Unsupervised Concept Discovery for Deep Weather Forecast Models with High-Resolution Radar Data

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Abstract

The global climate crisis is creating increasingly complex rainfall patterns, leading to a rising demand for data-driven artificial intelligence (AI) in short-term weather forecasting. However, the black-box nature of AI models acts as a critical obstacle against their integration into the existing forecasting operations. This study addresses this issue by developing an explainable AI framework that extracts precipitation mechanisms from the model's internal activation patterns when it predicts rainfall intensity in the future. The primary objective of this study is to enable the semi-automatic knowledge discovery of the weather mechanisms embedded in the nonlinear AI model by developing the unsupervised concept explanation method. A key challenge is the inherent fuzziness and the complexity of precipitation systems. We propose a probabilistic multi-label self-supervised clustering approach within the explainable framework to address this. Our algorithm refines an insufficient embedding space into perceptually meaningful representations. It improves the clustering performance over existing baselines, achieving an increase of 0.5358 in terms of a Silhouette Coefficient metric, which measures the similarity of intra-clusters and the dissimilarity of inter-clusters. We extract and characterize primary meteorological mechanisms through comprehensive case studies: convectional, frontal, orographic, and cyclonic precipitations. These findings are further validated by a user study involving forecasters at the Korea Meteorological Administration. We assess the distinguishability of the extracted rainfall patterns by conducting a user survey regarding the homogeneity of the extracted rainfall patterns. The results indicate comparable accuracies between existing human-annotated label-based examples (80%) and the unsupervised model-based ones (92%). Furthermore, the proposed method can effectively identify between polar low and typhoon cases, successfully capturing the different mechanisms while their cyclonic shapes are analogous. Our structured methodology can provide a pathway for detecting extreme weather events $\hat{a} \in \mathbb{C}$ such as heavy rainfall and isolated thunderstormsâ C"in near real-time, thereby supporting operational forecasting or posthoc analysis tasks.

Author summary

We develop an unsupervised concept discovery framework to understand precipitation patterns and meteorological processes and enhance the interpretability of AI-based

Fig 1. The outline of unsupervised concept discovery framework. The conceptual examples are provided: convectional, frontal, cyclonic, and orographic precipitations.

weather forecasting models. We extract rainfall patterns semi-automatically from a trained deep neural network model, such as convectional, frontal, orographic, and cyclonic precipitations. To address the fuzziness and complexity of the precipitation systems, we improve the previous concept discovery frameworks to distinguish complex and ambiguous weather patterns by incorporating an instance segmentation technique and refining the internal vector space to enhance the perceptually meaningful representation. We develop an algorithm to refine the feature vectors into a more disentangled manifold by incorporating self-supervised learning and a multi-label deep clustering method. We conducted a user study with five forecasters in the Korea Meteorological Administration and achieved the answer that the extracted rainfall patterns are as distinguishable as human-annotated examples. We provide comprehensive analyses of the clustered patterns grounded in meteorological theory, highlighting the potential of knowledge discovery of meteorological mechanisms from nonlinear, data-driven models.

Introduction

Due to increasingly chaotic weather conditions caused by the global climate crisis, the demand for faster and more accurate weather predictions is growing. Traditional weather forecasting relies on numerical weather prediction (NWP), which makes predictions by solving theory-based partial differential equations. Despite its theoretical soundness, NWP has several limitations. First, NWP is computationally expensive, often requiring extensive hypercomputing facilities for timely predictions. While relaxing assumptions through methods such as quasi-geostrophic approximations [1] or hydrostatic and anelastic approximations [2–4] can reduce the computation cost, it prevents the full utilization of available data. Data-driven machine learning models can circumvent these problems. For instance, the deep neural network (DNN) model from [5] predicts hundreds of weather variables globally for the next 10 days in one minute, while the model from [6] makes hourly predictions in 1.5 seconds. Furthermore, these models learn nonlinear weather patterns directly from data [7], fully utilizing all available information. The increasing availability of high-quality data [8,9] makes this aspect of DNNs even more attractive.

Despite these strengths, DNNs have a critical weakness preventing their integration into operational weather forecasting: black boxes. Since a DNN comprises complex interconnections of numerous neurons, it is challenging to understand the exact decision-making process. This opaqueness limits the trustworthiness of a DNN's predictions and, therefore, its worth to operational forecasters. This gap in trust is a ubiquitous problem across multiple domains, leading to the development of explainable AI techniques to aid users in interpreting the behavior of AI models [10].

Applying explainable algorithms to weather forecasting models is challenging due to the inherent ambiguity of weather systems, as shown in Fig. 2; different precipitation systems can co-occur in a single region. These systems often exhibit fuzzy edges, making establishing clear boundaries between neighboring systems difficult. The systems can also be sparse, consisting of small patches of observed rainfall that are difficult to identify without preprocessing. Furthermore, as shown in Fig. 3, real-world precipitation mechanisms exhibit ambiguous and entangled semantics. Consequently, explanations for weather forecasting models inherently require probabilistic approaches 2

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Fig 2. Radar images often contain multiple rainfall systems developed from different mechanisms. An example image with two precipitation cases: (1) frontal and (2) convective system.

Fig 3. The heatmap of cosine similarities of the pairs of human-annotated concept labels [11].

rather than deterministic methods to represent the degree of ambiguity and entanglement. This study considers the individual precipitation systems independently by applying a domain-tailored instance segmentation to separate the distinct rainfall mechanisms within a single data, enabling analysis at the rainfall system level.

One popular branch of explanation methods is *example-based explanations*, which uses user-familiar input space as the explanation results, making them understandable even for layperson users. In particular, example-based concept explanations offer examples illustrating human-comprehensible concepts captured by a model [12]. Such concepts in weather forecast models may include rainfall intensity, shape, or rainfall mechanisms (high-level semantics). Defining the term *concept* is challenging, even for human experts [13]. Concepts can be extracted by analyzing the internal vector space of a model even if it is not explicitly designed to capture the chosen concepts [12]. Several studies involve posthoc analysis and human annotation of extracted concepts to assign meaningful interpretations [14]. While there are several desiderata for concepts, this paper focuses on (1) possessing inherent meaning and (2) enabling distinction between or within concepts. The first desideratum is typically assessed through human expert evaluation [14–17], while the second can be measured using a Silhouette Coefficient score [18]. In this study, we conduct a user survey with expert forecasters to assess the first desideratum. We inherently address the second desideratum by employing a soft Silhouette coefficient-based deep clustering algorithm.

Example-based explanations can have several drawbacks, such as the insufficient representational power of given feature spaces, the risk of trivial clustering outcomes, and the gap between human perceptions and generated examples. First, the distance measurement in the concept analysis is sensitive to the chosen feature space [19, 20]. Although Euclidean distance in the feature space is known to reflect human perceptual distance when tested on benchmark datasets [21–23], the representational spaces are often insufficient in real-world applications due to constraints such as scarcity of data [24]. The efficient training properties of DNNs exacerbate the problem since the models may have an incomplete representation space that minimizes the objective function while concentrating on critical information from the data, which causes, for example, unsupervised clustering in the feature space often leads to trivial clusters that solely focus on color while ignoring object shapes [25, 26]. To this end, several studies suggest building refined manifolds to achieve more meaningful representations on top of the feature space of the original model [24]. Based on the ideas, this paper enhances the representational space of the target model under the metric learning scheme.

The second limitation is the gap between human understanding and the generated examples. Given a set of analogous examples an algorithm generates, a user may not necessarily identify their similarities when the samples are analytically similar (e.g., developing or dissipating rainfall) but intuitively different (e.g., having identical colors or intensities) [27,28]. To address this cognitive gap, we designed the questionnaire in a comparative format to measure the relative accuracy with which users can assess the homogeneity of the generated explanations versus human annotations. Based on the

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 $^{^0\}mathrm{We}$ denote the names of concepts in sanserif throughout this paper.

discussion above, example-based explanations can provide a useful understanding of a model's decision-making process if its shortcomings can be addressed. Therefore, this study proposes an *example-based concept explanation* framework (See Fig. 1) with the following components to enhance the interpretability and reliability of data-driven precipitation forecast models.

Recent research explores AI-based vector space analysis of weather and climate patterns. We discuss their limitations and highlight our contributions. [30] and [31] take a similar approach, using clustering algorithms to analyze heavy rainfall during the summer season in South Korea. These studies typically perform clustering on input data for their analysis; however, input-level clustering often captures visual similarities rather than semantic concepts. [32] distinguishes typhoon structures using a specific internal layer of a typhoon detection model. To our knowledge, the algorithms for concept analysis of extracting various precipitation mechanisms from the representation vector space captured by trained weather forecasting DNNs are yet to be explored. One issue with using the vector space is that it may be too entangled for meaningful analysis, which is critical for knowledge discovery. Hence, we address this problem by transforming the original space into a more meaningful, disentangled space through a multi-label deep clustering method. We will discuss this process in the next section.

To identify ambiguous and co-occurring meteorological concepts, we need to perform multi-label deep clustering to capture relationships among the multiple labels. The regular clustering methods [33, 34] use an objective function that optimizes the intra-class similarity while reducing the inter-class similarity. Directly measuring this concept, the Silhouette Coefficient score [18] is a popular evaluation metric for clustering tasks, and the Soft-Silhouette clustering [35] uses the metric as an objective function for optimizing clusters as a contrastive learning. However, these studies are often centered around single-label multi-class clustering. We instead adjust the Soft-Silhouette [35] to multi-label clustering based on the theoretical foundation of the Binary Relevance [36], which decomposes a classifier with k classes into k independent binary classifiers. Specifically, we modify the final activation function of the target model from a single multi-class label to several binary labels to enable probabilistic multi-label classification. One of the benefits of using the silhouette coefficients for optimization is that it naturally avoids the trivial solutions in clustering, a problem often associated with using cross-entropy loss [37], by leveraging its innate contrastive learning scheme.

Our contributions are threefold:

- Semi-Automatic Extraction of Rainfall Mechanisms from an AI Model: We extract 24 concepts and characterize them as identifiable weather patterns, including cyclonic, convectional, frontal, and orographic precipitations, which are verified to be distinguishable by forecasters.
- Probabilistic Deep Clustering for Ambiguous Rainfall Mechanisms: To explain ambiguous weather patterns with multiple rainfall mechanisms, we extend previous algorithms to support probabilistic multi-label clustering by incorporating binary sigmoid loss.
- Self-Supervised Learning for Enhanced Representation Spaces: We employ self-supervised learning techniques to generate perceptually more meaningful representations on top of the manifold of the target model, addressing the issue of insufficient or biased representations.

Materials and Methods

This section introduces our unsupervised concept discovery framework which consists of four parts (Fig. 4): (1) data preprocessing using instance segmentation tailored for

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meteorological data, (2) self-supervised learning-based representation space refinement ¹²³ for meaningful initial cluster centroids, (3) clustering in the feature space for ¹²⁴ pseudo-labels, (4) unsupervised concept activation vector (CAV) extraction and ¹²⁵ evaluation of alignment with domain knowledge.

Fig 4. The proposed framework for the unsupervised concept activation vector localization. (1) the input data is preprocessed by applying watershed instance segmentation on the activation space of the bottleneck layer of the given trained precipitation forecast model. (2) A masked autoencoder is trained with self-supervised learning on the processed activations to create a new representation space (\tilde{z}_{soft}^*) . (3) Pseudo-labels are created by performing multi-label deep clustering. (4) Concept vectors (v_c^l) are extracted from \tilde{z}_{soft}^* .

Model and Datasets

The target model is an unpublished variant of convolution-based DeepRaNE [38] 128 provided by the National Institute of Meteorological Sciences (NIMS) in South Korea. 129 The model consists of a denoising autoencoder and a U-Net. The input and target 130 output are precipitation intensities derived from radar reflectivity observations. Each 131 input instance consists of seven high-resolution radar observations at 10-minute 132 intervals, spanning from 60 minutes prior (T-60) to the reference time (T) and the 133 1-hour cumulative average, concatenated channel-wise with temporal information 134 (month, day, hour) and spatial coordinates (longitude, latitude) following an early fusion 135 approach in multimodal learning [39] which enhance the spatial and temporal 136 embedding. The training data for concept extraction spans 10-minute intervals from 137 2018 to 2021, inclusive. The data used for the explanation module is extracted from the 138 activation vectors of the bottleneck layer in the U-Net module. Detailed descriptions of 139 the model and radar preprocessing are provided in Section A.1 and A.2 in S1 Appendix, 140 respectively. 141

Instance Segmentation for Rainfall Systems

To address the ambiguity and individuality of precipitation systems in radar images, we 143 use the watershed¹ image segmentation algorithm [40], which considers both pixel 144 intensity and spatial distance, as shown in step (1) of Fig. 4, along with tailored pre-145 and post-processing techniques. In the pre-processing step, regions with precipitation 146 rates below 0.1 mm hr-1 are masked as non-precipitation areas [41], and the input is 147 binarized to delineate individual echo cells. Consequently, the watershed algorithm 148 operates on binary input and adjacency information only, which is nothing but the 149 Voronoi segmentation incorporating the boundary masks, thereby avoiding fine-grained 150 over-segmentation. In the post-processing step, directly adjacent segments are merged 151 into a single system. Each segment in the input space is then mapped into a 152 corresponding region in the vector space of the target layer. This region is subsequently 153 cropped and resized into a uniform shape, which improves computational efficiency 154 through dimensionality reduction while preserving distinct rainfall systems. We filter 155 out inactive channels throughout the training dataset to further reduce dimensionality, 156 retaining 280 out of the original 1,024 channels. The resulting feature vectors, 157 $z_i \in \mathbb{R}^{280 \times 9 \times 9}$, are utilized in all downstream tasks. For implementation details and 158 reproducibility, refer to Section B.1 in S1 Appendix. 159

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¹The algorithm gradually expands regions from the local minima (markers) until they converge at the local maxima(watershed boundaries).

Fig 5. The examples of four output clusters.

Self-Supervised Learning for Refining Feature Spaces

As discussed previously, two potential issues exist with the direct application of 161 clustering-based concept extraction on the feature manifold of a deep weather forecast 162 model. First, the embedding space may be insufficiently trained due to limited training 163 data compared to the model's size, leading to suboptimal clusters with incomplete 164 disentanglement and poorly estimated centroids. Second, weather patterns are often 165 ambiguous, requiring multiple concept labels to be assigned probabilistically rather than deterministically. We address the first problem by employing a self-supervised learning 167 scheme consisting of a masked autoencoder (MAE) [45] with mean-squared error (MSE) 168 loss to generate the refined representational activation vector space \tilde{z}_{pre} (step (2) of 169 Fig. 4). The MAE randomly masks a significant portion of the input, and the model 170 solves the task by reconstructing the missing patches based on the remaining visible 171 elements. This simple yet effective approach enhances the representation space by 172 reconstructing missing content and inferring absent parts solely from visible patches. 173

Multi-Label Deep Clustering for Co-Occurring Rainfall Systems

Multi-Label Deep Clustering to Cover Co-Occurring Rainfall Systems

To address the second issue, we introduce a multi-label deep clustering method. We 176 first transform the class assignment process of the traditional deep clustering method 177 into a multi-label classification problem, which binarizes each class into a one-hot label 178 using sigmoid functions. We then perform a modified three-stage deep clustering 179 from [42] (step (3) of Fig. 4): (i) refined embedding via the self-supervised MAE, (ii) 180 pseudo-class assignment via k-means clustering to generate initial clusters, (iii) 181 multi-label soft class assignment with the cluster adjustment. The last stage is 182 performed using soft-silhouette loss $[35]^2$. This loss function extends the Silhouette 183 Coefficient score [17, 18] by minimizing intra-cluster distance and maximizing 184 inter-cluster distance. Specifically, the average soft Silhouette score $S(\cdot)$ is defined as 185 the expected conditional Silhouette value s_{C_k} (Eq. 2) weighted by the *i*-th sample's k-th 186 cluster assignment probability P_{C_k} . The conditional silhouette value $s_{C_k}(z_i)$ is 187 computed based on two factors: $a_{C_k}(z_i)$, which is the distance between z_i and C_k 188 weighted by the expected probability of z_i compared to all other points $z_{i\neq i}$ belonging 189 to C_k , and b_{C_k} , the expected distance of z_i from the closest cluster $C_{l\neq k}$ to C_k . P_{C_k} is 190 computed using a radial basis function (RBF) kernel (Eq. 5) to account for the mean 191 and variance when computing distances between data points and clusters [35]. The RBF 192 distance features are scaled using the temperature factor τ [43] to mitigate the 193 overconfidence problem before computing the class assignment probabilities via the last 194 activation function. 195

$$S(z_i) = \frac{1}{N} \sum_{i=1}^{N} \sum_{k=1}^{K} P_{C_k}(z_i) s_{C_k}(z_i)$$
(1)

$$s_{C_{k}}(z_{i}) = \frac{b_{C_{k}}(z_{i}) - a_{C_{k}}(z_{i})}{\max\left\{a_{C_{k}}(z_{i}), b_{C_{k}}(z_{i})\right\}}$$
(2)

$$a_{C_{k}}(z_{i}) = \frac{\sum_{j=1}^{N} P_{C_{k}}(z_{j}) d(z_{i}, z_{j})}{\sum_{j=1, j \neq i}^{N} P_{C_{k}}(z_{j})}$$
(3)

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²https://github.com/gvardakas/Soft-Silhouette

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$$b_{C_k}(z_i) = \min_{l \neq k} \frac{\sum_{j=1}^{N} P_{C_l}(z_j) d(z_i, z_j)}{\sum_{j=1}^{N} P_{C_l}(z_j)} = \min_{l \neq k} a_{C_l}(z_i)$$
(4)

$$P_{C_k}(z_i) = \frac{1}{1 + \exp\left[-(K\langle z_i, c_k \rangle - 0.5)/\tau\right]}.$$
(5)

The overall loss consists of the soft Silhouette, entropy, and MSE loss. The entropy loss is a regularizer to prevent dominance by a specific cluster, while MSE loss is added to preserve the representational power of the learned embeddings [35]. These three loss functions refine the trained feature space, using the pseudo-class centroids as anchors to enhance clustering effectiveness:

$$\mathcal{L}_{AE} = \mathcal{L}_{MSE} + \lambda_1 \mathcal{L}_{Silhouette} - \lambda_2 \mathcal{L}_{Entropy} \tag{6}$$

$$\mathcal{L}_{MSE} = \frac{1}{N} \sum_{i=1}^{N} \|z_i - g_\theta \left(f_w \left(z_i \right) \right) \|^2$$
(7)

$$\mathcal{L}_{Silhouette} = 1 - S\left(h(z)\right) \tag{8}$$

$$\mathcal{L}_{Entropy} = \frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{K} h_j(z_i) \log h_j(z_i)$$
(9)

where f_w and g_θ are the encoder and decoder functions, respectively. The function $h_r(\cdot)$ 200 denotes the clustering function, which outputs the probability of assigning sample 200 $z_i = f_w(x_i)$ to the k-th cluster in the feature space. λ_1 and λ_2 are the scaling factors for 210 the soft silhouette and entropy losses, respectively. The model parameters w, θ , and r 211 are trained by gradient descent. 212

We set the temperature factor to 0.25 to shift the kernel output by -0.5 and achieve the sigmoid range of (0, 1) after applying the Gaussian RBF kernel $\exp(-\frac{||x-x'||^2}{2\sigma^2})$, where the input domain is in [0, inf) and the output range is in [0, 1]. Parameter σ is also trainable. The final refined vectors $\tilde{z}_{soft} \in \mathbb{R}^{280}$ and the clusters are obtained through iterative optimization.

Concept Activation Vector Localization

We then extract CAVs v_c^l from the refined vector space and cluster results as pseudo 219 labels to train individual linear probers, as introduced in the introduction section. 220 Unlike previous approaches, the output clusters are not entirely exclusive due to the 221 multi-label clustering manner. We use cluster labels with a probability threshold 0.5 as 222 pseudo labels for each concept. According to previous literature, clusters with fewer 223 than 50 samples can be omitted as a post-processing step [14]. To obtain CAVs and 224 concept probers, support vector machine linear classifiers are trained using a one-vs-all 225 setting. The L_1 regularizer can produce sparse and efficient CAVs as additional 226 techniques. Platt's sigmoid calibration method can alleviate the overconfidence issue of 227 the output logits. An ensemble mechanism that averages the coefficients from k models 228 through k-fold cross-validation can be employed to mitigate the overfitting of classifiers. 229 We provide the implementation details in Section B.2 in S1 Appendix for reproducibility. 230

Results and Discussion

Extracted Concepts Based on Semi-Automatic Clustering

Fig. 5 showcases the examples of output clusters generated via deep clustering in the refined representation space \tilde{z}_{soft} . The concept labels are derived through posthoc 234

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Methods	Vector Space	Silhouette Coefficient (s)
ACE [14]	z	-0.0291
Ours	z	-0.0039
Ours	$ ilde{z}_{pre}$	0.3441
Ours	\tilde{z}_{soft}	0.5067

Table 1. The Soft Silhouette Coefficient scores for different unsupervised concept extraction methods and vector spaces.

analysis and statistical analysis on a human-annotated label dataset [11]. Cluster 4 235 captures the east-coast-rainfall concept, which exhibits patterns along the eastern coasts 236 of the Korean Peninsula that are often influenced by orographic lifting. Cluster 8 237 corresponds to the convectional rainfall concept, which forms localized intense shower 238 patterns due to strong updrafts within cumulonimbus clouds. Cluster 12 is associated 239 with the typhoon concept, characterized by cyclonic patterns accompanied by heavy 240 rainfall. This mechanism involves a tropical cyclone with a central eye and strong spiral 241 rain bands. Cluster 20 corresponds to stationary-front concept, which forms elongated, 242 thick, linear rainfall band patterns. Cluster 23 is associated with the lake-effect snowfall 243 concept, which exhibits a distinctive wave-like pattern over a broad area. This 244 mechanism occurs when cold air moves over a warm sea surface, resulting in prolonged 245 snow showers downwind. Section C.4 in S1 Appendix provides additional output 246 examples and details of the posthoc analysis. 247

Evaluation of Representation Space for Concept Extraction

To verify that the refined vector space \tilde{z}_{soft} provides a high-quality representation space 249 for concept analysis, we compare the performance of Automatic Concept Extraction 250 (ACE) [14], which uses k-means clustering on the specific layer (l)'s embedding vector 251 $\phi_l(x)$, and our clustering method applied on three embedding vector spaces: $z, \tilde{z}_{pre},$ 252 and \tilde{z}_{soft} . Due to computational costs and memory constraints, we cannot use the original ACE implementation on $\phi(x) \in \mathbb{R}^{1024 \times 45 \times 36}$. Instead, we use z as an 253 254 alternative. We measure the discrete Silhouette Coefficient score, which ranges from -1 255 to 1, and a near-zero value indicates poor cluster separation. As shown in Table 1, both 256 ACE and our framework trained on z achieves a near-zero score (-0.0291 and -0.0039, 257 respectively), suggesting a high overlap of clusters. In contrast, our framework achieves 258 a score of 0.3441 with \tilde{z}_{pre} and 0.5067 with \tilde{z}_{soft} , showing a significant improvement in 259 clustering performance. The results indicate that self-supervised learning substantially 260 improves the disentanglement of the representational space, while the multi-label soft 261 silhouette coefficient further enhances this separation. The intuition behind the 262 improved performance is that, as shown in Fig. 6, the initial manifold z is too intricate 263 for direct concept extraction. The modified space \tilde{z}_{pre} obtained through self-supervised 264 learning is less entangled. The final optimized space \tilde{z}_{soft} is even more disentangled, 265 making it more amenable to clustering. 266

To evaluate the effectiveness of the proposed feature space, we conduct a nearest neighbor analysis using the Euclidean distance in z and \tilde{z}_{soft} , comparing the labels of the top three nearest neighbors as shown in Fig. 7. The results indicate that \tilde{z}_{soft} reflects more meaningful relationships, with the conceptual distance depending not only on shape or intensity-oriented information but also high-level semantic mechanisms such as stationary-front, lake-effect-snowfall, and east-coast-rainfall. This observation suggests that our probabilistic multi-label approach effectively aligns the feature representation 277

Fig 6. The t-Distributed Stochastic Neighbor Embedding (t-SNE) representation of the manifold of the embedding vector spaces at each stage of the proposed representation learning procedure: (a) ACE [14] implementation on segmented embedding vectors z, (b) initial clustering of our framework on z. (c) initial clustering on the self-supervised refined embedding vectors \tilde{z}_{pre} . (d) multi-label clustering on its embedding vectors \tilde{z}_{soft} . The same color represents samples within the same cluster. The black markers represent the centroids of individual clusters. Detailed experimental settings are provided in Section C.2 in S1 Appendix for replicability.

Fig 7. Examples of top three nearest neighbors by Euclidean distance in z

and \tilde{z}_{soft} : Each example indicates its date and time and corresponding human-annotated labels from relevant open-source data [11]. others refers to unclassified labels.

with domain knowledge, allowing the model to discern subtle similarities in weather mechanisms beyond simple visual patterns. Given the meaningful conceptual disentanglement in \tilde{z}_{soft} , we use the clusters constructed in this space, which represents the vector space in step (4) of Fig. 4, as pseudo labels in subsequent procedures.

Case Study of Polar Low vs. Typhoon

Polar lows and typhoons are precipitation mechanisms with similar cyclonic patterns and intensities. However, they are distinct weather systems in that the former occurs primarily in winter. A good weather concept explanation should be able to distinguish between the two systems despite their visual similarities. We examine whether the CAVs from our framework can capture this difference by performing a case study measuring the predictive probability of the typhoon prober (the linear classifier of **Concept 19**) for several polar low and typhoon cases. We use instances over the East Sea of Korea from May 20 to 21, 2021 for polar low cases, and Typhoon Mitag and Typhoon Soulik for typhoon cases. We use Mitag and Soulik as their radar patterns resemble polar lows during the dissipation phase of their life cycle.

As shown in Fig. 8, the typhoon prober assigns high probabilities to typhoon cases but low probabilities to polar low cases, demonstrating the model's ability to distinguish between cyclonic patterns in winter (polar low) and summer (typhoon) rather than merely detecting the rotational shapes. This result illustrates the effectiveness of CAVs in differentiating mechanically distinct but visually similar phenomena. Section C.1 in S1 Appendix provides detailed experimental settings and additional results.

Allocation of Meaning of Concept Vectors

We heuristically select the number of clusters as 30 to slightly exceed the number of annotated labels in the benchmark dataset (16) [11], allowing for redundancy in identifying concepts. We merge statistically insignificant clusters when p < 0.01 in the cluster-pair t-test based on previous research [14] and remove clusters with fewer than 50 samplesâ \mathfrak{C} the post-processing results in 24 final clusters. Example instances from different clusters are reported in Figs. 16 and 17 in S1 Appendix. The annotated

Fig 8. A comparison of polar low and typhoon cases. The score refers to the probabilistic score from probe 19. The middle image is from the advanced, very high-resolution radiometer (AVHRR) CH 01, observed by the meteorological operational satellite (METOP-1) on 2021-05-21 at 01:58 (UTC).

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Fig 9. An example of questionnaires and the survey result of the accuracy of detecting homogeneous concepts on annotated labels vs. concepts extracted from the target model.

concept label descriptions are also provided in S1 Appendix. The results indicate an alignment between the attributes of the concepts and human perception.

Survey with Domain Experts

To evaluate the degree of alignment of the extracted concepts with meteorological domain knowledge, we conduct a survey with domain experts using structured questionnaires and interviews. The questions involve identifying samples extracted from a homogeneous concept cluster compared to a set of random samples. To address cognitive biases in user surveys as discussed previously, where intuitive differences related to shape and intensity tend to dominate over analytical thinking such as innate mechanisms [27, 28], we design the questionnaires to be contrastive, comparing two label types in the same format. The labels consist of (1) human-annotated concept labels from open-source data [11] and (2) pseudo-labels obtained from the concept extraction method. We ask five questions for each category, presented in random order for both questions. We then conduct a comparative analysis of the results. The questionnaire is designed to be performed online, including animations to visualize the temporal progression of rainfall mechanisms. The user survey was conducted on June 24, 2024, with five Korea Meteorological Administration (KMA) forecasters. The left side of Fig. 9 illustrates examples of questions in the questionnaire. According to Fig. 9, the forecasters achieved an average accuracy of 80% for the annotated labels and 92% for the concept model identification task, indicating that humans recognize the extracted concepts with a relatively comparative level. Additional participant interviews and feedback are provided in S1 Appendix.

Conclusion

This study proposes an unsupervised example-based concept explanation framework for 325 a given precipitation forecast model based on high-resolution radar data, contributing to 326 understanding precipitation patterns and meteorological processes such as convectional, 327 frontal, orographic, and cyclonic precipitations. The framework allows for a probabilistic 328 representation of the simultaneous co-occurrence of meteorological mechanisms and 329 helps address common challenges with manual concept annotation in the weather 330 domain. We perform extensive analyses of the proposed algorithm, measuring clustering 331 performance and alignment between extracted concepts and weather domain knowledge 332 both quantitatively and qualitatively. Our experiments show that the framework can 333 identify the key precipitation mechanisms captured by the given rainfall forecast model 334 and distinguish between visually similar yet distinct mechanisms like polar lows and 335 typhoons. These results suggest that the extracted concepts encapsulate te not only 336 visual similarity of precipitation systems but also other high-level semantic information. 337

There are several future directions for this research. First, given the model-agnostic nature of the proposed framework, it may be extended to analyze other state-of-the-art weather forecast models, which would inherently embed richer rainfall patterns in the feature spaces to identify more complex patterns. We may also apply the method to multivariable models that take additional inputs such as temperature, pressure, wind direction, and wind speed, potentially discovering more complex and diverse weather mechanisms than those that can be extracted from radar data alone. 338

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Supporting information

S1 Appendix. Detailed Research Method and Additional Experimental Results. This appendix provides the model and data description; the implementational details of instance segmentation and concept vector extraction; the additional experimental results of concept prober, manifold analysis, forecasters' interviews, and more examples of clustering outputs. Also, the samples of the concept annotated label dataset we use [11] are showcased.

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Cluster	Concept		Examples	
4	East-Coast-Rainfall	5535 5910 631 06 Mar 2019 17:00 30 Mar 2019 22:00 24 Apr 201 00 Mar 2019 22:00 24 Apr 201	12 6911 10299 10707 19 00:00 30 May 2019 11:00 28 Nov 2019 19:00 19 Dec 2019 06:00 Image: Constrained and the second and the	11327 17 Jan 2020 20:00
12	Typhoon	8847 8870 908 01 Sep 2019 04:00 01 Sep 2019 22:00 08 Sep 201	82 15597 15609 15666 019 08:00 02 Sep 2020 01:00 02 Sep 2020 17:00 05 Sep 2020 02:00	15828 11 Sep 2020 08:00
14	Convectional	2511 2514 253 28 Aug 2018 03:00 28 Aug 2018 06:00 29 Aug 201 29 Aug 201 20 Aug 201 29 Aug 201	33 2613 2616 2684 018 05:00 01 Sep 2018 06:00 01 Sep 2018 10:00 03 Sep 2018 06:00 Image: Constrained and the second a	2877 12 Sep 2018 00:00
23	Lake-Effect-Snowfall	20848 20908 2094 30 Jan 2020 15:00 16 Feb 2020 14:00 16 Feb 202 16 Feb 2020 14:00 16 Feb 202	908 21936 21950 21999 020 14:00 29 Dec 2020 18:00 30 Dec 2020 11:00 17 Feb 2021 02:00 17 Feb 2021 02:00	22211 01 Dec 2021 03:00









Polar Low

on May 21, 2021, 01:58 UTC Center location: 39.46 °N, 132.07 °W







Model

