



# Observation and explanation of spurious seismic signals emerging in teleseismic noise correlations

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**Abstract.** Deep body waves have been reconstructed from seismic noise correlations in recent studies. The authors note their great potential for deep-Earth imaging. In addition to the expected physical seismic phases, some spurious arrivals having no correspondence in earthquake seismograms are observed from the noise correlations. The origins of the noise-derived body waves have not been well understood. Traditionally, the reconstruction of seismic phases from inter-receiver noise correlations is attributed to the interference between waves from noise sources in the stationary-phase regions. The interfering waves emanating from a stationary-phase location have a common ray path from the source to the first receiver. The correlation operator cancels the common path and extracts a signal corresponding to the inter-receiver ray path. In this study, with seismic noise records from two networks at teleseismic distance, we show that noise-derived spurious seismic signals without correspondence in real seismograms can arise from the interference between waves without a common ray path or common slowness. These noise-derived signals cannot be explained by traditional stationary-phase arguments. Numerical experiments reproduce the observed spurious signals. These signals still emerge for uniformly distributed noise sources, and thus are not caused by localized sources. We interpret the presence of the spurious signals with a less restrictive condition of quasi-stationary phase: providing the time delays between interfering waves from spatially distributed noise sources are close enough, the stack of correlation functions over the distributed sources can still be constructive as an effect of finite frequencies, and thereby noise-derived signals emerge from the source averaging.

## 1 Introduction

The technique of noise correlation is implemented simply via computation of correlation functions between ambient noise records at receivers. Theoretical and experimental studies (e.g. Lobkis and Weaver, 2001; Wapenaar, 2004) have shown that under restrictive conditions, the inter-receiver correlation function converges toward the response that would be recorded at one receiver if a source was located at the other. This is, by definition, Green's function of the medium between the two receivers. Great achievements have been realized with the introduction of the noise correlation technique into solid-Earth seismology (Campillo and Paul, 2003; Shapiro and Campillo, 2004). The most common applications are passive imaging (e.g. Sabra et al., 2005; Shapiro et al., 2005) and monitoring (e.g. Brenguier et al., 2008; Wegler et al., 2009) of subsurface using signals derived from seismic noise. We refer to Campillo and Roux (2015) for a systematic review of recent progress on its theoretical and methodological aspects, and various noise-based applications.

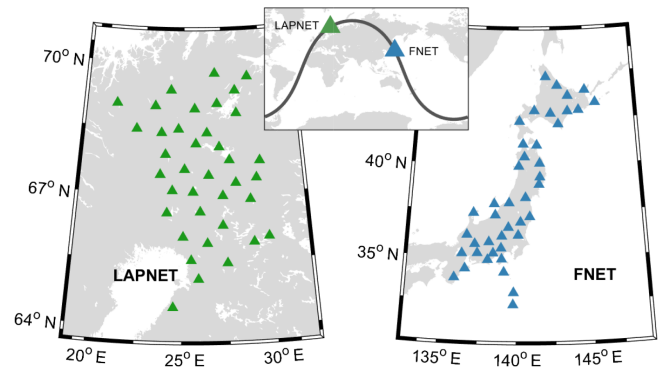
Both the surface-wave and body-wave parts of Green's function can be reconstructed from noise correlations. Surface waves are easier to extract due to their dominance in the noise spectra. There are relatively fewer, yet promising, examples of noise-derived body waves. Some authors have demonstrated that deep body-wave signals that propagate through the mantle and core can be extracted from the correlations of continuous seismograms recorded by seismic networks at regional to global scales (Boué et al., 2013b, 2014; Lin et al., 2013; Nishida, 2013). Several applications followed. For instance, Poli et al. (2015) imaged the core–mantle boundary (CMB) beneath Siberia with P-wave reflections derived from microseisms. Spica et al. (2017) used

higher-order correlations to retrieve the ScS arrivals and imaged the lateral variations of the CMB beneath Mexico. Besides ambient noise wavefields excited by ocean waves (Longuet-Higgins, 1950), another strategy to extract the deep body waves relies on the highly coherent late coda waves excited by large earthquakes (Lin and Tsai, 2013; Boué et al., 2014; Xia et al., 2016). The coda-derived deeply incident waves are dominantly related to reflected and refracted core phases (Boué et al., 2014; Phm et al., 2018). By estimating the differential times between coda-derived core phases, Wang et al. (2015) and Wang and Song (2017) inferred the equatorial anisotropy of the Earth's inner core. The coda correlations contain normal seismic phases as well as spurious phases. A seismic phase is termed normal if it is present in Green's function of the medium, and spurious if it is not observed in real seismograms and does not obey the theory of seismic wave propagation. Poli et al. (2017) ascribed the vertically travelling ScS-like signals in the vertical-vertical component of coda correlations to the interference of high-order modes that have low attenuations. Using ray theory and stationary-phase arguments, Phm et al. (2018) interpreted the spurious phases in global coda correlations as a result of the interferences between specific ray paths. Tkalčić and Phm (2018) inferred the shear properties of the Earth's inner core by modelling a spurious phase related to the  $J$  waves.

In contrast to the fact that spurious body waves in earthquake coda correlations have been observed and explained, the observation and explanation of the spurious phase in ambient noise correlations are still lacking. In this study, we focus our analysis on the interpretation of a spurious P-type phase that can be observed from the noise correlations between receivers separated at teleseismic distances. This paper is organized as follows. In Sect. 2, we describe the processing of seismic noise data. In Sect. 3, we correlate the processed noise records and show the observation of noise-derived spurious arrivals emerging earlier than the direct P waves. In Sect. 4, we develop a new double-array technique to estimate the slownesses of the interfering waves and analyse the origin of the observed spurious phase. In Sect. 5, we propose a mechanism to explain the generation of the spurious phase. More elaborate numerical experiments are implemented in Sect. 6 to reproduce the observed signals and to investigate the sensitivity to the distribution of seismic noise sources.

## 2 Noise data processing

Continuous seismograms recorded in 2008 by the broadband stations of the Full Range Seismograph Network of Japan (the FNET array) and the northern Fennoscandia POLNET/LAPNET seismic network in Finland (the LAPNET array) are used in this study to calculate the double-array noise correlations (Fig. 1). The aperture of the LAPNET array is  $\sim 700$  km, and that of the FNET array is nearly

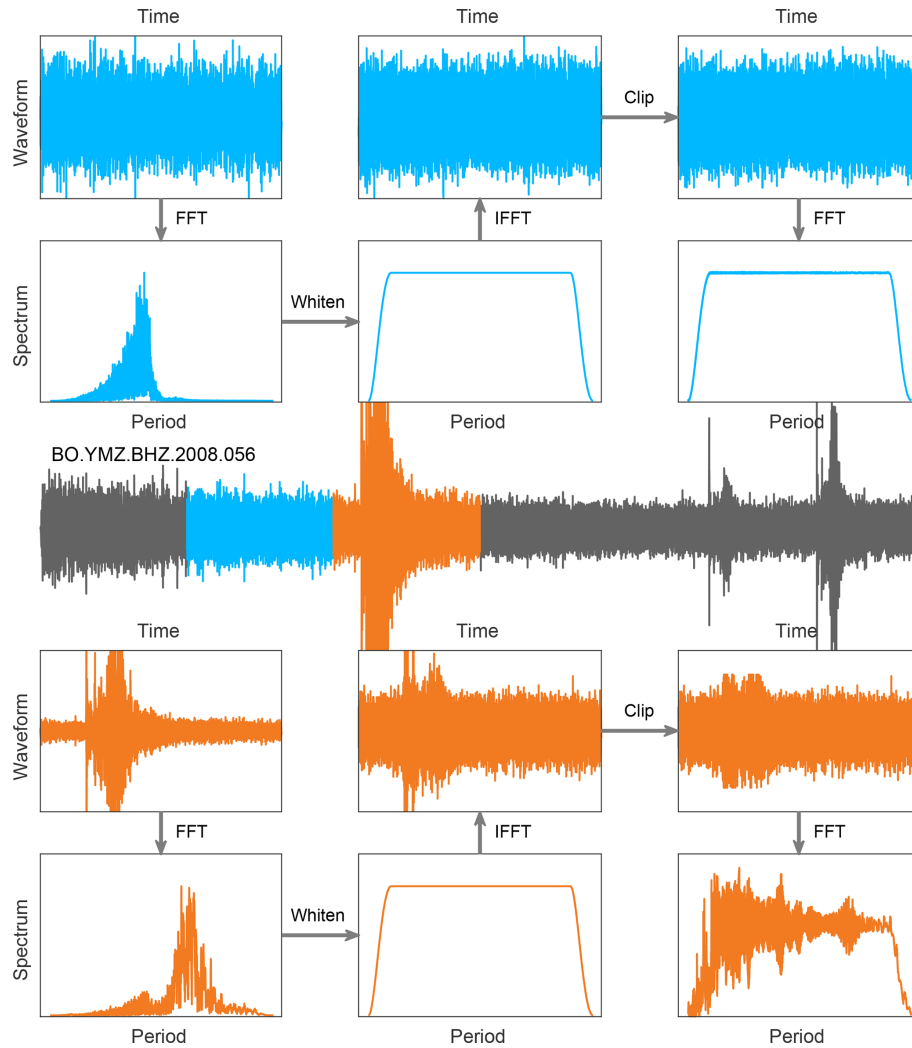


**Figure 1.** Geographic locations of the 38 stations of the LAPNET array in Finland and the 41 stations of the FNET array in Japan.

1400 km. There are 1558 FNET–LAPNET station pairs in all. The distance between the FNET and LAPNET stations ranges from  $\sim 56$  to  $\sim 70^\circ$ , with a centre-to-centre distance of  $63^\circ$ .

The processing of seismic noise data is segment-based, as demonstrated in Fig. 2. The processing is similar to that adopted by Poli et al. (2012) and Boué et al. (2013b). First, routine signal-processing operations are applied to the raw seismograms (including mean and linear trend removal, bandpass filtering, 5 Hz down-sampling, instrumental response deconvolution). Then, continuous seismograms are divided into 4 h segments. The frequency spectra of the segments are whitened between periods of 1 and 100 s. One may further clip the spectral-whitened waveform at several times the standard deviation to reduce large transients (e.g. 3.8 times as in the above-mentioned studies). A selection filter is applied to the segments to detect and reject those containing transient impulses like earthquakes and electronic glitches.

In the previously mentioned studies, the selection filter was based on the energy ratio between the segment and daily trace, which can be deemed as a coarse version of the classic STA / LTA method commonly used for earthquake detection (Allen, 1982). Here, we adopt a new kurtosis-based selection filter. The kurtosis, or fourth-order normalized central moment, is defined as  $\kappa = E[s^4] / E[s^2]^2 - 3$ , with  $E[\cdot]$  the expectation operator for arithmetic mean and  $s$  the demeaned waveform. It can be deemed as a measurement of deviation from the Gaussian distribution that has a kurtosis value of zero and is generally expected for stationary ambient seismic noise (Peterson, 1993). The kurtosis is highly sensitive to impulsiveness (Westfall, 2014), close to zero for stationary noise but increasing abruptly in the presence of transient impulses (see Fig. 3 for examples). The selection filter can be applied at any stages of the processing (raw, whitened, clipped waveforms). In this study, segments of kurtosis beyond an empirical threshold of 1.5 are discarded. The kurtosis, which has been applied to detect earthquakes and identify phases (e.g. Baillard et al., 2014; Saragiotis et al., 2002), is



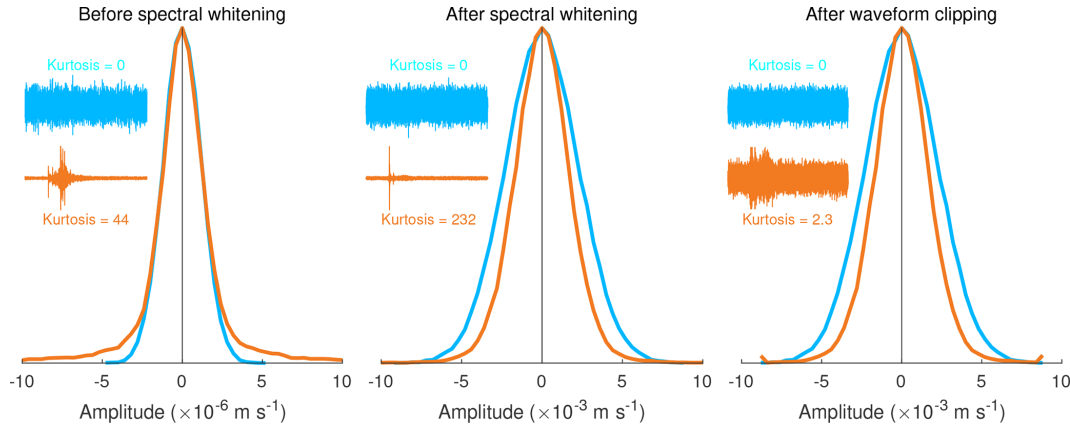
**Figure 2.** Examples of segment-based noise data processing. A segment with stationary noise and a segment containing a M7.2 teleseism from a daily trace recorded by FNET station BO.YMZ are used for demonstration.

used for noise data processing for the first time. Compared to the energy-based selection, the kurtosis-based selection depends on the statistics of the segment itself and is more robust when the strength of seismic noise changes rapidly.

### 3 Observation of the spurious phase

We correlate all of the available pairs of processed noise segments and stack them to produce the correlation function of the year-long data for each FNET–LAPNET station pair. A diagram showing the computation of the correlation function is found in Fig. S1 in the Supplement. The correlation function contains a causal part and an acausal part that correspond to the positive and negative time lags respectively. In this paper, the acausal correlations correspond to seismic waves that travel from FNET to LAPNET (causal: from LAPNET to FNET).

The noise correlations of all of the FNET–LAPNET station pairs are binned in an inter-station distance interval of  $0.1^\circ$ , to produce the waveform sections for the acausal and causal parts of the noise correlations. The filtered sections (periods of 5 to 10 s) of the vertical–vertical noise correlations are shown in Fig. 4 and the broadband sections in Fig. S2. The theoretical P and PcP waves marked on the panels are predicted using the TauP program (Crotwell et al., 1999) and the IASP91 Earth model (Kennett and Engdahl, 1991). A coherent arrival between 410 and 450 s is clearly visible in the acausal section of noise correlations, about 200 s earlier than the direct P wave that should be the primary arrival. The early arrival has no correspondence in the true Green’s function of the Earth medium, and thereby is undoubtedly a spurious phase. Spectral analysis indicates that the spurious phase has a peak period of 6.2 s (Fig. S3), typical for secondary microseisms. As estimated from the acausal



**Figure 3.** Kurtosis-based selection filter to determine if a segment contains large-amplitude transients. The two segments used here are the same as in Fig. 2. For display, waveforms are plotted at varying scales. The amplitude histograms are normalized by their own maximums. Histogram tails outside the horizontal axis limits are cropped.

vespagram in Fig. 4, the emerging time and apparent slowness of the spurious phase at  $63^\circ$  distance are about 430 s and 4.6 s per degree respectively. The spurious phase is only observed in the vertical–vertical noise correlations, indicating that it is likely a P-type phase. In the causal correlations, a corresponding spurious phase is hardly discriminable.

#### 4 Origin of signals from P–PKPab correlations

In the previous section, a prominent spurious phase was observed in the FNET–LAPNET noise correlations, and its apparent slowness and emerging time were estimated. The double-array configuration offers the possibility to estimate the respective azimuths and magnitudes of the slownesses of the correlated wavefields that should be responsible for the spurious phase. Given a wave with slowness  $\mathbf{p}^A$  at FNET and a wave with slowness  $\mathbf{p}^B$  at LAPNET, the time difference between the time delay of the  $i$ th FNET station and the  $j$ th LAPNET station and the centre-to-centre reference time can be determined from Eq. (1):

$$\Delta t_{ij} = \mathbf{x}_i^A \cdot \mathbf{p}^A - \mathbf{x}_j^B \cdot \mathbf{p}^B, \quad (1)$$

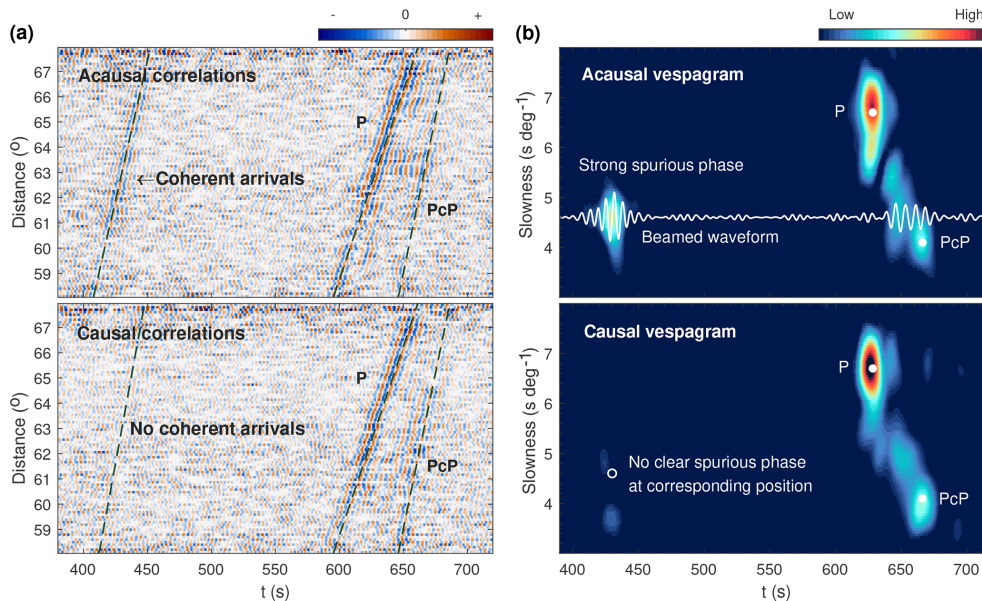
where  $\mathbf{x}$  are the local coordinates of the station with respect to the array centre, and superscripts A and B distinguish between FNET and LAPNET. For a given pair of  $(\mathbf{p}^A, \mathbf{p}^B)$ , the noise correlations of all station pairs are shifted and stacked by Eq. (2):

$$B(t, \mathbf{p}^A, \mathbf{p}^B) = \langle C_{ij}(t + \Delta t_{ij}) \rangle, \quad (2)$$

where  $\langle \cdot \rangle$  denotes the ensemble average and  $C_{ij}$  is the correlation function between the  $i$ th FNET station and the  $j$ th LAPNET station. This delay-and-sum process for the double-array data is known as the double-beam method, which has been applied to earthquake data (e.g. Krüger et al.,

1993; Rost and Thomas, 2002) and noise correlations (e.g. Boué et al., 2013a; Roux et al., 2008). Repeating the double-beamforming for a range of  $\mathbf{p}^A$  and  $\mathbf{p}^B$ , the power map of the double-beamed waveforms  $\langle |B(\mathbf{p}^A, \mathbf{p}^B)|^2 \rangle$  provides the optimal slowness estimates for the interfering waves. Here we call this method the double-array slowness analysis.

The results of the double-array slowness analysis for the observed spurious phase are shown in Fig. 5a. The azimuths of the correlated waves responsible for the spurious phase are confined to the great-circle direction across FNET and LAPNET, implying that the corresponding microseism noise source should be located on the great circle. The slowness at FNET is distinct from that at LAPNET. The 4.7 s per degree slowness at FNET is valid for deep mantle phases, while the 4.2 s per degree slowness at LAPNET is characteristic of core phases. To investigate the resolution capability of the double-array slowness analysis for the FNET–LAPNET geometry, we make numerical experiments by presuming (a) the same slowness at FNET and LAPNET (4.6 s per degree) and (b) different slownesses at FNET (4.7 s per degree) and LAPNET (4.2 s per degree). Assuming plane waves passing through FNET and LAPNET, the time delays between FNET and LAPNET station pairs can be calculated from Eq. (1). The wavelet of the observed spurious phase (5 to 10 s bandpass filtered) is convolved with the time delays to synthesize the correlation functions. The synthesized correlations are shifted and stacked by Eq. (2) for various slownesses. The results are plotted in Fig. 6. In both cases, the slownesses of the correlated waves at FNET and LAPNET are well resolved, justifying the reliability of our slowness discrepancy estimation in Fig. 5a. To investigate if this discrepancy is caused by the lateral heterogeneity of structure beneath the seismic networks, we apply the double-array slowness analysis to the acausal P waves in the FNET–LAPNET correlations as reference (Fig. S4). If lateral heterogeneity causes the slowness discrepancy for the spurious



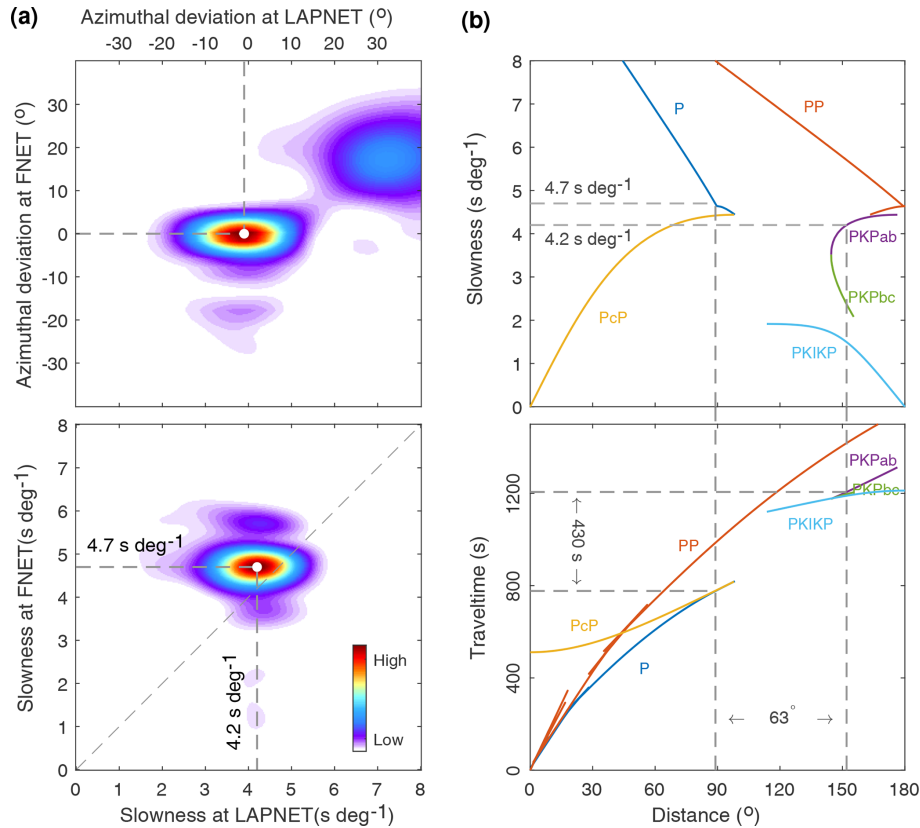
**Figure 4.** (a) Waveform sections and (b) vespagrams of the acausal and causal parts of the vertical–vertical noise correlations filtered in the period band from 5 to 10 s. The acausal section for negative time lags is flipped to share a common time axis with the causal section.

phase, one should also observe a similar phenomenon for the inter-receiver P wave. It is revealed that the slownesses of the interfering waves for the P wave coincide with each other and are close to the predicted value (6.7 s per degree in IASP91 model). The P wave results again justify the reliability of our slowness estimates, and indicate that lateral heterogeneity is not the reason for the slowness discrepancy observed from Fig. 5a.

The peak period of the spurious phase is a typical value for secondary microseisms, which are dominantly excited by ocean wave–wave interactions (Hasselmann, 1963; Longuet-Higgins, 1950). It implies that the noise sources are mainly distributed on the global ocean surface. We propose a slowness-track method to identify the ray paths of the interfering waves from source to receivers that produce the spurious phase (Fig. 5b). Body-wave phases that are discernible in the vertical-component earthquake seismograms are considered as candidates (see labels in Fig. 7). For each seismic phase, we compute a distance–travel time table and a distance–slowness table using the TauP program. The source–receiver distance can be derived from the distance–slowness table, and subsequently, the travel time can be obtained from the distance–travel time table. A pair of seismic phases are rejected if the difference between their source–receiver distances differs from the reference FNET–LAPNET distance ( $63^\circ$ ) or if their time delay deviates from the emerging time of the spurious phase (430 s). For clarity, only some typical P-type phases (P, PcP, PP and PKP branches) are shown in Fig. 5b. Finally, we find that only the correlation between the P wave at FNET and the PKPab wave at LAPNET, emitted from noise source on the great cir-

cle  $\sim 89^\circ$  away from FNET and  $\sim 152^\circ$  from LAPNET, can satisfy all the constraints. As can be seen from Fig. 5b, at  $89^\circ$  distance, the PcP wave arrives almost simultaneously with the P wave, suggesting that PcP–PKPab also has a time delay of  $\sim 430$  s at  $63^\circ$  inter-receiver distance. However, the PcP slowness (4.1 s per degree) is inconsistent with the estimated 4.7 s per degree slowness at FNET. We ascribe this to PcP being a faint phase, so that signals generated from PcP–PKPab correlations are much weaker than those generated from P–PKPab correlations. The slownesses estimates are crucial for the exclusive determination of the interfering waves. There are also other pairs of seismic phases meeting the constraints other than the slowness estimates. Another example of PcS–PcPPcP correlations that roughly meets the inter-receiver distance ( $63^\circ$ ) and time delay (430 s), is provided in Fig. S5. The correlated PcS and PcPPcP waves have a common slowness of 3.6 s per degree. The PcS–PcPPcP correlations, as shown by Phm et al. (2018), may lead to conspicuous signals in coda correlations. However, compared with the direct P and PKP waves in the ambient noise wavefields, the two correlated waves are too weak to have significant contributions to the spurious phase observed in this study. Furthermore, the difference in slowness estimates refutes the PcS–PcPPcP correlation as the dominant term in our case. This example reflects the discrepancies between ambient noise correlations and earthquake coda correlations.

It is logical that the spurious phase is observable in the vertical–vertical noise correlations only, as the correlated waves are both P type and their amplitudes are dominantly projected onto the vertical components (the lower quality of the horizontal components could be another reason). From



**Figure 5.** (a) Results of the double-array slowness analysis for the observed spurious phase. (b) Tracking the interfering waves responsible for the spurious phase using the slowness estimates.

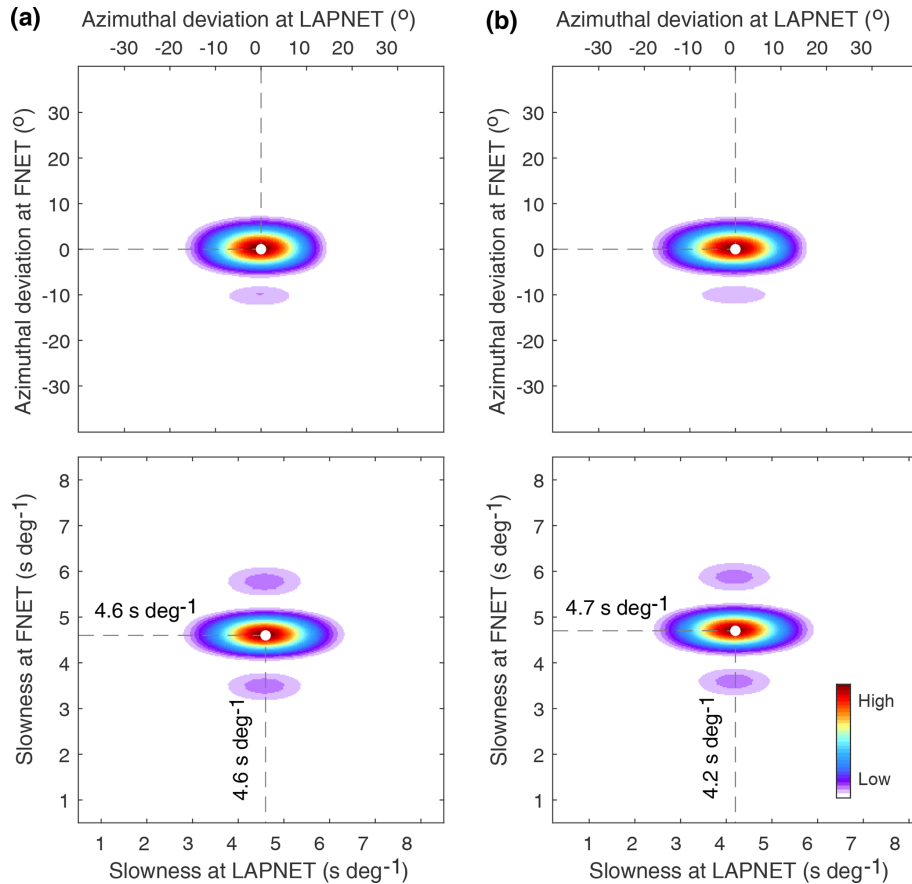
the receiver locations and source–receiver distances, one can locate the source responsible for the acausal and causal spurious phase, at around ( $45^{\circ}$  S,  $174^{\circ}$  E) and ( $12^{\circ}$  S,  $28^{\circ}$  W) respectively. Recall that the spurious phase is not observable in the causal correlations. Comparisons with global oceanic microseism noise sources (Fig. 8) indicate that this time asymmetry can be explained by the difference in the strength of the acausal and causal noise sources: the acausal source in the ocean south of New Zealand is energetic, whereas the causal source in the low-latitude Atlantic east of Brazil is much weaker.

## 5 Explanation of the quasi-stationary phase

The observed spurious phase originates from the correlation between teleseismic P waves and PKPab-waves that emanate from the oceanic microseism noise source south of New Zealand. In this section, we explain how such spurious signals can be generated from the interference between waves having distinct slownesses and no common path. Considering ambient noise wavefield as a superposition of waves from uncorrelated sources distributed on Earth’s surface (Fig. 9a), the correlation function between the noise records at two receivers is equivalent to a stack of the correlation functions for

individual sources (i.e. source averaging; see, e.g. Ruigrok et al., 2008). We first simulate the source-wise correlation functions by convolving a wavelet of 6.2 s period with the time delays between the two correlated seismic phases. The final inter-receiver correlation function is obtained from a stack over all sources. In this ray-based simulation, amplitude information is neglected for simplicity. The result for the source averaging of the P–PKPab correlations is shown in Fig. 9b, while that of the P–PKPbc correlations is shown in Fig. 9c for comparison.

The construction of seismic signals from noise correlations has usually been explained with the stationary-phase condition (e.g. Wapenaar et al., 2010). We show such an example in Fig. S4, which is the reconstruction of the inter-receiver P wave from the correlation between the P and PP waves. The P-wave reconstruction is linked to the presence of the extreme (stationary) point on the curve of the P–PP time delay. The P and PP waves from the source at the stationary-phase location (Fig. S4, source A) have a common path and a common slowness. However, as for the spurious phase observed between FNET and LAPNET, the correlated P and PKPab waves have no slowness or ray path in common, and there is no stationary point on the curve of the P–PKPab time delay (Fig. 9b). The strict stationary-phase condition is



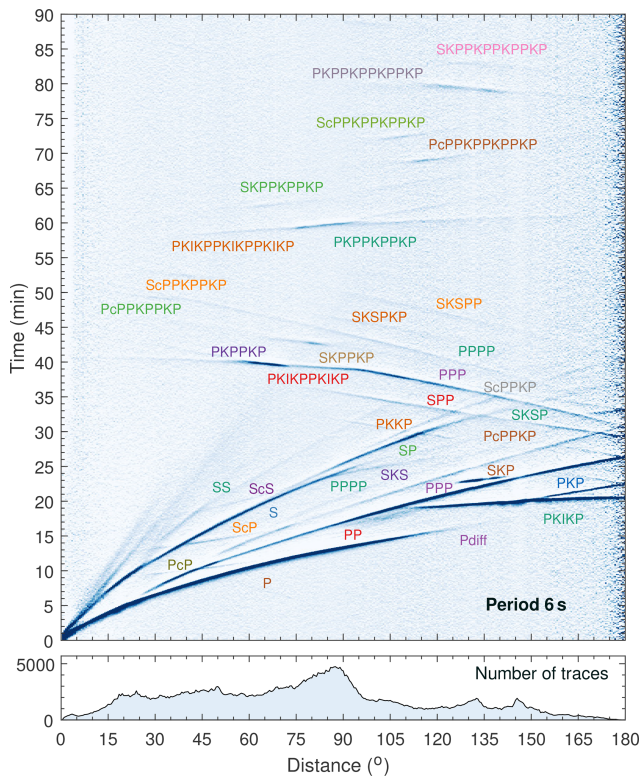
**Figure 6.** Numerical tests for the double-array slowness analysis of the FNET–LAPNET correlations at a seismic period of 6.2 s. The input azimuths of the interfering waves are confined to the great circle crossing FNET and LAPNET. The azimuthal deviation refers to the clockwise azimuthal deviation of slowness from the great circle. The input slownesses of the interfering waves are (a) 4.6 s per degree at both LAPNET and FNET and (b) 4.2 s per degree at LAPNET and 4.7 s per degree at FNET, which are well resolved by the slowness analysis.

not fulfilled, and thus the emergence of the spurious phase cannot be explained by this argument. Despite the missing of stationary points on the curve of the P–PKPab time delay, the interference between finite-frequency P and PKPab waves is constructive over the shaded range in Fig. 9b. This leads to the presence of a pulsive signal in the final inter-receiver correlation by source averaging. In contrast to the strict condition of the stationary phase, we propose to call this mechanism the condition of quasi-stationary phase, and refer to this range of sources as the quasi-stationary-phase region or effective source region. Recall that the spurious phase has a peak period of 6.2 s. We emphasize that this typical dominant period for secondary microseisms is resultant from the distribution of spectral content of seismic noise sources – secondary microseisms correspond to the largest peak in the seismic noise spectra (Peterson, 1993). Numerical tests of source averaging for the P–PKPab correlations indicate that, even at short periods (1 s or less), the spurious phase can be constructed, with narrower effective source region shrinking toward larger source–receiver distances.

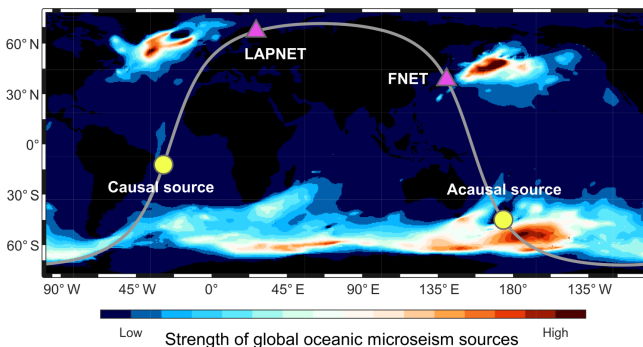
Experiences from earthquake observations indicate that PKPbc waves are generally the dominant PKP branch at distances from  $\sim 144^\circ$  (the PKP-wave caustic) to  $\sim 153^\circ$  (Kulhánek, 2002). Microseism studies have also reported that PKPbc waves can be more prominent (e.g. Gerstoft et al., 2008; Landés et al., 2010). However, our analysis reveals that the spurious phase originates from the interference of P waves with PKPab waves, rather than with PKPbc waves. From the source-averaging experiment for the P–PKPbc correlations (Fig. 9c), one can see that the P–PKPbc time delay varies almost linearly against the source–receiver distance, and that the dynamic range of the time delay is broad. Consequently, the signals in the source-wise correlations are out of phase, which leads to a destructive source averaging.

## 6 Effect of source distribution

The above-described ray-based simulation is simple to implement and efficient at revealing the origin of the spurious phase. It uses only the phase information and neglects the ef-



**Figure 7.** Global stacks of the vertical components of the seismograms selected from over 2500 shallow earthquakes (event depth  $\leq 50$  km and magnitude  $\geq 5.4$ ) occurring between 1995 and 2013. The seismograms are filtered around 6 s period and converted into traces of STA / LTA ratios. The STA / LTA traces are binned by epicentral distances at an interval of  $0.5^\circ$  and normalized for plotting. More details can be found on the IRIS Data Services Products website.



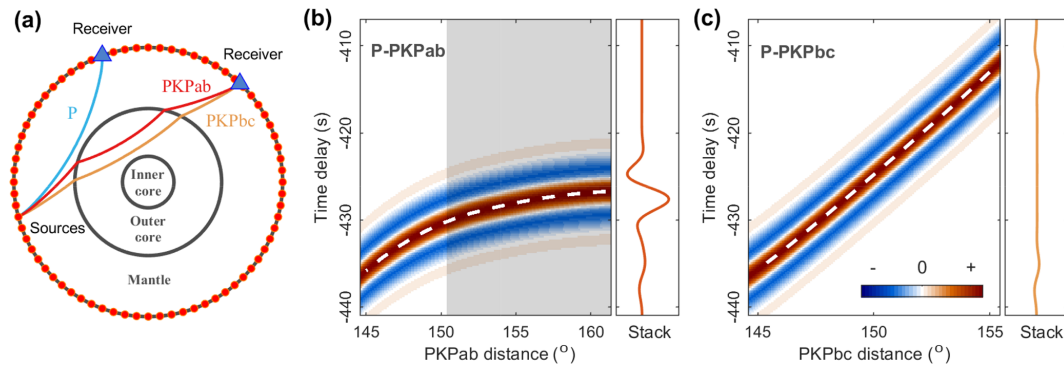
**Figure 8.** The global map of oceanic microseism excitation in 2008, at a seismic period of 6.2 s (Rascle and Arduin, 2013). The source responsible for the acausal spurious phase is located in the ocean south of New Zealand.

fect of amplitude variations. This simplification ensures that the spurious phase is not likely to be caused by a strong localized source. To confirm, in this section, we implement a formal wave-based simulation to show that the observed spurious arrivals can be well reproduced under an ideally uniform source distribution. As shown in Fig. 8, the spatial variations of the power of global microseism sources are heavily fluctuated. The spurious phase is observable in the acausal correlations because the corresponding source is strong, and is hardly observable in the causal correlations because the responsible source is too weak. It is worth confirming whether the spurious phase can be eliminated with an ideally uniform source distribution or not.

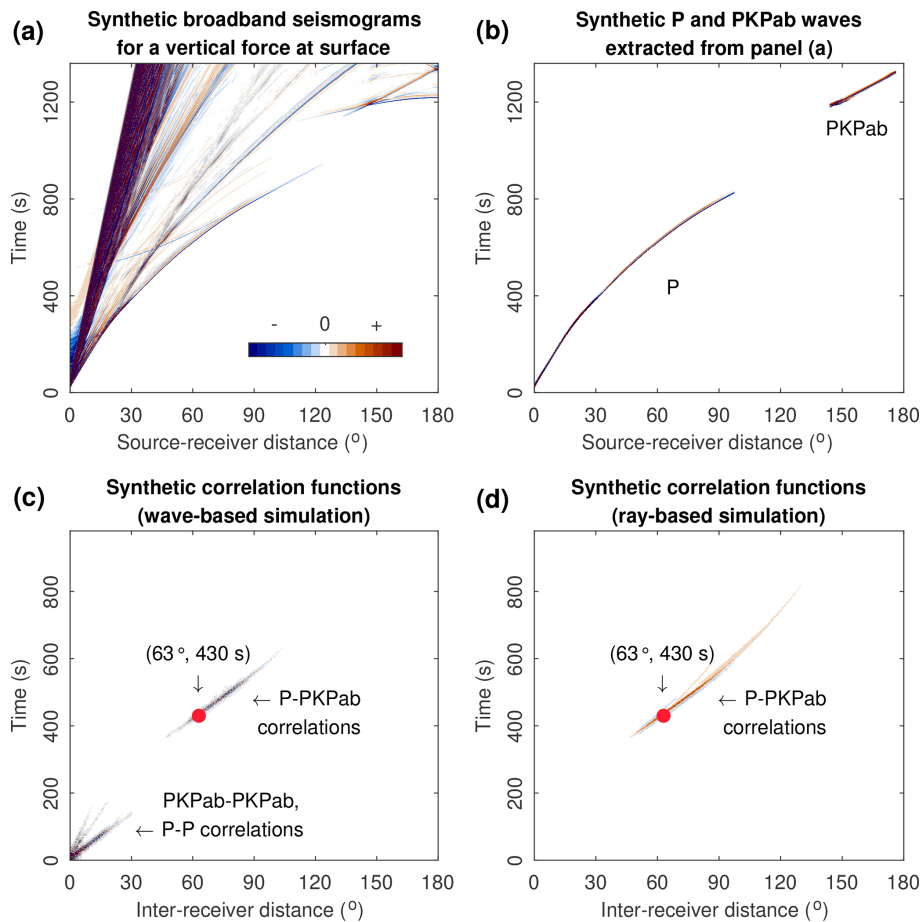
We request the vertical components of the synthetic global broadband seismogram for the *iasp91\_2s* model from the IRIS Syngine Data Service (Krischer et al., 2017) powered by the spectral-element program AxiSEM (Nissen-Meyer et al., 2014) and the Python packages Obspy (Krischer et al., 2015) and Instaseis (Van Driel et al., 2015). A mask is applied to the full waveforms (Fig. 10a) to extract the P waves and the PKPab waves (Fig. 10b). Providing that the uncorrelated noise sources are distributed evenly on the global surface, we compute the source-wise correlations and stack them for each inter-station distance, using the data in Fig. 10b. A global section of synthetic P–PKPab correlations is obtained accordingly (Fig. 10c). The spurious phase is clearly reproduced, which suggests that it is not caused by unevenly distributed noise sources.

Repeating the ray-based simulation in Fig. 9b for various inter-receiver distances, one can also obtain a full section of the P–PKPab correlations. Due to the neglect of amplitude information, the ray-based simulation overestimates the observable range of inter-receiver distances for the spurious phase. The wave-based simulation in this section is undoubtedly more realistic. The theoretical time–distance curve of the spurious phase can be picked from the synthetic sections. It is almost identical for the ray- and wave-based simulations in the observable distance range, and fits well with the observed spurious arrivals in Fig. 4. We also compare the results of the wave-based simulations for the two-dimensional plane model (sources along the great circle) and three-dimensional spherical model (sources on global surface). As shown in Fig. S6, the reduction of the source dimension leads to an overestimation of the observable distance range of the spurious phase. The time–distance curves picked from the synthetic P–PKPab correlations of two models are identical in the common distance range, while the amplitudes of signals are different. In the case of uniformly distributed sources, it is safe to implement a two-dimensional simulation for efficiency.





**Figure 9.** (a) Geometry of the model to synthesize the inter-receiver correlation function of teleseismic P and PKP waves via source averaging. (b) Source-averaging experiment for the P-PKPab correlations at an inter-receiver distance of 63°. The source-wise P-PKPab correlation functions are synthesized by convolving a 6.2 s period wavelet with the P-PKPab time delays. The final inter-receiver correlation function is obtained by stacking the source-wise correlations. (c) Source-averaging experiment for the P-PKPbc correlations.



**Figure 10.** (a) Global section of synthetic broadband (2 to 100 s) seismograms obtained from the IRIS Syngine Data Service. (b) Seismograms containing P and PKPab waves only, by muting other seismic phases in (a). (c) Global section of inter-receiver correlations using the waveform data in (b). (d) Global section of synthetic P-PKPab correlations using the ray-based method in Fig. 9.

## 7 Conclusions

We observe early spurious arrivals in the teleseismic noise correlations between the Japan and Finland stations. These signals are prominent and isolated from other strong seismic phases, making it a good agency to unveil the generation mechanism of such spurious phases. In contrast to previous studies that observed a strong correlation between signal amplitudes and large earthquakes, the spurious signals in this study have no connections to seismicity. We provide evidence supporting that the observed signals originate from the interference between ballistic P waves and PKPab waves that emanate from oceanic microseism noise sources south of New Zealand. The interfering waves have no ray path or slowness in common, and do not meet the traditional condition of stationary phase. The effective source location responsible for the spurious phase does not correspond to a stationary point. We propose a less restrictive condition of quasi-stationary phase, which explains our finite-frequency observations. The strict stationary-phase condition has been used by Phm et al. (2018) to interpret the spurious phases in the earthquake coda correlations. We expect to see if the quasi-stationary-phase arguments can be generalized to the explanation of the coda-derived spurious phases.

The interfering P and PKPab waves have deterministic ray paths that sample the deep mantle and the core. We expect a way to use the spurious phase to investigate the deep Earth structure. The strength of the spurious phase is linked to the power of microseism excitation in a definite, constrained region of noise sources. There is potential to use it to monitor ocean wave activities and microseism excitations in that specific region. Ambient noise wavefields are dominated by the ballistic waves that persistently emanate from oceanic microseism events, while late coda wavefields after large earthquakes are dominated by highly coherent deep reverberations/high-order core modes separable at intermediate periods of 20 to 50 s (Boué et al., 2014; Maeda et al., 2006; Poli et al., 2017). We call for differentiation between global noise correlations and global coda correlations. Multiple spurious arrivals have been observed from the global coda correlation wavefield (Boué et al., 2014; Lin and Tsai, 2013; Phm et al., 2018). The P–PKPab correlation could not be the unique spurious phase emerging in the global noise correlation wavefield. The double-array slowness analysis and slowness-track method proposed in this paper are also applicable to the analysis of other coda- and noise-derived signals.

*Code and data availability.* The continuous seismograms of FNET and LAPNET were provided by the National Research Institute for Earth Science and Disaster Resilience (<http://www.fnet.bosai.go.jp>, last access: 30 June 2018) and the Réseau Sismologique & Géodésique Français (<http://www.resif.fr>, last access: 30 June 2018) respectively. The global earthquake seismograms were obtained from the IRIS GlobalStacks Data Ser-

vice (<https://doi.org/10.17611/DP/GS.1>, IRIS-DMC, 2014). The global synthetic seismograms were obtained from the IRIS Syn-gine Data Service (<https://doi.org/10.17611/DP/SYNGINE.1>, IRIS-DMC, 2015). The data of synthetic global microseism noise sources were provided by the IOWAGA products (Rasclé and Arduin, 2013). The TauP program (Crotwell et al., 1999) and the IASP91 Earth model (Kennett and Engdahl, 1991) were used to calculate the theoretical travel times and ray parameters of seismic phases.

*Supplement.* The supplement related to this article is available online at: <https://doi.org/10.5194/se-11-173-2020-supplement>.

*Author contributions.* LL performed data processing and designed the synthetic experiments. The code for noise data processing was developed based on an early version by PB. All authors contributed to the analysis of the results. LL prepared the manuscript with contributions from all co-authors. MC wrote the proposal leading to this publication.

*Competing interests.* The authors declare that they have no conflict of interest.

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*Supplement of*

## **Observation and explanation of spurious seismic signals emerging in teleseismic noise correlations**

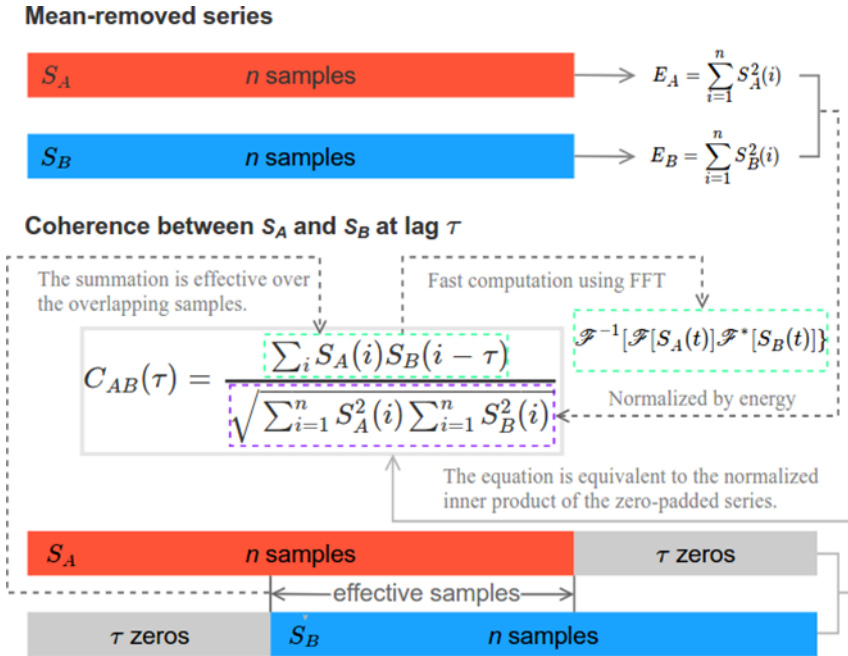
**Lei Li et al.**

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## Computation of correlation function

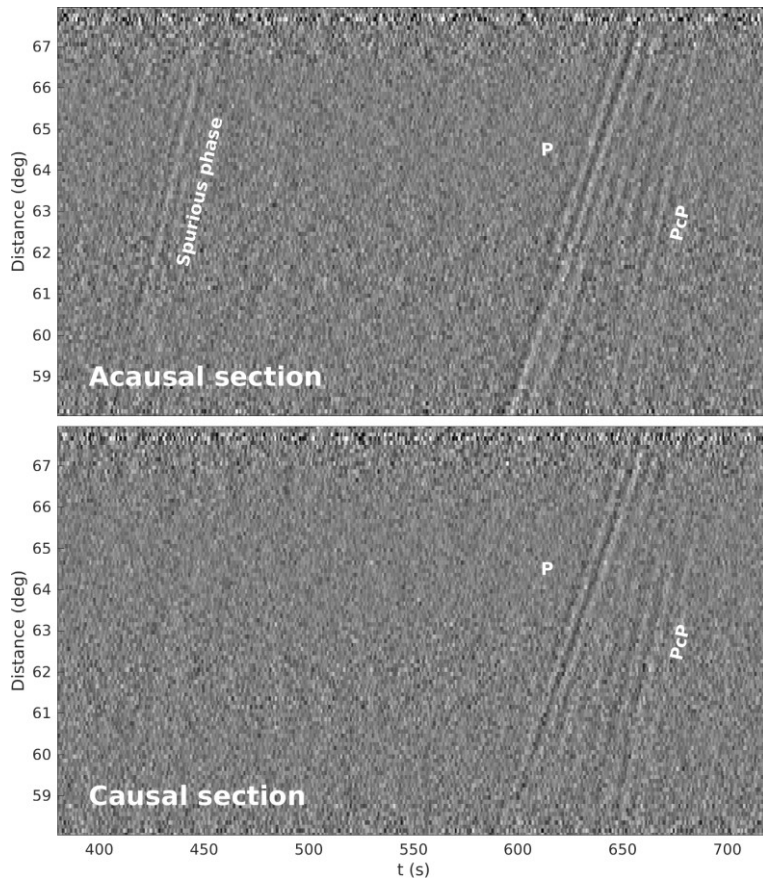
Figure S1 describes the computation of the correlation function between two time series. The diagram is self-explained.



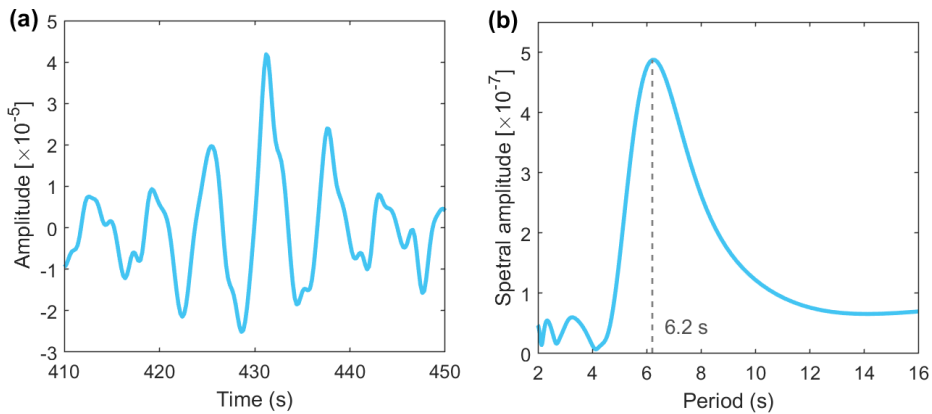
5 Figure S1: Schematic for the computation of the correlation function between two mean-removed time series.

## Broadband double-array correlations

Figure S2 shows the FNET-LAPNET correlations in the period band of 1 s to 100 s. The spurious phase is clearly visible in the acausal section. The beamed waveform of the acausal spurious phase and its frequency spectrum are plotted in Fig. S3. It has a peak period of 6.2 s.



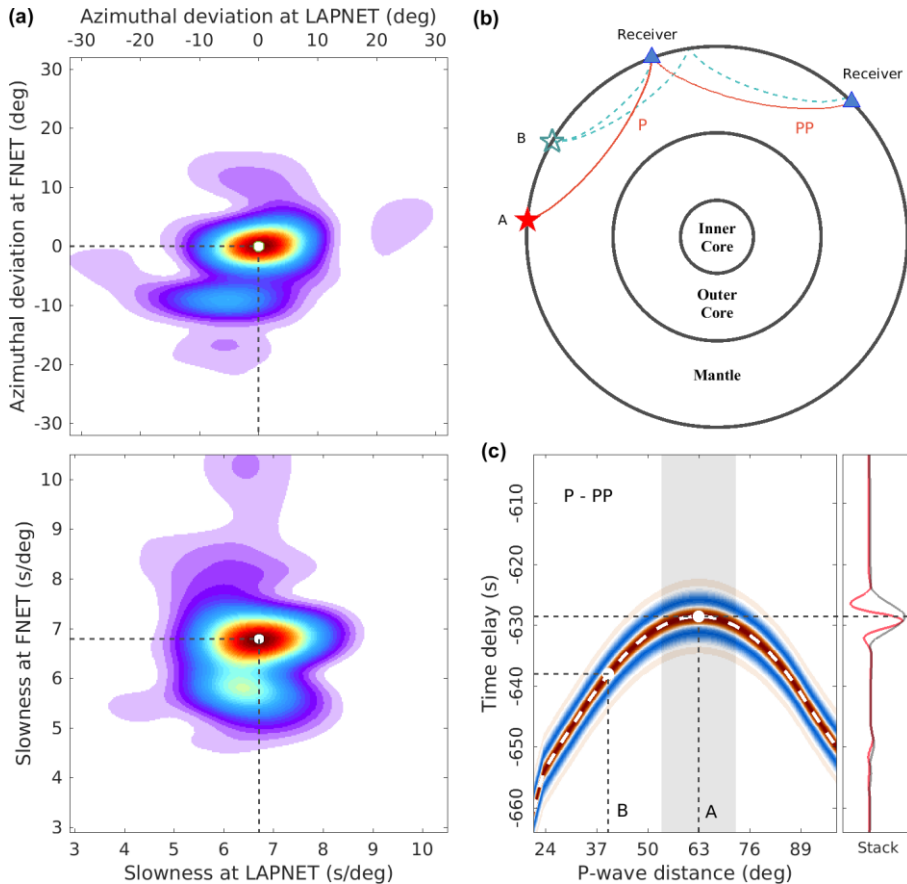
**Figure S2:** Broadband (1 to 100 s) sections of the acausal and causal parts of the vertical-vertical noise correlations stacked in  $0.1^\circ$  distance bins.



**Figure S3:** (a) Beamed waveform and (b) amplitude spectrum of the spurious phase in the broadband of 1 to 100 s.

## Stationary-phase examples

Figure S4 shows the double-array slowness analysis for the noise-derived acausal P wave and the synthetic experiment for the generation of the inter-receiver P wave from P-PP correlations that can be explained by the traditional stationary-phase arguments, in contrast to the results of slowness analysis for the acausal spurious phase in Fig. 5 and the quasi-stationary-phase explanation in Fig. 9. Slowness analysis in Fig. S4a indicates the correlated waves responsible for the inter-receiver P wave have almost identical slowness. The schematic in Fig. S4b shows that the P wave emanating from the stationary location (label A) to the first receiver and the PP wave to the second receiver have a common slowness and a common P path. The correlation operator cancels the common path and accordingly extracts the phase delay between two receivers. Fig. S4c shows the synthetic source averaging experiment for P-PP correlations. The stationary location corresponds to the extreme point on the dashed time-delay curve. Amplitudes in the P-PP correlations for sources outside the shaded stationary-phase region cancel out by the averaging. The time delay at the maximum of the envelope of the stacked waveform matches exactly with the theoretical travel time of the inter-receiver P wave.

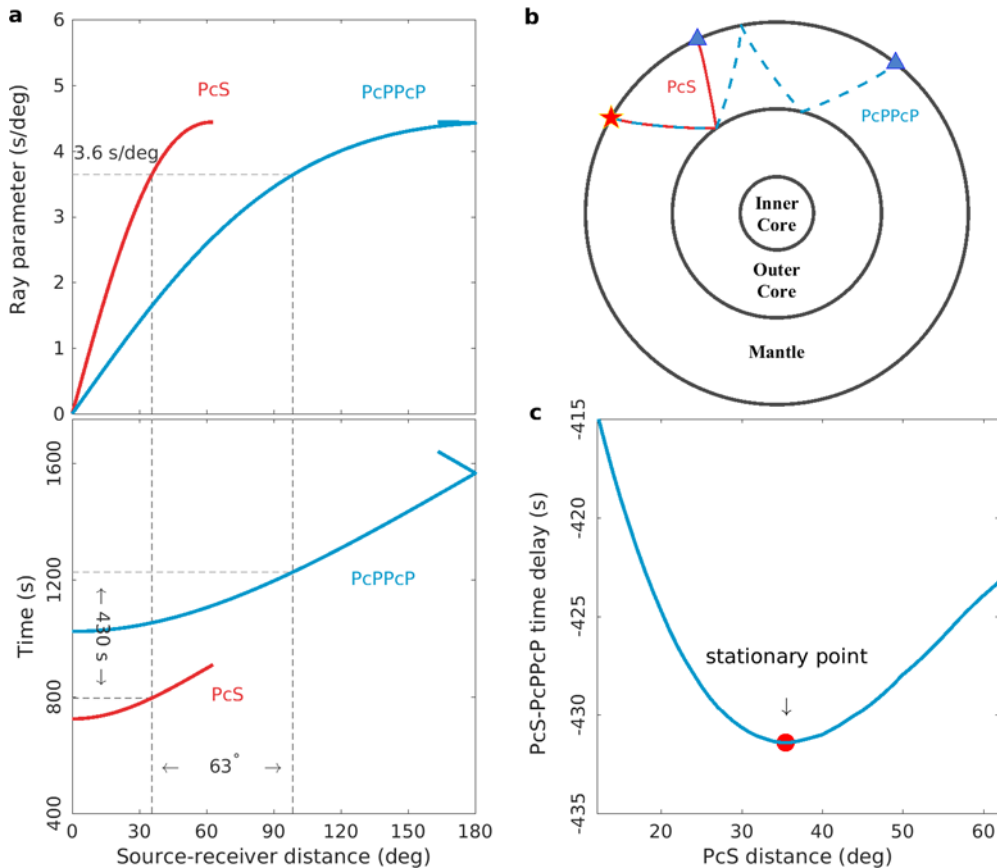




5 **Figure S4:** (a) Results of double-array slowness analysis for the acausal P wave. (b) Ray paths of the correlated P and PP waves from distributed sources. Source A is placed at the stationary location. Label B denotes any noise source on the global surface outside the stationary-phase region. For simplicity, the correlations between higher-order multiples like PP-PPP that can also give rise to P waves are neglected. (c) Reconstruction of the inter-receiver P wave from the P-PP correlations by source averaging, explained by the traditional stationary-phase theory.

In the global section of coda correlations by Pham et al. (2018), there is also a spurious signal at  $\sim 430$  s time delay and  $63^\circ$  separation distance (see their fig. 2). Pham et al. (2018) ascribed the signal to the correlation between cS and cPPcP phases for sources distributed on the core-mantle boundary (phase naming in their customized conventions; equivalent to s and pPcP phases in IASPEI convention). Here we consider the PcS-PcPPcP correlation, which is an equivalence to their cS-cPPcP correlation but for sources on the global surface. Figure S5 depicts the stationary-phase arguments for the PcS-PcPPcP correlation. However, similar to the discussion about the PcP-PKPab correlation in the main text, the correlated waves are too weak in the ballistic wavefield to be responsible for the spurious phase observed in this study (cf. Fig. 7 in main text). And another strong argument is that, the slownesses of PcS and PcPPcP are quite distinct from the slowness estimates in Fig. 2a.

15

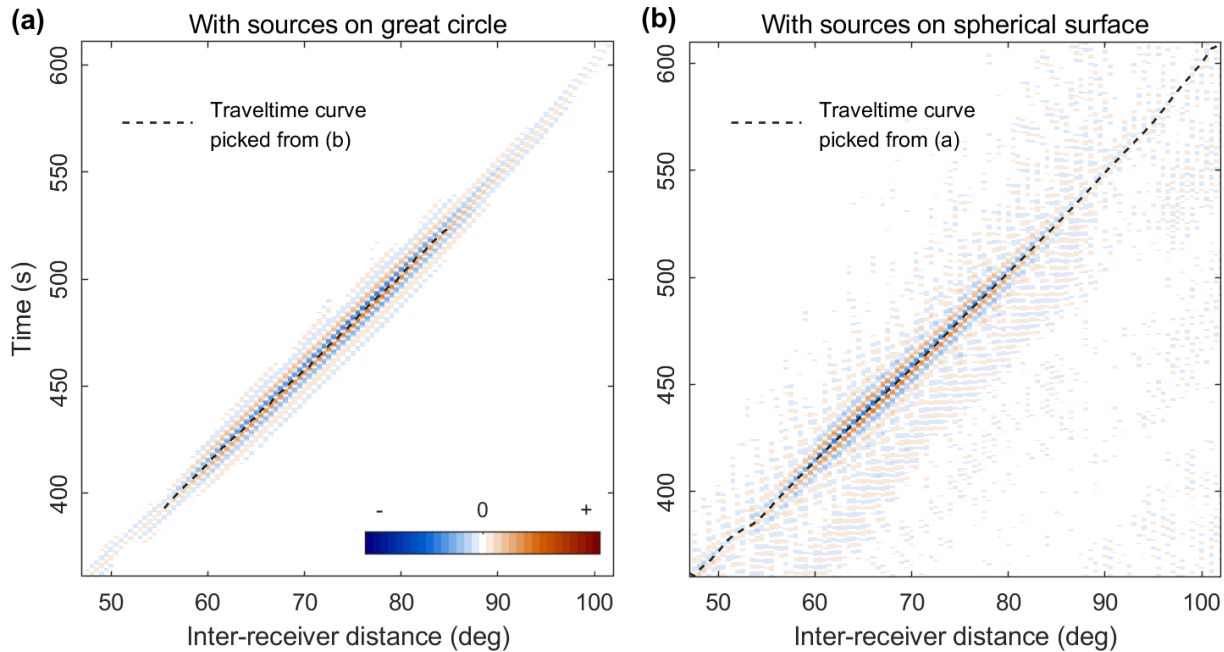


**Figure S5:** (a) Theoretical curves of ray parameters and travel times of PcS and PcPPcP. (b) Ray paths of PcS and PcPPcP from source at stationary location. (c) PcS-PcPPcP time delays for distributed sources.

## Numerical simulations of P-PKPab correlations

Figure S6 shows the synthetic P-PKPab correlations for the planar model with sources along the great circle (one-dimensional source distribution) and the spherical model with sources over the global surface (two-dimensional source distribution), using the wave-based method described in section 6 of main text. The synthetic correlations are filtered between 5 s and 10 s periods.

- 5 The spurious phase is visible in a broader distance range in Fig. S6a than in Fig.S6b. The time-distance curves are picked from the maximum on the envelope of each trace. In the common distance range, the two time-distance curves agree well with each other.



10 **Figure S6: Wave-based simulations of P-PKPab correlations with sources (a) on the great circle and (b) on the global surface.**