

## **A Constraint-Convergent Framework for Tornado Formation (the ARCH Equation)**

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## Abstract

Despite significant advances in meteorological observation and modeling, the precise prediction of tornado occurrence remains a persistent challenge. Traditional forecasting approaches often rely on additive or probabilistic frameworks, assuming that the likelihood of a tornado increases as favorable parameters accumulate. However, many environments that appear highly conducive to tornadoes fail to produce them, while tornadoes occasionally form in marginal conditions. This paper proposes a conceptual shift: viewing tornado genesis as a constraint-convergent execution event, governed by the simultaneous satisfaction of multiple independent and necessary conditions. Drawing on analogies from systems biology, the ARCH equation is a conjunctive, multiplicative model in which tornado formation requires the co-occurrence of surface boundary presence, thermodynamic instability, contextual dynamics, upper-level forcing, and phase alignment. Case studies and integration with statistical, machine learning, and numerical modeling approaches demonstrate how this framework explains both false alarms and unexpected tornadoes. The constraint-convergent perspective also clarifies the limitations of existing composite indices and highlights the importance of identifying specific failure modes in tornado prediction. Beyond tornadoes, this logic applies to other threshold-governed atmospheric phenomena, suggesting a broadly applicable systems approach to meteorological transitions. The ARCH model offers new avenues for empirical research, interdisciplinary collaboration, and operational application, with the potential to improve warning systems, risk communication, and resilience in a changing climate.

## **Advances in Meteorological Observation and Modeling**

Recent decades have seen remarkable progress in the observation and modeling of severe weather. Technologies such as Doppler radar, satellite remote sensing, and high-resolution numerical weather prediction (NWP) models now enable meteorologists to identify environments conducive to severe convective storms with increasing accuracy (Bluestein, 2013; Stensrud et al., 2009; Markowski & Richardson, 2011). Key parameters—including convective available potential energy (CAPE), storm-relative helicity (SRH), vertical wind shear, and low-level moisture—are routinely analyzed to assess tornado risk (Thompson et al. 2003; Davies-Jones 2015). Composite indices, such as the Significant Tornado Parameter (STP) and Energy-Helicity Index (EHI), integrate these variables into single metrics used in both research and operational forecasting (Doswell et al. 1996; Doswell and Schultz 2006). These advances have improved tornado warning lead times and the identification of high-risk regions (Simmons and Sutter 2011).

## **The Persistent Challenge of Tornadogenesis**

Despite these advances, the precise prediction of tornado occurrence—especially the timing and location of tornadogenesis—remains elusive (Davies-Jones 2015; Schultz and Stensrud 2010). Many environments that appear highly favorable for tornadoes fail to produce them, while tornadoes occasionally occur in seemingly marginal conditions (Johns and Doswell 1992; Brooks and Doswell 2001). Even among supercell storms, only a subset produce tornadoes, and the transition from a non-tornadic to a tornadic phase is often abrupt and poorly understood (Thompson et al. 2003; Maddox et al. 1980). This unpredictability suggests deeper gaps in our conceptual understanding. Traditional additive or probabilistic frameworks—which assume

tornado likelihood increases as more favorable parameters accumulate—may not fully capture the process (Doswell and Schultz 2006).

### The 2011 Joplin, Missouri Tornado

On 22 May 2011, a catastrophic EF5 tornado struck Joplin, Missouri, resulting in 158 fatalities and over \$2.8 billion in damage—making it the deadliest single tornado in modern U.S. history.

Forecast guidance earlier that day suggested a moderate risk of severe weather, with increasing concern as mesoscale conditions evolved. However, the scale and destructiveness of the tornado far exceeded expectations, despite the presence of many classic environmental indicators, such as CAPE, vertical shear, and boundary-layer moisture.

From a constraint-convergent perspective, the Joplin event represents a textbook case of execution: all critical constraints—surface boundary presence, thermodynamic instability, contextual wind shear, upper-level forcing, and temporal phase alignment—were strongly and simultaneously satisfied. This suggests that the tornado was not merely the result of a probabilistic stacking of favorable parameters, but rather the conjunctive realization of independent, necessary conditions.

The case underscores the limitations of additive or compensatory forecasting models and supports the utility of a conjunctive framework, where the simultaneous satisfaction of all constraints is necessary for tornadogenesis. As such, it serves as a compelling entry point for reconsidering how tornado formation is conceptualized, diagnosed, and predicted.

## **Constraint-Convergent Execution: Insights from Systems Biology**

In cellular biology, researchers have long grappled with explaining how complex, high-stakes transitions—such as DNA replication or cell division—are regulated. Such models conceptualize these transitions as “execution events” that occur only when a specific set of independent constraints are simultaneously satisfied (Tyson and Novak 2010; Ferrell 2012). In this framework, execution is not triggered by the additive accumulation of favorable factors but by the conjunctive satisfaction of necessary and independent conditions.

This biological logic prompts a provocative analogy: could tornado formation similarly depend on the convergence of independent, necessary constraints, rather than the mere accumulation of favorable conditions? In meteorology, the “ingredients-based” forecasting paradigm recognizes the need for multiple factors—moisture, instability, lift, and wind shear—but often treats them as additive or compensatory, rather than conjunctive and threshold-based (Schultz and Stensrud 2010; Doswell et al. 1996). Notably, Fujita’s foundational work emphasized the critical role of intersecting surface boundaries, microbursts, and mesoscale vorticity sources as necessary precursors to tornado formation, describing their convergence as “mesoscale accidents”—rare alignments of atmospheric processes (Fujita 1981). His recognition that tornadoes frequently fail to materialize despite otherwise favorable environments reflects an early appreciation for the idea that tornadogenesis is governed by the conjunctive satisfaction of multiple independent conditions.

## Mapping the Analogy: A Systems Framework for Tornadogenesis

### Identifying the Critical Constraints

Translating Fujita's classic logic into multiplicative terms, we can propose a set of independent constraints, now widely recognized with modern data, as necessary for tornado formation:

- **Surface Boundary Presence:** The presence of a surface boundary (dryline, frontal, or outflow boundary) can focus storm initiation and enhance low-level vorticity (Hane and Ray 1985; Markowski et al. 2002).
- **Thermodynamic Instability:** Sufficient CAPE and moisture are essential for sustaining deep convection and robust updrafts (Emanuel 1994; Davies-Jones 2015).
- **Contextual Dynamics:** Favorable wind shear (especially low-level and deep-layer shear) and local terrain effects can enhance storm organization and rotation (Weisman and Rotunno 2000; Thompson and Mead 2007).
- **Upper-Level Forcing:** The presence of upper-level divergence, jet streaks, or vorticity maxima can provide the necessary lift and dynamic support for storm intensification (Uccellini and Johnson 1979).

Within this schema, tornado formation occurs only if all these factors are present and collectively exceed system-specific thresholds. The absence or inadequacy of any one constraint may be sufficient to suppress tornadogenesis, regardless of the strength of the others.

This logic can be formalized as the ARCH equation, which captures the conjunctive execution of tornado formation:

$$\text{Execution} = A \times R \times C \times H \times \Phi$$

where:

- A = Availability of a triggering surface boundary (e.g., dryline, front),
- R = Readiness of the environment via thermodynamic instability (e.g., CAPE, moisture),
- C = Contextual dynamics such as favorable shear and terrain-modulated flow,
- H = High-level support from upper-level forcing (e.g., jet streaks, divergence),
- $\Phi$  = Phase-alignment or stochastic synchronizer (e.g., mesoscale convergence or time-critical factors).

Here, ARCH refers to Availability, Readiness, Contextual dynamics, and High-level support, with  $\Phi$  denoting phase alignment—a stochastic synchronizer not captured by the acronym but essential to execution. In this conjunctive, multiplicative model, execution occurs only when all ARCH constraints are independently satisfied. The absence of any one constraint nullifies the

entire product, precluding tornado genesis despite favorable values of the others.

#### ARCH Constraint-Convergent Execution Model



#### Conjunctive vs. Additive Logic

The ARCH framework stands in contrast to traditional additive or probabilistic models, which often assume that increasing the magnitude of one or more favorable parameters can compensate for the lack of others. In a constraint-convergent execution model, the logic is fundamentally conjunctive: all critical constraints must be satisfied for tornado formation to occur (Doswell and Schultz 2006).

Implications for Atmospheric Science

Rethinking Predictive Indices and Diagnostics



If tornado formation is indeed a constraint-convergent execution event, existing composite indices may need to be reevaluated. Many current indices, such as the STP, are constructed as additive or multiplicative combinations of favorable parameters (Doswell and Schultz 2006). While these indices have demonstrated skill at identifying broad regions of tornado risk, they may not fully capture the conjunctive logic of tornadogenesis. A systems-based approach would encourage the development of new metrics or diagnostic tools that explicitly account for the necessity of all critical constraints—for example, indices that reflect the minimum or limiting value among the set of necessary conditions.

### **Understanding Failure Modes in Tornado Prediction**

Early empirical work by Eagleman (1967) recognized that tornado path characteristics—such as length and width—were not randomly distributed but appeared to reflect specific environmental preconditions. While not framed in constraint logic, such findings align with the idea that tornado structure and occurrence depend on the satisfaction of multiple, condition-dependent thresholds. A constraint-convergent framework also provides a more nuanced understanding of “failure modes” in tornado prediction. Rather than attributing non-formation to a general lack of favorability, forecasters and researchers could investigate which specific constraint was not met and why. This could lead to more targeted research questions, such as:

- In environments with high CAPE and shear but no tornadoes, was the absence of a surface boundary the limiting factor?
- In cases with strong boundaries and upper-level forcing but weak instability, did insufficient thermodynamic support preclude tornadogenesis?

- How do local terrain features or mesoscale processes modulate the satisfaction of critical constraints?

By systematically analyzing cases of both tornado occurrence and non-occurrence, researchers could identify patterns and develop more robust conceptual models of tornadogenesis.

### Encouraging Interdisciplinary Collaboration

The parallels between atmospheric and biological phase transitions suggest that common principles may underlie emergent phenomena across the natural world. Systems theory, network science, and the study of critical transitions have all highlighted the importance of threshold effects, constraint satisfaction, and conjunctive logic in complex systems (Scheffer et al. 2009; Barabási 2016; Newman 2010). By embracing a systems perspective, atmospheric scientists can engage with a broader scientific community, drawing on tools and concepts from other disciplines such as network analysis, information theory, or machine learning (Bishop 2006).

## **Empirical Testing and Research Directions**

### Comparative Case Studies

A promising avenue for empirical research is the systematic comparison of environments that are similar in most respects but differ in tornado outcome. By analyzing cases where all but one critical constraint are satisfied, researchers can test the hypothesis that the absence of a single necessary ingredient is sufficient to suppress tornadogenesis. Such studies could leverage high-resolution observational datasets, reanalysis products, and targeted field campaigns (e.g., VORTEX, TORUS) to document the presence or absence of surface boundaries, instability,

shear, and upper-level forcing in both tornadic and non-tornadic environments (Wurman et al. 2012; Kosiba and Wurman 2014).

### **Statistical and Machine Learning Approaches**

Advanced statistical and machine learning techniques offer powerful tools for identifying conjunctive patterns in complex datasets. Decision tree algorithms, for example, are well suited to discovering threshold effects and necessary conditions, as they naturally partition data based on the satisfaction of critical constraints (Breiman et al. 1984). Researchers could apply these methods to large samples of convective environments, seeking to identify combinations of parameters that are jointly necessary for tornado formation.

### **Integration with Numerical Modeling**

High-resolution numerical simulations provide another avenue for testing the constraint-convergent execution hypothesis. By systematically varying individual parameters in idealized or real-case simulations, researchers can assess the sensitivity of tornadogenesis to the presence or absence of specific constraints (Orf et al. 2017).

#### **Illustrative Case Applications of the Constraint-Convergent Framework**

##### **Case 1: False Alarm—High CAPE and Shear, but No Tornado**

On 10 May 2010, central Oklahoma was placed under a high-risk convective outlook, with widespread expectations of a tornado outbreak. Atmospheric parameters such as CAPE exceeded  $3000 \text{ J kg}^{-1}$ , and low-level shear values were strongly supportive of supercell formation.

Composite indices, such as the Significant Tornado Parameter (STP) and the Energy-Helicity

Index (EHI), were elevated across much of the region. Despite these signals, tornadic activity was far less extensive than forecasted. Within a constraint-convergent framework, the failure of tornadogenesis can be explained by the absence of a discrete surface boundary capable of focusing low-level vorticity and initiating organized storm-scale convergence. While thermodynamic and kinematic conditions were highly favorable, the absence of this key constraint rendered the environment non-executable for tornadic development, highlighting a false positive scenario under additive logic.

#### Case 2: Marginal Forecast, Real Tornado—All Constraints Marginally Satisfied

On 23 July 2016, a marginal risk was issued across northern Illinois, with modest CAPE values ( $\sim 1500 \text{ J kg}^{-1}$ ), weak low-level shear, and only subtle upper-level support. Nevertheless, an EF1 tornado briefly touched down, causing localized damage. The event was surprising given the low values of conventional indices. Under a constraint-convergent model, however, the event is interpretable: a small mesoscale outflow boundary was present, intersected by weak but sufficient convection. Though each constraint was only marginally met, none were absent. The critical convergence of all factors—surface focus, sufficient instability, contextual wind shear, subtle upper-level ascent, and timely boundary interaction—allowed for tornadogenesis to occur. This illustrates that when all constraints are minimally but jointly satisfied, tornado formation remains possible, even in otherwise unremarkable environments.

#### Case 3: High-Risk Synoptic Setup, Null Tornado Outcome

On 25 March 2021, a high-risk outlook was issued for portions of Mississippi and Alabama in advance of a deep mid-level trough and strongly diffluent jet dynamics. Forecasts suggested the potential for strong tornadoes, supported by extreme shear, abundant low-level moisture, and

strong upper-level divergence. Despite this, tornado activity was substantially more limited than expected. From a constraint-convergent perspective, the null outcome can be attributed to a temporal misalignment of critical ingredients. Convection initiated early and ahead of key surface boundaries, prematurely stabilizing the boundary layer and limiting subsequent convective potential. While shear and upper-level forcing were present, the  $\Phi$ -phase synchronizer—reflecting temporal alignment and mesoscale timing—was not met. This case illustrates how the absence of temporal or spatial coordination, even in highly favorable synoptic conditions, can suppress tornadogenesis.

## **Operational and Societal Implications**

### **Improving Warning Systems**

A more accurate conceptual model of tornadogenesis has direct implications for operational forecasting and public safety. By identifying the necessary set of constraints for tornado formation, forecasters could issue more precise and reliable warnings, reducing false alarms and improving public trust (Brooks and Correia 2018).

### **Enhancing Communication and Education**

A constraint-convergent framework also offers a more intuitive way to communicate tornado risk to the public and decision-makers. Rather than relying on abstract indices or probabilistic statements, forecasters could explain tornado potential in terms of the “ingredients” required and whether they are all present. This approach aligns with the “ingredients-based” forecasting paradigm but adds a systems-level rigor that may improve understanding and response (Doswell et al. 1996; Schultz and Stensrud 2010).

## Limitations and Future Directions

### The Challenge of Defining Constraints

One challenge in operationalizing a constraint-convergent execution model is the precise definition and measurement of critical constraints. For example, what constitutes a “sufficient” surface boundary, or how much CAPE is “enough” for tornadogenesis? These thresholds may vary depending on storm type, regional climatology, or mesoscale context (Thompson and Mead 2007; Doswell and Schultz 2006). Future research should aim to refine these definitions through empirical analysis, modeling, and expert consensus.

### The Role of Stochasticity and Uncertainty

While a constraint-convergent framework emphasizes the necessity of multiple independent conditions, it does not preclude the role of stochasticity or inherent unpredictability in tornado formation. Small-scale processes, chaotic dynamics, and observational limitations will always introduce some degree of uncertainty (Lorenz 1963). The goal of this perspective is not to eliminate uncertainty but to provide a more robust conceptual foundation for understanding and managing it.

A constraint-convergent model like ARCH is amenable to empirical testing through structured comparative analysis. Rather than assuming linear correlations between individual variables and tornado occurrence, ARCH posits that multiple independent constraints must each exceed a threshold—i.e., a conjunctive requirement. Empirically, this implies that even a single unmet constraint should be sufficient to suppress execution, regardless of the magnitude of others.

To operationalize this, each ARCH constraint—Availability (A), Readiness (R), Contextual dynamics (C), High-level support (H), and Phase alignment ( $\Phi$ )—can be scored on a binary or ordinal scale (e.g., 0 = absent, 0.5 = marginal, 1 = satisfied). These scores could be derived from reanalysis data, radar diagnostics, mesoanalysis, and storm reports. For instance, A might reflect the presence of a well-defined surface boundary near storm initiation, while  $\Phi$  might be assessed via timing alignment of storm-scale lift with mesoscale convergence zones. While the proposed scoring rubric (0, 0.5, 1) introduces a degree of subjectivity, it reflects common practices in operational diagnostics and environmental classification. Future work should prioritize inter-observer calibration and, where possible, integrate automated diagnostics from reanalysis, radar, or satellite-derived indices to enhance reproducibility.

Importantly, the ARCH framework is non-compensatory: it does not assume that high values in one domain can offset deficiencies in another. Therefore, multiplicative logic is preferred to additive weighting. A simple product ( $A \times R \times C \times H \times \Phi$ ) serves as a first-order operationalization, yielding an execution score of zero if any constraint is absent. However, more sophisticated versions may introduce soft thresholds or logistic gating functions to account for observational uncertainty.

Future empirical studies could test ARCH logic by applying these scoring methods to historical datasets of both tornadic and null events, identifying whether tornado occurrence correlates with full constraint satisfaction, and whether constraint failure predicts tornadogenesis collapse. Matched-pair designs, where environments differ by only one constraint, could be especially powerful in testing necessity claims. This approach lends itself to machine learning classification

methods, including decision trees and random forests, which are well suited for identifying combinatorial threshold effects.

## Conclusion

Tornado formation remains one of the most challenging problems in atmospheric science. This paper proposes a conceptual shift: viewing tornadogenesis as a constraint-convergent execution event, inspired by systems theory and biological regulation. Rather than relying on additive or probabilistic frameworks, the ARCH model posits that tornado formation occurs only when multiple independent and necessary constraints are simultaneously satisfied.

This logic is formalized in the expression:

$$\text{Execution} = A \times R \times C \times H \times \Phi$$

where  $A$  represents the availability of a triggering surface boundary (such as a dryline or front),  $R$  denotes thermodynamic readiness (including parameters like CAPE and low-level moisture),  $C$  refers to contextual dynamics (such as low-level wind shear or terrain-modulated flow),  $H$  captures upper-level support (such as jet streaks or divergence aloft), and  $\Phi$  reflects phase alignment or mesoscale timing (such as convergence timing or other synchronizing mechanisms). Execution is binary: if any one term is zero—i.e., any constraint is unmet—tornadogenesis is precluded, regardless of the magnitude of the others.

Importantly, this conjunctive logic is not unique to tornadoes. Several other atmospheric phenomena similarly depend on the simultaneous satisfaction of multiple gating conditions. For example, hurricane formation requires warm sea surface temperatures, low vertical wind shear, sufficient mid-level moisture, and a pre-existing atmospheric disturbance. The absence of any



one of these elements—such as excessive shear—can suppress cyclogenesis altogether.

Snowfall, likewise, depends on adequate vertical lift, sufficient atmospheric moisture, and a thermal profile cold enough to sustain frozen precipitation through the atmospheric column.

Failure in any one of these domains nullifies accumulation, regardless of how favorable the others may be.

Fog development similarly depends on the alignment of high humidity, radiative or advective cooling to the dew point, and minimal wind to prevent dispersal—conditions that must co-occur.

Cloud formation depends not only on saturation, but also on vertical ascent and the presence of condensation nuclei; the lack of any one prevents sustained cloud growth. Thunderstorm

electrification, while often treated in isolation, also reflects this logic: it requires strong updrafts, mixed-phase microphysics, and collisional processes for charge separation to occur. In all these

examples, failure of a single necessary condition results in failure of the entire phenomenon.

These examples suggest that constraint-convergent execution may be a broadly applicable conceptual model in meteorology, describing a class of threshold-governed transitions in which the absence of any one critical element precludes system evolution. Yet most existing forecasting systems rely on additive indices or composite parameters, which may overlook these conjunctive dependencies and obscure critical failure modes.

This logic takes on increasing importance in the context of climate change. Anthropogenic warming alters not only the magnitude of individual atmospheric parameters but also their spatial and temporal alignment. For instance, rising surface temperatures may increase CAPE (R), while simultaneously disrupting upper-level jet dynamics (H), or reducing the frequency and clarity of surface boundaries (A) due to changing land use or shifting frontal patterns. As a result,

environments may become increasingly characterized by “near misses”—favorable values in isolation, but incomplete convergence in execution-critical domains.

Ultimately, the constraint-convergent model encourages a more diagnostic, systems-oriented view of tornadogenesis and related meteorological events. It reframes atmospheric transitions as conjunctive phenomena—requiring not just favorable conditions, but the right conditions, working together, at the right time. The ARCH perspective opens new avenues for empirical study, interdisciplinary collaboration, and operational application in a changing and increasingly complex climate system.

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No new data were generated or analyzed in this study.

Conflict of Interest Statement:

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