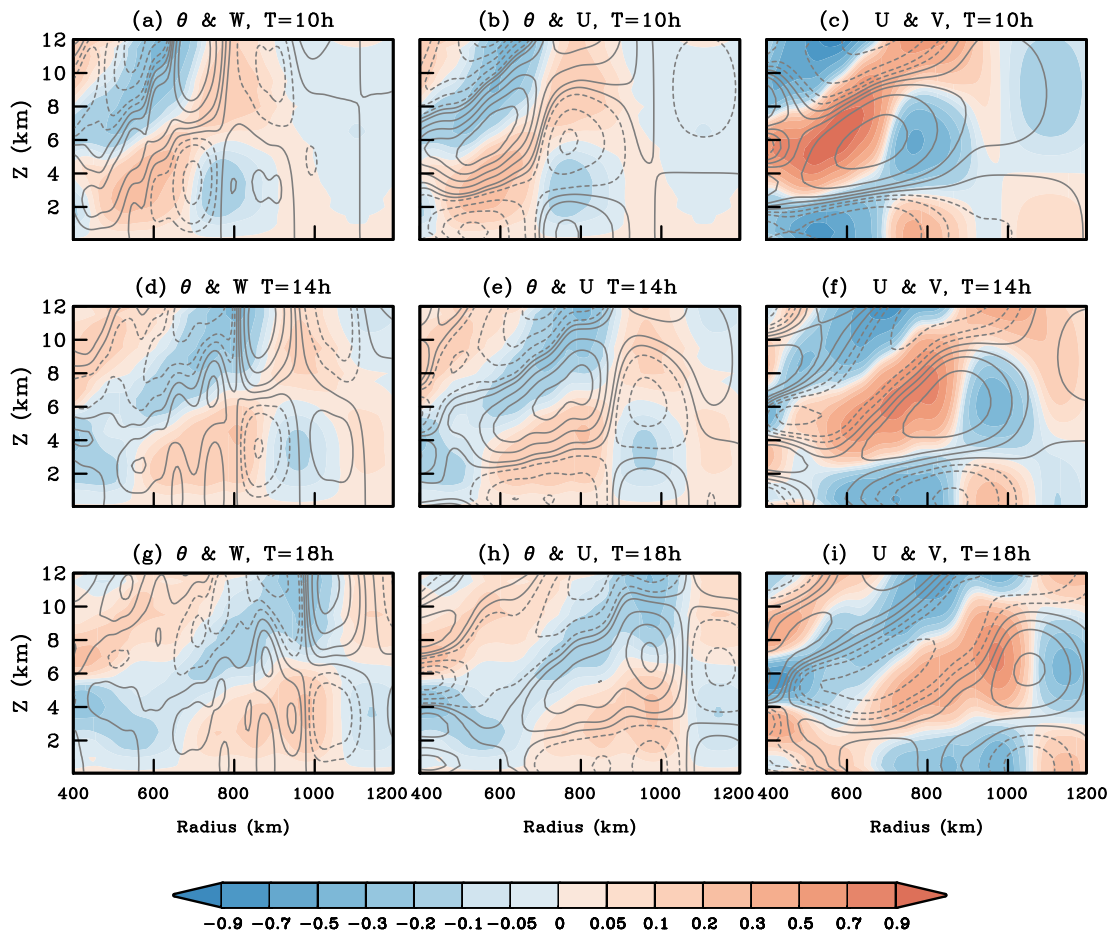
400 We have shown that in dry simulations, an air column perturbed by a stratiform
401 heating profile exhibits internal damped oscillations, which alter low-level buoyancy in
402 ways that would be expected to support oscillations of precipitating convection if
403 condensation occurred. Given that the simulations are conducted on an f-plane within
404 a stratified atmosphere, these oscillations are likely inertia-gravity oscillations. An air
405 column being disturbed usually serves as a wave source, which excites waves that are
406 characterized by specific spatial structures of dynamical and thermodynamic variables.
407 To confirm the inertia-gravity nature of the oscillation, we will now study the property
408 of the waves triggered by the oscillation and compare the characteristics with linear
409 inertia-gravity wave theory.

410 The radius-height structures of several key variables outside the disturbance region
411 in Dry2_F10, as shown in Fig. 12, indicate an outward propagating wave signal. The
412 first wave front at 10 h exhibits subsidence at upper levels and ascent at lower levels at
413 radii between 400-500 km, and consists of an outward-propagating structure with
414 respective warm and cold anomalies one-fourth of a wavelength behind the vertical
415 motion (Figs. 10a, d & g). This structure aligns with findings from previous studies

416 (e.g., Nicholls et al. 1991; Mapes 1993).

417 In a linear inertia-gravity wave, when a cold anomaly is situated above a warm
418 anomaly, ascent and outward radial velocity anomalies should exist between these
419 temperature anomalies (e.g., Fig. 5.12 of Holton and Hakim 2012). The left and middle
420 columns in Fig. 12 illustrate that the relationships between temperature and vertical and
421 radial velocity are consistent with this theoretical expectation. Furthermore, theory
422 predicts that tangential velocity maxima should occur where the radial velocity changes
423 sign. As depicted in the right column of Fig. 12, a similar phase relationship is seen in
424 the Dry2_F10 simulation. The similarity of the wave structure with linear theory
425 reinforces the conclusion that the oscillations produced by the initial diabatic forcing in
426 the dry simulations are inertia-gravity oscillations

427



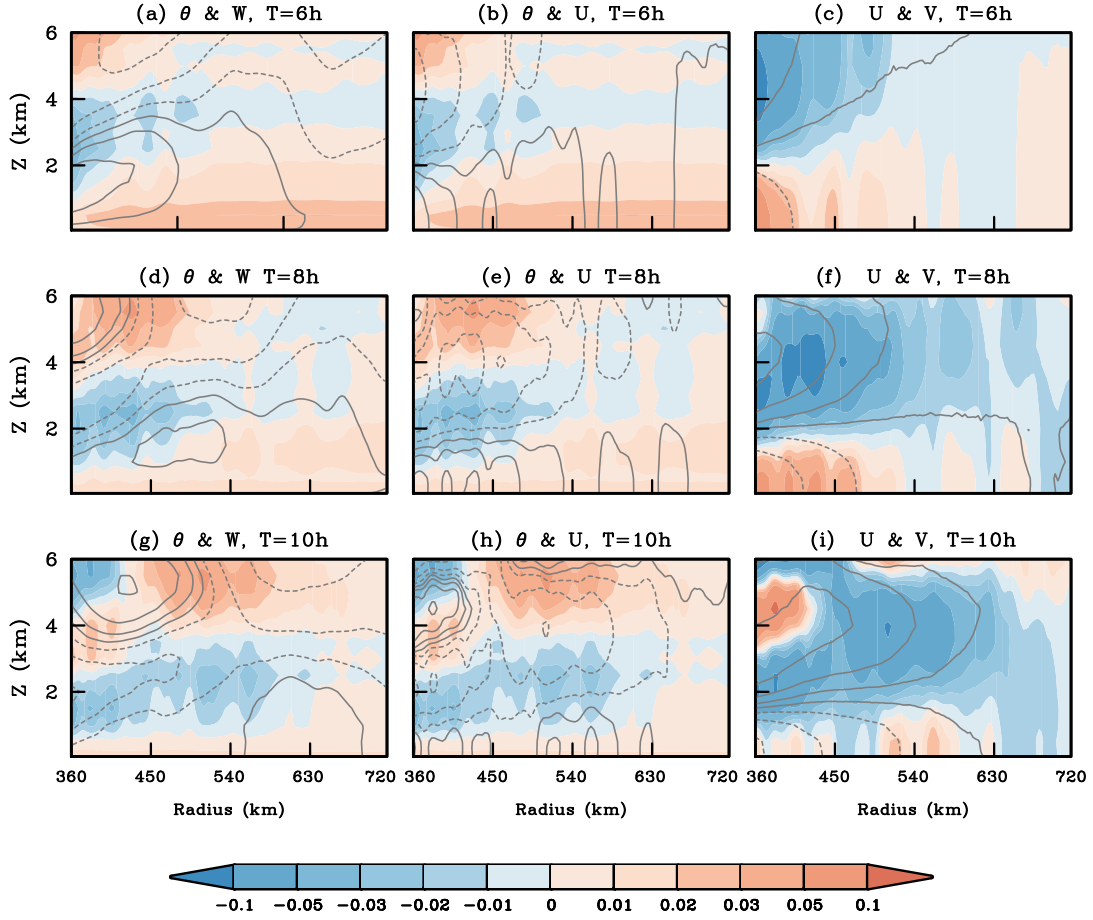
428

429 **Fig. 12** Radius-height plots of azimuthal-mean (a) horizontal potential temperature
430 anomaly (K, shading) and vertical velocity (contours at -3, -2, -1, -0.5, 0, 0.5, 1, 2 and

431 3 cm s⁻¹, with solid lines indicating non-negative values and dashed lines indicating
432 negative values), (b) horizontal potential temperature anomaly (K, shading) and radial
433 velocity (contours at 0.9, -0.7, -0.5, -0.3, -0.1, 0, 0.1, 0.3, 0.5, 0.7 and 0.9 m s⁻¹), and (c)
434 radial velocity (cm s⁻¹, shading) and tangential velocity (contours at -0.6, -0.4, -0.2, -
435 0.1, -0.05, 0, 0.05, 0.1, 0.2, 0.4 and 0.6 m s⁻¹). The upper, middle and lower panel are
436 for 10 h, 14 h and 18 h in Dry2_F10, respectively.

437

438 For comparison, we present radius-height plots of the same variables from the full-
439 physics simulation CTLF10 (Fig. 13). Due to a systematic warming tendency above 7
440 km, which may obscure the wave signal, we focus only on the structures below 6 km.
441 In CTLF10, diabatic heating does not have the simple, idealized vertical structure
442 imposed in the dry simulations, so the wave structures are not as clearly defined as
443 those in the dry simulations. Nevertheless, several dominant features of inertia-gravity
444 waves remain evident. For instance, downward motion (dashed lines in Figs. 13a, d &
445 g) consistently precedes the warm anomaly (red shading in Fig. 13a, d & g), the phase
446 lines separating cold and warm anomalies align with peak radial velocity anomalies
447 (Figs. 13b, e & h), and the tangential velocity maxima correspond to points where the
448 radial velocity changes sign (Fig. 13i). These features suggest that even in full-physics
449 simulations, the oscillation generally retains its inertia-gravity characteristics.



450
451 **Fig. 13** As in Fig.12, but for CTLF10 at 6 h (upper) 8 h (middle) and 10 h (lower).

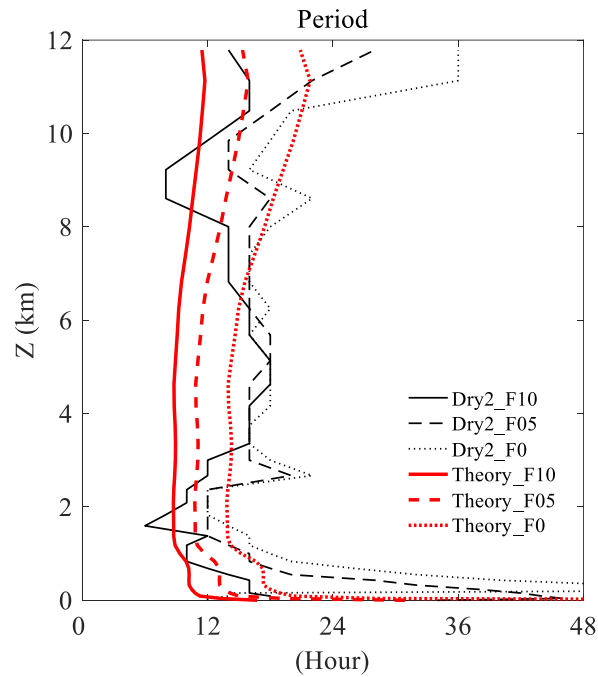
452
453 While the structure of the wave aligns with inertia-gravity wave theory, more
454 quantitative evidence would come from consistency in the dispersion relationship.
455 According to linear inertia-gravity wave theory,

$$456 \quad \nu^2 = f^2 + N^2(k^2 + l^2)m^{-2} \quad (3)$$

457 In Eq. (3), ν is the frequency of the oscillation, f is the Coriolis parameter and N^2 is the
458 buoyancy frequency. k and l are wavenumbers in the x and y directions, respectively,
459 and $k^2 + l^2$ is thus the square of the wavenumber in the radial direction. m is the
460 wavenumber in the vertical direction.

461 Since we have applied a stratiform heating structure in the disturbance as shown in
462 Fig. 4b, the wavelength in the vertical direction should be 12 km. Potential temperature,
463 vertical motion, and radial velocity exhibit a radial wavelength of around 600 km (Fig.
464 12), consistent with a linear response to the forcing which has that same wavelength

465 (the diameter of the impose heating is 300 km, so the wavelength trigger by the heating
 466 should be 600 km). However, the tangential velocity displays a slightly longer
 467 wavelength (Figs. 12f & h), so we use a general wavelength of 750 km. Together with
 468 the profile of N^2 averaged in the first 2 hours over the disturbed area (Fig. 4c), we can
 469 estimate the oscillation period using Eq. (3). The estimated oscillation period is similar
 470 to the period simulated in Dry2_F10 (Fig. 14) and exhibits slightly larger values in the
 471 upper troposphere and substantially larger values just above the surface, due to smaller
 472 values of N^2 at both upper and lower altitudes. Since the horizontal wavelengths in
 473 Dry2_F05 and Dry2_F0 are slightly longer compared to those in Dry2_F10 (Fig. 15),
 474 we estimate the general wavelengths in Dry2_F05 and Dry2_F10 to be 900 km and
 475 1050 km, respectively, and the estimated periods are also consistent with those
 476 observed in the dry simulations (Fig. 14).



477
 478 **Fig. 14** Vertical profiles of period (in hours) in Dry2_F10 (black solid), Dry2_F05
 479 (black dashed) and Dry2_F0 (black dotted). Red lines are their counterparts estimated
 480 by the linear theory.

481

482 From the dispersion relationship, we can further infer the phase speed of the wave.

483 The phase speed is written as:

484

$$c = v / \sqrt{k^2 + l^2} \quad (4)$$

485

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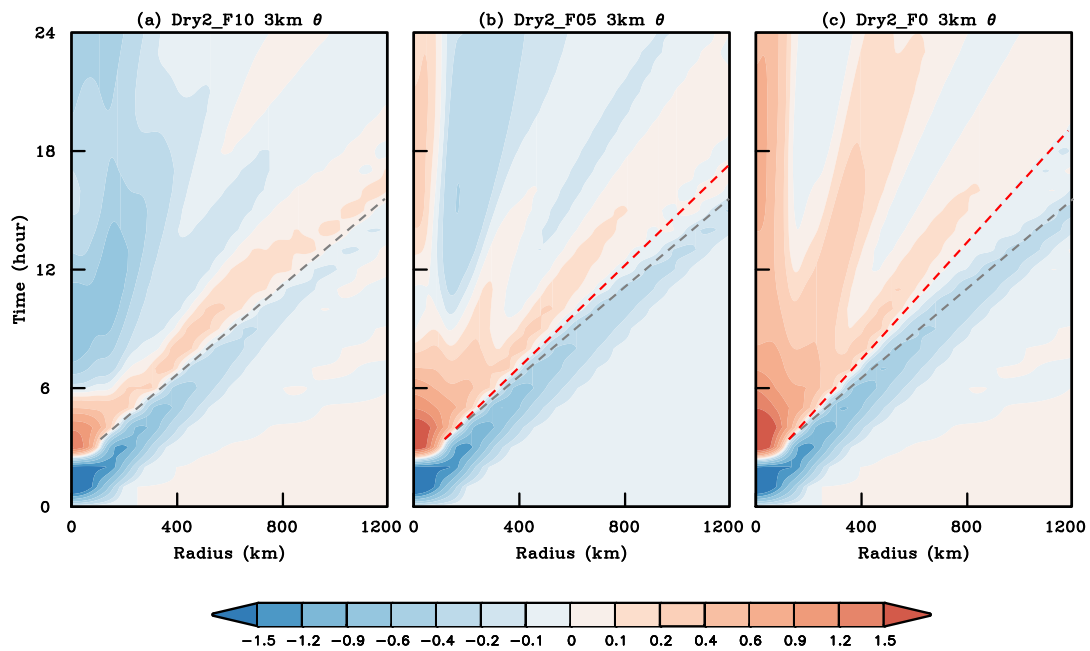
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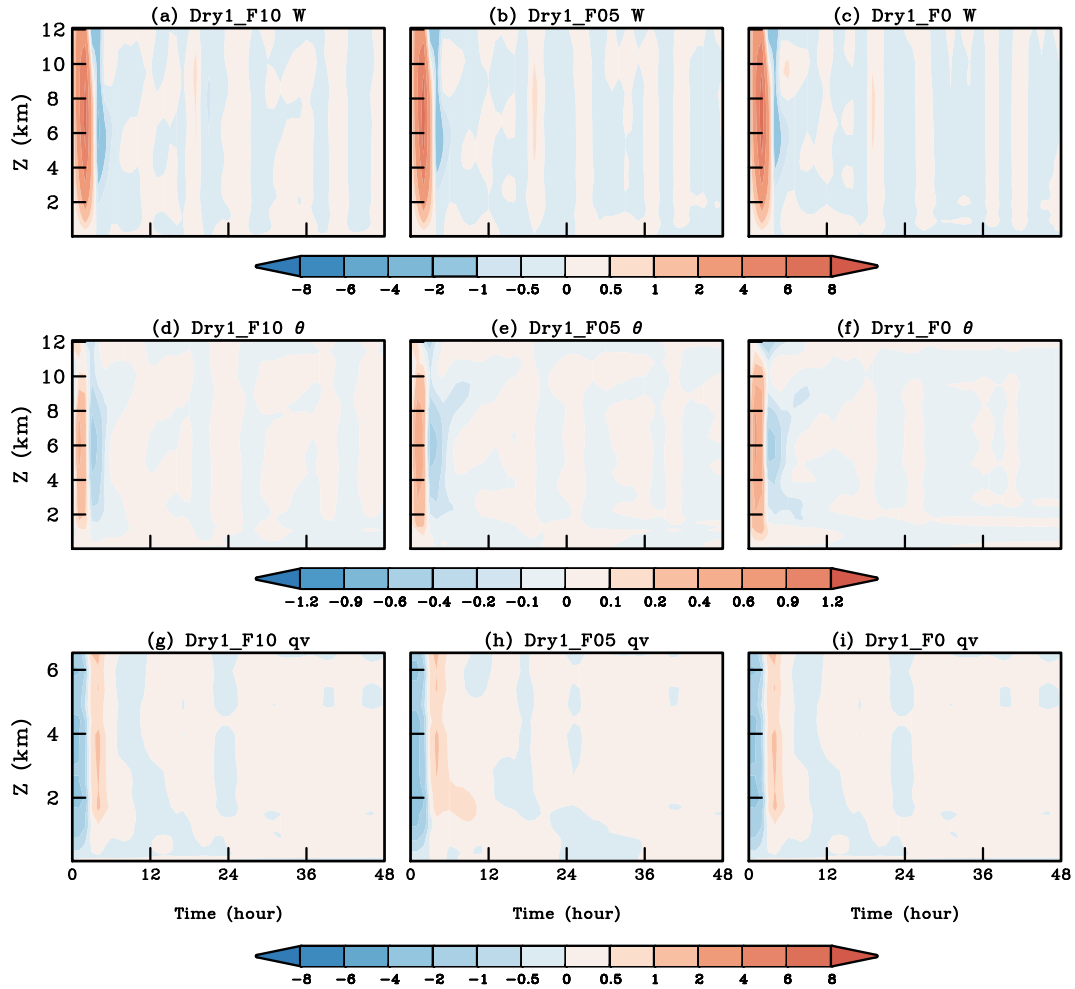
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Fig. 15 Radius–time Hovmöller diagram of the azimuthal-mean of horizontal potential temperature anomaly (K) at 3 km height in (a) Dry2_F10, (b) Dry2_F05 and (c) Dry2_F0. The dashed black lines show the phase line where potential temperature anomaly changes sign in Dry2_F10, and the dashed red lines show those in Dry2_F05 and Dry2_F0, respectively.

Finally, we examine the response of the dry atmosphere to the first baroclinic

503 heating mode, as this heating mode is also a dominant feature in tropical MCDs. The
504 set of ‘Dry1’ simulations is designed similarly to the ‘Dry2’ simulations (Table 2), with
505 the only difference being the application of the first baroclinic heating mode in the
506 vertical direction (Fig. 4b). Upon model initialization, the deep heating triggers upward
507 motion throughout the entire column (Figs. 16a-c). Although this upward motion
508 induces adiabatic cooling, it is insufficient to counterbalance the diabatic heating,
509 resulting in warming across the entire column during the first 2 hours (Figs. 16d-f).
510 After the heating ceases, the upward motion continues, cooling and moistening the
511 lower atmosphere. This free-tropospheric cooling and moistening would be expected to
512 invigorate deep convection and prolong the presence of the first heating mode in full-
513 physics simulations. After 6 hours, the vertical velocity becomes negative in the
514 disturbance region (Figs. 16a-c), which reduces the cold and wet anomalies in the
515 column (Figs. 16d-i). However, there is no clear recovery of upward motion or low-
516 level buoyancy following this subsidence, so that any oscillation is sufficiently damped
517 so as to exist for only one period. Furthermore, the magnitude of the response in the
518 ‘Dry1’ simulations is significantly smaller than that of the ‘Dry2’ simulations. These
519 results strongly suggest that it is the second baroclinic heating mode that is responsible
520 for the inertia-gravity oscillation, especially in real-world scenarios.

521



522
 523 **Fig. 16** As in Fig. 11, but for Dry1_F10, Dry1_F05 and Dry1_F0.

524

525 From the dry simulations in this section, we have demonstrated that in a
 526 background with rotation and stratification, an air column disturbed by mesoscale
 527 diabatic heatings can lead to oscillations, with the underlying mechanism being an
 528 inertial-gravity oscillation. In real-world scenarios, the stratiform heating profile plays
 529 a crucial role in the recovery of low-level buoyancy. Although the immediate response
 530 to the stratiform cooling in the lower free-troposphere does not favor low-level
 531 buoyancy recovery, the inertia-gravity oscillation triggered by the entire stratiform
 532 heating (vertical wavenumber 1) profile soon results in ascent at the lower levels of the
 533 disturbed air column. This upward motion cools and moistens the lower atmosphere,
 534 facilitating the recovery of low-level buoyancy and, consequently, initiating a new
 535 episode of deep convection.

536 During such oscillation of MCDs, the waves are internally excited by convection
537 itself. Diabatic heating serves not only as a source for the subsequent oscillations of the
538 air column but also as a consequence of the preceding oscillations. The wave source—
539 namely, the convective heating—redevelops with each oscillation period, thereby
540 establishing this phenomenon as a convectively coupled inertia-gravity oscillation.
541 Although the oscillation of MCDs within convectively coupled inertia-gravity waves
542 shown in previous studies (e.g., Haertel and Kiladis 2004; Kuang 2008) has also been
543 termed a ‘convectively coupled inertia-gravity oscillation’, those oscillations are
544 different from the one examined in this study. Those previous studies have primarily
545 examined the influence of waves with characteristic scales of 2000-4000 km on
546 convective activity in a region through which the waves horizontally propagate. To
547 distinguish the phenomenon examined here from concepts presented in previous studies,
548 we refer to the oscillation in this study as a "convectively coupled internal oscillation."

549

550 **6. Discussion and Summary**

551 Gravity waves serve as a crucial link between convective disturbances and their
552 surrounding environments. On one hand, large-scale waves propagating across a region
553 may produce quasi-periodic behavior of convection in that region by modifying the
554 environmental conditions (e.g., Haertel and Kiladis 2004; Kuang 2008a; Kuang 2010;
555 Tulich and Mapes 2010). On the other hand, latent heating within a convective
556 disturbance can also initiate gravity waves that propagate away from the disturbance.
557 While research on such convectively generated waves typically focuses on how these
558 waves affect the remote environment—such as by radiating momentum and energy
559 away from the disturbance (e.g., Bretherton and Smolarkiewicz 1989; Nicholls et al.
560 1991; Mapes 1993)—the influence of these waves on the subsequent behavior of the
561 convective disturbance has received comparatively little attention. A useful analogy is
562 that of a stone dropped into a calm pond: the disturbed water column not only generates
563 gravity waves that propagate outward, but itself continues to oscillate after the initial
564 disturbance.

565 In this study, we employ a series of idealized convective-permitting simulations to

566 investigate the evolution of an atmospheric column being disturbed. Full-physics
567 simulations demonstrate that the disturbed column typically exhibits internal damped
568 oscillations in convective activity. Detailed analysis reveals that the oscillations in
569 convection are primarily driven by oscillations in low-level buoyancy, which in turn
570 arise from oscillations in temperature and moisture in the lower free-troposphere. By
571 comparing dry simulations with linear gravity wave theory, we further show that the
572 oscillations in lower-tropospheric temperature and moisture within the disturbed
573 column are a consequence of inertia-gravity oscillations forced by an initial pulse of
574 diabatic heating.

575 The convective oscillation seen in our research is internally generated, during
576 which diabatic heating serves not only as a source for the subsequent inertia-gravity
577 oscillations of the air column but also as a consequence of the preceding oscillations.
578 Although inertia-gravity oscillations and convection can occur almost anywhere on
579 Earth, we suggest that ‘mesoscale’ convective disturbances over ‘tropical’ oceans offer
580 more favorable conditions for this oscillation to occur. Regarding disturbance size, a
581 disturbance that is too small corresponds to a high frequency, which may be easily
582 damped, while a disturbance too large tends to achieve a quasi-geostrophic balance,
583 rendering convergence (and vertical velocity) negligible. Environmentally, the
584 troposphere over tropical oceans has a relatively high background low-level buoyancy,
585 so a small variation in low-level buoyancy there will lead to a larger variation in
586 precipitation (Ahmed et al. 2020).

587 Two important points are highlighted from this research. The first is the critical role
588 of low-level buoyancy in the life cycle of convective disturbances. In previous studies,
589 latent heat release in convective disturbances is often linked to BL convergence. This
590 concept has been incorporated into many cumulus parameterizations (e.g., Hayashi and
591 Sumi 1986; Lau and Peng 1987), but can lead to unphysical growth at the finest grid
592 scales (sometimes termed the CISK catastrophe, e.g., Crum and Dunkerton 1992;
593 Matthews and Lander 1999). Recent studies by Liu et al. (2019, 2022) proposed that
594 latent heat release actually lags BL convergence, and cumulus parameterizations

595 accounting for this time lag yield significantly better performance. Here we provide
596 evidence that the variation of precipitation in a tropical MCD is not directly controlled
597 by changes in the BL, but by variations in the lower-free tropospheric buoyancy. In our
598 simulations, the time lag identified in Liu et al. (2019, 2022) would represent the time
599 required for the system to transition from a low-level vertical velocity maximum to a
600 temperature minimum, approximately one-fourth of the oscillation period (Fig. 8). Thus,
601 recognizing the critical role of low-level buoyancy and its coupling with convection in
602 inertia-gravity waves provides insights for improving cumulus parameterizations,
603 especially for those based on the ‘wave-CISK’ perspective.

604 Our second important point concerns the critical role of stratiform heating in real-
605 world tropical MCDs. Although stratiform heating initially leads to lower-tropospheric
606 subsidence and a reduction in lower-tropospheric buoyancy, which does not favor
607 convection, the subsequent phase of the oscillation results in upward motion and a
608 recovery of buoyancy that triggers the next episode of convection. Compared to deep
609 convective heating, stratiform heating is more effective in inducing oscillations. This
610 sensitivity arises from the larger vertical wavenumber associated with stratiform
611 heating, which results in slower outward propagation of energy, allowing more energy
612 to remain available for maintaining the oscillation of the air column (e.g., Wu 2000;
613 2003). In real-world scenarios, stratiform heating is typically weaker than deep
614 convective heating, making the internal oscillation susceptible to contamination and
615 influence from other signals, such as large-scale waves and the diurnal cycle of
616 insolation. Therefore, tropical MCDs with stronger intensity are more likely to exhibit
617 an internal quasi-periodic oscillation. In a separate work, we will examine the role of
618 this internal quasi-periodic oscillation in tropical cyclone precursors.

619 The internal oscillation identified in this work offers a new perspective for
620 understanding and predicting the variations of observed tropical MCDs. The
621 identification of this internal oscillation suggests that interactions between moist
622 convectively coupled dynamics (in MCDs) and periodic forcings may be understood
623 through the superposition of the internal mode with externally forced modes with

624 differing amplitudes and periods. For example, the internal oscillation of an MCD that
625 serves as a TC precursor could interact with the diurnal cycle of insolation, accelerating
626 or delaying TC genesis depending on the phase of the superposition. To fully understand
627 the internal oscillation, we need to identify the factors influencing the oscillation period.
628 This study indicates that, in addition to the Coriolis parameter and stratification, a
629 significant influence may arise from the coupling of convection. When coupled with
630 convection, the recovery of low-level buoyancy occurs more swiftly than in dry cases,
631 particularly when the Coriolis parameter is smaller (Figs. 5, 10b). This interplay of
632 convection complicates the oscillation, necessitating further investigation.

633

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642 Supercomputing Center in Wuzhen for computing resources.

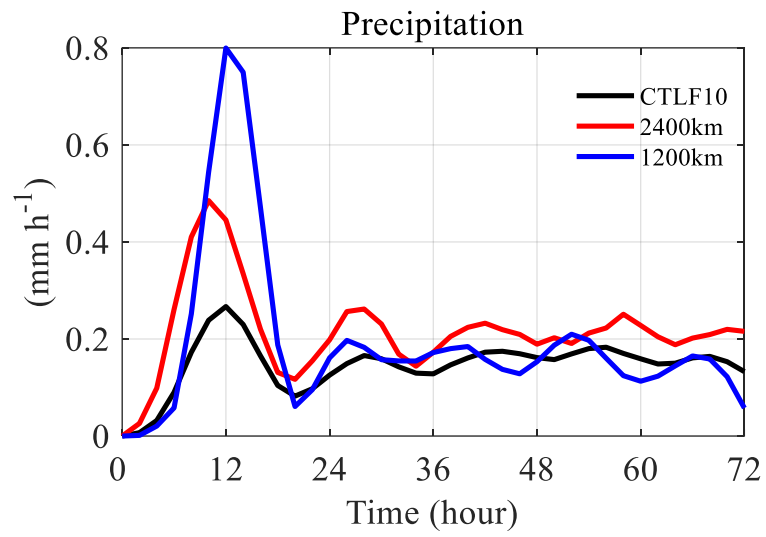
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644 **Data availability statement.**

645 All data and software for this paper are properly cited: the Jordan sounding found
646 in Jordan (1958) and the WRF model found in Skamarock et al. (2019).

647

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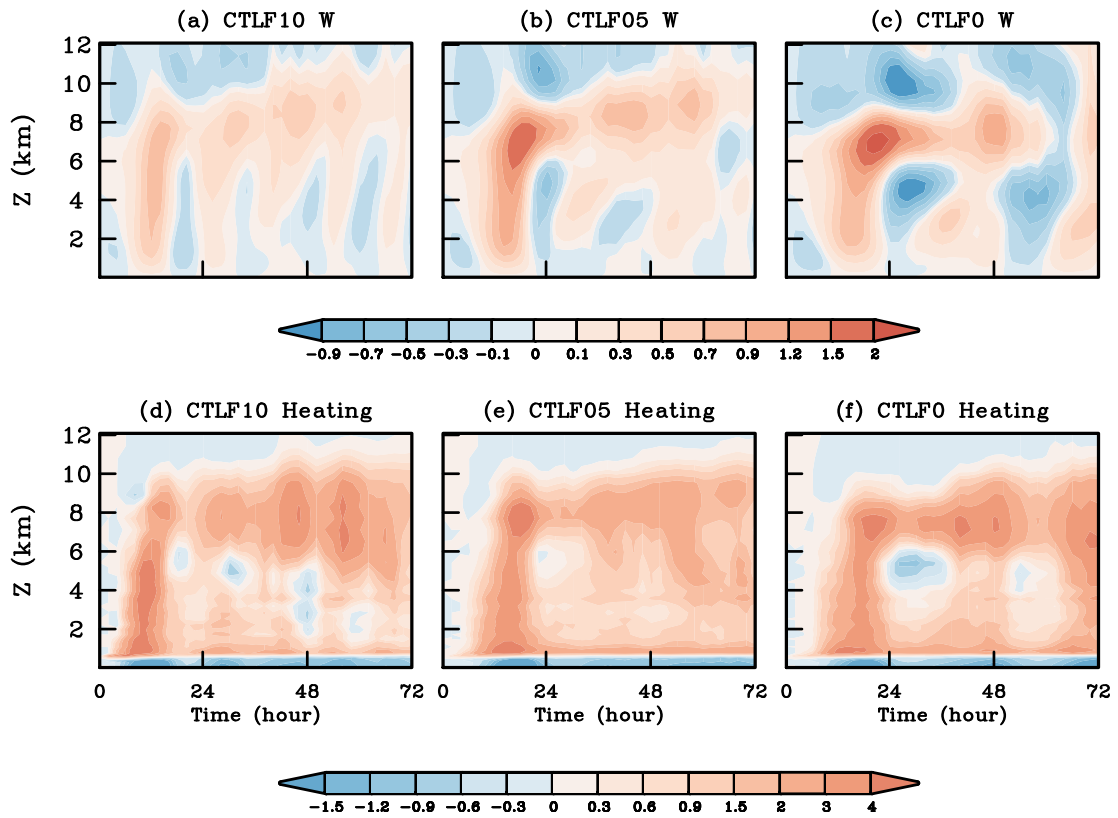


650

651 **Fig. A1** Time series of precipitation (mm h⁻¹) averaged over the inner 150 km radii of
652 the disturbance in full-physics simulations based on CTLF10 with different domain
653 sizes.

654

655



657

658 **Fig. A2** Time-height plot of (a) vertical velocity (cm s^{-1}) and (d) diabatic heating
 659 (K day^{-1}), all averaged in the inner 150 km radii of the domain in CTLF10. (b) and (e)
 660 are the corresponding variables in CTLF05, and (c) and (f) are those in CTLF0,
 661 respectively.

662

663

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